

Group Assignment 1

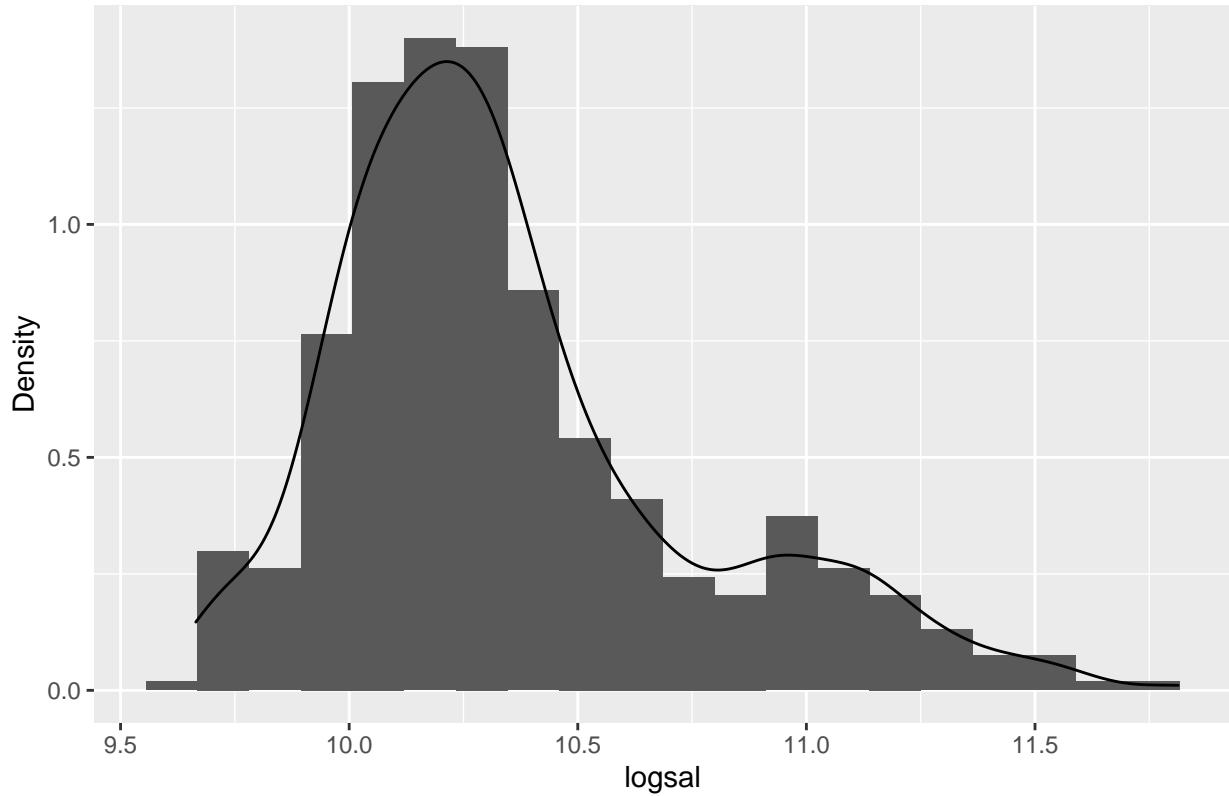
Alex Wong, Chelaka Paranahewa, Harjot Channa, Jonas Tiong

Question 1

Part A

Section i Histogram of logsal

Histogram of logsal



Section ii

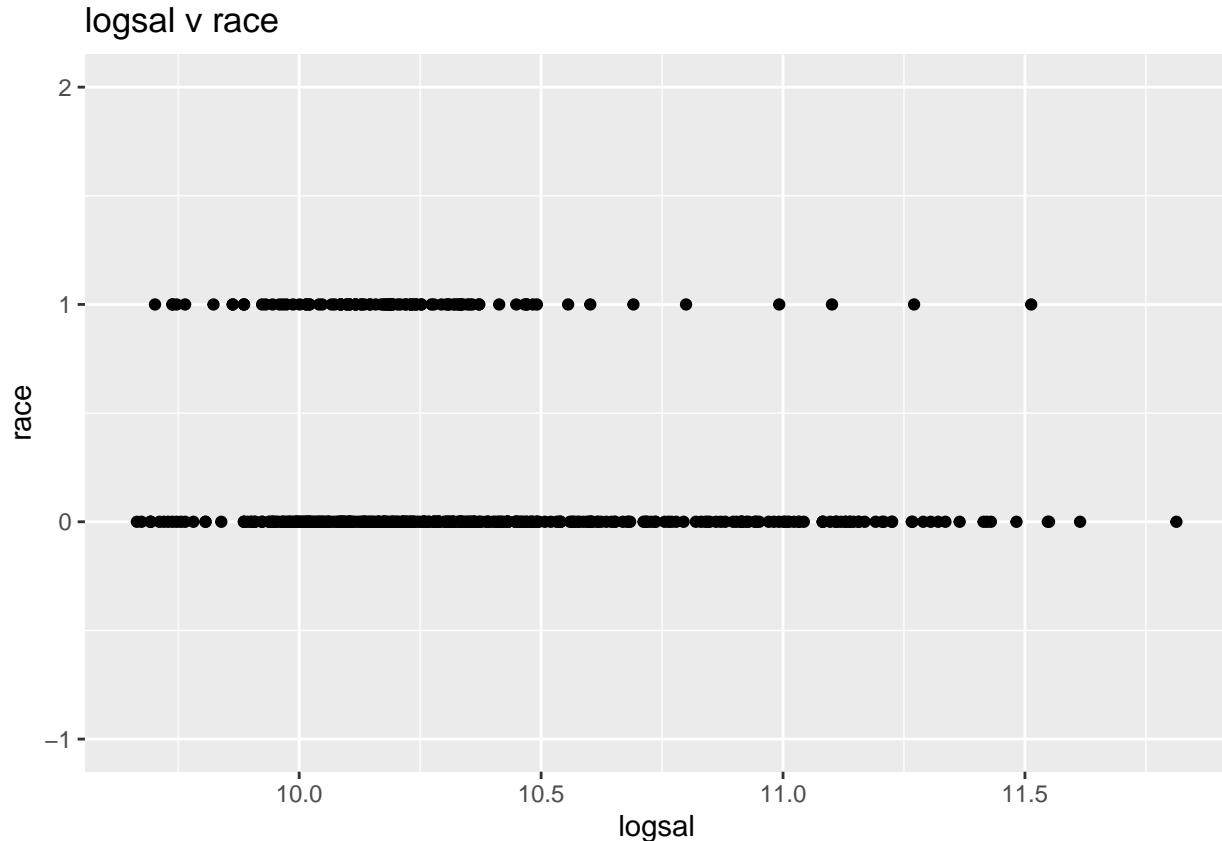
n	mean	median	min	max	sd	skew	kurtosis
474	10.35679	10.27073	9.664596	11.81303	0.3973342	0.994876	0.6471944

As the mean is greater than the median, the distribution is positively skewed indicating that there are high valued outliers (those earning high annual wages). Since the skewness is 0.99, we can say that this distribution is moderately skewed.

On average, an individual in this bank will have a log of annual salary of around 10.36 or, in other words, an annual salary of around $e^{10.36} = 31,470.09$. The maximum annual salary, empirically, is around $e^{11.81} = 135,000.00$ and the lowest salary in the bank is around $e^{9.66} = 15,750.00$. That is a difference of around 119,250.00.

Part B

Section i Scatterplot of logsal and race



Section ii Recall from part (a)ii) that the mean of logsal was around 10.36. From the scatterplot it is evident that in this bank, an individual who does not belong to an ethnic minority earns in a wide range of salaries from slightly below to 10.0 to slightly above 11.0 (as per where all the data points are clustered). In contrast, for an individual who does belong to an ethnic minority this is range is far smaller, somewhere slightly below 10.0 to around 10.5. Hence, the gap from the mean wage of 10.36 is larger for non-minorities which may suggest larger mobility for this category of employees which would be indicative of racial discrimination.

Part C

Section i

$$\widehat{\text{logsal}} = 10.396 - 0.180 \text{ race}$$

```
##  
## Call:  
## lm(formula = logsal ~ race, data = dat)  
##  
## Residuals:
```

```

##      Min     1Q   Median     3Q    Max
## -0.73180 -0.27303 -0.06764  0.16623  1.41664
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.39639   0.02031 511.915 < 2e-16 ***
## race        -0.18049   0.04336 -4.163 3.74e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3906 on 472 degrees of freedom
## Multiple R-squared:  0.03541, Adjusted R-squared:  0.03337
## F-statistic: 17.33 on 1 and 472 DF, p-value: 3.737e-05

```

Section ii

$$H_0 : \beta_1 = 0$$

$$H_1 : \beta_1 > 0$$

Significant Level : $\alpha = 0.05$

Test statistic and null distribution : $\frac{\hat{\beta}_1}{se(\hat{\beta}_1)} \sim t_{n-k-1} = t_{472}$

$$t_{calc} = 4.162804$$

$$t_{crit} = 1.9650027$$

Decision rule : reject H_0 if $|t_{calc}| > t_{crit}$

Decision : Since $4.162804 > 1.9650027$, reject H_0

In conclusion, at 0.05 level of significance, we reject the null hypothesis that race has no effect on (the log of) an individual's annual salary in favour of the alternative hypothesis race has an effect.

Section iii $\hat{\beta}_1$ measures the average difference in the log of an individual's annual salary in the bank (thus proportionate difference) between someone who belongs to an ethnic minority and someone who does not.

Hence, the average difference, according to our model, in an individual's annual wage between someone who belongs to an ethnic minority is $e^{-0.180}$ times the annual salary of someone who does not belong to an ethnic minority.

Section iv This model does not provide conclusive evidence of racial discrimination in salaries paid by the bank. This is because it does not account for (condition on) confounding variables - variables that causally effect an individual's annual salary and whether they belong to an ethnic minority. For example, an individual's level of education may be a variable of interest; the individual may be an immigrant to which US' immigration policy and its skill stream for accepting immigrants (based on education) may decide whether or not someone (in America) belongs to an ethnic minority. And, for an individual's annual salary, may be effected by if the company values (and thus willing to pay wages that are higher) for someone based on the education that they have.

Section v As the coefficient of determination is around $R = 0.035$, this means that around 3.5 per cent of the sample variation in the log of an individual's annual salary is explained by race in this bank. Hence, this model is a very low fit for describing what variables effect an individual's annual salary, where the remaining 96.5 per cent may be caused be unaccounted for variables like education (as aforementioned) or inherent variability.

```
## [1] 0.03541368
```

Section vi β_0 measures the conditional mean of the log of an individual's annual salary in this bank who does not belong to an ethnic minority. This value is 10.396. In other words, the conditional mean of an individual's annual salary who is not part of an ethnic minority is $e^{10.396}$.

Section vii

2.5 %	97.5 %
10.35649	10.4363

Section viii We are 95 per cent confident, on average, that the population value of the log of an individual's annual salary in this bank for someone who does not belong to an ethnic minority is between 10.356 and 10.436. That is, the population value of an individual's annual salary in this bank is between $e^{10.356}$ and $e^{10.436}$, on average 95 per cent of the time.

Section ix Since $\beta_0 = 0$, in a hypothesis test of individual significance at 0.05, does not fall within the 95 per cent confidence interval 10.356, 10.436 we conclude that $\hat{\beta}_0$ is statistically significant.

Part D

Section i

```


$$\widehat{logsal} = 4.026 - 0.024 \text{ educ} + 0.601 \text{ logssal} + 0.061 \text{ gender} - 0.043 \text{ race} + 0.121 \text{ jobcat}$$


## Call:
## lm(formula = logsal ~ educ + logssal + gender + race + jobcat,
##      data = dat)
##
## Residuals:
##       Min     1Q   Median     3Q    Max 
## -0.41156 -0.11677 -0.01430  0.09835  0.91176 
## 
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 4.025756  0.390102 10.320 < 2e-16 ***
## educ        0.024382  0.003653  6.675 7.01e-11 ***
## logssal     0.600624  0.044518 13.492 < 2e-16 ***
## gender      0.060849  0.018852  3.228  0.00134 **  
## race        -0.042609  0.019187 -2.221  0.02685 *   
## jobcat      0.120894  0.015717  7.692 8.65e-14 ***
## ---        
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## 
## Residual standard error: 0.1666 on 468 degrees of freedom
## Multiple R-squared:  0.8261, Adjusted R-squared:  0.8242 
## F-statistic: 444.6 on 5 and 468 DF,  p-value: < 2.2e-16

```

Section ii A regressor is individually insignificant at 0.001 level of significance if its p-value is larger than 0.001, p-value > 0.001 . So, according to our model only gender and race are individually insignificant at this level as p-value_{gender} = 0.0013 > 0.001 and p-value_{race} = 0.027 > 0.001 , respectively.

Section iii

$$H_0 : \beta_1 = \beta_2 = \beta_3 = \beta_4 = \beta_5 = 0$$

$$H_1 : \exists_{i \in \{1,2,3,4,5\}} \beta_i \neq 0$$

Significant Level : $\alpha = 0.05$

$$\text{Test statistic and null distribution : } \frac{(SSR_R - SSR_{UR})}{SSR_{UR}} \frac{(n - k - 1)}{q} \sim F_{(q,n-k-1)} = t_{5,468}$$

$$t_{calc} = 444.6423804$$

$$F_{crit} = 2.5936131$$

Decision rule : reject H_0 if $t_{calc} > F_{crit}$

Decision : Since $444.6423804 > 2.5936131$, reject H_0

In conclusion, at 0.05 level of significance, we reject the null hypothesis that an individual's number of years of education, their gender, the job category within the bank, their log of their starting annual salary, and if they belong to an ethnic minority are jointly insignificant in effecting (the log of an) individual's annual salary in favour of the alternative hypothesis that at least one of these variables are significant.

Section iv $\hat{\beta}_4$ measures the average difference in the log of an individual's annual salary in the bank (thus proportionate difference) between someone who belongs to an ethnic minority and someone who does not, controlling for the the number of years of education, the gender, the job category within the bank, and the log of an individual's starting salary.

Hence, *this* average difference, according to our model, for an individual who belongs to an ethnic minority is $e^{-0.043}$ times the annual salary of someone who does not belong an ethnic minority.

Section v

[1] 0.1034585

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$\hat{\beta}_3 - \hat{\beta}_4 = 0.103$ does not have a meaningful interpretation. This is because $\hat{\beta}_3$ is the conditional mean of the log of an individual's annual salary given that they are male and ceteris paribus minus the conditional mean of the log of an individual's annual salary given that they are female and ceteris paribus. $\hat{\beta}_4$ is the conditional mean of the log an individual's annual salary given that they belong to an ethnic minority and ceteris paribus minus the conditional mean of the log of an individual's annual salary given that the do not belong to an ethnic minority and ceteris paribus. Hence, the difference between $\hat{\beta}_3$ and $\hat{\beta}_4$ is the sum of the conditional mean of an individual's annual salary given that they are male, ceteris paribus (including one's racial status), plus the salary given that they are not part of the ethnic minority, ceteris paribus (including one's gender), minus the salary given that they are female, ceteris paribus (including one's racial status), minus the salary given that they are part of an ethnic minority, ceteris paribus (including one's gender). The fact that this sum of different means is conditional on different set of variables makes any descriptive application inapplicable to the bank.

Section vi It is likely that this model does provide conclusive evidence of racial discrimination in salaries paid by the bank, as per the individual significance of the regression coefficient for `race` and the joint significance of all regressors. This is because the model takes into account possible confounding variables to `race` and `logsal` — years of education, one's gender, the job category, and the (log of) starting salary — which would allow us to make causal statements about an individual's racial status on the (log of their) annual salary. In other words, we are unlikely to have committed **omitted variable bias** in this model by our specification of variables.

Section vii The new model has $R^2 = 0.826$, meaning around 82.6 per cent of the sample variation in the log of an individual's annual salary is explained by the independent variables. This is a much better comparison to the old model where only 3.5 per cent was explained by the independent variables, leaving much variation unexplained (about a $(0.826 - 0.035) \times 100\% = 79.1\%$ difference).

Moreover, given that the variance inflation factor (VIF) is not more than 10, which would be indicative of high correlation between regressors, but rather very small at below 2 for each, this suggests that our new model has not overspecified and that this R^2 is not high largely because of adding more variables.

Model	R-Squared
Old	0.0354137
New	0.8261007

VIF
1.892869
4.205978
1.505895
1.077052
2.517574

Part E

We are working with the same model prior:

$$\widehat{\log sal} = 4.026 - 0.024 \text{ educ} + 0.601 \text{ logssal} + 0.061 \text{ gender} - 0.043 \text{ race} + 0.121 \text{ jobcat}$$

$$H_0 : \beta_3 = \beta_4 = 0$$

$$H_1 : \exists_{i \in \{3,4\}} \beta_i \neq 0$$

Significant Level : $\alpha = 0.1$

Test statistic and null distribution : $\frac{(SSR_R - SSR_{UR})}{SSR_{UR}} \frac{(n - k - 1)}{q} \sim F(q, n - k - 1) = F(2, 468)$

$$t_{calc} = 6.4746026$$

$$F_{crit} = 3.0149905$$

Decision rule : reject H_0 if $t_{calc} > F_{crit}$

Decision : Since $6.4746026 > 3.0149905$, reject H_0

In conclusion, at 0.05 level of significance, we reject the null hypothesis that an individual's gender and whether they belong to ethnic minority has no effect on the (log of their) annual salary in favour of the alternative hypothesis that their gender and/or their race does effect the individual's (log of their) annual salary.

Part F

Section i Given that

$$\mathbb{E}[\log sal | \text{educ}, \text{logssal}, \text{gender}, \text{race}, \text{jobcat}] = \beta_0 + \beta_1 \text{ educ} + \beta_2 \text{ logssal} + \beta_3 \text{ gender} + \beta_4 \text{ race} + \beta_5 \text{ jobcat}$$

then our estimated conditional mean has form:

$$\hat{\beta}_0 + \hat{\beta}_1 \text{ educ} + \hat{\beta}_2 \text{ logssal} + \hat{\beta}_3 \text{ gender} + \hat{\beta}_4 \text{ race} + \hat{\beta}_5 \text{ jobcat}$$

For population A, i.e. for the population of female managers with 12 years of education who belong to a racial minority and received a given starting salary, the average `logsal` is:

$$\begin{aligned}\mathbb{E}[\text{logsal} | \text{educ} = 12, \text{gender} = 0, \text{race} = 1, \text{jobcat} = 3, \text{logssal}] &= \beta_0 + \beta_1 12 + \beta_2 \text{ logssal} + \beta_4 + \beta_5 3 \\ &= (\beta_0 + 12\beta_1 + \beta_4 + 3\beta_5) + \beta_2 \text{ logssal}\end{aligned}$$

Section ii Likewise, for population B, i.e. for the population of male managers with 11 years of education who are not members of a ethnic minority and receives the same starting salary as the individuals in population A, the average `logsal` is:

$$\begin{aligned}\mathbb{E}[\text{logsal} | \text{educ} = 11, \text{gender} = 1, \text{race} = 0, \text{jobcat} = 3, \text{logssal}] &= \beta_0 + \beta_1 11 + \beta_2 \text{ logssal} + \beta_3 + \beta_5 3 \\ &= (\beta_0 + 11\beta_1 + \beta_3 + 3\beta_5) + \beta_2 \text{ logssal}\end{aligned}$$

Section iii Given the null hypothesis that the average `logsal` of population A is equal to that of population B $\mathbb{E}[\text{logsal} | \text{educ} = 12, \text{gender} = 0, \text{race} = 1, \text{jobcat} = 3, \text{logssal}] = \mathbb{E}[\text{logsal} | \text{educ} = 11, \text{gender} = 1, \text{race} = 0, \text{jobcat} = 3, \text{logssal}]$, it follows that:

$$\mathbb{E}[\text{logsal} | \text{educ} = 12, \text{gender} = 0, \text{race} = 1, \text{jobcat} = 3, \text{logssal}] - \mathbb{E}[\text{logsal} | \text{educ} = 11, \text{gender} = 1, \text{race} = 0, \text{jobcat} = 3, \text{logssal}] = 0$$

$$(\beta_0 + 12\beta_1 + \beta_4 + 3\beta_5) + \beta_2 \text{ logssal} - (\beta_0 + 11\beta_1 + \beta_3 + 3\beta_5) - \beta_2 \text{ logssal} = \beta_1 + \beta_4 - \beta_3 = 0$$

So the restriction that follows from the null hypothesis is that $\beta_1 + \beta_4 = \beta_3$. The negation of this statement is that $\beta_1 + \beta_4 \neq \beta_3$ which is the alternative hypothesis, where the average `logsal` of population A is not equal to that of population B.

Section iv Under the null hypothesis, $\beta_1 + \beta_4 = \beta_3$. So, rearranging to get $\beta_1 = \beta_3 - \beta_4$ we can substitute this into our unrestricted model (the population model):

$$\mathbb{E}[\text{logsal} | \text{educ}, \text{logssal}, \text{gender}, \text{race}, \text{jobcat}] = \beta_0 + \beta_1 \text{ educ} + \beta_2 \text{ logssal} + \beta_3 \text{ gender} + \beta_4 \text{ race} + \beta_5 \text{ jobcat}$$

to get:

$$\begin{aligned}&\beta_0 + (\beta_3 - \beta_4) \text{ educ} + \beta_2 \text{ logssal} + \beta_3 \text{ gender} + \beta_4 \text{ race} + \beta_5 \text{ jobcat} \\ &= \beta_0 + \beta_3 \text{ educ} - \beta_4 \text{ educ} + \beta_2 \text{ logssal} + \beta_3 \text{ gender} + \beta_4 \text{ race} + \beta_5 \text{ jobcat} \\ &= \beta_0 + \beta_2(\text{educ} + \text{logssal}) + \beta_3 \text{ gender} + \beta_4(\text{race} - \text{educ}) + \beta_5 \text{ jobcat}\end{aligned}$$

let $U = \text{educ} + \text{logssal}$ and $V = \text{race} - \text{educ}$, so

$$\beta_0 + \beta_2 U + \beta_3 \text{ gender} + \beta_4 V + \beta_5 \text{ jobcat}$$

This expression is our restricted model. We will use these two models for our F-test when we come to test the null hypothesis that $\beta_1 + \beta_4 = \beta_3$ (tantamount to holding that the two populations A and B have the same `logsal`) against the alternative hypothesis that $\beta_1 + \beta_4 \neq \beta_3$ (that the two populations A and B do not have the same average `logsal`).

Section v

```

## 
## Call:
## lm(formula = logsal ~ U + gender + V + jobcat, data = dat)
## 
## Residuals:
##      Min    1Q   Median    3Q   Max 
## -0.46457 -0.12666 -0.01398  0.12058  0.85875 
## 
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 8.28172   0.16386  50.541 < 2e-16 ***
## U          -0.12024   0.01994  -6.029 3.34e-09 ***
## gender      0.16001   0.01916   8.353 7.57e-16 ***
## V          -0.16023   0.01860  -8.615 < 2e-16 *** 
## jobcat      0.22745   0.01459  15.595 < 2e-16 *** 
## --- 
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## 
## Residual standard error: 0.1893 on 469 degrees of freedom
## Multiple R-squared:  0.7749, Adjusted R-squared:  0.773 
## F-statistic: 403.6 on 4 and 469 DF, p-value: < 2.2e-16

```

So our restricted model is:

$$\widehat{\text{logsal}} = 8.282 - 0.120U + 0.160 \text{gender} - 0.160V + 0.227 \text{jobcat}$$

Section vi

$$H_0 : \beta_3 = \beta_4 = 0$$

$$H_1 : \exists_{i \in \{3,4\}} \beta_i \neq 0$$

Significant Level : $\alpha = 0.1$

Test statistic and null distribution : $\frac{(SSR_R - SSR_{UR})}{SSR_{UR}} \frac{(n - k - 1)}{q} \sim F(q, n - k - 1) = F(2, 468)$

$$t_{calc} = 137.8538771$$

$$F_{crit} = 3.8614052$$

Decision rule : reject H_0 if $t_{calc} > F_{crit}$

Decision : Since $137.8538771 > 3.8614052$, reject H_0

In conclusion, at 0.05 level of significance, we reject the null hypothesis that the average of the `logsalary` for population A is the same population B in favour of the alternative hypothesis that they are not equal. In other words, there is a difference between an individual who is female, a manager, with 12 years of education, belongs to an ethnic minority, and has a starting salary *and* an individual who is male, a manager, has 11 years of education, is not an member of a ethnic minority, and also has a starting salary.

Part G

Section i By definition, the racial pay gap for males is:

$$\mathbb{E}[\text{logsal} | \text{gender} = 1, \text{race} = 1, \text{educ}, \text{logssal}, \text{jobcat}] - \mathbb{E}[\text{logsal} | \text{gender} = 1, \text{race} = 0, \text{educ}, \text{logssal}, \text{jobcat}]$$

Given

$$\mathbb{E}[\logsal | \text{educ}, \logssal, \text{gender}, \text{race}, \text{jobcat}] = \beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_3 \text{gender} + \beta_4 \text{race} + \beta_5 \text{jobcat}$$

it follows that:

$$\begin{aligned} \mathbb{E}[\logsal | \text{gender} = 1, \text{race} = 1, \text{educ}, \logssal, \text{jobcat}] - \mathbb{E}[\logsal | \text{gender} = 1, \text{race} = 0, \text{educ}, \logssal, \text{jobcat}] \\ = \beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_3 + \beta_4 + \beta_5 \text{jobcat} - (\beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_3 + \beta_5 \text{jobcat}) \\ = \beta_4 \end{aligned}$$

So the racial pay gap for males is β_4 .

Section ii By definition, the racial pay gap for females is:

$$\mathbb{E}[\logsal | \text{gender} = 0, \text{race} = 1, \text{educ}, \logssal, \text{jobcat}] - \mathbb{E}[\logsal | \text{gender} = 0, \text{race} = 0, \text{educ}, \logssal, \text{jobcat}]$$

Given

$$\mathbb{E}[\logsal | \text{educ}, \logssal, \text{gender}, \text{race}, \text{jobcat}] = \beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_3 \text{gender} + \beta_4 \text{race} + \beta_5 \text{jobcat}$$

it follows that:

$$\begin{aligned} \mathbb{E}[\logsal | \text{gender} = 0, \text{race} = 1, \text{educ}, \logssal, \text{jobcat}] - \mathbb{E}[\logsal | \text{gender} = 0, \text{race} = 0, \text{educ}, \logssal, \text{jobcat}] \\ = \beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_4 + \beta_5 \text{jobcat} - (\beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_5 \text{jobcat}) \\ = \beta_4 \end{aligned}$$

So the racial pay gap for females is also β_4 .

These results make sense, for another interpretation of β_4 is the partial effect of being in an ethnic minority on the log of an individual's starting salary against not being in an ethnic minority, that is, holding all else constant. Hence, whether or not we are looking at male or female racial pay gap is already accounted for in this model by β_4 .

Part H

Section i To allow in our model for the racial pay gap to vary by gender, we may introduce the interaction term $\text{race} \times \text{gender}$, allowing race to vary as a function of gender . Thus,

$$\mathbb{E}[\logsal | \text{educ}, \logssal, \text{gender}, \text{race}, \text{jobcat}] = \beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_3 \text{gender} + \beta_4 \text{race} + \beta_5 \text{jobcat} + \beta_6 \text{race} \times \text{gender}$$

Section ii

The racial pay gap for males, controlling for education, starting salary, and job category is:

$$\mathbb{E}[\logsal | \text{gender} = 1, \text{race} = 1, \text{educ}, \logssal, \text{jobcat}] - \mathbb{E}[\logsal | \text{gender} = 1, \text{race} = 0, \text{educ}, \logssal, \text{jobcat}]$$

According to our new model, this is

$$\begin{aligned} \mathbb{E}[\logsal | \text{gender} = 1, \text{race} = 1, \text{educ}, \logssal, \text{jobcat}] - \mathbb{E}[\logsal | \text{gender} = 1, \text{race} = 0, \text{educ}, \logssal, \text{jobcat}] \\ = \beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_3 + \beta_4 + \beta_5 \text{jobcat} + \beta_6 - (\beta_0 + \beta_1 \text{educ} + \beta_2 \logssal + \beta_3 + \beta_5 \text{jobcat}) \\ = \beta_4 + \beta_6 \end{aligned}$$

So this racial pay gap for males is equal to $\beta_4 + \beta_6$.

Section iii The racial pay gap for females, controlling for education, starting salary, and job category is:

$$\mathbb{E}[\log sal \mid gender = 0, race = 1, educ, logssal, jobcat] - \mathbb{E}[\log sal \mid gender = 0, race = 0, educ, logssal, jobcat]$$

According to our new model, this is

$$\begin{aligned}\mathbb{E}[\log sal \mid gender = 0, race = 1, educ, logssal, jobcat] - \mathbb{E}[\log sal \mid gender = 0, race = 0, educ, logssal, jobcat] \\ = \beta_0 + \beta_1 \text{educ} + \beta_2 \text{logssal} + \beta_4 + \beta_5 \text{jobcat} - (\beta_0 + \beta_1 \text{educ} + \beta_2 \text{logssal} + \beta_5 \text{jobcat}) \\ = \beta_4\end{aligned}$$

So *this* racial pay gap for females is equal to β_4 .

Section iv The null hypothesis is that, controlling for education, starting salary, and job category, the racial pay gap for males and females is the same. Hence, from part (h)ii) and part (h)iii) this statement is equivalent to the stating that $\beta_4 + \beta_6 = \beta_4$ which in other words is to say that $\beta_6 = 0$.

$$H_0 : \beta_1 = 0$$

$$H_1 : \beta_1 \neq 0$$

Significant Level : $\alpha = 0.1$

$$\text{Test statistic and null distribution : } \frac{\hat{\beta}_1}{se(\hat{\beta}_1)} \sim t_{n-k-1} = t_{467}$$

$$t_{calc} = 0.4901646$$

$$t_{crit} = 1.648123$$

Decision rule : reject H_0 if $|t_{calc}| > t_{crit}$

Decision : Since $0.4901646 > 1.648123$, reject H_0

In conclusion, at 0.10 level of significance, we reject the null hypothesis that, controlling for education, starting salary, and job category, the racial pay gap for males and females is the same in favour of the alternative hypothesis that they are not.