

HW #2

EEU 101

Jonathan Lim
33104333

HW #2

1)

$$C = (S + N_A + N_P)A$$

(a)

$$\begin{aligned} \text{VAR}(C) &= \text{VAR}(S) + \text{VAR}(N_A) + \text{VAR}(N_P) \\ &= A^2 \text{VAR}(S) + A^2 \text{VAR}(N_A) + A^2 \text{VAR}(N_P) \\ &= A^2 + A^2 \text{mean}(S) + \text{VAR}(C) \\ &= A^2 + A^2 S = A^2(1+S) \end{aligned}$$

(b)

$$\text{Signal-to-noise} = \frac{E(C)}{\sigma(C)}$$

$$\begin{aligned} &= \frac{E(C)}{\sqrt{\text{VAR}(C)}} \\ &= \frac{AE(S) + AE(N_A) + AE(N_P)}{A\sqrt{1+S}} \\ &= \frac{E(S) + 0 + E(N_P)}{\sqrt{1+S}} \quad \text{problem} \\ &= \frac{S + \text{VAR}(N_P)}{\sqrt{1+S}} \\ &= \frac{S + E(S + \text{VAR}(N_P))}{\sqrt{1+S}} \\ &= \frac{2S}{\sqrt{1+S}} \end{aligned}$$

(c)

$$\begin{aligned} \frac{2S}{\sqrt{1+S}} &> 100 \\ \Rightarrow \frac{4S^2}{1+S} > 100 &\Rightarrow \frac{4S_{\text{min}}^2}{1+S_{\text{min}}} = 10000 \end{aligned}$$

$$2) \quad S_{\text{min}} - 2\text{VAR}(S_{\text{min}}) - 2\text{VAR} = 0$$

$$2) \quad \boxed{S_{\text{min}} = 2501}$$

$$\frac{1}{z'} + \frac{1}{z} = \frac{1}{f} \quad f = 0.04 \text{ m}, d = 0.02 \text{ m}$$

$$\frac{b}{d} = \frac{|z' - z|}{z'}$$

$$\frac{1}{z'} + \frac{1}{z} = \frac{1}{f} \Rightarrow \frac{1}{0.06} + \frac{1}{z} = \frac{1}{0.04}$$

$$\Rightarrow z = \frac{1}{\frac{1}{0.04} - \frac{1}{0.06}} = \boxed{0.12 \text{ m}}$$



$$\text{size of one potential well} = \frac{0.02}{\sqrt{2}} = 0.0141 \text{ cm}$$

$$\frac{b}{d} = \frac{0.004}{d} \Rightarrow b = 0.004 \text{ cm}$$

$$\frac{b}{d} = \frac{|z' - z|}{z'} \Rightarrow \frac{b}{d} = \frac{z' - z}{z'} = 1 - \frac{z}{z'}$$

$$\Rightarrow \frac{z}{z'} = \frac{1 - \frac{b}{d}}{1} = \frac{1 - 0.004}{1} = 0.996$$

$$\frac{1}{z'} + \frac{1}{-z} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{6.006} + \frac{1}{-z} = \frac{1}{4}$$

$$\Rightarrow \bar{z} = \frac{1}{\frac{1}{6.006} - \frac{1}{4}} = -11.976 \text{ cm}$$

$$|z - \bar{z}| = |-12 - (-11.976)| = \boxed{0.024 \text{ cm}}$$

3)

$$D = (I + N_A + N_P)A + N_Q$$

$$\text{VAR}(N_A) = \sigma_A^2$$

$$\text{VAR}(N_P) = S$$

$$\text{VAR}(N_Q) = \sigma_Q^2$$

(a)

$$E(D) = AE(I) + \cancel{AE(N_A)}^0 + \cancel{AE(N_P)}^0 + \cancel{AE(N_Q)}^0$$

$$= \boxed{AS}$$

$$\text{VAR}(D) = A^2 \cancel{\text{VAR}(I)}^0 + A^2 \text{VAR}(N_A) + A^2 \text{VAR}(N_P) + \text{VAR}(N_Q)$$

$$= A^2 \sigma_A^2 + AS + \sigma_Q^2$$

$$= \boxed{AE(D) + \underbrace{A^2 \sigma_A^2 + \sigma_Q^2}_{\sigma_D^2}}$$

(b) Separate paper.

(c) Separate paper.

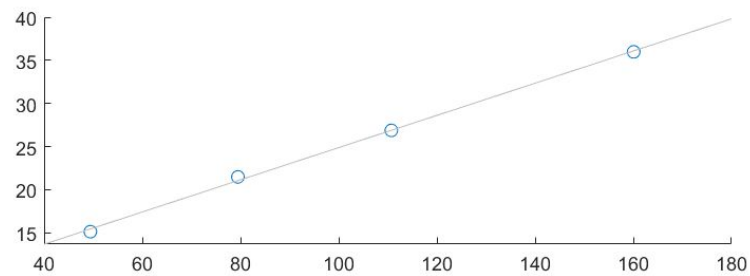
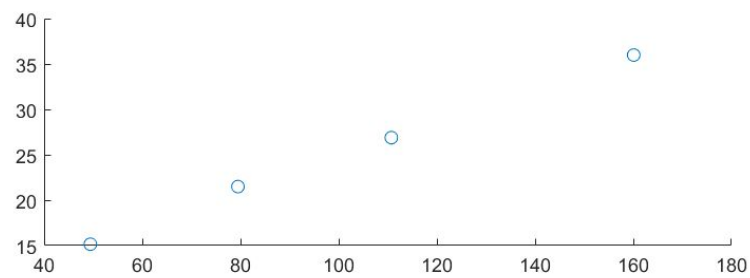
3.

Part b:

```
Select C:\Users\jcylin\Documents\Visual Studio 2017\EECS 101\HW2\Debug\HW2.exe
image1.raw: 49.422600 15.144367
image2.raw: 79.478500 21.492956
image3.raw: 110.721100 26.886707
image4.raw: 160.079193 35.986778
Press any key to exit: █
```

Part c:

This part was done on MATLAB, and the estimated A is .1866 and σ_C^2 is 6.2344.



```
>> hw2

A =

    0.1866

variance_of_C =

    6.2344
```