

Compiler Design
Assignment 7 : Predicative Parsing Table

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1. Given the following CFG (no programming required).

$E \rightarrow E + T$

$E \rightarrow T$

$T \rightarrow T * F$

$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow a$

- (a) Eliminate left-recursions

- (b) find members of FIRST and FOLLOW

State	FIRST	FOLLOW
E		
E'		
T		
T'		
F		

- (c) Construct its predictive Parsing Table

- (d) trace $a*(a+a)\$$ by showing the content of the stack and the leftover of the input string during tracing: Stack input

Programming part:

1. Given the following CFG and the Predictive Parsing table. Write a program to trace input strings (1) $(i+i)*i\$$, (2) $i*(i-i)\$$, (3) $i(i+i)\$$. Show the content of the stack after each match.

$E \rightarrow E+T; E \rightarrow E-T; E \rightarrow T; T \rightarrow T*F; T \rightarrow T/F; T \rightarrow F; F \rightarrow i; F \rightarrow (E)$

states	i	+	-	*	/	()	\$
E	TQ					TQ		
Q		+TQ	-TQ				λ	λ
T	FR					FR		
R		λ	λ	*FR	/FR		λ	λ
F	i					(E)		

2. Same as problem no. 2, include the $S \rightarrow aW$, $W \rightarrow E$ rules to the beginning of the grammar so that the grammar becomes this :

$S \rightarrow aW$ $W \rightarrow E$

$E \rightarrow E+T$

$E \rightarrow E-T$

$E \rightarrow T$

$T \rightarrow T*F$ $T \rightarrow T/F$ $T \rightarrow F$

$F \rightarrow a$ $F \rightarrow (E)$

NOTE: S is the starting state

Construct the parsing table (not exactly the same as above) and modify your program to trace input statements (i) $a=(a+a)*a\$$, (ii) $a=a*(a-a)\$$, (iii) $a=(a+a)a\$$

① a) $E \rightarrow E+T$ \rightsquigarrow $E \rightarrow TE'$ $F \rightarrow (E)$
 $E \rightarrow T$ $E' \rightarrow +TE'$ $F \rightarrow \alpha$
 $T \rightarrow T*F$ $E' \rightarrow \lambda$
 $T \rightarrow F$ $T \rightarrow FT'$
 $F \rightarrow (E)$ $T' \rightarrow *FT'$
 $F \rightarrow \alpha$ $T' \rightarrow \lambda$

b)

state	First	Follow
E	{ (α }	{ #) }
E'	{ + λ }	{ #) }
T	{ (α }	{ + λ #) }
T'	{ * λ }	{ + λ #) }
F	{ (α }	{ + λ #) }

c)

states	α	+	*	()	#
E	TE'			TE'		
E'		$+TE'$			λ	λ
T	FT'			FT'		
T'		λ	$*FT'$		λ	λ
F	α			(E)		

d) stack	input
push \$ push E stack: \$E	a*(a+a)\$
pop: E read: a go to [E,a]=TE' push E', push T stack: \$E'T	*(a+a)\$
pop: T go to [T,a]=FT' push T' push F stack \$E'T'F	
pop: F go to [F,a]=a push a stack \$E'T'a	
pop: a match w/ input a stack \$E'T'	
pop: T' read: * go to [T',*]=*FT' push T', push F, push * stack \$E'T'F*	(a+a)\$

stack	input
pop: * match w/ input * stack \$E'T'F	
pop: F read: (go to [F,(]=E) push) push E push (stack \$E'T')E(a+a)\$
pop: (match w/ input (stack \$E'T')E	
pop: E read a go to [E,a]=TE' push E' push T stack \$E'T')E'T	+a)\$
pop: T go to [T,a]=FT' push T' push F stack \$E'T')E'T'F	
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stack	input
pop: F go to [F, a] = a push a stack #E'T')E'T'a	
pop: a match w/ input a stack #E'T')E'T'	
pop: T' read: + go to [T', +] = λ stack #E'T')E'	a) #
pop: E' go to [E', +] = +TE' push E', T, + stack #E'T')E'T+	
pop: + match w/ input + stack #E'T')E'T	
pop: T read: a go to [T, a] = FT' push T', F stack #E'T')E'T'F) #

stack	input
pop: F go to [F, a] = a push a stack #E'T')E'T'a	
pop: a match w/ input a stack #E'T')E'T'	
pop: T' read:) go to [T',)] = λ stack #E'T')E'	#
pop: E' go to [E',)] = λ stack #E'T')	
pop:) match w/ input) stack #E'T'	
pop: T' read: # go to [T', #] = λ stack #E'	Done w/ input string
pop: E' go to [E', #] = λ stack #	
pop: # match w/ input #	Accepted

$$\begin{array}{lcl} \textcircled{2} & S \rightarrow aW & \\ & W \rightarrow =E & \end{array} \quad \rightarrow \quad \begin{array}{lcl} & S \rightarrow aW & \\ & W \rightarrow =E & \end{array}$$

First (S) = {a}

First (W) = {=}

The rest is
the same

states	a	+	-	*	/	()	#	=
S	aW								
W									=E
E	TQ					TQ			
Q		+TQ	-TQ				λ	λ	
T	FR					FR			
R		λ	λ	*FR	/FR		λ	λ	
F	a					(E)			