# Co-occurrence Code Documentation

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# August 17, 2017

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# 1 co\_occ\_funs.py

Module of python functions used in the rest of the project.

#### 1.1 both\_occ

Function that counts the number of times both r1 and r2 are within a range, and then returns the fraction of times this occurs. The range is half open: (a, b].

- Input:
  - r1, r2 numpy arrays
- Optional input:
  - 1bd lower bound, default 0.
  - ubd upper bound, default 1.
- Output: int count of indices i such that  $r1(i) \in (lbd, ubd]$  and  $r2(i) \in (lbd, ubd]$ .

### 1.2 both\_same\_bin

Function that counts the number of times the two occur in the same abundance range.

- Input:
  - r1, r2 numpy arrays
  - lthresh float, abundances lower are ignored.
  - numthresh number of ranges (bins) to use.
- Optional input:
  - rel bool, whether or not to normalize rows, default True.
- Output: count of indices i such that such that  $r1(i) \in (lbd_j, ubd_j]$  and  $r2(i) \in (lbd_j, ubd_j]$  for j = 0, ..., numthresh.

Divides the interval [0,1] into numthresh intervals  $(a_j,b_j]$  and calls both\_occ(r1,r2,lbd = a\_j, ubd = b\_j) for each.

## 1.3 color\_picker

Function that classifies nodes by which type of sample they have the highest abundance in. If it's a dataframe it will return the column head of the winner'

- Input:
  - r array or row of dataframe
- Optional input: none
- Output: index or column name of argmax of  $\mathbf{r}$ , if the max is greater than  $1.5 * \sigma + \mu$ , where  $\sigma$  is the sample standard deviation, and  $\mu$  is the sample mean

### 1.4 matchyn

- Input:
  - a, b scalars or list to be compared
- Optional input: none
- Output: a if a = b, otherwise ['Intertype', grey], where grey is the hex value for grey

purpose is to compare two lists that look like ['Class', color].

## 1.5 occ\_probs

Calculate probability of occurrence at an abundance level in a random graph, binomial distribution with parameters edge degree and sample degree/total edges, as in [4].

- Input:
  - abund\_array dataframe of GOTTCHA output
  - lthresh float lower bound, abundances below are ignored
  - numthresh int number of bins
- Optional input:
  - rel bool, whether or not to normalize GOTTCHA data, default True
- Output: array occ\_prob, the probability of an abundance level in a null model that assumes abundances are binomial with parameters coming from the number of taxa appearing in the sample and number of times a taxa appears.

#### 1.6 random\_coocc\_prob

Calculate a poisson-binomial...P(X > wij) where X is the number of times i and j co occur in random graph (X is a random variable) [4].

- Input:
  - occ numpy array of probabilities (output of occ\_probs)
  - wij float the abundance to test
  - i, j the indices of the taxa pair tested
- Optional input: none
- Output: float, probability that the null model produces taxa i and taxa j in the same bin more than wij times.

First gets the probability for each sample-level they are both present, then calculates a probability of the number of times this happens. Very very slow, do not use. This is because there are many ways 2 things can co-occur some number of times.

# 1.7 approx\_rand\_prob

Calculate an approximation of a poisson-binomial...P(X > wij) where X is the number of timesi and j co occur in random graph (X is a random variable) The paper [4] calls it bi-binomial because its as if you had two probabilities in the above.

- Input:
  - occ numpy array of probabilities (output of occ\_probs)
  - wij float the abundance to test
  - -i, j the indices of the taxa pair tested
- Optional input: none
- Output: float, approximate probability that the null model produces taxa i and taxa j in the same bin more than wij times.

First gets the probability for each sample-level they are both present, then calculates an approximate probability.

### 1.8 mc\_pearson

MC approximation for pearson coefficient where X is a random vector of binomial(n1,p1) and Y is a random vector of binomial(n2,p2), where p1,p2 are vectors. Expected value is identity matrix.

- Input:
  - N numpy array of of number of trials parameter for binomial RV
  - P numpy array of probabilities of success
  - W the observed correlation matrix
- Optional input:
  - num\_samps, default = 1000. Number of Monte Carlo draws
- Output: matrix giving the percentage of MC draws that had higher correlation than observed.

If n is the number of samples m the number of taxa in the network being built (number of taxa in data at given level, minus any that do not correlate with any other taxa), then N and P should be  $m \times n$  matrices. The MC draw is an  $m \times m$  matrix of "correlations" made from the null model.

#### 1.9 make\_null

Companion to mc\_pearson for palatalization

- Input:
  - N numpy array of of number of trials parameter for binomial RV
  - P numpy array of probabilities of success
  - W the observed correlation matrix
- Optional input: none
- Output: sample A binary matrix of bools (simulated correlation), observed correlation)

The null model assumes that the abundance of a taxa in a sample is binomial (n,p) where n is the number of times the taxa is seen in the real data, and p is the proportion of non-zero entries in the real data that occur in the sample. A simulated data array of abundances of taxa in sample is created. Then, the correlation matrix is computed for this. Finally, this is compared to the observed correlation matrix.

## 1.10 mc\_pearson\_thr

MC approximation for pearson coefficient where X is a random vector of binomial(n1,p1) and Y is a random vector of binomial(n2,p2), where p1,p2 are vectors. Expected value is identity.

- Input:
  - N numpy array of of number of trials parameter for binomial RV
  - P numpy array of probabilities of success
  - W the observed correlation matrix
- Optional input:
  - num\_samps, default = 1000. Number of Monte Carlo draws.
- Output: matrix giving the percentage of MC draws that had higher correlation than observed.

Same as the two above (in combination), with the only difference being that simulated data is thresholded before correlations are computed. Should compare to observed correlations of thresholded data.

### $1.11 \quad min_nz$

Find minimum non-zero value

- Input:
  - arr numpy array
- Optional input:
  - row bool, whether or not to compute minimum by row, default False.
- Output: the minimum nonzero value in a 1D array (if row is false), or an array containing the min nonzero in each of row of a 2D array

#### 1.12 build\_network

Build a cooccurrence network from a pandas dataframe. Data should all come from same taxonomic level, with columns ['LEVEL', 'TAXA', 'SAMPLE\_1',..., 'SAMPLE\_N']

- Input:
  - abundance\_array abundance array dataframe at one tax level
- Optional input:
  - cotype str, way to compute correlations, default 'pearson', options 'pearson' and 'bins'.
  - thr bool default False, whether to threshold data before computing correlations.
  - list\_too bool default True, whether or not to return an edge list as well as adjacency matrix
- Output: adjacency matrix as dataframe with index and columns taxa names. If list\_too, a dataframe of edges, each row is Node, Node, Weight.

bins counts the number of times row have the same binned value in a columns, while pearson computes a correlation matrix. Networks are filtered by the null model described in the above functions  $approx_rand_prob$ ,  $mc_pearson_thr$ . Edges are kept if p < 0.05 according to these null models. List output (result of list\_too True) is formatted for easy loading into cytoscape, using the "import network from file" option.

#### 1.13 make\_meta

Make separate node attribute table, and add edge metadata to the existing network data frame (given as list of edges). Node table needs columns for node frequency, sample most commonly seen in, and sample type color. Edges need sample type and color.

- Input:
  - edges dataframe list of Node, Node, Weight.
  - ab\_by\_sample\_type, dataframe abundance array with columns of same class (location on body, for example) summed.
  - orig\_array dataframe given to build\_network.
- Optional input: none
- Output: dataframe list of Node, Node, Weight, Edge Classification, Edge Classification Color. dataframe of node attributes sample most seen in, color with that sample.

The node data table is formatted for easy input into cytoscape using the "import table from file" option, after the network has been imported.

#### 1.14 make\_meta\_from\_file

'Make a node attribute table using sample metadata file. edges is the network dataframe while metadata is a dataframe of metadata, and orig\_array is the array of abundances (at the appropriate taxonomic level). The index set of the metadata should correspond columns [2:] of the orig\_array

- Input:
  - edges DF of Node, Node, Weight, (can have additional columns).
  - metadata dataframe table of metadata indexed by sample ID.
  - orig\_array the dataframe used to build network.
- Optional input:
  - existing\_table dataframe of node data, default []. If a dataframe is passed, node data columns will be added to this.
- Output: dataframe table of node data

The node data table is formatted for easy input into cytoscape using the "import table from file" option, after the network has been imported.

#### 1.15 mc\_network\_stats

Construct a random network and compute statistics, compare these to the statistics of the statistics of the given adjacency matrix. abdata is the data values (numpy array) and network is the adjacency matrix. Random graph is made from null model detailed in the writeup

- Input:
  - abdata numpy array, abundance array used to build network.
  - network adjacency matrix as numpy array.
- Optional input:
  - thr bool, whether or not data was thresholded in building the network, default False.
  - bins bool, whether or not the binning method was used (as opposed to correlation), default False.
  - sims number of MC draws used to estimate statistics, default 1000
- Output: the probability of seeing a greater mean degree, variance (in degree), minimum eigenvalue, maximum eigenvalue, and number of edges in a draw generated by the null model.

Null model is the same as in network construction, as described in make\_null

### 1.16 sim\_pears

Construct a MC draw simulating correlation

- Input:
  - N numpy array of of number of trials parameter for binomial RV
  - P numpy array of probabilities of success
- Optional input: none
- Output: mean degree, variance (in degree), minimum eigenvalue, maximum eigenvalue, and number of edges in the draw (given as list)

Constructs an abundance array as in make\_null

# 1.17 sim\_pears\_thr

Construct a MC draw simulating thresholded correlation

- Input:
  - N numpy array of of number of trials parameter for binomial RV
  - P numpy array of probabilities of success
- Optional input: none
- Output: mean degree, variance (in degree), minimum eigenvalue, maximum eigenvalue, and number of edges in the draw (given as list)

Constructs an abundance array as in make\_null

#### 1.18 sim\_bins

Construct a MC draw simulating binning

- Input:
  - N numpy array of of number of trials parameter for binomial RV
  - P numpy array of probabilities of success
- Optional input: none
- Output: mean degree, variance (in degree), minimum eigenvalue, maximum eigenvalue, and number of edges in the draw (given as list)

Constructs an abundance array as in make\_null

#### 1.19 edge\_prob

calculate probability of seeing an edge in a graph with that many edges if edge prob is p and we see m edges,  $p \approx 2m/n^2$  (n nodes)

- Input:
  - network dataframe list Node, Node, Weight (can have additional columns)
- Optional input: none
- Output: probability of an edge in a random graph with the same number of edges.

## 1.20 random\_sub\_graph

Calculate probability that the subnetwork has as many edges as it has

- Input:
  - network dataframe list Node, Node, Weight, edge\_sample
  - types types of sample to look for, string
- Optional input:
  - p float, probability of an edge, default 0.5
- Output: expected number of edges in a subgraph that size, actual number

## 1.21 exp\_cut\_edges

Calculate the probability of seeing that many intertype edges, or edges between some certain set of types, or out of some set of types.

- Input:
  - network dataframe list Node, Node, Weight, edge\_sample
  - types types of sample to look for, string
- Optional input:
  - p float, probability of an edge, default 0.5
- Output: expected number, actual number

### 1.22 cut\_cond

**Depreciated** Calculate conductance of cuts that cut out a type or set of types

- Input:
  - network dataframe of Node, Node, Weight, with column for sample type this column has been moved to the node data file and so this function must be rewritten
  - types string, type of nodes to look for
- Optional input: none
- Output: the conductance of a cut which removes the nodes of type specified.

Cut conductance [2] is

$$\phi(S, \overline{S}) = \frac{\sum_{i \in S, j \in \overline{S}} a_{ij}}{\min(a(S), a(\overline{S}))}$$

where

$$a(S) = \sum_{i \in S, j \in V} a_{ij}$$

#### 1.23 com\_clust

Clustering using Girvan and Newman algorithm. This means we try to maximize the quantity modularity over all possible community groupings. Modularity is the quantity: (Fraction of edges that are inside a community) - (expected fraction in a random graph) I'd like to weight this, so I'll maximize (( $\delta$  is Kronecher, d is sum of weights of edges on that vertex (generalized degree)) Also, the undirectedness means I only have to take the sum over the subdiagonal.

- Input:
  - network dataframe of adjacency matrix for graph

- Optional input: none
- Output: list of such that entry i tells us what cluster node i is in, and the modularity Q

Community clustering minimizes a function of the graph called modularity [1][5]. That is

$$Q = \frac{1}{2m} \sum_{i,j} \left( w_{ij} + \frac{d_i d_j}{2m} \right) \delta(c_i, c_j)$$

where  $m = \sum_{i \sim j} w_{ij}$ ,  $d_i$  is the (weighted) degree of vertex i,  $c_i$  is the community containing vertex i, and  $\delta$  is the Kronecker  $\delta$ . This done by a gradient search/greedy algorithm.

## 1.24 spectral\_cluster

Clustering using spectral clustering.

- Input:
  - adj\_mat numpy array of adjacency matrix for graph
- Optional input: none
- ullet Output: list of such that entry i tells us what cluster node i is in.

Spectral clustering performs a k-means clustering on the rows of the matrix whose columns are the k eigenvectors of the graph Laplacian corresponding to the smallest k eigenvalues [6]. Intuitively, this means it clusters points together that are close in the first k (slowest decaying) modes of the diffusion equation on the graph.

# 1.25 clust\_judge

Create a dataframe containing the percentage of each class in the metadata category appears in each cluster. clust\_type should be either commun or spect. node\_data should be a dataframe indexed by nodes, with a column for clusters and columns classifying nodes by meta data categories. meta\_col should be the name of a column of node\_data.

- Input:
  - node\_data dataframe of node data (including cluster number)
  - meta\_col string, name of a column of node\_data to asses
  - clust\_type string, options 'commun' or 'spect'
- Optional input: none
- Output: the percentage of each class that appears in each cluster (dataframe)

#### 1.26 color\_picker2

Takes in vector r and maps to hex colors

- Input:
  - r a 1D array or list of values to be mapped to colors
- Optional input:
  - the\_map matplotlib colormap to pull colors from, default cm.rainbow.
  - weighted bool, whether color values should be taken according values, as opposed to evenly distributed.
- Output: A list of colors (hex values)

# 1.27 est\_prob

#### Unclear if this function is working correctly

Use distribution factorization from random markov field to estimate the probability of seeing the subset of taxa in the sample. Takes in the ROW NUMBERS of the represented edges, along with the whole network.

- Input:
  - source list of row numbers of edges represented in the sample
  - induced list of edges such that both nodes are in sample
  - whole dataframe adjacency matrix of the network
  - N number of nodes
- Optional input: none
- Output: log probability of a sample.

We can consider the network a Markov random field [3]. This can give us a way to calculate the probability a group of taxa occurs together. The main idea of a MRF is that nodes are conditionally independent of nodes they aren't neighbors of (conditioned on ones they are neighbors of). If c are the (maximal) cliques of the graph (complete sub-graphs), then the probability of configuration x is

$$P(\boldsymbol{x}) = \frac{1}{Z} \prod_{c} \psi_c(x_c)$$

where Z is a normalizing constant and  $\psi_c$  are some functions, often called "potential functions" [3].

## 1.28 find\_cliques

find all the maximal cliques containing a given node, where network is an adjacency graph given as a numpy array

- Input:
  - node indices of the node of interest
  - network numpy array of adjacency matrix
- Optional input: none
- Output: list of maximal cliques involving the given node

## 1.29 psi\_over\_psi

calculate ratio between  $\psi(k+1) \& \psi(k)$ 

- Input:
  - k1, k2 scalar values, should be number of nodes present in the clique in sample 1 and 2
  - cliq list of nodes in a clique
- Optional input:
  - rm scalar constant effecting formula, default 0.8
- Output: value of  $\frac{\psi(k+1)}{\psi(k)}$  estimate

## 1.30 diff\_cliques

Take two different samples and identify which cliques are different. Then, compute the ratio of probabilities between the two configurations based on the rule that  $\frac{\psi(k+1)}{\psi(k)}$  depends on whether or not k is above or below half the size of the clique.

- Input:
  - s1, s2 abundance samples, given as numpy 1D arrays
  - network numpy array of adjacency matrix
- Optional input: none
- Output: comparison of two samples.

## 1.31 diffusion\_ivp

Using diffusion on the graph, rank the nodes we don't know about. Solve diffusion with initial condition being 1 for known on nodes and -1 for known off nodes. Network should be the adjacency graph (probably unweighted) given as a numpy array. Output is list of node indices ordered by the ranking procedure, with ties grouped in sublists

- Input:
  - known\_on list of nodes considered present, can be empty
  - known\_off list of nodes considered absent, can be empty
  - network numpy array of adjacency matrix
- Optional input:
  - suspected value to give nodes not in known\_on or known\_off, default 0.5.
  - non\_suspected value to give nodes in known\_off, default 0.
  - probably value to give nodes in known\_on, default 1.
  - sample a sample of data covering all nodes, to use as the initial condition. Default []
  - all bool, whether or not to rank all the nodes as opposed to just those not in known\_on or known\_off, default False
- Output: list of nodes in rank order, with nodes on the same connected component grouped and ties grouped. Rank is first over equilibrium solution, and secondly over transient.

#### 1.32 diffusion\_bvp

Using diffusion on the graph, rank the nodes we don't know about. Find equilibrium of solution with "boundary values" given by known node values (0,1). Network should be the adjacency graph (probably unweighted) given as a numpy array.

- Input:
  - known\_on list of nodes considered present, can be empty
  - known\_off list of nodes considered absent, can be empty
  - network numpy array of adjacency matrix
- Optional input: none
- Output: list of nodes in rank order, with ties grouped.

## 1.33 diffusion\_forced

Using diffusion on the graph, rank the nodes we don't know about. Find equilibrium of solution with forcing (pm 1) on the known nodes. Network should be the adjacency graph (probably unweighted) given as a numpy array

- Input:
  - known\_on list of nodes considered present, can be empty
  - known\_off list of nodes considered absent, can be empty
  - network numpy array of adjacency matrix
- Optional input: none
- Output: list of nodes in rank order, with ties grouped.

# 1.34 ivp\_score

Calculate a fit score based on IVP ranking

- Input:
  - network\_adj dataframe of network adjacency matrix
  - the\_samp dataframe of sample to be judged
- Optional input:
  - con scalar constant used in score calculation.
- Output: fit score:

$$F_j(s) = \frac{1}{\|s\|} \sum_{i=0}^{n-1} c^i s_i$$

where  $\mathbf{s} = (u_{j_1}(0), u_{j_2}(0), ..., u_{j_n}(0))$  such that if

$$\frac{d}{dt}\mathbf{u} = -L\mathbf{u}$$

and  $U_l = \int_0^\infty u_l(t)dt$  then

$$U_{j_1} \ge U_{j_2} \ge \cdots \ge U_{j_n}$$

# 1.35 get\_sample

create a random sample with the organsims in the real data. Made with the null model

- Input:
  - templ dataframe template that the fake sample should look like
- Optional input:
  - numb number of samples to make, default 1
- Output: dataframe of sample generated by the null model, as in make\_null

### 1.36 make\_sample

grab a real sample (column) from the template data. Option to choose the sample from a set of holdout columns that are not training data

- Input:
  - daata template data to get a column of
- Optional input:
  - holdouts list of columns held out of the network building, one of these will be chosen if there are any, default [].
- Output: chosen sample and its type.

#### 1.37 flat\_two\_deep

Flattens doubly nested lists to lists. Allows originals like [x, [x,x], [x, x,x]]

• Input:

- li - list with entries that may be lists or lists of lists.

Optional input: none Output: flattened list

## 1.38 flat\_one\_deep

Flattens nested lists to lists. Allows originals like [x, [x,x], x, x, x, x]

• Input:

- li - list with entries that may be lists.

Optional input: none Output: flattened list

# 2 co\_occurrence.py

This script builds three networks at each specified taxonomic level. Those are, a network build from the binning procedure, a network built from correlation, and a network built from correlations of thresholded data.

Command line input (all required):

- csv\_name The name of the GOTTCHA output data file. This should be a .txt or .csv with *space as separation character between columns*. To change the separation character, change line 61. Uses pandas pandas.read\_csv to import the data.
- level list of taxonomic levels to make networks for, or 'all'.
- net\_name name of a *folder* that the networks will be saved in.
- sample\_types bool that specifies whether networks should be made with subsets of the data corresponding to different body locations the samples were taken from.
- numbled the number of columns that should be removed from the data for future testing.

The GOTTCHA output data should have a column specifying taxonomic level headed "LEVEL", and another column with taxa names headed "TAXA". The remaining columns should be of the form "Body\_Part\_gender\_LLL#######" where the gender is optional, and can be "male", "female', or "NA".

The script combines abundances of samples from the same body part (referred to as the sample type) in order to classify nodes in the network according to where they are found in the highest abundance. This is saved in the pandas dataframe samp\_type\_abund.

Samples can be separated by metadata to make separate networks. If sample\_types is true, then new data matrices are made, containing only samples of a single type(body location), and only types with more than 50 samples. The full array is also kept. This script can instead separate by gender, if this is in the column headings of data, by inputting sample\_types as false, and switching gender to true (line 117). There is also the option to use some other type of metadata to create subsets of data and make networks, by setting gender to false and other\_meta to true. Then, one must also input meta\_file file name of a file that can be parsed by pandas read\_csv, as well as meta\_column, the name of the column of interest in the metadata. The file should be separated by spaces and the first column should be sample IDs. This last possibility has not been tested and may contain bugs.

Networks are made using build\_network and make\_meta from co\_occ\_funs.py.

Networks and node data .tsv files are created. The folder specified must have subfolders "bins" and "pears". The bin networks will be saved in "bins" and correlation in "pears". with the network file (list of edges: Node, Node, Weight, Edge Data, Edge Data) saved as "...\_list.tsv", the adjacency matrix "...\_adj.tsv", and the node data table as "...\_node\_data.tsv". In the "pears" folder, correlation of abundances and correlation of thresholded abundances can be distinguished by "cor" and "thr" respectively. If there were held out columns, a list of their indices is saved in "...\_held.tsv". All of these files are saved as tab-separated text files using pandas to\_csv.

# 3 cluster\_net.py

This script takes networks and adds to the node data table the result of two clustering algorithms. Command line input (required):

• folder - The folder where the network or networks in question are saved. Networks are assumed to have been saved as by co\_occurrence.py, so adjacency matrices must end with "adj.tsv" and node data must end with "data.tsv".

This script will cluster all the networks in the folder. For each network found in the file, community clustering is run using com\_clust, and spectral clustering is run using spectral\_cluster, both from co\_occ\_funs.py. Both of these return a list such that entry i is the cluster number of node i.

Rather than producing a new output file, this script adds columns to the existing node data table. It adds four columns - the spectral cluster, the community cluster, a color (hex value) assigned to the spectral cluster, and a color (hex value) assigned to the community cluster. These colors can be shown in cytoscape using a "passthrough" mapping for node color.

# 4 network\_stats.py

The purpose of this script is to determine the significance of the network build compared to the null model described in make\_null.

Command line input (all required)

- csv\_name the data file used to build the network
- level the taxonomic level at which the network was built
- sample\_types whether or not a network was made for each sample type.
- adj\_name name of the adjacency matrix file
- type 'pears' correlation, 'pears\_thr' thresholded correlation, or 'binned' binned.

Computes the following statistics for the network given:

- Number of edges
- Mean node degree
- Probability the null model produces a higher mean degree
- Probability the null model produces a higher degree variance
- Probability the null model produces a larger maximum eigenvalue
- Probability the null model produces a larger minimum eigenvalue
- Probability the null model produces more edges

The function mc\_network\_stats from co\_occ\_funs.py is used.

It outputs these to a file called stats.txt in the same folder as the network. If the file already exists, this will append to the end of it.

These statistics are meant to give some indication of how expected the network would be given the null model: Let

$$N_i = |\{i : r_{ij} \neq 0\}|$$

and

$$P_i = \frac{|\{j : r_{ij} \neq 0\}|}{|\{(i,j) : r_{ij} \neq 0\}|}$$

then I take

$$\hat{r}_{ij} = binom(N_j, P_i)$$

as randomly generated abundance data. The values  $N_i$  are the counts of appearances of taxi i, while the values  $P_j$  are the proportions of all appearances which happen within each sample.

Then, I construct our random graph from this random data. If  $\hat{r}_i$  is the vector of random "abundances" of taxa i, I have edges

$$w_{ik}^{null} = \frac{1}{N} \frac{(\hat{\boldsymbol{r}}_i - \hat{\mu}_i \mathbf{1}) \cdot (\hat{\boldsymbol{r}}_k - \hat{\mu}_k \mathbf{1})}{\hat{\sigma}_i \hat{\sigma}_k}$$

# 5 falsepm.py

This script is used for verification of the methods. It attempts to measure how well the network fitting procedure works, and how whether or not the ranking procedure can identify false negatives in a sample.

Command line input (all required):

- abund\_name the name to the original array used to construct the networks
- folder the folder all the networks are stored in.

The folder should have networks made from all of the data as well as subsets by sample type (body location) - adjacency matrices saved as files ending with "adj.tsv". It should also have at least one file saved ending in "held.tsv" listing the nodes that were held out of network making.

The held out nodes are all tested for fit to the full network as well as fit to each of the networks made from subsets of the data, using ivp\_scores from co\_occ\_funs.py. Then, each of the 30 highest abundance entries are set to 0 from the sample (one at a time) and the rank of the node is found using diffusion\_ivp. We record this rank (minus the number of non-zero nodes).

Next, random samples are generate (equal in number to the number of hold outs) and tested for fit to the whole network.

Finally, this script produces the following plots, saved in a subfolder "validation\_plots":

- histogram of fit scores to the full (correlation) network of the holdouts and the randomly generated samples
- histogram of fit scores to the full (thresholded) network of the holdouts and the randomly generated samples
- A bar chart of the proportion of samples of each type that were correctly classified (by the best fit score)
- Bar charts of the proportion of classification of the samples of each type
- scatter plot of abundance rank vs diffusion rank (after abundance is set to 0)

# 6 net\_making.sh

This script creates a folder and networks (co\_occurrence.py) at the genus and species level using the data in merged2.txt. It also runs clustering on these networks (cluster\_net.py), computes network significance statistics (network\_stats.py). Finally, it runs method validation (falsepm.py).

# 7 rand\_samp.py

This script creates modified samples for method validation with sample\_analysis.py.

Command line input (all required):

- template\_name file name of data used to create network, or similar
- level taxonomic level the sample should "look like"
- flder folder the sample should be saved in
- cols\_not\_used numbers of the columns held out of network building.

Takes a column of the data (possibly a hold-out column) used to the create the full network. Creates a dataframe with the column's abundances, and a bool column of whether or not the abundance is nonzero. Optionally can modify the sample, and creates two columns of bools whether or not the abundance has been artificially set to 0 or artificially set to non-zero.

Additionally, if rand\_samp is true, creates a sample from the null model and does the same to it. Saves the sample or samples as .tsv files.

# 8 sample\_analysis.py

Runs the diffusion procedures on a given sample.

Command line input (all required):

- sample\_name filename of sample should be able to be interpreted by pandas read\_csv.
- node\_atts\_name the filename of the node attribute table of the network to be used
- cocc\_mat\_name name of adjacency matrix file.
- level taxonomic level of the network

This script ranks the nodes but all three possible diffusion rankings, diffusion\_ivp, diffustion\_bdvp, and diffusion\_forced. It also assigns colors to these ranks. It saves the sample with abundances, non-zero nodes identified, rankings, and colors in a .tsv that can be imported into cytoscape as a node table.

# 9 sample\_test.sh

Script that makes folders for samples, creates samples using rand\_samp.py, and runs sample\_analysis.py on these samples.

# 10 examples.py

Script to create some examples. If

Command line input (only if tiny is false):

• sample\_name - file output from sample\_analysis.py

If tiny is true, runs diffusion\_ivp on three small toy networks. Then, computes their fit score. Finally, it plots abundance vs rank and displays the fit score.

If tiny is false, it takes a sample that has rankings associated with it already, computes the fit score, and plots abundance vs fit score and displays fit score. It also tries to classify the sample by the clusters of the network, and which clusters the highest rank nodes appear in.

# 11 adding\_data.py

Script to build networks using growing subsets of the data.

Command line input (all required):

- csv\_name the GOTTCHA output data array
- level the taxonomic level to be tested
- sample\_types whether or not the data should be separated by sample types (body locations).

Builds a network and, if monte is true, runs mc\_network\_stats using random subset of the data, increasing in size. Creates plots of how number of edges, mean degree, and if monte is true, the stats computed by mc\_network\_stats change as data is added.

# 12 mc\_speed.py

A script to test how the length of time it takes to build a network and run mc\_network\_stats takes as data is added. Command line input (required):

• csv\_name - the GOTTCHA output data

Script is similar to adding\_data.py, except that it repeats the process. Rather than saving the stats, it saves the length of time it takes to build and compute the stats of each network. It plots how time increases as data is added.

# References

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