Lecture 2 - defects

Lecture summary

- Introduction to defects
- Types of defect
- Instrinsic and extrinsic defects
- Defect equations

Defects

All crystals contain defects of some sort, for example:

- Missing atoms (vacancies)
- Atoms in the 'wrong' place
 - interstitials (between lattice sites) or substitutions (different atom types)
- Extended defects of lines or planes of atoms

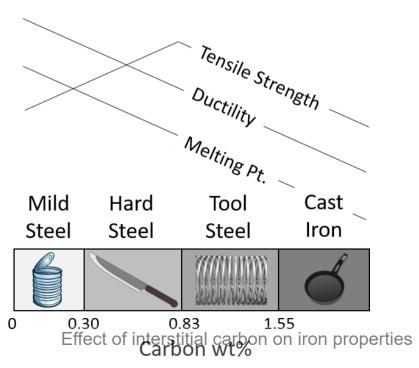
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Defects are often the source of interesting properties

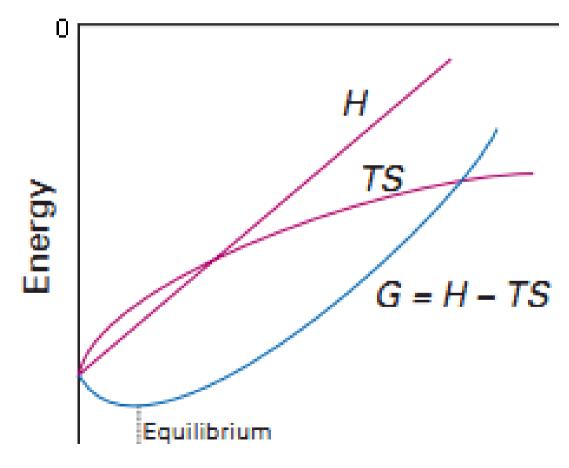




Defect amounts

The number of defects is a fine balance of entropy and enthalpy

• Defects gain entropy but have a (often large) formation energy



Types of defect

The three most common defect types in ionic solids are:

Vacancy						Interstitial								Substitution			
M	X	M	X	М	X	М	X	M	X	M	X	M	X	M	X	M	X
X	M	X	M	X	M	X	M	X	M	X	М	X	M	X	M	X	M
M	X	М	X	М	X	M	X	М	X	M	X	M	X	M	X	M	X
X	M	X		X	M	X	M	X	M	X	M	X	M	X	M	X	M
M	X	M	X	M	X	M	X	M	X	M	X	M	X	N	X	M	X
X	M	X	M	X	M	X	M	X	M	X	M	X	M	X	M	X	M
M	X	M	X	M	X	M	X	M	X	M	X	M	X	M	X	M	X
X	M	X	M	X	M	X	M	X	M	X	M	X	M	X	M	X	М

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M	X	M	X	М	X	M	X	М	X	M	X	M	X	M	X	M	X
X	М	X		X	M	X	M	X	X M	X	M	X	M	X	M	X	M
M	X	M	X	M	X	M	X	M	X	M	X	M	X	N	X	M	X
X	M	X	M	X	М	X	M	X	M	X	M	X	M	X	M	X	M
M	X	M	X	M	X	M	X	M	X	M	X	M	X	M	X	M	X
X	M	X	M	X	M	X	M	X	M	X	M	X	M	X	M	X	M

Additionally, defects can be either

- *intrinsic* (maintaining stoichiometry) or
- extrinsic (non-stoichiometric)

Intrinsic defects

Two of the most common stoichiometric defects are:

Schottky

Charge-balanced combination of anion and cation vacancies



Ions displaced to interstitial sites

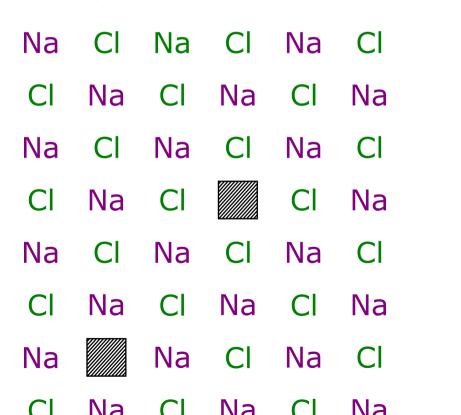
Defects observed depend on both structure type and atoms involved.

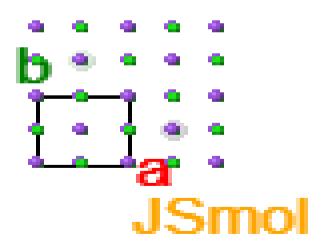




Schottky defects

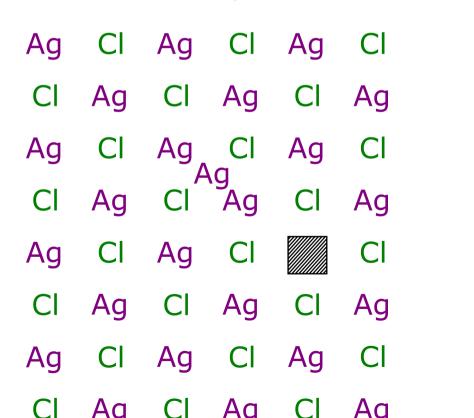
- Typically occur when anions and cations have similar size (e.g. NaCl structure)
- Reduced density compared with the ideal material
- e.g. NaCl equal numbers of Na and Cl vacancies

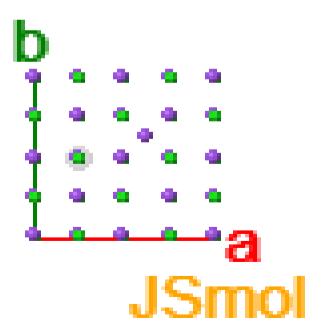




Frenkel defects

- Smaller ion normally displaced
- Only one ion type shows defect
- e.g. AgCl (NaCl-type)
 - ∘ Smaller Ag⁺ ion displaced to tetrahedral holes in CCP Cl[−] structure





Useful to write equation for defects, using **Kroger-Vink** notation:

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- \circ for 1+, •• for 2+, etc.;
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- For example:
 - \circ Na vacancy in NaCl: ${
 m V_{Na}}'$
 - Ag interstital in AgCl: Ag_i

Defect equations (2)

Defect equations must balance for:

- mass (atoms)
- charge
- sites
 - positions created/destroyed must balance

Examples

AgCl interstitial formation again:

$$\mathrm{Ag}_{\mathrm{Ag}}
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NaCl Schottky formation:

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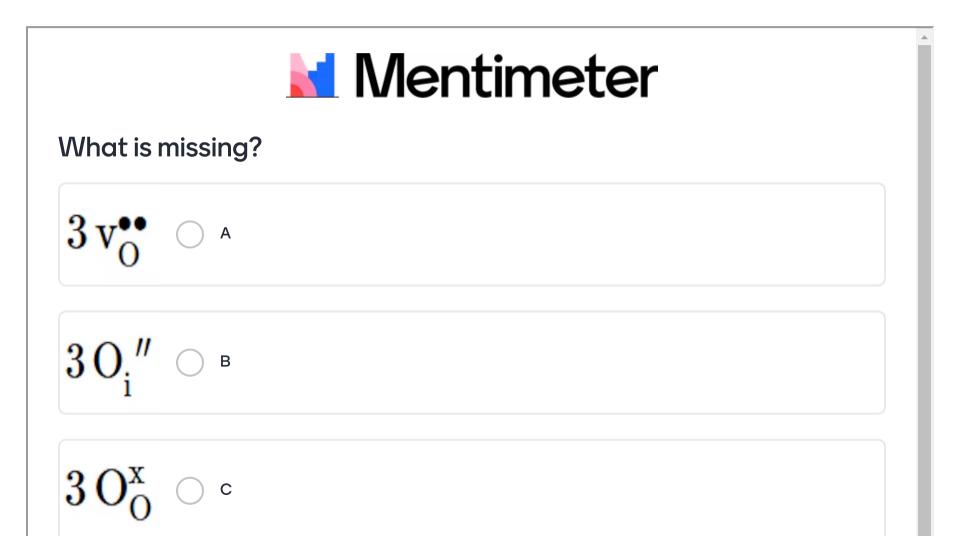
$$\mathrm{Na_{Na}} + \mathrm{Cl_{Cl}} \Longrightarrow \mathrm{V_{Na}}' + \mathrm{V_{Cl}^{ullet}} + \mathrm{NaCl}$$

Easily extended to substitutions, e.g. substituting ${\rm Al}^{3\,+}$ with ${\rm Cr}^{3\,+}$ in ${\rm Al}_2{\rm O}_3$ (ruby):

$$2\operatorname{Al}_{\operatorname{Al}}+\operatorname{Cr}_2\operatorname{O}_3 \Longrightarrow 2\operatorname{Cr}_{\operatorname{Al}}+\operatorname{Al}_2\operatorname{O}_3$$

Quick test - $BaTiO_3$ Schottky Formation

$$\mathrm{Ba_{Ba}} + \mathrm{Ti_{Ti}} + 3\,\mathrm{O_{O}} \Longrightarrow \mathrm{V_{Ba}}'' + \mathrm{V_{Ti}}'''' + ?? + \mathrm{BaTiO_{3}}$$



$$\mathrm{Ba_{Ba}} + \mathrm{Ti_{Ti}} + 3\,\mathrm{O_{O}} \rightleftharpoons \mathrm{V_{Ba}}'' + \mathrm{V_{Ti}}''' + ?? + \mathrm{BaTiO_{3}}$$

Go to www.menti.com and use the code 8133 7714

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Ionic Substitution

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- While an integer number are substituted across a crystal, the average can be non-stoichiometric
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- Substitution can dramatically affect properties:
 - \circ e.g. $La_{2-x}Sr_xCuO_4$:
 - semiconducting for x=0
 - superconducting (below 40 K) for x=0.15

Extrinsic defects

Substitution can also drive formation of defects, e.g. doping NaCl with $CaCl_2$:

Overall synthesis reaction:

$$(1-2x)\mathrm{NaCl} + x\mathrm{CaCl}_2
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Kroger-Vink notation:

More complex example

Sometimes, substitution (or 'doping') can give rise to multiple potential defects.

For example, replacing ${\rm La^3}^+$ by ${\rm Sr^2}^+$ in ${\rm LaCoO_3}$ could occur:

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For example, replacing ${\rm La^3}^+$ by ${\rm Sr^2}^+$ in ${\rm LaCoO_3}$ could occur:

by creating oxygen vacancies;

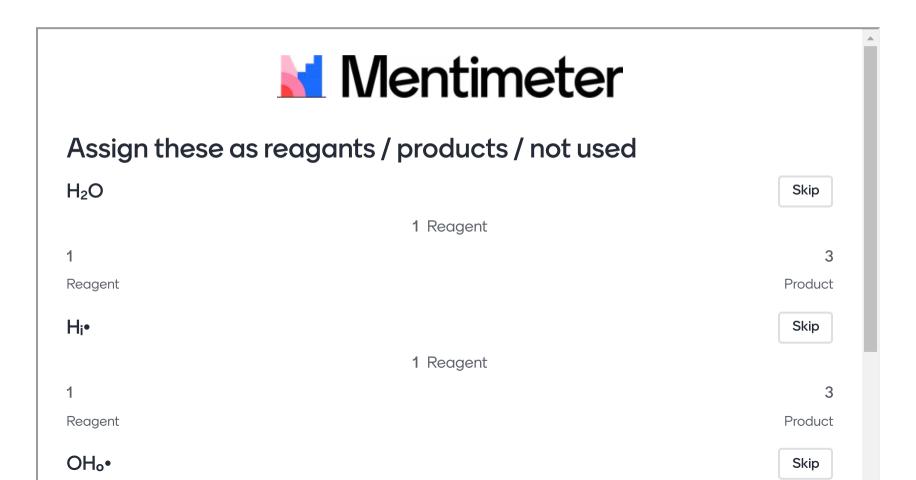
$$2\operatorname{La}_{\operatorname{La}} + 2\operatorname{SrO} + \operatorname{O_O} \Longrightarrow 2\operatorname{Sr_{\operatorname{La}}}' + \operatorname{V_O^{ullet}} + \operatorname{La_2O_3}$$

• or by oxidising $\mathrm{Co}^{3\,+}$ to $\mathrm{Co}^{4\,+}$

$$2\operatorname{La_{La}} + 2\operatorname{SrO} + \frac{1}{2}\operatorname{O_2} + 2\operatorname{Co_{Co}} \Longrightarrow 2\operatorname{Sr_{La}}' + 2\operatorname{Co_{Co}}^{\bullet} + \operatorname{La_2O_3}$$

Quiz 2 - Extrinsic defects

At high pressure, oxygen vacancies in ${
m Mg}_2{
m SiO}_4$ can react with ${
m H}_2{
m O}$ to form new defects.



Results - Extrinsic defects

Go to www.menti.com and use the code 6370 0300

Assign these as reagants / products / not used

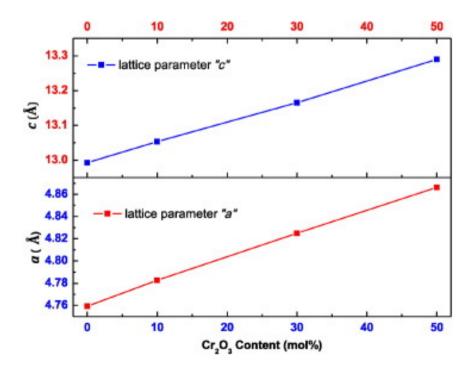


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Solid solutions

Frequently, substitutional defect concentrations can exceed 1%

- known as a 'solid solution'
- Very important for tuning properties via synthesis
- Often useful to think of the "average ion" properties at each site
 - ∘ e.g. ionic radius, resulting in *Vegard's Law*
 - Lattice parameter is weighted average of the end-members, e.g. $Al_{2-x}Cr_xO_3$:







Non-stoichiometry

Some materials are naturally non-stoichiometric even without extrinsic defects

- Very common in transition metal compounds
 - multiple oxidation states available
- Example: FeO (wustite, NaCl structure) cannot actually form stoichiometrically at ambient pressure
 - \circ Actually Fe_{1-x}O, with $0.05 \le x \le 0.15$

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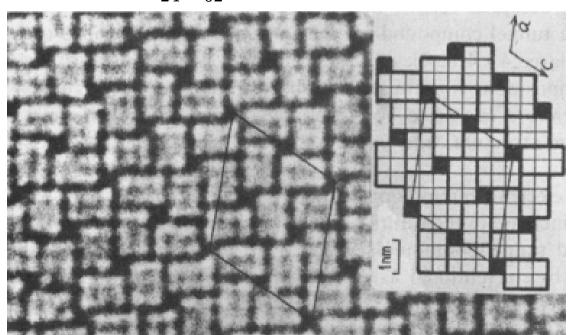
N.B. From cation:anion ratio alone you cannot determine the defect types

e.g. Fe:O ratio of 0.9 could equally be $Fe_{0.9}O$ or $FeO_{1.11}!$

Defect ordering

- At large defect concentrations, defects can interact
 - minimises enthalpy
- Can occur as
 - clusters ('0D')
 - lines ('1D')
 - ∘ planes ('2D')

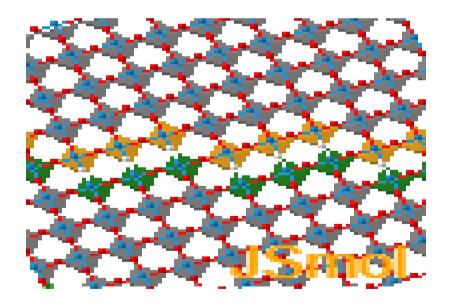
Often seen in microscopy, e.g. ${\rm ZrNb_{24}O_{62}}$ shows 2D order in two directions:



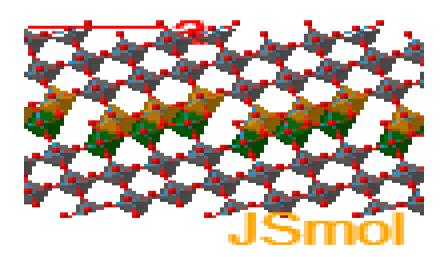
Example - WO_3

Plane-like defects often described as shear phases

 WO_3



$$\mathrm{WO}_{2.90}$$
 or $\mathrm{W}_{10}\mathrm{O}_{29}$



Lecture recap

- Crystals are never perfect!
 - defects favoured at higher temperature
- Three main types of defect:
 - vacancy (called Schottky if stoichiometry maintained)
 - interstitial (called Frenkel if stoichiometry maintained)
 - substitution
- Kroger-Vink notation is a way to write defect equations
- Some materials can form solid solutions and/or non-stoichiometric compositions
- If defects order, this can lead to new stoichiometric structure types

Feedback



What did you like or dislike about this lecture?

Short answers are recommended. You have 250 characters left.

You can submit multiple answers

250

Submit

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