

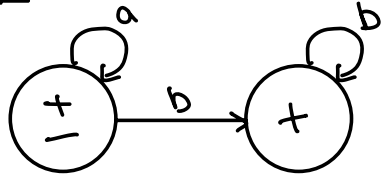
1. (5 points) Find the language and its CFG of this FA

FA	CFG and Language
	$L = (a^2 + b^2 + ab + ba)^*$ <p>CFG:</p> $\begin{aligned} X &\rightarrow a^2 X & X &\rightarrow ba X \\ X &\rightarrow b^2 X & X &\rightarrow \lambda \\ X &\rightarrow ab X \end{aligned}$

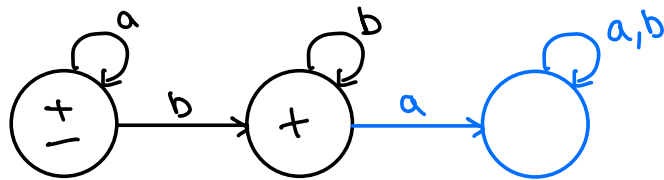
2. (5 points) Given $L = a^*b^*$. Find the complement of L . Show all steps for full credit
3. (10 points) Given CFG below which is not deterministic. Convert the CFG to a deterministic grammar.
- $S \rightarrow aB \mid bA$
 $B \rightarrow bB \mid bA \mid \lambda$
 $A \rightarrow aA \mid aB$
4. (5 points) Remove λ from this CFG
- $S \rightarrow XYZ$
 $X \rightarrow aX \mid bX \mid \lambda$
 $Y \rightarrow aY \mid bY \mid \lambda$
 $Z \rightarrow aZ \mid \lambda$
5. (5 points) Remove the unit production from this CFG
- $S \rightarrow aXYb$
 $X \rightarrow S$
 $Y \rightarrow bY \mid b$

② Given $L = a^*b^*$

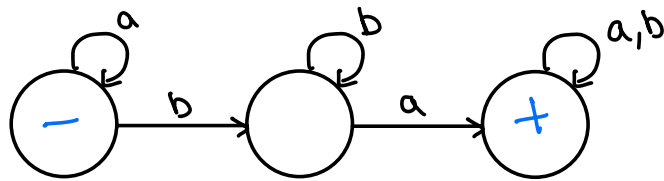
step 1



step 2

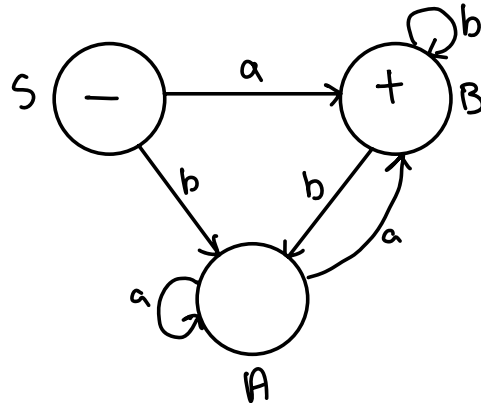


step 3

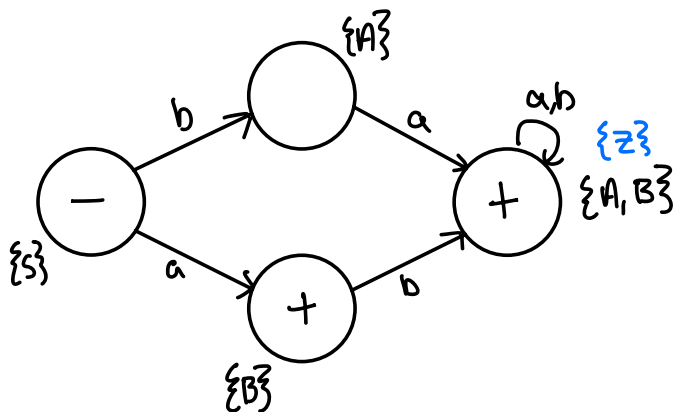


$$\bar{L} = a^* b b^* a (a+b)^*$$

③ Given $S \rightarrow aB \mid bA$
 $B \rightarrow bB \mid bA \mid \lambda$
 $A \rightarrow aA \mid aB$



input state	a	b
$\{S\}$	$\{B\}$	$\{A\}$
$\{A\}$	$\{A, B\}$	$\{\}$
$\{B\}$	$\{\}$	$\{A, B\}$
$\{z\} \{A, B\}$	$\{A, B\}$	$\{A, B\}$



CFG:

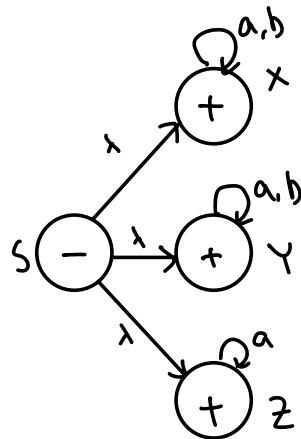
$S \rightarrow aB \mid bA$

$A \rightarrow aZ$

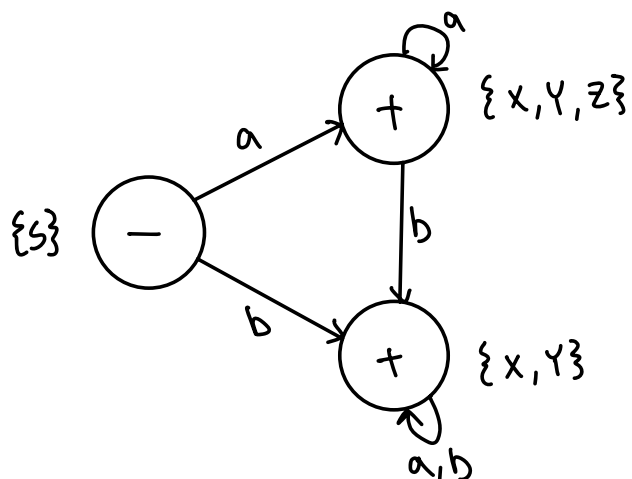
$B \rightarrow bZ \mid \lambda$

$Z \rightarrow aZ \mid bZ \mid \lambda$

④ Given $S \rightarrow XYZ$
 $X \rightarrow aX \mid bX \mid \lambda$
 $Y \rightarrow aY \mid bY \mid \lambda$
 $Z \rightarrow aZ \mid \lambda$



input state	a	b
$\{S\}$	$\{X, Y, Z\}$	$\{X, Y\}$
$\{X\}$	$\{X\}$	$\{X\}$
$\{Y\}$	$\{Y\}$	$\{Y\}$
$\{Z\}$	$\{Z\}$	$\{\}$
$\{X, Y\}$	$\{X, Y\}$	$\{X, Y\}$
$\{X, Y, Z\}$	$\{X, Y, Z\}$	$\{X, Y\}$



⑤ Given $S \rightarrow aX/Yb$
 $X \rightarrow S$
 $Y \rightarrow bY/b$

$X \rightarrow S \rightarrow Y$

$Y \rightarrow b$ $S \rightarrow S \begin{cases} a \\ b \end{cases}$

$X \rightarrow S$

$S \rightarrow a/b$
 $X \rightarrow a/b$
 $Y \rightarrow b$