JAYPEE INSTITUTE OF INFORMATION TECHNOLOGY

Electronics and Communication Engineering

Signals and Systems (18B11EC214) - 2020 ODD-SEM

SOLUTION TUTORIAL-2

Sol. 1

CO₁

(a)
$$E_{\infty} = \int_0^{\infty} e^{-4t} dt = \frac{1}{4}$$
, $P_{\infty} = 0$, because $E_{\infty} < \infty$

$$\begin{array}{l} f_0 \\ \text{(b)} \ x_2(t) = e^{j(2t+\frac{\tau}{4})}, \ |x_2(t)| = 1. \ \text{Therefore,} \ E_\infty = \int_{-\infty}^\infty |x_2(t)|^2 dt = \int_{-\infty}^\infty dt = \infty, \ P_\infty = \lim_{T\to\infty} \frac{1}{2T} \int_{-T}^T |x_2(t)|^2 dt = \lim_{T\to\infty} \frac{1}{2T} \int_{-T}^T dt = \lim_{T\to\infty} 1 = 1 \end{array}$$

(c)
$$x_3(t) = \cos(t)$$
. Therefore, $E_{\infty} = \int_{-\infty}^{\infty} |x_3(t)|^2 dt = \int_{-\infty}^{\infty} \cos^2(t) dt = \infty$, $P_{\infty} = \lim_{T \to \infty} \frac{1}{2T} \int_{-T}^{T} \cos^2(t) dt = \lim_{T \to \infty} \frac{1}{2T} \int_{-T}^{T} \left(\frac{1 + \cos(2t)}{2} \right) dt = \frac{1}{2}$

(d)
$$x_1[n] = \left(\frac{1}{2}\right)^n u[n], |x_1[n]|^2 = \left(\frac{1}{4}\right)^n u[n].$$
 Therefore, $E_{\infty} = \sum_{n=-\infty}^{\infty} |x_1[n]|^2 = \sum_{n=0}^{\infty} \left(\frac{1}{4}\right)^n = \frac{4}{3}.$

$$\lim_{T \to \infty} \frac{1}{2^T} \int_{-T} |x_2(t)|^2 dt = \lim_{T \to \infty} \frac{1}{2^T} \int_{-T}^{T} dt = \lim_{T \to \infty} \frac{1}{1 - x}$$
(c) $x_3(t) = \cos(t)$. Therefore, $E_{\infty} = \int_{-\infty}^{\infty} |x_3(t)|^2 dt = \int_{-\infty}^{\infty} \cos^2(t) dt = \infty$,
$$P_{\infty} = \lim_{T \to \infty} \frac{1}{2T} \int_{-T}^{T} \cos^2(t) dt = \lim_{T \to \infty} \frac{1}{2T} \int_{-T}^{T} \left(\frac{1 + \cos(2t)}{2} \right) dt = \frac{1}{2}$$
(d) $x_1[n] = \left(\frac{1}{2}\right)^n u[n], |x_1[n]|^2 = \left(\frac{1}{4}\right)^n u[n]$. Therefore, $E_{\infty} = \sum_{n=-\infty}^{\infty} |x_1[n]|^2 = \sum_{n=0}^{\infty} \left(\frac{t}{4}\right)^n = \frac{4}{3}$.
$$P_{\infty} = 0, \quad \text{because } E_{\infty} < \infty.$$
(e) $x_2[n] = e^{j(\frac{n\pi}{2} + \frac{\pi}{6})}, |x_2[n]|^2 = 1$. Therefore, $E_{\infty} = \sum_{n=-\infty}^{\infty} |x_2[n]|^2 = \infty$,
$$P_{\infty} = \lim_{N \to \infty} \frac{1}{2N + 1} \sum_{n=-N}^{N} |x_2[n]|^2 = \lim_{N \to \infty} \frac{1}{2N + 1} \sum_{n=-N}^{N} 1 = 1$$
.

(f)
$$x_3[n] = \cos(\frac{\pi}{4}n)$$
. Therefore, $E_{\infty} = \sum_{n=-\infty}^{\infty} |x_3[n]|^2 = \sum_{n=-\infty}^{\infty} \cos^2(\frac{\pi}{4}n) = \infty$,
$$P_{\infty} = \lim_{N \to \infty} \frac{1}{2N+1} \sum_{n=-N}^{N} \cos^2(\frac{\pi}{4}n) = \lim_{N \to \infty} \frac{1}{2N+1} \sum_{n=-N}^{N} \left(\frac{1+\cos(\frac{\pi}{2}n)}{2}\right) = \frac{1}{2}$$

Sol. 2

$$x(t) = 2\cos(10t + 1) - \sin(4t - 1)$$

CO₁

Period of first term in RHS = $\frac{2\pi}{10} = \frac{\pi}{5}$ Period of second term in RHS = $\frac{2\pi}{4} = \frac{\pi}{2}$

Therefore, the overall signal is periodic with a period which is the least common multiple of the periods of the first and second terms. This is equal to π .

$$x[n] = 1 + e^{j\frac{4\pi}{7}n} - e^{j\frac{2\pi}{5}n}$$

CO₁

Period of the first term in the RHS = 1

Period of the second term in the RHS = $m(\frac{2\pi}{4\pi/7}) = 7$ (when m = 2)

Period of the third term in the RHS = $m(\frac{2\pi}{2\pi/5}) = 5$ (when m = 1)

Therefore, the overall signal x[n] is periodic with a period which is the least common multiple of the periods of the three terms in x[n]. This is equal to 35.

(a) Periodic, period = $2\pi/(4) = \pi/2$. Sol. 4

CO₁

- (b) Periodic, period = $2\pi/(\pi) = 2$.
- (c) $x(t) = \{1 + \cos(4t 2\pi/3)\}/2$. Periodic, period = $2\pi/(4) = \pi/2$.
- (a) Periodic, period = 7. Sol. 5

CO1

CO1

- (b) Not periodic.
- (c) Periodic, period = 8.
- (d) $x[n] = (1/2)[\cos(3\pi n/4) + \cos(\pi n/4)]$. Periodic, period = 8.
- (e) Periodic, period = 16.
- Sol. 6

 $y(t) = \int_{-\infty}^{t} x(\tau)dt = \int_{-\infty}^{t} (\delta(\tau+2) - \delta(\tau-2))dt =$

Therefore,

$$E_{\infty} = \int_{-2}^{2} dt = 4$$