

# ELECTRICAL SCIENCE-II

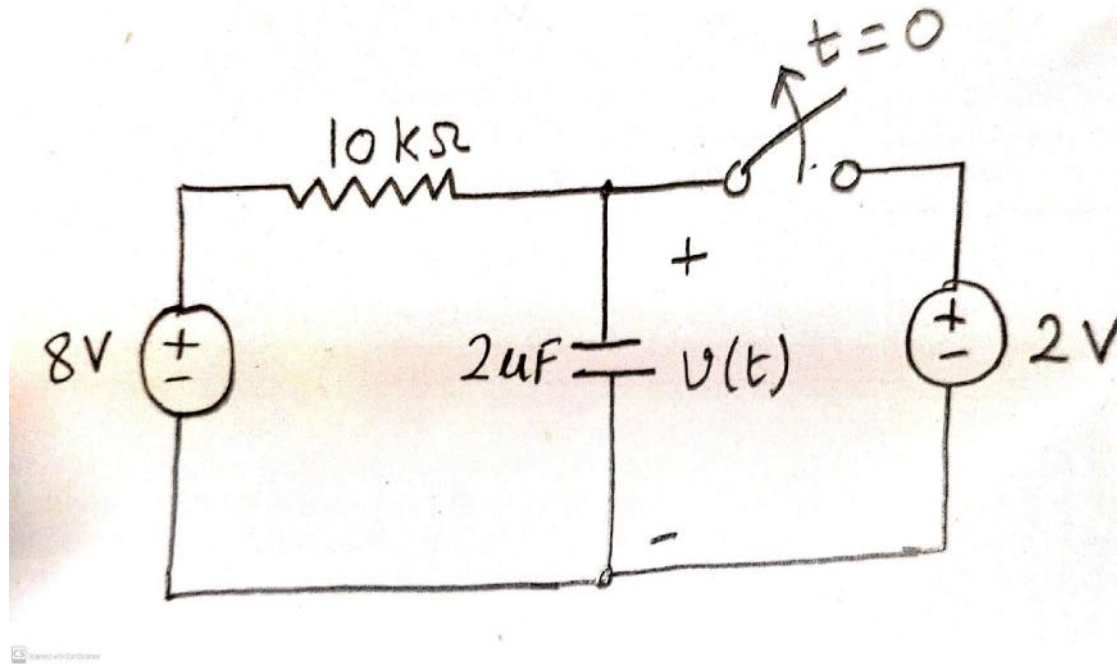
## (15B11EC211)

# Content

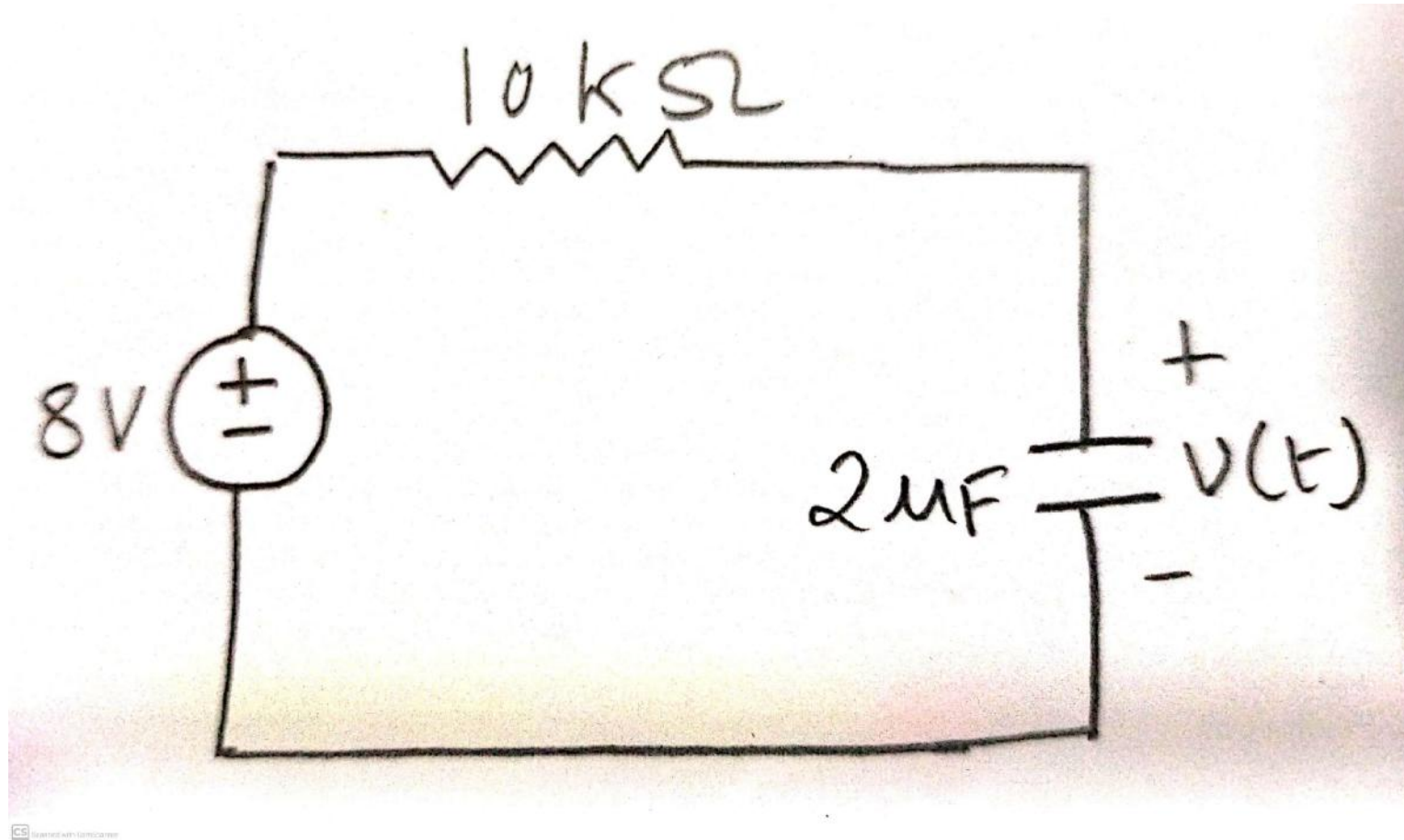
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## Example1

Find the capacitor voltage after the switch opens in the circuit shown in Figure. What is the value of the capacitor voltage 50ms after the switch opens?



an equivalent circuit after the switch opens



# Solution

- The 2-volt voltage source forces the capacitor voltage to be 2volts until the switch opens.
- Because the capacitor voltage cannot change instantaneously, the capacitor voltage will be 2volts immediately after the switch opens.
- Therefore, the initial condition is
$$v(0) = 2V$$

The circuit after the switch opens is

$$V_{oc} = 8V, \text{ \& } R_t = 10K\Omega$$

- The time constant for this first-order circuit containing a capacitor is

$$\tau = R_t C = (10 \times 10^3)(2 \times 10^{-6}) = 20 \times 10^{-3} = 20 \text{ ms}$$

- Complete response of RC circuit is

$$v(t) = V_{oc} + (v(0) - V_{oc})e^{-t/\tau}$$

- Putting values we get

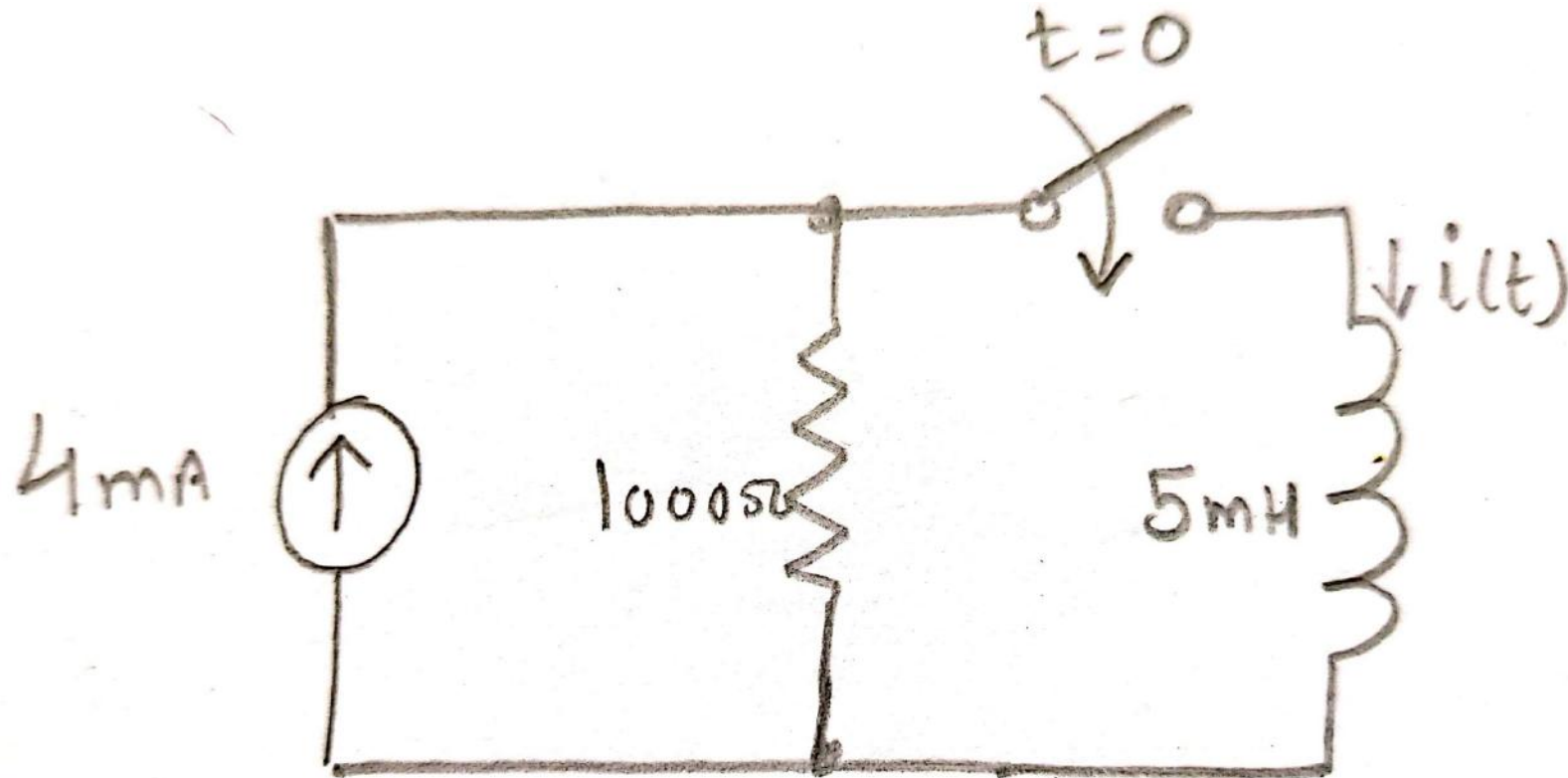
$$v(t) = 8 - 6 e^{-t/20} \text{ V}$$

- Where t has units of ms. To find the voltage 50 ms after the switch opens, let

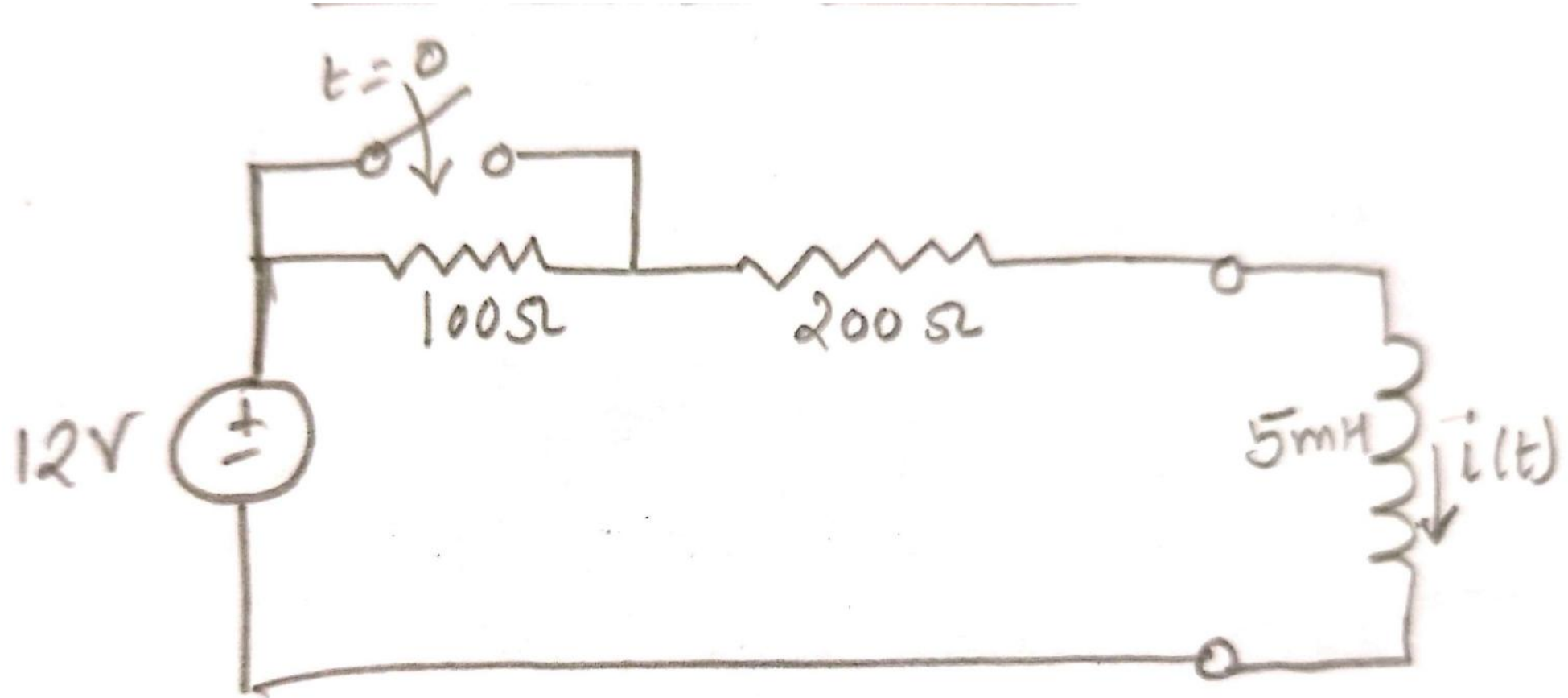
t = 50 ms. Then,

$$v(50 \text{ ms}) = 8 - 6 e^{-50/20} \text{ V} = 7.51 \text{ V}$$

Find the inductor current after the switch closes in the circuit shown in Figure. How long will it take for the inductor current to reach 2mA?



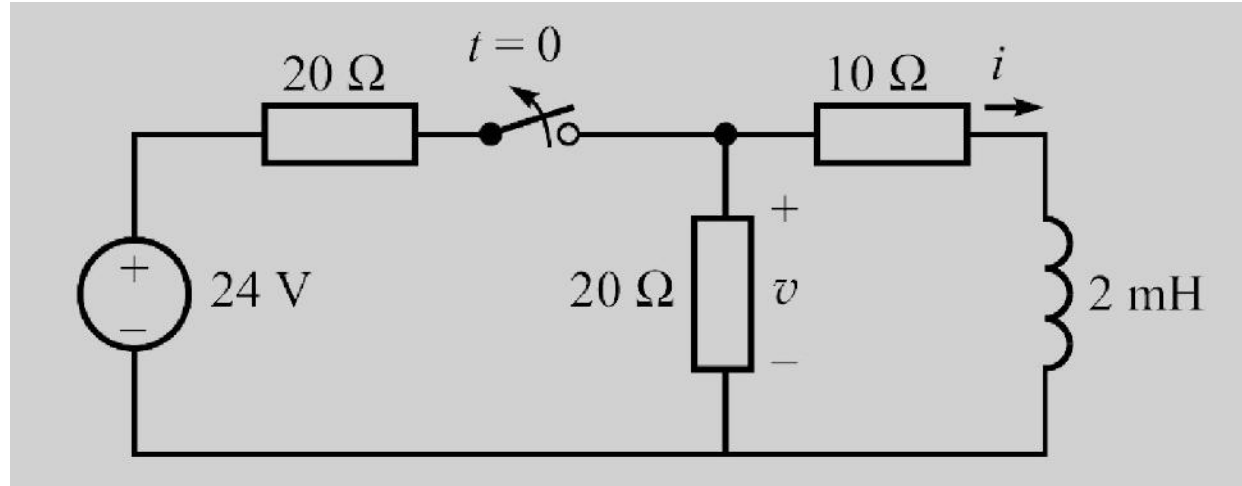
The switch in Figure has been open for a long time, and the circuit has reached steady state before the switch closes at time  $t = 0$ . Find the inductor current for  $t \geq 0$ .



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## Example 2



The circuit has been in the condition shown for a long time. The switch is opened at  $t = 0$ .

- (i) Determine the current  $i(0+) = I_0$ .
- (ii) Find  $v_R$  across 20- $\Omega$  resistor at the instant just after the switch is opened.

**Solution :** (i) Under steady-state condition, the voltage drop across an inductor is zero and it behaves as a short-circuit. The equivalent resistance faced by the 24-V source is

$$R_{eq} = 20\ \Omega + (20\ \Omega \parallel 10\ \Omega) = 26.67\ \Omega$$

The current supplied by the 24-V source,

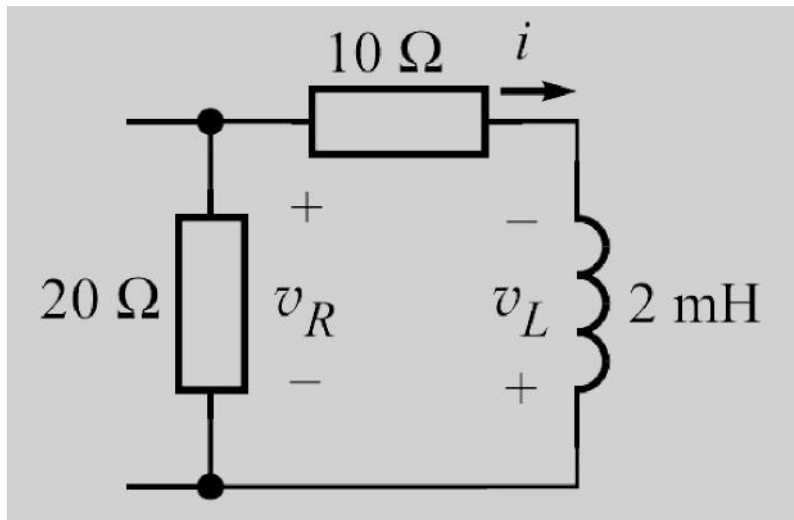
$$I = \frac{V}{R_{eq}} = \frac{24}{26.67} = 0.9\ \text{A}$$

By current division,

$$I_L = 0.9 \times \frac{20}{20 + 10} = 0.6\ \text{A}$$

Immediately after the switch is opened, the current through the inductor remains the same. Hence,

$$i(0^+) = I_0 = \mathbf{0.6 \text{ A}}$$

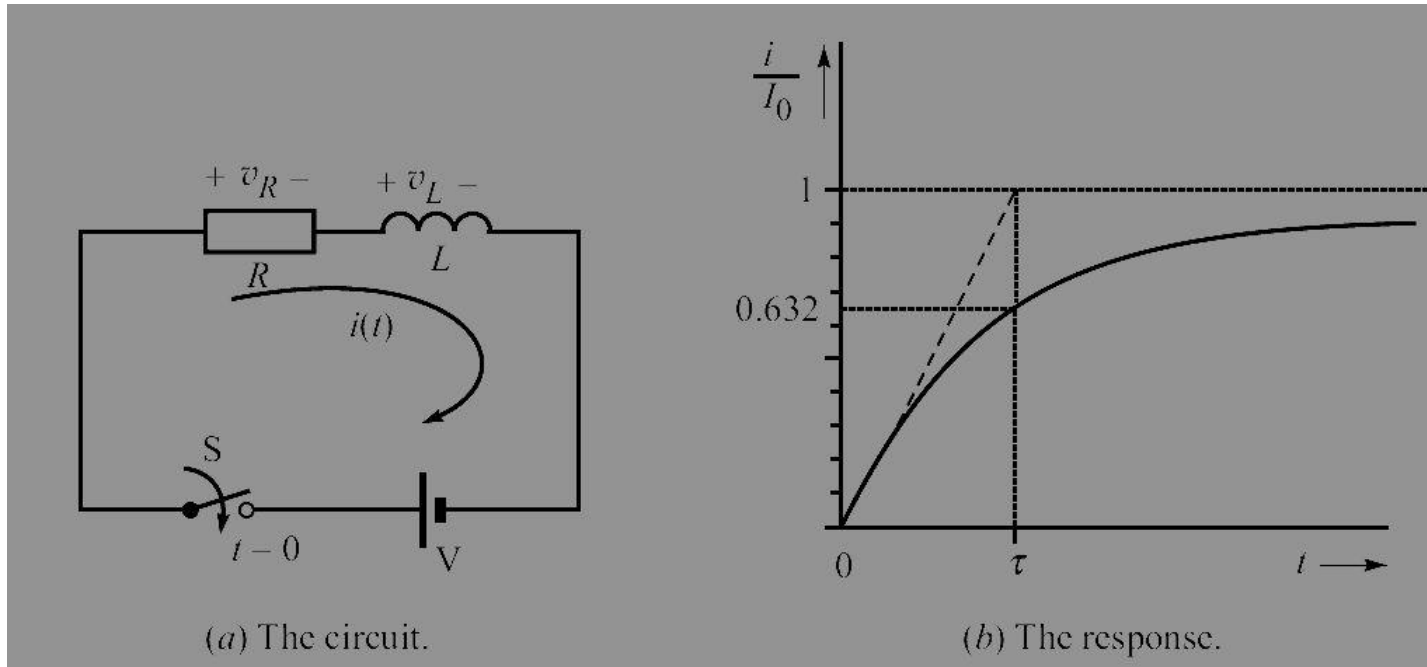


The circuit after the switch is opened ( $t > 0$ ).

(ii) The voltage across the 20-Ω resistor,

$$v_R = (-I_0)R = -0.6 \times 20 = \mathbf{-12 \text{ V}}$$

# Growth of Current in Series *RL* Circuit



- Since the current in an inductor cannot change by a finite amount in zero time, we must have  $i(0+) = 0$ .
- After  $t = 0$ , the current slowly increases and approaches its steady state value  $I_0 = V/R$ .

The response to this circuit for  $t > 0$  can be found as

$$i(t) = I_0(1 - e^{-t/\tau})$$

The value of  $i(t)/I_0$  at  $t = \tau$ ,

$$\frac{i(\tau)}{I_0} = (1 - e^{-1}) = (1 - 0.368)$$

or  $i(\tau) = 0.632I_0$

- Thus, in one time constant the response rises to 63.2 % of its final value.
- It takes about five time constants for the current to grow to its final steady state value.

# Rate of Growth of Current

The initial rate of growth of current is given by the slope of the curve at the origin.

$$\left. \frac{di}{dt} \right|_{t=0} = - \left( - \frac{I_0}{\tau} \right) e^{-t/\tau} \Big|_{t=0} = \frac{I_0}{\tau} = \frac{V}{R} \frac{R}{L} = \frac{V}{L}$$

- Thus, the smaller the value of  $L$ , the faster the current rises to its final value.

## Example 3

A coil having an inductance of 14 H and a resistance of 10  $\Omega$  is connected to a dc voltage source of 140 V, through a switch.

- (a) Calculate the value of current in the circuit at an instant 0.4 s after the switch has been closed.
- (b) Once the current reaches its final steady state value, how much time it would take the current to drop to 8 A after the switch is opened ?

## Solution :

The time constant,  $\tau = L / R = 14 / 10 = 1.4 \text{ s}$

(a) The final steady state value of the current,

$$I_0 = \frac{V}{R} = \frac{140}{10} = 14 \text{ A}$$

The value of current at  $t = 0.4 \text{ s}$  is given by

$$i = I_0(1 - e^{-t/\tau}) = 14(1 - e^{-0.4/1.4}) = \mathbf{3.479 \text{ A}}$$

(b) For decaying current,

$$i(t) = I_0 e^{-t/\tau} \quad \text{or} \quad 8 = 14e^{-t/1.4} \quad \text{or} \quad e^{-t/1.4} = 0.5714$$

$$-\frac{t}{1.4} = \ln 0.5714 = -0.5596 \quad \Rightarrow \quad t = \mathbf{0.7834 \text{ s}}$$