# PAYG, Current Account and Fertility Rates: Consequences for Savings

Jeff Clawson

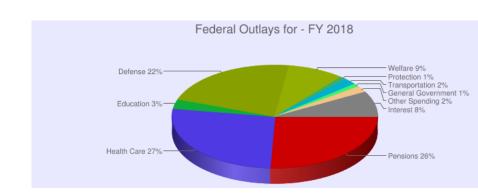
December 7, 2017



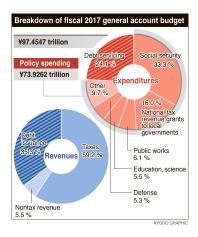
#### **Overview**

- Motivating Graphs
- Quick Literature Review
- Endgame Model
- Current Model
- Steady State Calculations
- Dynamic Preview

# **US Budget**

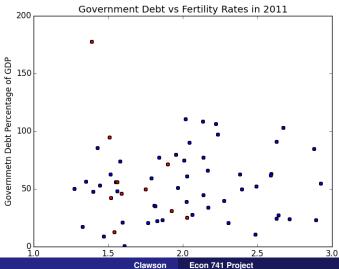


#### Japan Budget



Motivation Lit Review Ideal Model **Current Model Steady State** Next Steps...

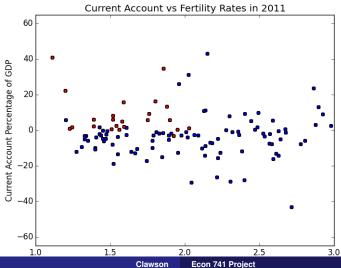
# **Government Debt and Fertility**





Motivation Lit Review Ideal Model **Current Model Steady State** Next Steps...

# **Current Account and Fertility**





# **Underlying Question**

- What is the impact of a Pay-As-You-Go Pension System and a shrinking population on international financial allocation?
- Based on my data search, I hypothesize that countries with a PAYG pension and shrinking populations will have current account surpluses.
- I will begin this exploration by building a model. This will be an overlapping generations model (OLG).

#### **A Brief Review**

#### OLG in International Trade/Finance

- Stavely-O'Carroll and Stavely-O'Carroll (2017): Comparing two countries with and without PAYG system.
- Eugeni (2015): Differences in PAYG execution lead to impact on current accounts
- Sayan (2005): Two Countries growing at different (but constant) rates

#### OLG/Pension and Saving

Samwick (2000): Pension system's impact on savings,
 Empirical evidence that it does distort savings decision.



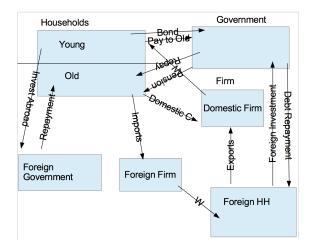
#### **Unique Features**

I am working to build a two good, two country OLG Trade Model with the following features:

- Both countries have a Pay-As-You-Go (PAYG) pension system and exhibit population growth.
- However, one will have stochastic population growth and the other will grow at a constant rate.
- The governments will be permitted to borrow to finance pensions
- Households can purchase good from either firms.
- The intent is to examine the differences savings behavior between these two countries.



# Full Model Diagram



# **Starting from the Ground Up (Households)**

First, I'll focus on the stochastic population mechanic before adding the other features. The Household's problem is:

$$\max_{s_t, c_t^y, c_{t+1}^o} u(c_t^y) + \beta \mathbb{E}_t u(c_{t+1}^o)$$

$$c_t^y = w_t - x_t - s_t$$

$$c_{t+1}^o = p_{t+1} + (1 + r_{t+1})s_t$$

Where the population grows:

$$N_t = (1 + g_t e^{z_t}) N_{t-1}$$

Where  $z_t = \rho z_{t-1} + \epsilon_t \; \epsilon_t \sim N(0, \sigma_t^2)$ 



#### **Households Continued**

Households also have CRRA Preferences:

$$u(c) = \frac{c^{1-\gamma}}{1-\gamma} \tag{1}$$

We normalize all of the variables in the following way:

$$\hat{\theta} = \frac{\theta}{N}$$

#### **Firm and Government**

Pensions must equal contributions

$$N_t x_t = N_{t-1} p_t \implies p_t = (1 + e^{z_t} g_t) x_t$$

Then the firm's (per capita) problem is:

$$\max_{k_t} k_t^{\alpha} - w_t - r_t k_t$$

With the standard factor prices:

$$r_t = \alpha k_t^{\alpha - 1}$$

$$\mathbf{w}_t = (\mathbf{1} - \alpha)\mathbf{k}_t^{\alpha}$$



# **Equilibrium Conditions**

Given factor prices  $(w_t, r_t)$ ,  $x_t$  and  $k_t$ 

$$(c_t^y)^{-\gamma} = \beta \mathbb{E}_t (1 + r_{t+1}) (c_{t+1}^o)^{-\gamma}$$
  
 $k_t^\alpha = c_t^y + c_t^o + k_t + x_t$ 

Using the constraints defined before.

#### "Calibrations"

| Parameter       | Value |
|-----------------|-------|
| g               | 0.03  |
| $\beta$         | 0.95  |
| $\alpha$        | 0.35  |
| $\delta$        | 0.04  |
| $\gamma$        | 3     |
| ho              | 8.0   |
| $\sigma_{m{e}}$ | 0.03  |
|                 |       |

#### "Results" unconstrained

| Steady State         | Value            |
|----------------------|------------------|
| k <sub>ss</sub>      | 0.00155394127258 |
| X <sub>SS</sub>      | 0.0387485406436  |
| r <sub>ss</sub>      | 23.4226243488    |
| W <sub>SS</sub>      | 0.0675951392773  |
| $c_{ss}^y$           | 0.0272926573611  |
| $C_{\rm SS}^{\it O}$ | 0.0778623208233  |

#### Next Stage

- Expand to the dynamic model (VFI)
- Next, I'll incorporate bond markets.
- Then, I'll add trade.

You can follow my progress at:

https://github.com/jdclawson/JeffPhDRepo