

# Physics-2 "ISB11PH211" Tutorial 10 (solution)

① from mass action law  $n \cdot p = n_i^2$

$$n = \frac{n_i^2}{p}$$

$$= \frac{2.25 \times 10^{20}}{2.25 \times 10^{15}}$$

$$= 10^5 / \text{cm}^3$$

② At 300K  $2kT = 2 \times 8.614 \times 10^{-5} \times 300 \text{ eV} = 0.052 \text{ eV}$

Now intrinsic concentration of charge carrier is

$$n_i = 2 \left( \frac{2\pi kT}{h^2} \right)^{3/2} (m_e^* m_h^*)^{3/4} \exp \left( -\frac{E_g}{2kT} \right)$$

$$\exp \left( \frac{E_g}{0.052} \right) = \frac{1.713 \times 10^{24}}{2.29 \times 10^{19}} = 0.748 \times 10^6$$

or  $E_g = 0.052 [\ln(0.748) + 6 \ln 10]$

$$E_g = 0.7 \text{ eV}$$

③ Given  $E_c - E_F = 0.44 \text{ eV}$  below conduction band,  
 $T = 300 \text{ K}$ ,  $kT = 0.026 \text{ eV}$ ,  $N_D = 5 \times 10^{15}$ ,  $E_c - E_F' = ?$

For an n-type Semiconductor, the electron density is given by

$$n = N_D = N_c \exp \left( -\frac{E_c - E_F}{kT} \right)$$

Similarly  $n' = 5 \times 10^{15} = N_c \exp \left( -\frac{E_c - E_F'}{kT} \right)$

Now  $\exp \left( -\frac{E_c - E_F'}{kT} \right) = 5 \exp \left( -\frac{E_c - E_F}{kT} \right)$

$$\exp \left( -\frac{E_c - E_F'}{kT} + \frac{E_c - E_F}{kT} \right) = 5$$

$$E_c - E_F' = E_c - E_F - kT \ln 5$$

$$= 0.44 - 0.026 \times \ln 5$$

$$= 0.398 \text{ eV}$$

⑥ Given-

$$l = 0.2 \text{ cm} = 0.2 \times 10^{-2} \text{ m},$$

$$b = 0.12 \text{ cm} = 0.12 \times 10^{-2} \text{ m},$$

$$h = 0.2 \text{ cm} = 0.02 \times 10^{-2} \text{ m}$$

$$V_a = 1.0 \text{ Volts}$$

$$I_n = 2.5 \times 10^{-3} \text{ A}$$

$$B_z = 0.5 \text{ T}$$

$$n = ?$$

$$R_H = \frac{E_y}{I_n B_z} \quad \text{where } E_y = \frac{V_H}{l} \quad \& \quad I_n = \frac{I_n}{bh}$$

$$\therefore R_H = \frac{V_H b}{I_n B_z} = -\frac{1}{ne} \quad (\text{for n-type})$$

$$= -\frac{1}{be} \quad (\text{for p-type})$$

Assuming the charge carrier to be electrons

$$n = \frac{I_n B_z}{V_H b e} = \frac{2.5 \times 10^{-3} \times 0.5}{10^{-2} \times 0.12 \times 10^{-2} \times 1.6 \times 10^{-19}}$$

$$= 6.5 \times 10^{20} / \text{m}^3$$

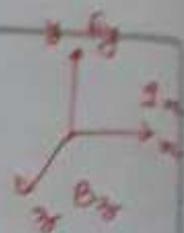
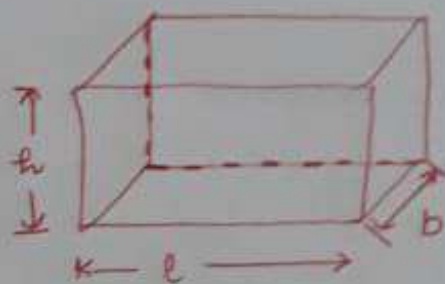
$$\text{Now } E_n = \frac{V_a}{l}, \therefore \sigma_n = \frac{I_n}{E_n} = \frac{I_n / bh}{V_a / l} = \frac{I_n l}{bh V_a}$$

$$= \frac{2.5 \times 10^{-3} \times 0.2 \times 10^{-2}}{0.12 \times 10^{-2} \times 0.02 \times 10^{-2} \times 1}$$

$$= 20.8 \, \Omega^{-1} \text{ m}^{-1}$$

$$\text{Hence } \mu_e = \frac{\sigma_n}{ne} = \frac{20.8}{6.5 \times 10^{20} \times 1.6 \times 10^{-19}}$$

$$= 0.2 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$$





- (4) Given - ~~density~~  $n_i = 1.5 \times 10^{16} / \text{m}^3$ ,  $\mu_e = 0.13 \text{ m}^2 \text{V}^{-1} \text{s}^{-1}$ ,  $\mu_h = 0.05 \text{ m}^2 \text{V}^{-1} \text{s}^{-1}$ , impurity atom = 1 atom /  $10^8$  Silicon atoms, density (Si) =  $2.33 \times 10^3 \text{ kg/m}^3$ , atomic weight (Si) = 28.09,  $\sigma_i = ?$ ,  $\sigma_{en} = ?$

$$\sigma_i = n_i e (\mu_e + \mu_h)$$

$$= 0.432 \times 10^{-3} \Omega^{-1} \text{m}^{-1}$$

No. of Si atoms per unit volume is given by

$$n = \frac{\rho N}{M} = \frac{2.33 \times 10^3 \times 6.026 \times 10^{26}}{28.09}$$

$$= 5 \times 10^{28} / \text{m}^3$$

Now density of donor atoms (impurity) will be

$$N_D = \frac{5 \times 10^{28}}{10^8} = 5 \times 10^{20} / \text{m}^3$$

Therefore the intrinsic conductivity

$$\sigma_{en} = N_D e \mu_e$$

$$= 5 \times 10^{20} \times 1.6 \times 10^{-19} \times 0.13$$

$$= 10.4 \Omega^{-1} \text{m}^{-1}$$

- (5) Given:  $E = 100 \text{ V/m}$ ,  $R_H = -0.0125 \text{ m}^3/\text{C}$ , Sample is n-type Semiconductor  $\mu_e = 0.36 \text{ m}^2 \text{V}^{-1} \text{s}^{-1}$ ,  $J = ?$   
For n-type Semiconductor, the Hall Coefficient is

$$R_H = \frac{1}{ne} \quad \text{or} \quad n = \frac{1}{e R_H} = 5 \times 10^{20} / \text{m}^3$$

Further, electron conductivity is given by  $\sigma_e = n e \mu_e$

$$\& \sigma_e = J/E$$

Therefore  $J = \sigma_e E$   
 $= n e \mu_e E$

$$= 5 \times 10^{20} \times 1.6 \times 10^{-19} \times 0.36 \times 100$$

$$= 2880 \text{ A/m}^2$$

Teacher's Signature: \_\_\_\_\_