


# An Introduction to Network Analysis



A **network** is  
made up of a  
set of objects  
and their  
connections.

# EXAMPLES OF NETWORKS

- Friend network

Objects: friends

Connections: friendships

- Twitter

Objects: Twitter users

Connections: who follows who

- International trade

Objects: countries

Connections: international exchanges of goods

- Citation network

Objects: articles

Connections: citations

- Infectious disease networks

Objects: people

Connections: infections

- Neural networks in the brain

Objects: neurons

Connections: synapses

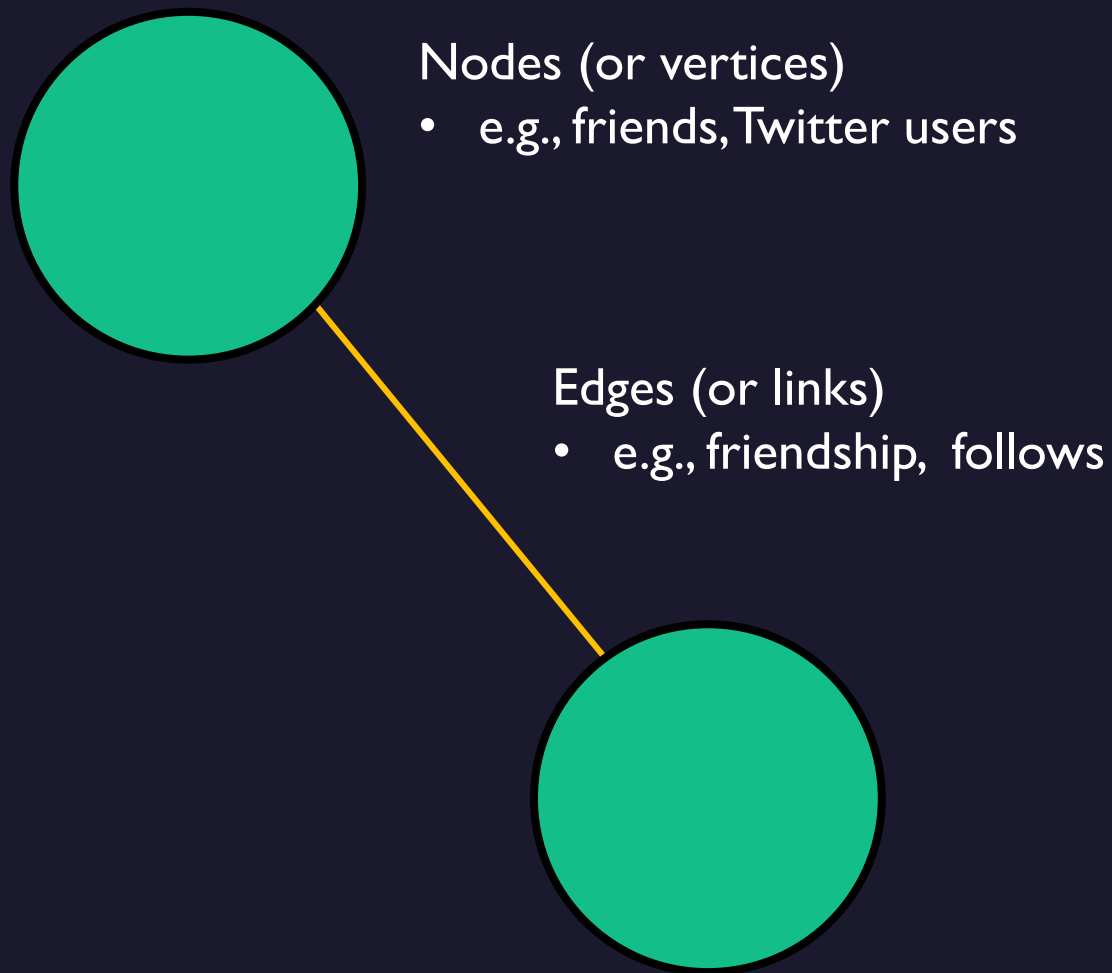




# Network Analysis

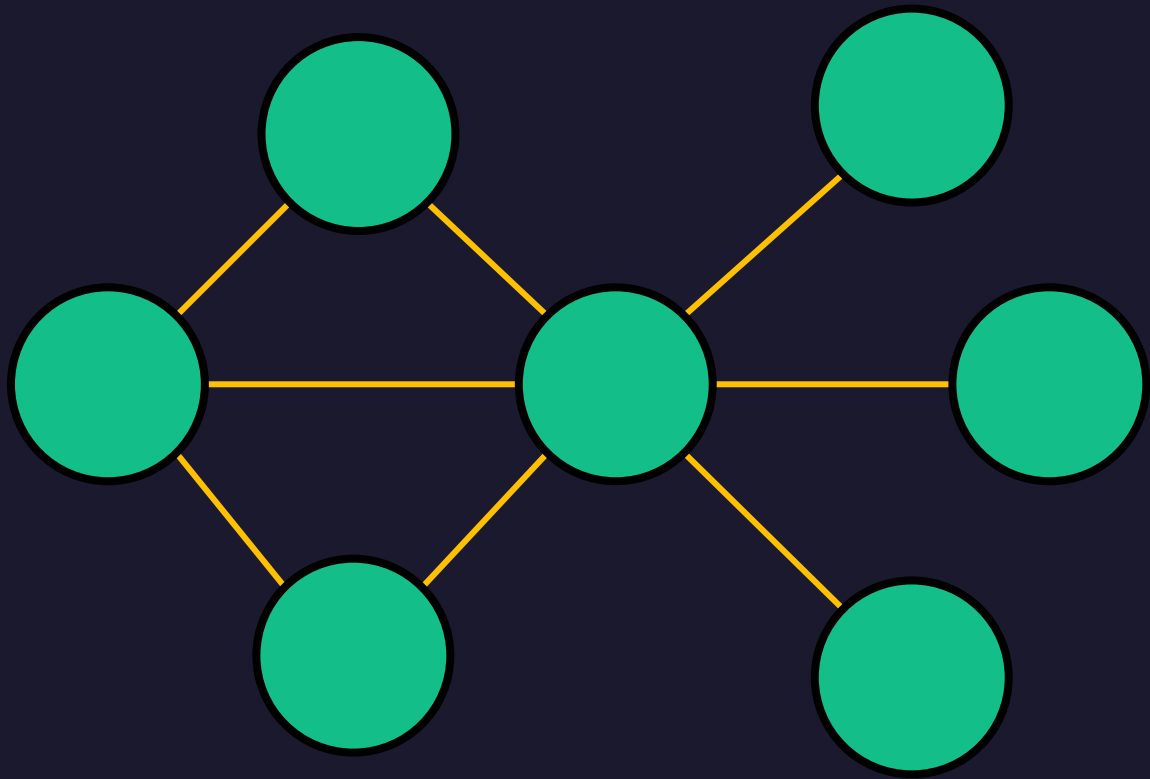
**Network analysis** is a tool for representing the relationships between objects in a network.

# A Basic Network



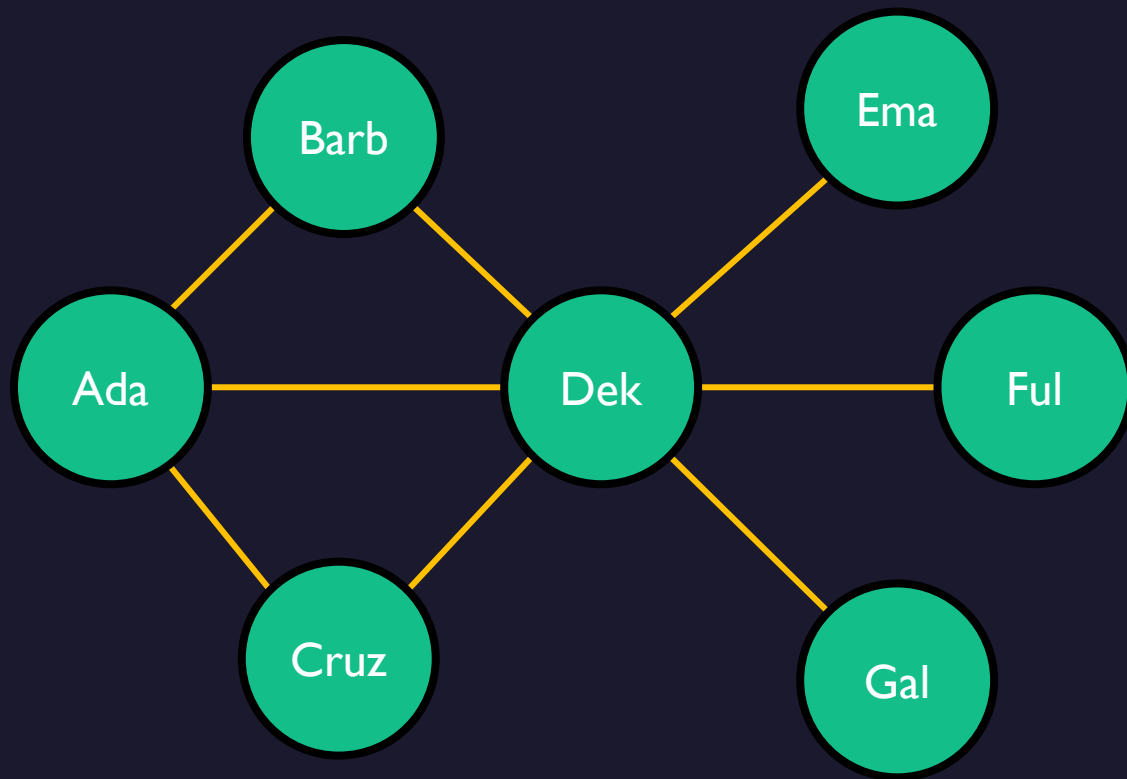
The researcher decides what **objects**, and what nature of **relationship** between objects, they want to represent in their network.

# Networks can get much more complex



Network analysis provides a **simplification** of a complex, real-world phenomenon.

# Lists for describing networks



## Node List

Ada

Barb

Cruz

Dek

Ema

Ful

Gal

## Edge List

(Ada, Barb)

(Ada, Cruz)

(Ada, Dek)

(Barb, Dek)

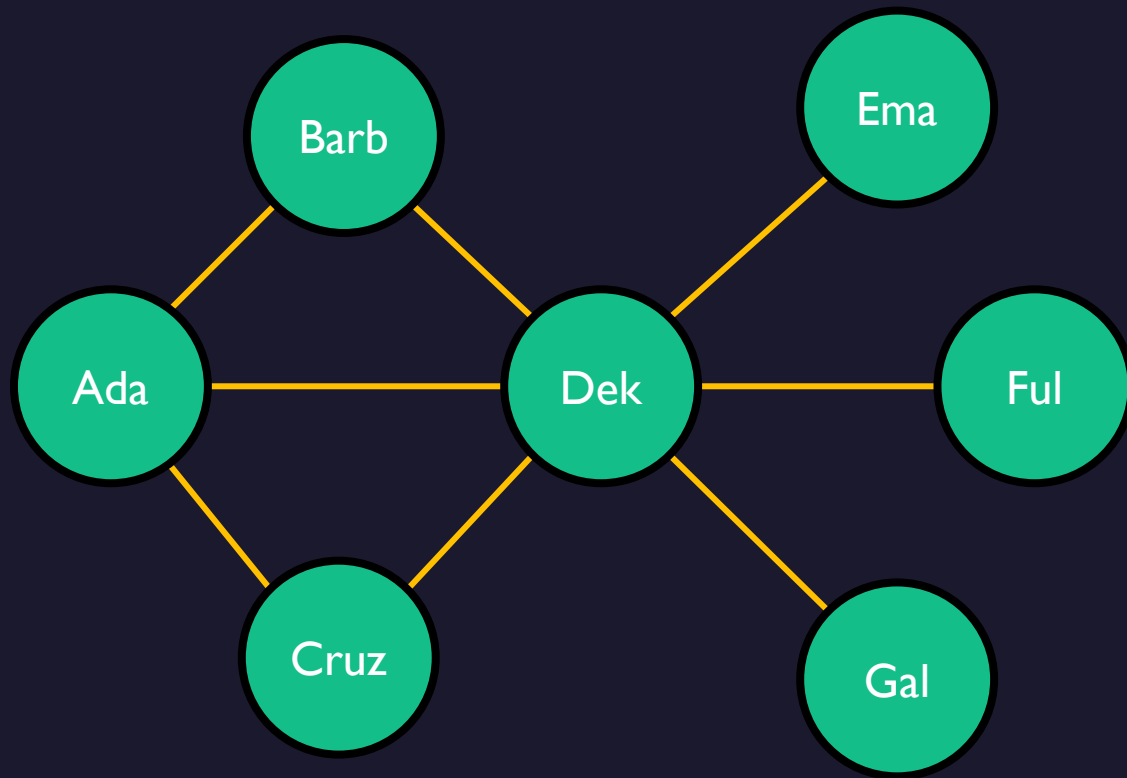
(Cruz, Dek)

(Dek, Ema)

(Dek, Ful)

(Dek, Gal)

# Adjacency Matrix



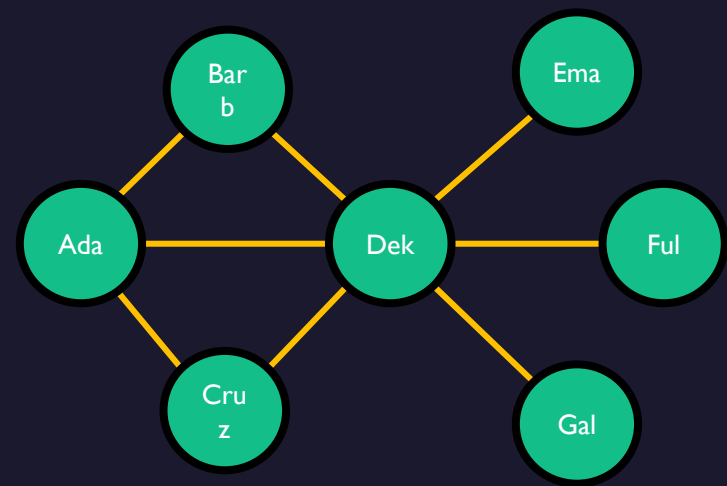
Adjacency Matrix

	Ada	Barb	Cruz	Dek	Ema	Ful	Gal
Ada	0	1	1	1	0	0	0
Barb	1	0	0	1	0	0	0
Cruz	1	0	0	1	0	0	0
Dek	1	1	1	0	1	1	1
Ema	0	0	0	1	0	0	0
Ful	0	0	0	1	0	0	0
Gal	0	0	0	1	0	0	0



# Directed vs Undirected Networks

Undirected Network



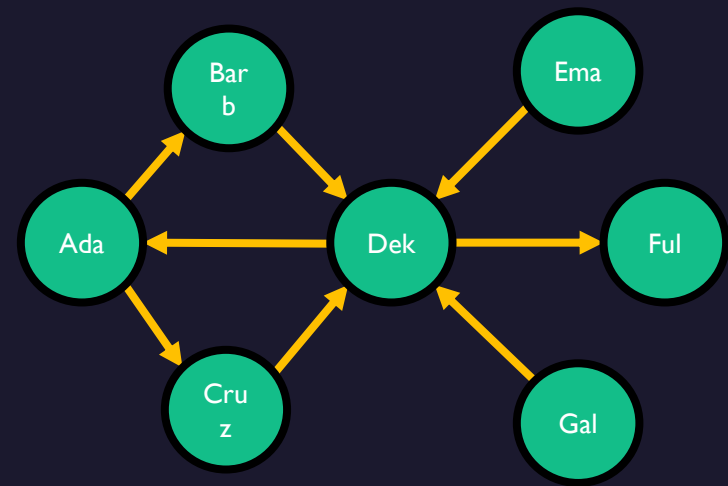
Edge List

(Ada, Barb)  
(Ada, Cruz)  
(Ada, Dek)  
(Barb, Dek)  
(Cruz, Dek)  
(Dek, Ema)  
(Dek, Ful)  
(Dek, Gal)

Adjacency Matrix

	Ada	Barb	Cruz	Dek	Ema	Ful	Gal
Ada	0	1	1	1	0	0	0
Barb	1	0	0	1	0	0	0
Cruz	1	0	0	1	0	0	0
Dek	1	1	1	0	1	1	1
Ema	0	0	0	1	0	0	0
Ful	0	0	0	1	0	0	0
Gal	0	0	0	1	0	0	0

Directed Network



(Ada, Barb)  
(Ada, Cruz)  
(Barb, Dek)  
(Cruz, Dek)  
(Dek, Ada)  
(Dek, Ful)  
(Ema, Dek)  
(Gal, Dek)

	Ada	Barb	Cruz	Dek	Ema	Ful	Gal
Ada	0	1	1	0	0	0	0
Barb	0	0	0	1	0	0	0
Cruz	0	0	0	1	0	0	0
Dek	1	0	0	0	0	1	0
Ema	0	0	0	1	0	0	0
Ful	0	0	0	0	0	0	0
Gal	0	0	0	1	0	0	0

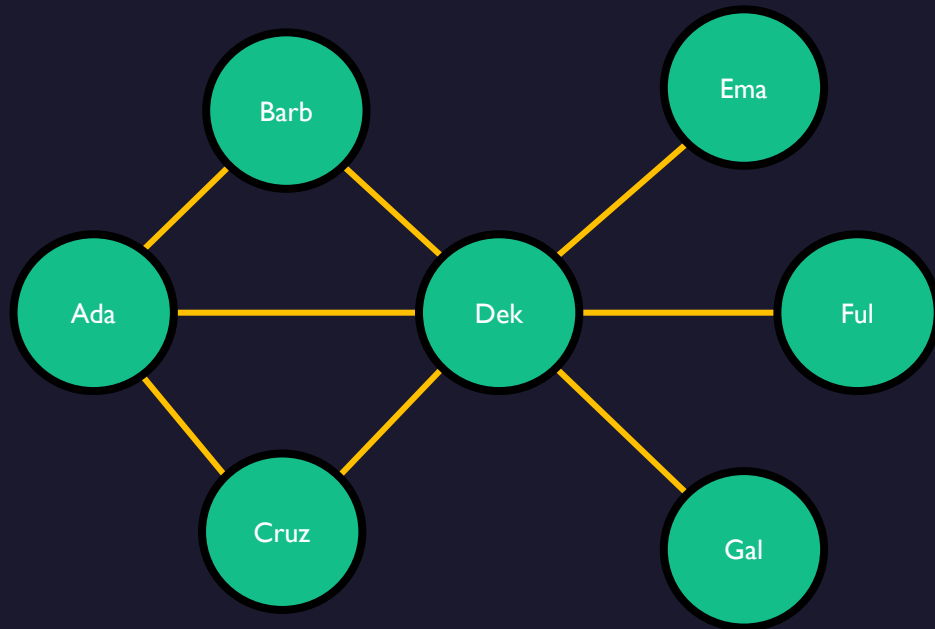
# Assessing Centrality

One aspect of networks that researchers may be interested in is which actors are most \*central\* to the network.



# Degree Centrality

Determining centrality based on how many connections a node has to other nodes  
+ A node's 'degree' is the number of edges connected to it

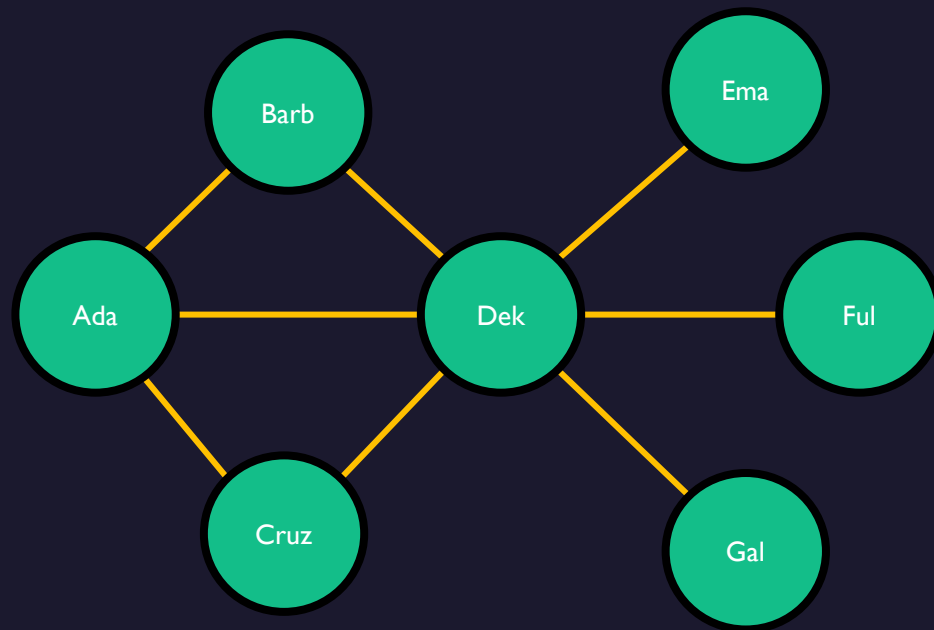


<u>Node List</u>	<u>Degree</u>
Ada	3
Barb	2
Cruz	2
Dek	6
Ema	1
Ful	1
Gal	1

# Eigenvector Centrality

Determining centrality based on how many connections a node's neighbor has

- + Requires some complex matrix calculations
- + Higher values indicate greater centrality

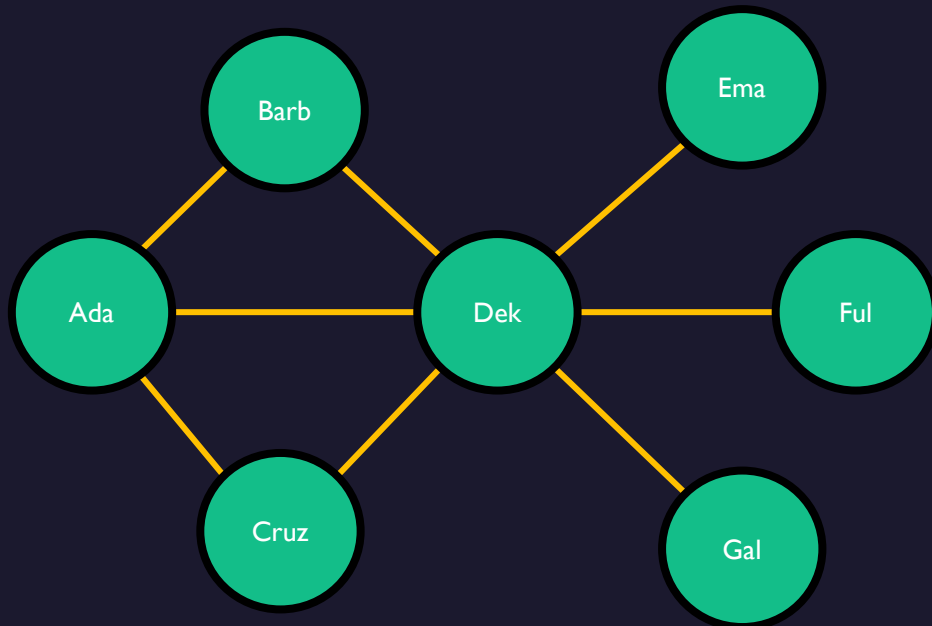


<u>Node List</u>	<u>Eigenvector Centrality</u>
Ada	0.46
Barb	0.37
Cruz	0.37
Dek	0.62
Ema	0.21
Ful	0.21
Gal	0.21

# Betweenness Centrality

Determining centrality based on how many direct connections between other nodes a node is involved in

+ To calculate, look at each pair of nodes and calculate the number of times another node can interrupt the path between them



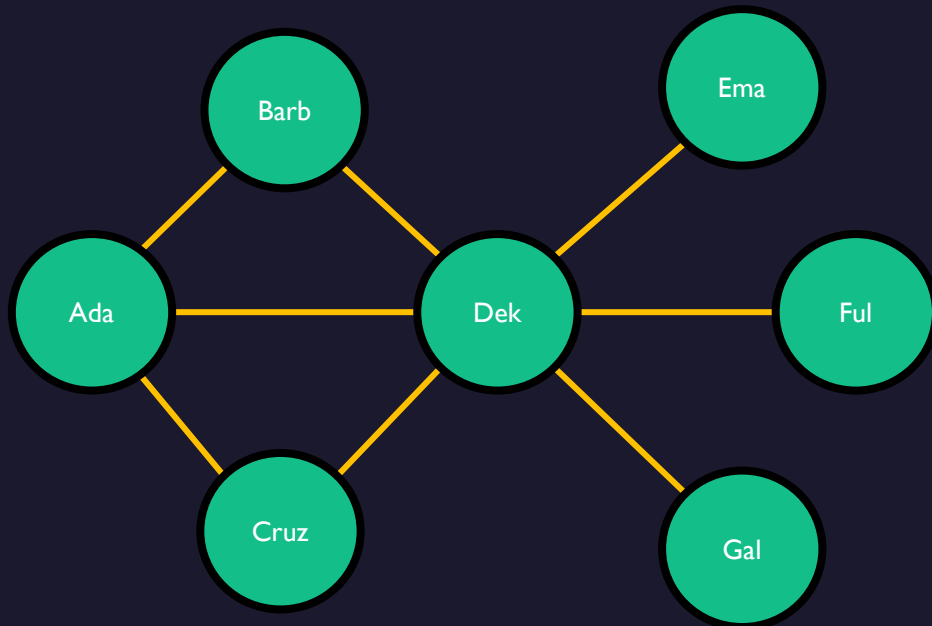
<u>Node List</u>	<u>Betweenness Centrality</u>
Ada	2
Barb	0
Cruz	0
Dek	18
Ema	0
Ful	0
Gal	0

\*Note: The calculation in R is slightly more complicated and provided in the .rmd file.

# Closeness Centrality

Determining centrality based on the average distance between a node and all other nodes

+ Calculate by taking the average of the shortest path length from a particular node to every other node, and then take the inverse



<u>Node List</u>	<u>Closeness Centrality</u>
Ada	$1 / (1+1+1+2+2+2)/6 = .67$
Barb	$1 / (1+2+1+2+2+2)/6 = .6$
Cruz	$1 / (1+2+1+2+2+2)/6 = .6$
Dek	$1 / (1+1+1+1+1+1)/6 = 1$
Ema	$1 / (2+2+2+1+2+2)/6 = .55$
Ful	$1 / (2+2+2+1+2+2)/6 = .55$
Gal	$1 / (2+2+2+1+2+2)/6 = .55$

\*Note: In R, these closeness values are multiplied by  $1/(n-1)$  to standardize the maximum possible value.



# Describing Communities

**Network Density:** a measure of how “dense” the network is, calculated by dividing the number of edges in the network by the total number of possible edges

**Clustering:** a measure of which nodes tend to cluster together, calculated using different algorithms (e.g., Louvain)

**Transitivity:** also called the “clustering coefficient”; a measure of the probability that each node in a network will be connected to adjacent nodes

