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[Code](#)[Issues](#) 0[Pull requests](#) 0[Projects](#) 0[Pulse](#)[Graphs](#)

Branch: master ▾

[ctf-writeup](#) / [Crypto](#) / [\[picoCTF 2017\] - Weird RSA - 90](#) / [kapi-note.md](#)[Find file](#)[Copy path](#)

zionspike add weir RSA

0b5fa52 14 days ago

1 contributor

122 lines (99 sloc) 3.68 KB

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Weird RSA - 90

Problem:

red some data. It was labeled as RSA, but what in the world are "dq" and "dp"? Can you decrypt the ciphertext for us?



This is the data file they gave us: [RSA.txt](#)

The challenge said about **dp** and **dq** in RSA so we googled them and we found dp and dq related to [Chinese Remainder Theorem to RSA](#).

By implementing Chinese remainder algorithm

1. p and q are the primes
2. $dp = d \bmod (p - 1)$
3. $dq = d \bmod (q - 1)$
4. $Qinv = 1/q \bmod p$ This is not integer division but multiplicative inverse
5. $m1 = pow(c, dp, p)$
6. $m2 = pow(c, dq, q)$ $h = Qinv(m1 - m2) \bmod p$; if $m1 < m2$ $h = Qinv * (m1 + q/p)$
7. $m = m2 + hq$

We implement the algorithm and solve the problem.

```
import binascii
import struct

# return (g, x, y) a*x + b*y = gcd(x, y)
def egcd(a, b):
    if a == 0:
        return (b, 0, 1)
    else:
        g, x, y = egcd(b % a, a)
        return (g, y - (b // a) * x, x)

def decryptRSA(p, q, e, ct):
    # compute n
    n = p * q
    phi = (p - 1) * (q - 1)
    gcd, a, b = egcd(e, phi)
    d = a
    print "d: " + str(d)
    pt = pow(ct, d, n)
    return pt

def encryptRSA(p, q, e, pt):
    # compute n
    n = p * q
    phi = (p - 1) * (q - 1)
```

```

gcd, a, b = egcd(e, phi)
d = a
print "d: " + str(d)
ct = pow(pt, e, n)
return ct

def convert(int_value):
    encoded = format(int_value, 'x')
    length = len(encoded)
    encoded = encoded.zfill(length+length%2)
    return encoded.decode('hex')

# x = mulinv(b) mod n, (x * b) % n == 1
def mulinv(b, n):
    g, x, _ = egcd(b, n)
    if g == 1:
        return x % n

def main():
    # By implementing Chinese remainder algorithm
    # 1) p and q are the primes
    # 2) dp = d mod (p - 1)
    # 3) dq = d mod (q - 1)
    # 4) Qinv = 1/q mod p *This is not integer division but multiplicative inverse
    # 5) m1 = pow(c, dp, p)
    # 6) m2 = pow(c, dq, q)
    # 7-1) h = Qinv(m1 - m2) mod p ; if m1 < m2
    # 7-2) h = Qinv * (m1 + q/p)
    # 8) m = m2 + hq

    # m = 65
    # p = 61
    # q = 53
    # dp = 53
    # dq = 49
    # c = 2790

    p = 113874805849098549851253358482403842266539299427577563844893812422061571979865552439953351583287819703106
    q = 12972228752180865474258189614772579151055157059822837268518335080796004605424792679720502168386046497428
    dp = 8191957726161118808660282299501667422241476531368942480886782445488150867448106567655298762846228298844
    dq = 35706957575801480933702426085061914647564259547039302369245830658117305489322705955680883724418095359176
    c = 952727959864751895055189802511370035092926211401663838878548538637206924202041424484240748346571493268535

    Qinv = mulinv(q,p)
    print "Qinv: " + str(Qinv)

    m1 = pow(c, dp, p)
    print "m1: " + str(m1)

    m2 = pow(c, dq, q)
    print "m2: " + str(m2)

    h = (Qinv * (m1 - m2)) % p
    print "h: " + str(h)

    m = m2 + (h*q)
    print "m: " + str(int(m))

    hexadecimals = str(hex(m))[2:-1]
    print "solved: " + str(binascii.unhexlify(hexadecimals))
    # solved: Theres_more_than_one_way_to_RSA

if __name__ == "__main__":
    main()

# http://crypto.stackexchange.com/questions/19413/what-are-dp-and-dq-in-encryption-by-rsa-in-c
# https://en.wikipedia.org/wiki/RSA_(cryptosystem)#Using_the_Chinese_remainder_algorithm
# https://zzundel.blogspot.com/2011/02/rsa-implementation-using-python.html

```

The flag was:

- flag{Theres_more_than_one_way_to_RSA}