

## CMSC 170: Supervised Learning

K-Nearest Neighbors

Katherine Loren M. Tan Institute of Computer Science University of the Philippines Los Baños

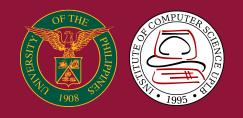
#### LEARNING OUTCOMES



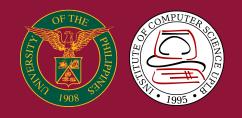


At the end of the session, the students should be able to:

- understand the K-Nearest Neighbor classification algorithm;
- implement the KNN algorithm; and
- Apply the KNN algorithm in classifying data.



It is a non-parametric machine learning algorithm that classifies new data based by finding its k-nearest neighbors in the data set.



The algorithm chooses the classification that represented the other data points the most.

#### **HOW DOES THE ALGORITHM WORKS?**





x <sub>00</sub>	<b>x</b> <sub>01</sub>	${\sf x}_{02}^{}$	•••	$x_{0n}$	->	Υ <sub>0</sub>
x <sub>10</sub>	x <sub>11</sub>	<b>x</b> <sub>12</sub>		x <sub>1n</sub>	->	$Y_1$
x <sub>20</sub>	<b>x</b> <sub>21</sub>	x <sub>22</sub>		X <sub>2n</sub>	->	$Y_2$
			i			
X <sub>m0</sub>	X <sub>m1</sub>	X <sub>m2</sub>		X <sub>mn</sub>	->	$Y_{m}$

#### **HOW DOES THE ALGORITHM WORKS?**





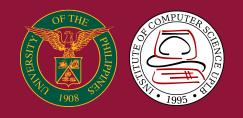
					Data Points	
x <sub>00</sub>	x <sub>01</sub>	x <sub>02</sub>		x <sub>on</sub>	->	$Y_0$
x <sub>10</sub>	x <sub>11</sub>	<b>x</b> <sub>12</sub>		x <sub>1n</sub>	->	$Y_1$
<b>x</b> <sub>20</sub>	x <sub>21</sub>	<b>x</b> <sub>22</sub>		$\mathbf{x}_{2n}$	->	$Y_2$
			:			
$\mathbf{x}_{\text{m0}}$	$\mathbf{x}_{m1}$	X <sub>m2</sub>		X <sub>mn</sub>	->	$\mathbf{Y}_{m}$

#### **HOW DOES THE ALGORITHM WORKS?**

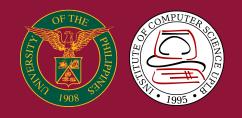




				I	Label		
x <sub>00</sub>	x <sub>01</sub>	x <sub>02</sub>		x <sub>0n</sub>	-> /	$Y_0$	
x <sub>10</sub>	x <sub>11</sub>	x <sub>12</sub>	•••	X <sub>1n</sub>	->	$Y_1$	
x <sub>20</sub>	x <sub>21</sub>	x <sub>22</sub>	•••	X <sub>2n</sub>	->	$Y_2$	
			:				
X <sub>m0</sub>	X <sub>m1</sub>	X <sub>m2</sub>		$\mathbf{x}_{mn}$	-> \	$Y_{m}$	



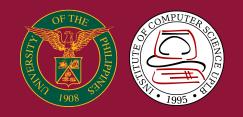
# K-Nearest Neighbor Classification Algorithm uses distance algorithms.



Common distance algorithms are euclidean, manhattan, and minkowski distance.



The classification of a new feature vector x=(x0,x1,x2,...,xn) is determined by computing its distance from all the other feature vectors in the training data set



choosing the *k* nearest neighbors, where *k* is a given value.



1. Provide a k and a feature vector x.





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$$d = \sqrt{\sum_{i}^{n} (x_i - v_i)^2}$$





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- 4. The class with the maximum count will be the classification of x.

#### TRAINING DATASET

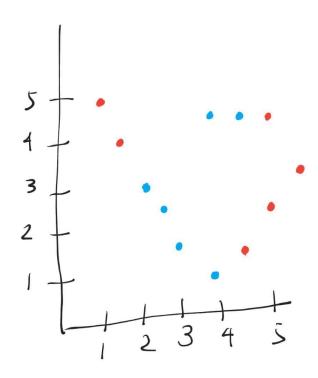


x	у	class
1	5	0
1.5	4	0
2	3	1
2.5	2.5	1
3	1.5	1
4	1	1
4	4.5	1

Х	у	class
4.5	1.5	0
4.5	4.5	1
5	2.5	0
5	4.5	0
5.5	3.5	0



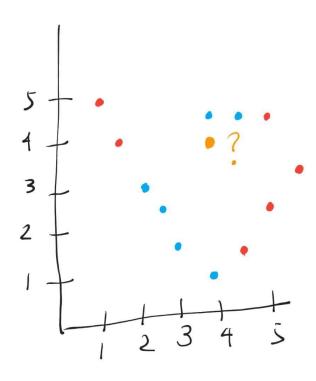




### **VISUAL REPRESENTATION OF** TRAINING SET



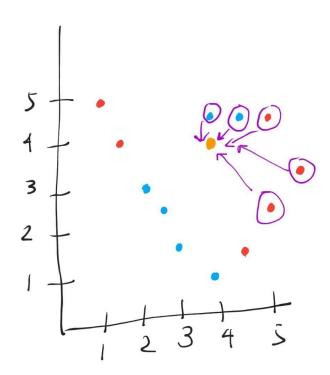




## Input 4 4 What is its class?

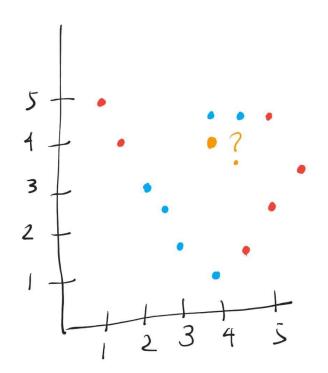








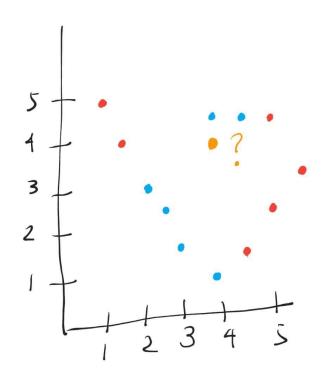




x	у	class	Distance from 4 4
1	5	0	3.1622
1.5	4	0	2.5000
2	3	1	2.2360
2.5	2.5	1	2.1213
3	1.5	1	2.6925
4	1	1	3
4	4.5	1	0.5





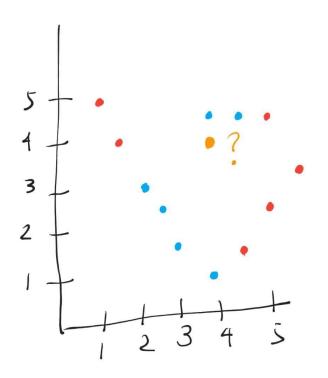


Х	у	class	Distance from 4 4
4.5	1.5	0	2.5495
4.5	4.5	1	0.7071
5	2.5	0	1.8027
5	4.5	0	1.1180
5.5	3.5	0	1.5811

#### k=5



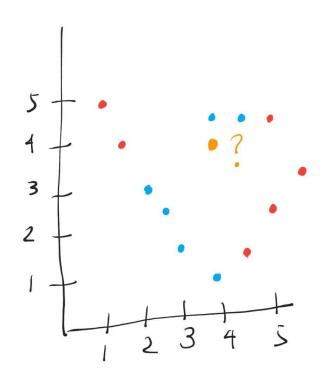




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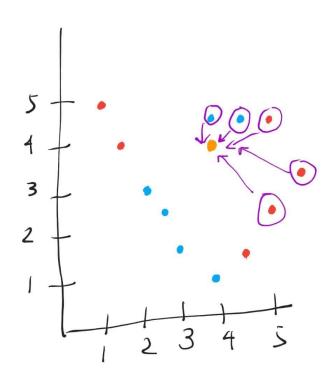






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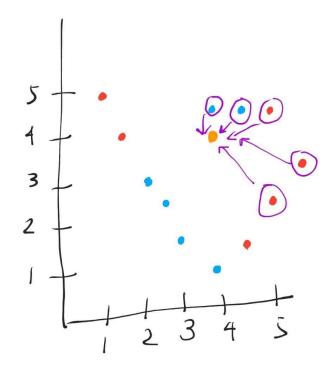




5 nearest neighbors of (4,4) are: (4, 4.5), (4.5, 4.5), (5, 2.5), (5, 4.5) and (5.5, 3.5)

#### Get the classes of the nearest neighbors





The class of the 5 neighbors are:

(4, 4.5) 1,

(4.5, 4.5) 1,

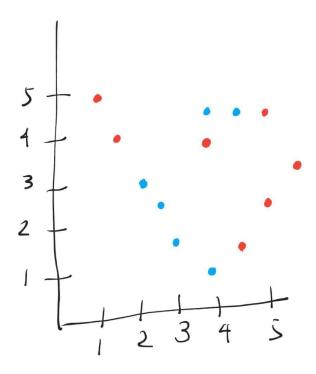
(5, 2.5) 0,

(5, 4.5) 0 and

(5.5, 3.5)0

#### Get the classes of the nearest neighbors





The new point (4,4) is labelled as class 0.





# For questions and inquiries, you can email me at

kmtan4@up.edu.ph

#### **EXERCISE on KNN**



A dataset containing diabetes information will be used. The task is to classify the next points from **diabetes.csv**. The test file contains information regarding the no of pregnancies, glucose value, blood pressure, skin thickness, insulin value, bmi, diabetes pedigree function, age, and outcome of a person. The person can be classified as either diabetic or non-diabetic. The results must be placed on **output.txt**.

#### **SOME REMINDERS:**

- Naming convention for exercise: surname\_knn.
- Python or Java can only be used for the exercise.
- Do not used built-in libraries for KNN.
- Do not forget to put a journal in your ReadMe file in Github.
- Lastly, Honor and Excellence.