

Signals and Systems

Systems and their classifications-II

Causal & Non-causal Systems

Linear & Nonlinear Systems

Causal & Non-causal Systems

(2) Causal & Non-Causal System →

* causal → * If o/p of sys. is independent of future values of i/p at each & every instant of time then sys. will be causal.

* These sys. are practical (or) physically realisable sys.

Eg:- (1) $y(t) = x(t)$

(2) $y(t) = x(t-1)$

(3) $y(t) = x(t) + x(t-1)$

* Non-Causal system → * If o/p of sys. depends on future values of i/p at any instant of time then sys. will be non-causal.

Cont..

Eg:- (1) $y(t) = \underline{x(t+1)}$

(2) $y(t) = x(t) + \underline{x(t+1)}$

(3) $y(t) = x(t+1) + \underline{x(t+1)}$

(4) $y(t) = x(t) + x(t-1) + \underline{x(t+1)}$

* Anti Causal System \rightarrow * If o/p of sys depends only on future value of i/p then sys will be anticausal.

Eg:- $y(t) = x(t+1)$

* All anti-causal systems are non-causal but converse of this statement is not true.

Cont..

Que. → Check Causal & Non-Causal system.

(1.) $y(t) = x(2t)$

(7.) $y(t) = \int_{-\infty}^t x(\tau) d\tau$

(2.) $y(t) = x(-t)$

(8.) $y(t) = \int_{-\infty}^{t+1} x(\tau) d\tau$

(3.) $y(t) = x(\sin t)$

(9.) $y(t) = \int_{-\infty}^{2t} x(\tau) d\tau$

(4.) $y(t) = \begin{cases} x(2t) & ; t < 0 \\ x(t-1) & ; t \geq 0 \end{cases}$

(5.) $y(t) = \text{Odd}[x(t)]$

(6.) $y(t) = \sin(t+2) \cdot x(t-1)$

Cont..

Soln \rightarrow (i) $y(t) = x(2t)$
($t=1$) \downarrow

$y(t) = x(2)$ (system is non-causal)

(ii) $y(t) = x(-t)$
($t=-1$)

$y(-1) = x(1)$ (system is Non-causal)

(iii) $y(t) = x(\sin t)$
($t=-\pi$)

$y(-\pi) = x(0)$

$-3.14 = x(0)$ (system is non-causal)

(iv) $y(t) = \begin{cases} x(2t), & t < 0 \rightarrow \text{past} \\ x(t-1), & t \geq 0 \rightarrow \text{past} \end{cases}$

(system is causal)

Cont..

(v.) $y(t) = \text{odd } x(t)$
$$= \frac{x(t) - x(-t)}{2}$$

$(t = -1)$ $y(-1) = \frac{x(-1) - x(1)}{2}$ (system is non-causal) ↗ future

(vi) $y(t) = \sin(t+2) \cdot x(t-1)$
↓ (coefficient) ↓ past
(system is causal.)

(vii) $y(t) = \int_{-\infty}^t x(z) dz$ ↗ $x(t)$
$$= \int_{-\infty}^t x(t) dt$$
 (system is causal)

Cont..

$$\text{viii)} \quad y(t) = \int_{-\infty}^{(t+1)} x(z) dz \quad \xrightarrow{\quad} x(t+1)$$

(system is non-causal)

$$\text{(ix)} \quad y(t) = \int_{-\infty}^{2t} x(z) dz \quad \xrightarrow{\quad} x(2t)$$

(system is non-causal)

Linear & Nonlinear Systems

(2.) Linear & Non-linear system →

linear → * A linear sys. follows the law of superposition.

* This law is necessary & sufficient to prove linearity of system.

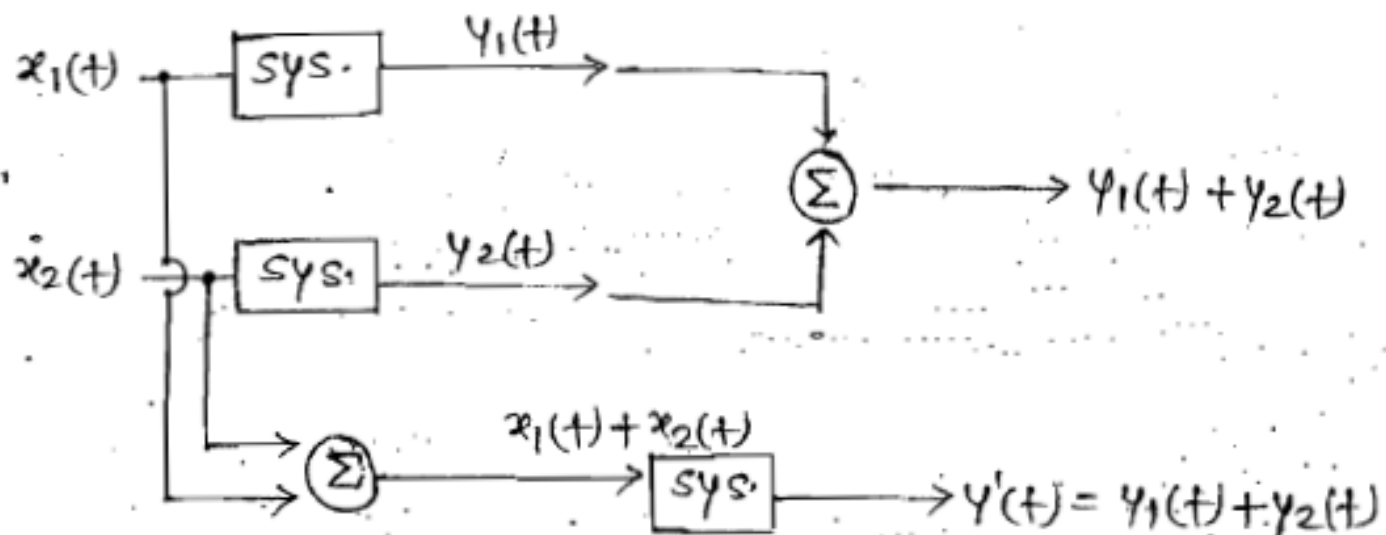
* It is a combination of two laws:-

(i) Law of additivity.

(ii) Law of homogeneity.

Cont..

(1) Law of additivity \rightarrow

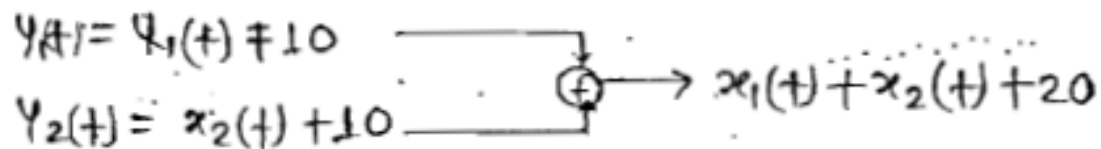


Ex:- $y(t) = x(t) + 10$

o/p = i/p + 10

$$y_1(t) = x_1(t) + 10$$

$$y_2(t) = x_2(t) + 10$$

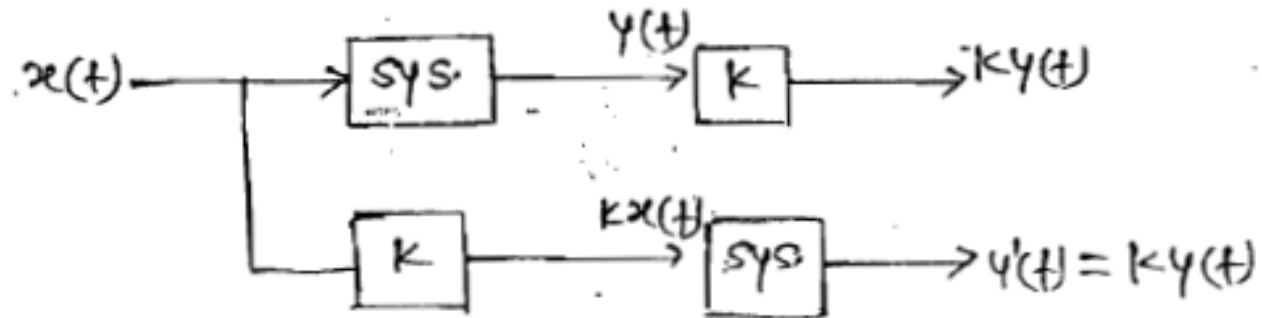


$$y'(t) = x_1(t) + x_2(t) + 10$$

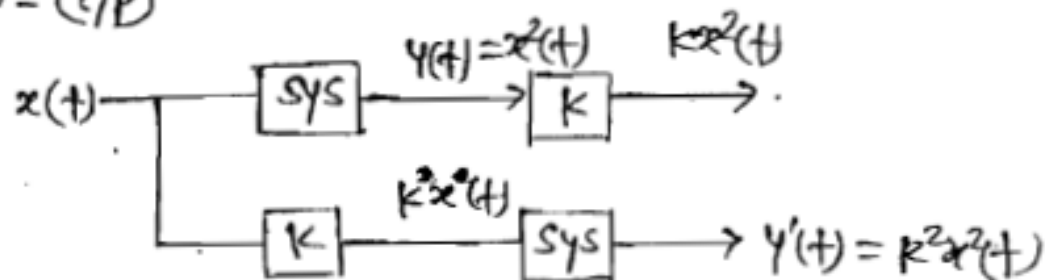
$$y(t) \neq y'(t) \quad [\text{Sys is NL}]$$

Cont..

(2.) Law of Homogeneity \rightarrow



Eg:- $y(t) = x^2(t)$
o/p = (i/p)²

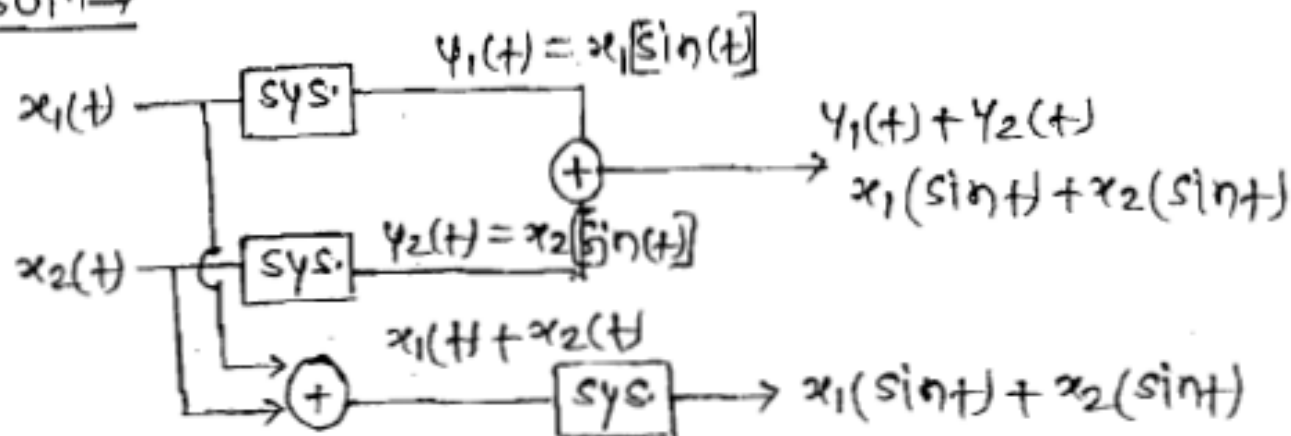


Cont..

Que. → Check linear / Non-linear sys.

(1) $y(t) = x(\sin t)$ (2) $y(t) = x(t) \sin t$ (3) $y(t) = x(t^2)$

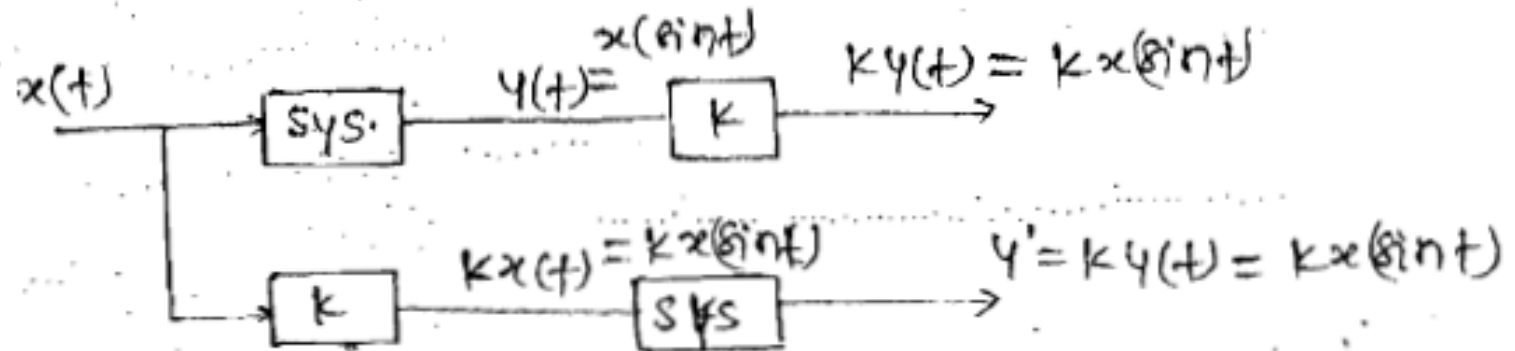
Soln →



Cont..

Note →

Linearity of sys. is independent of time scaling.

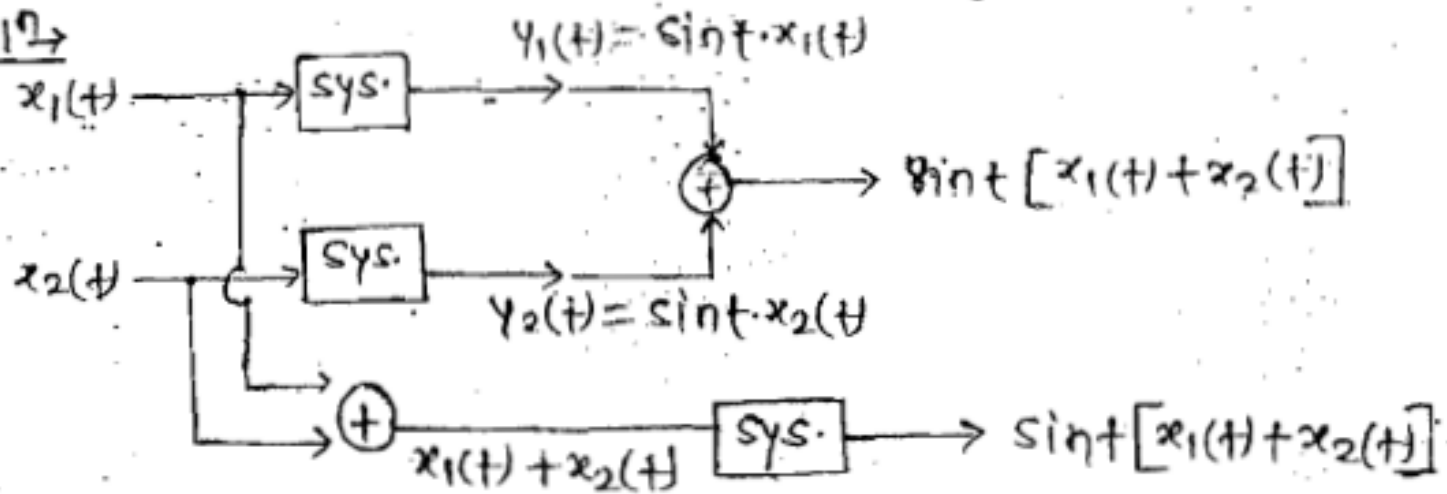


Cont..

(2) $y(t) = \sin t \cdot x(t)$

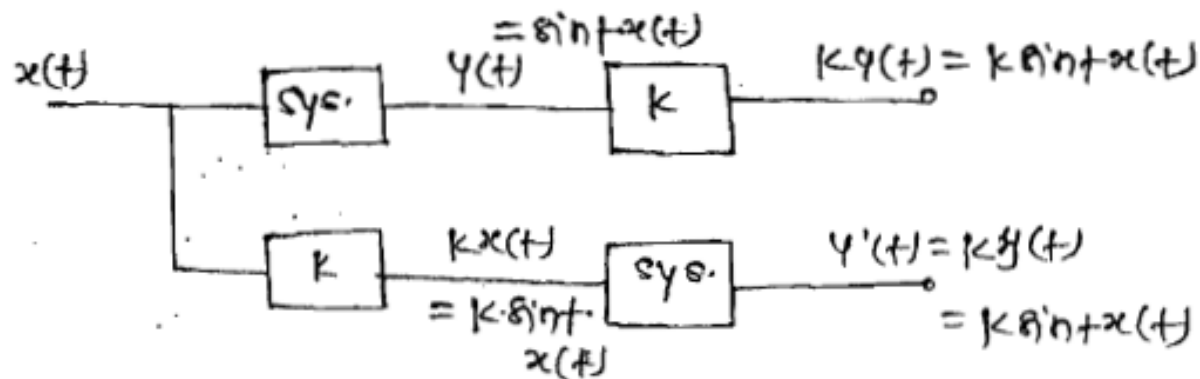
(3) $y(t) = \log t \cdot x(t)$

Solⁿ →



Cont..

Note:- linearity of sys. is independent of coefficient used in sys. relationship.



Cont..

2nd method →

for linearity :-

(i) O/p should be 0 for 0 i/p.

(ii) There should ^{not} be any 'NL' operation.

eg:- [sin, cos, tan, sec, cosec, cot,
log, exponential, modulus, sq, cube,
....., root, Sq(), sinc(), ... Sgn() etc
either on 'x' or 'y'.]

Cont..

Q. → Check linear/NL sys.

(i) $y(t) = x(t) + 2 \rightarrow$ put $t=0$ then $y(0) \neq x(0) + 2 \rightarrow \text{NL}$

(ii) $y(t) = e^{x(t)} \rightarrow$ Because of $e^{x(t)}$ it is **NL** & also both condⁿ not satisfying.

(iii) $y(t) = x(t \sin t) \rightarrow \text{Linear}$

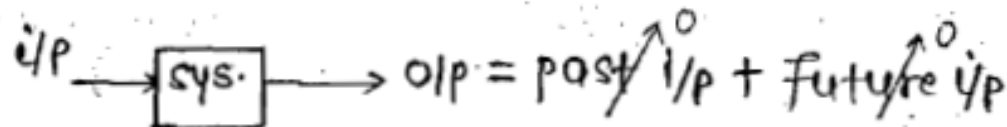
(i) If $t=0$, then $y(0) = x(0)$ means no i/p no o/p

(ii) above fⁿ is not operating on 'x', it is operating on the 't'.

(iv) $y(t) = \tan[x(t)]$

system is **NL**

(v) $y(t) = x(t-1) + x(t+1)$



No any NL fⁿ so this is **linear**

Cont..

Note →

(1.) Integral & derivative operators are linear.

(2.) Even & odd operators are linear.

$$(ix) \quad y(t) = \int_{-\infty}^t x^2(z) dz$$

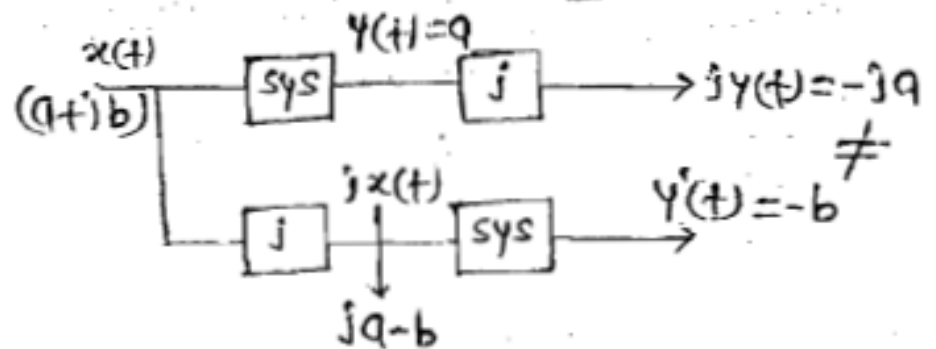
$$y(t) = \int_{-\infty}^t x^2(z) dz \rightarrow \text{NL}$$

$$(xi) \quad y(t) = e^t x(t)$$

$$y(t) = e^t x(t) \rightarrow \text{linear}$$

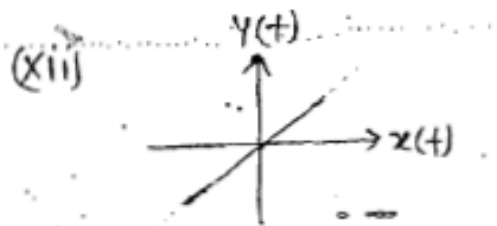
$$(xi) \quad y(t) = \text{Re} \{ x(t) \}$$

$$y(t) = \frac{x(t) + x^*(t)}{2} \rightarrow \text{NL}$$

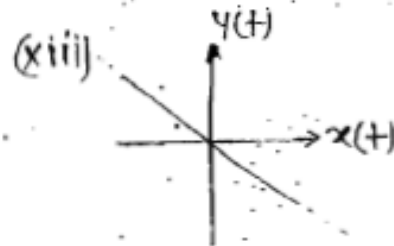


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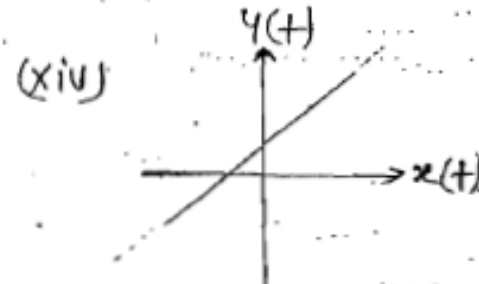
Note → Real & imaginary operators are NL.



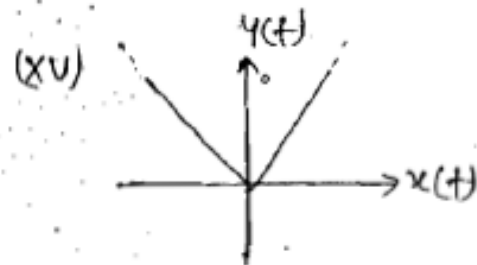
$y(t) = m x(t)$
system is linear



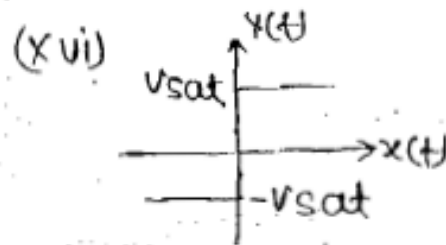
$y(t) = -m x(t)$
system is L



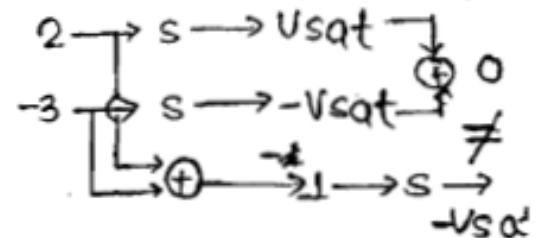
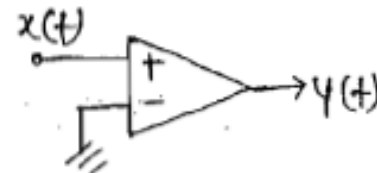
When i/p 0 then we got
o/p NL



$y(t) = |x(t)|$
NL



$y(t) = V_{sat} \text{sgn}[x(t)]$ (or)
NL



Thank You