

# GPU Multiplication Algorithms

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Dec 14 2025

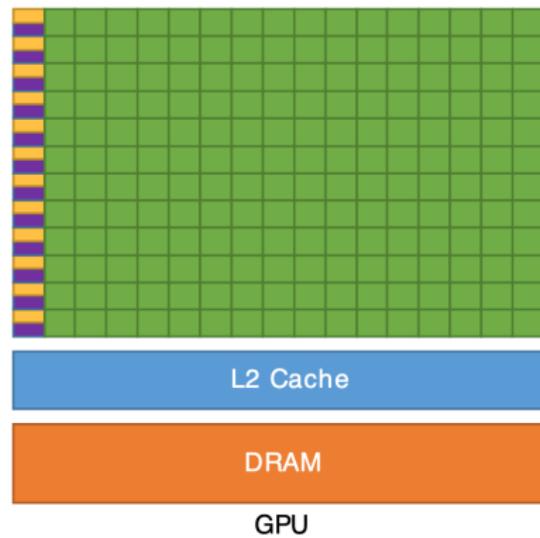
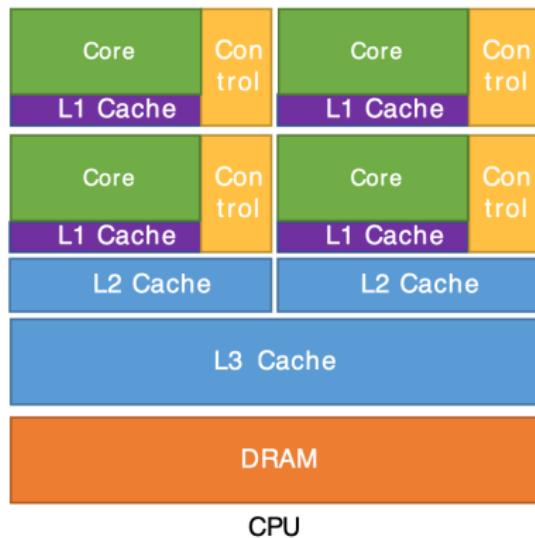


GPUs

# Why GPUs?

- Why are GPUs so expensive?
  - It turns out everyone loves to do matrix multiplication
- Why is matrix multiplication so popular?
  - Deep learning and AI are all pretty much just a bunch of matrix multiplications. Analogous: think about the closed form solution of linear regression
- How do GPUs help with matrix multiplication?
  - Matrix multiplication is a bunch of independent arithmetic
  - This can be parallelized via a GPU

# How GPUs?



# Attacking a Village

- If we are a fantasy warlord and we need to destroy all the houses in a village, should we send in our 4 trolls or our army of 100 goblins?
  - Our trolls are really strong, but there are only a few of them. They will need to destroy a house, move to the next house, destroy it, ect.
  - Our goblins are not as strong but there are a lot of them and they are quick. Each goblin can concentrate on destroying an individual house.

**IOWA**

# GPU Computation

- Units are threads, blocks, and grids
- Little green boxes/goblins are threads
  - This is the primary computational unit
- Blocks are groups of threads, can share memory
- Grids are the entire workspace
- For matrix multiplication, this maps nicely. Each thread is an element of the output matrix, the entire output matrix is the grid. Blocks are less intuitive.

## Matrix Multiplication

# By Hand Approach

- Why is this a good candidate for parallel computing?
- How does this work within the thread, block, grid structure?

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \times \begin{bmatrix} 10 & 11 \\ 20 & 21 \\ 30 & 31 \end{bmatrix}$$

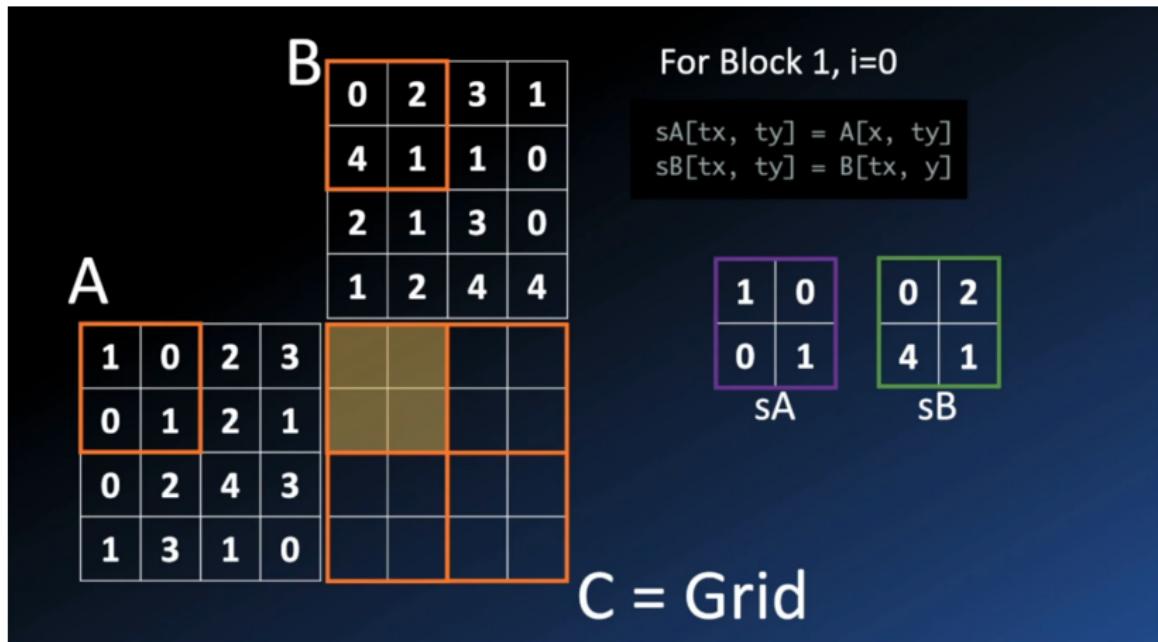
=  $\begin{bmatrix} 1x10 + 2x20 + 3x30 & 1x11 + 2x21 + 3x31 \\ 4x10 + 5x20 + 6x30 & 4x11 + 5x21 + 6x31 \end{bmatrix}$

=  $\begin{bmatrix} 10+40+90 & 11+42+93 \\ 40+100+180 & 44+105+186 \end{bmatrix} = \begin{bmatrix} 140 & 146 \\ 320 & 335 \end{bmatrix}$

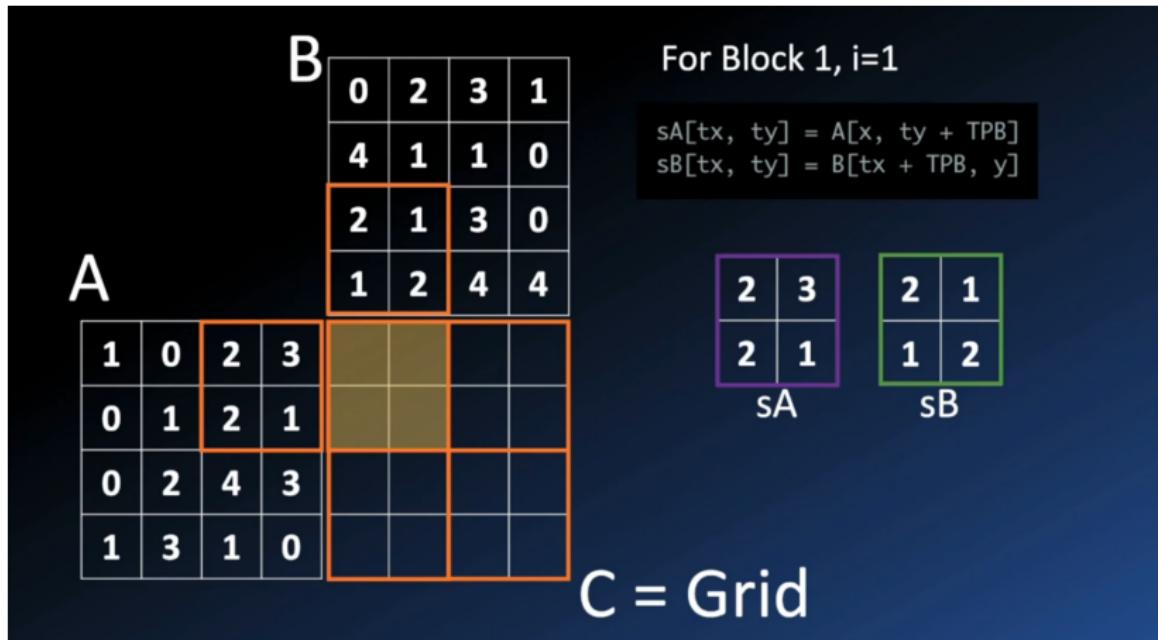
# By Hand Approach Considerations

- Perfect use of parallel computing!
- Not very memory efficient. For multiplying two 4x4 matrices, each value is loaded in 4 times
- Tile method improves on this, each value loaded just 2 times

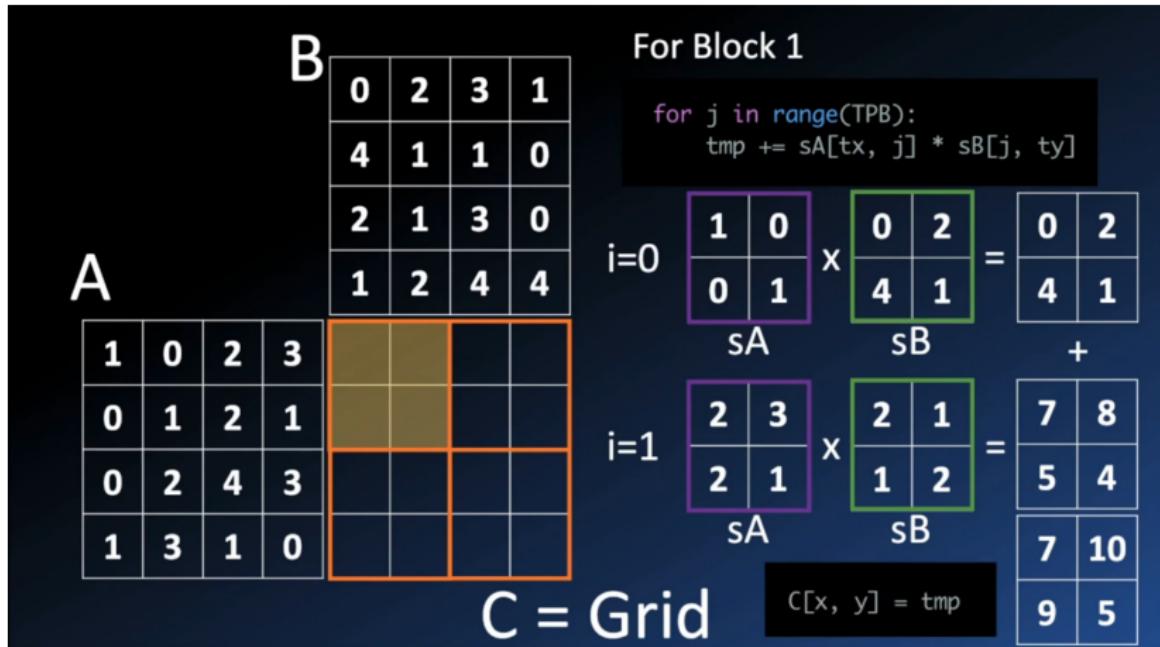
# Tiled Approach



# Tiled Approach



# Tiled Approach



## Other Approaches

- Matrix multiplication is essential and this problem has been studied a ton
- There are many, MANY complex algorithms that are much faster than these. However, these give a flavor of how complex ones work with the computational system.

# Computation

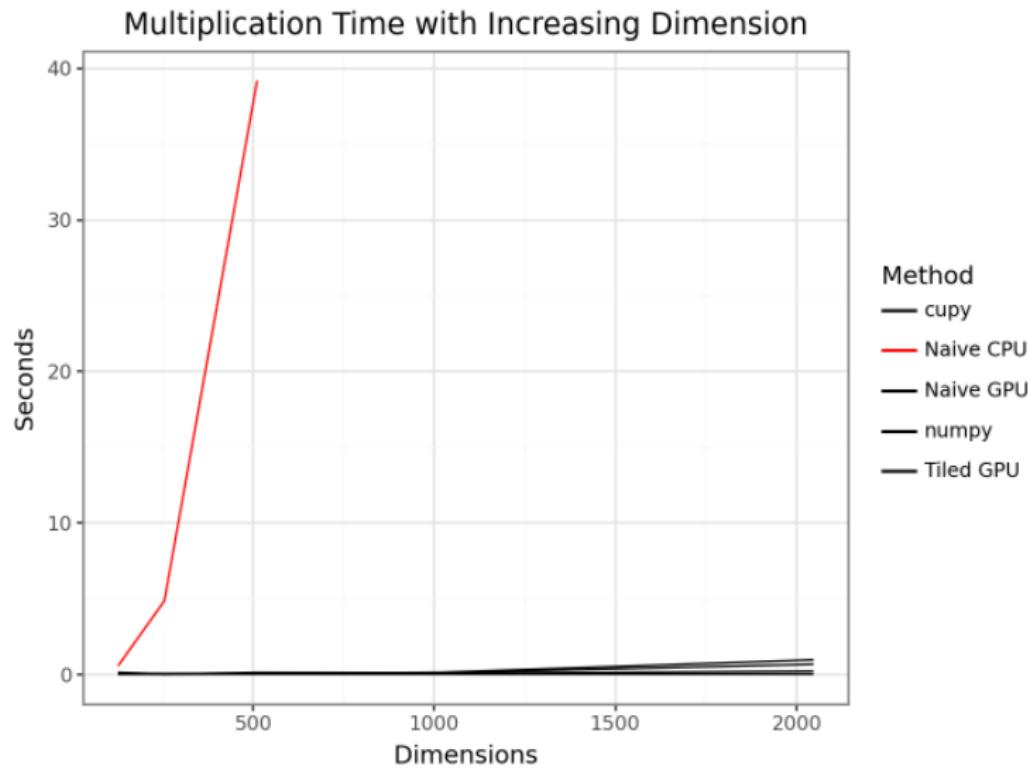
# Interfacing

- GPUs (specifically Nvidia GPUs) can be communicated with via a C-like language called CUDA
- Instructions are passed to threads in things called kernels, function-like syntax
- Most softwares have tools and extensions for interfacing with GPUs (R, python, Julia, ect)
- Good python packages: cupy and numba

# Simulation 1

- Goal: compare speed with increasing matrix dimension for the following algorithms
  - naive method on CPU
  - pre-built in method on CPU (numpy)
  - naive method on GPU
  - tiled method on GPU
  - pre-built in method on GPU (cupy)
- Square matrices of dimension 128, 256, 512, 1024, and 2048
- Threads: 16

# Simulation 1 Results



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