Algebra is Clifford(1,4) over the reals : $Cl_{1,4}(\mathbb{R})$ The five dimensions are (t,x,y,z,w). It defines two sets of quaternions with one imaginary unit

CoQuaternions $(1, \mathbf{i}, \mathbf{j}, \mathbf{k})$

$$\mathbf{i} = \gamma_t$$

$$\mathbf{j} = \gamma_t \gamma_x \gamma_y \gamma_z$$

$$\mathbf{k} = \gamma_x \gamma_y \gamma_z$$

$$i^2 = 1$$

$$j^2 = -1$$

$$\mathbf{k}^2 = 1$$

$$\mathbf{ij} = \gamma_x \gamma_y \gamma_z$$

$$\mathbf{ji} = -\gamma_x \gamma_y \gamma_z$$

$$\mathbf{j}\mathbf{k} = \gamma_t$$

$$\mathbf{kj} = -\gamma_t$$

$$\mathbf{ki} = -\gamma_t \gamma_x \gamma_y \gamma_z$$

$$\mathbf{ik} = \gamma_t \gamma_x \gamma_y \gamma_z$$

$$ijk = 1$$

Quaternions (1, i, j, k)

$$oldsymbol{i} = \gamma_y \gamma_z$$

$$oldsymbol{j} = -\gamma_x \gamma_z$$

$$\mathbf{k} = \gamma_x \gamma_y$$

$$i^2 = -1$$

$$j^2 = -1$$

$$k^2 = -1$$

$$m{ij} = \gamma_x \gamma_y$$

$$oldsymbol{j}\,oldsymbol{i} = -\gamma_x\gamma_y$$

$$oldsymbol{j} oldsymbol{k} = \gamma_y \gamma_z$$

$$m{kj} = -\gamma_y \gamma_z$$

$$oldsymbol{k}oldsymbol{i}=-\gamma_x\gamma_z$$

$$m{i}m{k}=\gamma_x\gamma_z$$

$$ijk = -1$$

Imaginary unit i

$$i = \gamma_w$$
$$i^2 = -1$$

Gradient

$$\nabla = \left(\gamma_t \frac{\partial}{\partial t} + \gamma_x \frac{\partial}{\partial x} + \gamma_y \frac{\partial}{\partial y} + \gamma_z \frac{\partial}{\partial z} + \gamma_w \frac{\partial}{\partial w}\right)$$

Wavefunction: A is a constant and f is a function of (t, x, y, z, w)

$$\psi = Ae^f$$
$$\nabla \psi = A(\nabla f)e^f$$

The following symbols are defined : (a positive value is NOT required) $F: \mathcal{L} \subset \mathbb{R}^n$

E is for energy, $E \in \mathbb{R}$

m is for mass, $m \in \mathbb{R}$

p is the momentum. $p_x, p_y, p_z \in \mathbb{R}$

$$\mathbf{p} = p_x \mathbf{i} + p_y \mathbf{j} + p_z \mathbf{k}$$

$$\mathbf{p} = p_z \gamma_x \gamma_y - p_y \gamma_x \gamma_z + p_x \gamma_y \gamma_z$$

Exponential function f

$$f_1 = -mw + (p_y y + p_x x + p_z z - Et) \gamma_w$$

$$f_2 = mw + (-p_z z - p_u y - p_x x - Et) \gamma_w$$

$$f_3 = mw + (p_y y + p_x x + p_z z - Et) \gamma_w$$

$$f_4 = -mw + (-p_z z - p_u y - p_x x - Et) \gamma_w$$

Gradient for f

$$\nabla f_1 = m\gamma_w - E\gamma_t\gamma_w - p_x\gamma_x\gamma_w - p_y\gamma_y\gamma_w - p_z\gamma_z\gamma_w$$

$$\nabla f_2 = -m\gamma_w - E\gamma_t\gamma_w + p_x\gamma_x\gamma_w + p_y\gamma_y\gamma_w + p_z\gamma_z\gamma_w$$

$$\nabla f_3 = -m\gamma_w - E\gamma_t\gamma_w - p_x\gamma_x\gamma_w - p_y\gamma_y\gamma_w - p_z\gamma_z\gamma_w$$

$$\nabla f_4 = m\gamma_w - E\gamma_t\gamma_w + p_x\gamma_x\gamma_w + p_y\gamma_y\gamma_w + p_z\gamma_z\gamma_w$$

Square of the gradient

$$\nabla f_1^2 = -m^2 - p_z^2 + E^2 - p_y^2 - p_x^2$$

$$\nabla f_2^2 = -m^2 - p_z^2 + E^2 - p_y^2 - p_x^2$$

$$\nabla f_3^2 = -m^2 - p_z^2 + E^2 - p_y^2 - p_z^2$$

$$\nabla f_4^2 = -m^2 - p_z^2 + E^2 - p_y^2 - p_x^2$$

Dirac

$$0 = (\gamma_0 \frac{\partial}{\partial t} + \gamma_1 \frac{\partial}{\partial x} + \gamma_2 \frac{\partial}{\partial y} + \gamma_3 \frac{\partial}{\partial z} + im)\psi$$

With the above gradients, identify the Dirac algebra aka gamma matrices

$$\gamma_0 = \gamma_t \gamma_w$$

$$\gamma_0^2 = 1$$

$$\gamma_1 = -\gamma_x \gamma_w$$

$$\gamma_1^2 = -1$$

$$\gamma_2 = -\gamma_y \gamma_w$$

$$\gamma_2^2 = -1$$

$$\gamma_3 = -\gamma_z \gamma_w$$

$$\gamma_3^2 = -1$$

$$\gamma_5 = -\gamma_t \gamma_x \gamma_y \gamma_z \gamma_w$$

$$\gamma_5^2 = 1$$

Simple Constants K (exactly the gradient)

$$K_{1} = \mathbf{j}i(\mathbf{k}E - \mathbf{j}m + \mathbf{i}\mathbf{p})$$

$$K_{1} = m\gamma_{w} - E\gamma_{t}\gamma_{w} - p_{x}\gamma_{x}\gamma_{w} - p_{y}\gamma_{y}\gamma_{w} - p_{z}\gamma_{z}\gamma_{w}$$

$$K_{2} = \mathbf{j}i(\mathbf{k}E + \mathbf{j}m - \mathbf{i}\mathbf{p})$$

$$K_{2} = -m\gamma_{w} - E\gamma_{t}\gamma_{w} + p_{x}\gamma_{x}\gamma_{w} + p_{y}\gamma_{y}\gamma_{w} + p_{z}\gamma_{z}\gamma_{w}$$

$$K_{3} = \mathbf{j}i(\mathbf{k}E + \mathbf{j}m + \mathbf{i}\mathbf{p})$$

$$K_{3} = -m\gamma_{w} - E\gamma_{t}\gamma_{w} - p_{x}\gamma_{x}\gamma_{w} - p_{y}\gamma_{y}\gamma_{w} - p_{z}\gamma_{z}\gamma_{w}$$

$$K_{4} = \mathbf{j}i(\mathbf{k}E - \mathbf{j}m - \mathbf{i}\mathbf{p})$$

$$K_{4} = m\gamma_{w} - E\gamma_{t}\gamma_{w} + p_{x}\gamma_{x}\gamma_{w} + p_{y}\gamma_{y}\gamma_{w} + p_{z}\gamma_{z}\gamma_{w}$$

Mixed Constants A (built from simple constants and the coquaternions) A_1

$$\begin{pmatrix} A_1^1 \\ A_1^2 \\ A_1^3 \\ A_1^4 \end{pmatrix} = \begin{pmatrix} +K_1 - K_4 \mathbf{i} - K_3 \mathbf{j} + K_2 \mathbf{k} \\ +K_1 + K_4 \mathbf{i} + K_3 \mathbf{j} + K_2 \mathbf{k} \\ -K_1 + K_4 \mathbf{i} - K_3 \mathbf{j} + K_2 \mathbf{k} \\ -K_1 - K_4 \mathbf{i} + K_3 \mathbf{j} + K_2 \mathbf{k} \end{pmatrix}$$

 A_2

$$\begin{pmatrix} A_2^1 \\ A_2^2 \\ A_2^3 \\ A_2^4 \end{pmatrix} = \begin{pmatrix} +K_2 - K_3 \mathbf{i} - K_4 \mathbf{j} + K_1 \mathbf{k} \\ +K_2 + K_3 \mathbf{i} + K_4 \mathbf{j} + K_1 \mathbf{k} \\ -K_2 + K_3 \mathbf{i} - K_4 \mathbf{j} + K_1 \mathbf{k} \\ -K_2 - K_3 \mathbf{i} + K_4 \mathbf{j} + K_1 \mathbf{k} \end{pmatrix}$$

 A_3

$$\begin{pmatrix} A_3^1 \\ A_3^2 \\ A_3^3 \\ A_3^4 \end{pmatrix} = \begin{pmatrix} +K_3 - K_2 \mathbf{i} - K_1 \mathbf{j} + K_4 \mathbf{k} \\ +K_3 + K_2 \mathbf{i} + K_1 \mathbf{j} + K_4 \mathbf{k} \\ -K_3 + K_2 \mathbf{i} - K_1 \mathbf{j} + K_4 \mathbf{k} \\ -K_3 - K_2 \mathbf{i} + K_1 \mathbf{j} + K_4 \mathbf{k} \end{pmatrix}$$

 A_4

$$\begin{pmatrix} A_4^1 \\ A_4^2 \\ A_4^3 \\ A_4^4 \end{pmatrix} = \begin{pmatrix} +K_4 - K_1 \mathbf{i} - K_2 \mathbf{j} + K_3 \mathbf{k} \\ +K_4 + K_1 \mathbf{i} + K_2 \mathbf{j} + K_3 \mathbf{k} \\ -K_4 + K_1 \mathbf{i} - K_2 \mathbf{j} + K_3 \mathbf{k} \\ -K_4 - K_1 \mathbf{i} + K_2 \mathbf{j} + K_3 \mathbf{k} \end{pmatrix}$$

Details about full solutions (built from mixed constants and the imaginary unit) ψ_1

$$\psi_{1}^{1} \equiv (A_{1}^{1} + iA_{1}^{1}) = +K_{1} - K_{4}\mathbf{i} - K_{3}\mathbf{j} + K_{2}\mathbf{k} + i(+K_{1} - K_{4}\mathbf{i} - K_{3}\mathbf{j} + K_{2}\mathbf{k})$$

$$\psi_{1}^{1} = E - m$$

$$+ (-E + m)\gamma_{t} - p_{x}\gamma_{x} - p_{y}\gamma_{y} - p_{z}\gamma_{z} + (-E + m)\gamma_{w}$$

$$+ p_{x}\gamma_{t}\gamma_{x} + p_{y}\gamma_{t}\gamma_{y} - p_{z}\gamma_{x}\gamma_{y} + p_{z}\gamma_{t}\gamma_{z} + p_{y}\gamma_{x}\gamma_{z} - p_{x}\gamma_{y}\gamma_{z} + (-E + m)\gamma_{t}\gamma_{w} - p_{x}\gamma_{x}\gamma_{w} - p_{y}\gamma_{y}\gamma_{w} - p_{z}\gamma_{z}\gamma_{w}$$

$$+ p_{z}\gamma_{t}\gamma_{x}\gamma_{y} - p_{y}\gamma_{t}\gamma_{x}\gamma_{z} + p_{x}\gamma_{t}\gamma_{y}\gamma_{z} + (E + m)\gamma_{x}\gamma_{y}\gamma_{z} - p_{x}\gamma_{t}\gamma_{x}\gamma_{w} - p_{y}\gamma_{t}\gamma_{y}\gamma_{w} + p_{z}\gamma_{x}\gamma_{y}\gamma_{w} - p_{z}\gamma_{t}\gamma_{z}\gamma_{w} + p_{x}\gamma_{y}\gamma_{z}\gamma_{w}$$

$$+ (-E - m)\gamma_{t}\gamma_{x}\gamma_{y}\gamma_{z} + p_{z}\gamma_{t}\gamma_{x}\gamma_{y}\gamma_{w} - p_{y}\gamma_{t}\gamma_{x}\gamma_{z}\gamma_{w} + p_{x}\gamma_{t}\gamma_{y}\gamma_{z}\gamma_{w} + (E + m)\gamma_{x}\gamma_{y}\gamma_{z}\gamma_{w}$$

$$+ (E + m)\gamma_{t}\gamma_{x}\gamma_{y}\gamma_{z}\gamma_{w}$$

$$\psi_1^1 K_1 = 0$$

$$\psi_1^2 \equiv (A_1^1 - iA_1^1) = +K_1 - K_4 \mathbf{i} - K_3 \mathbf{j} + K_2 \mathbf{k} - i(+K_1 - K_4 \mathbf{i} - K_3 \mathbf{j} + K_2 \mathbf{k})$$

$$\begin{split} & \psi_1^2 = -E + m \\ & + (E - m) \gamma_1 + p_x \gamma_x + p_y \gamma_y + p_z \gamma_z + (-E + m) \gamma_w \\ & + p_z \gamma_1 \gamma_x - p_y \gamma_1 \gamma_y + p_z \gamma_z \gamma_y - p_z \gamma_1 \gamma_z + (-E + m) \gamma_w \\ & - p_z \gamma_1 \gamma_x - p_y \gamma_1 \gamma_y + p_z \gamma_z \gamma_y - p_z \gamma_1 \gamma_z + (-E - m) \gamma_z \gamma_y \gamma_z - p_z \gamma_1 \gamma_z \gamma_w - p_y \gamma_1 \gamma_y \gamma_w + p_z \gamma_z \gamma_w - p_z \gamma_z \gamma_w \\ & - p_z \gamma_1 \gamma_x - p_y \gamma_1 \gamma_y \gamma_z + p_z \gamma_1 \gamma_y \gamma_z + (-E - m) \gamma_z \gamma_y \gamma_z - p_z \gamma_1 \gamma_y \gamma_w - p_y \gamma_1 \gamma_y \gamma_w + p_z \gamma_2 \gamma_w - p_z \gamma_1 \gamma_z \gamma_w - p_y \gamma_2 \gamma_w \\ & + (E + m) \gamma_1 \gamma_z \gamma_y \gamma_z \gamma_w \\ & + (E + m) \gamma_1 \gamma_z \gamma_y \gamma_z \gamma_w \\ & \psi_1^2 K_1 = 0 \\ & \psi_1^2 = (A_1^1 + iA_1^2) = + K_1 - K_4 \mathbf{i} - K_3 \mathbf{j} + K_2 \mathbf{k} + i(+K_1 + K_4 \mathbf{i} + K_3 \mathbf{j} + K_2 \mathbf{k}) \\ & \psi_1^2 = -E - m \\ & + (-E - m) \gamma_1 - p_x \gamma_x - p_y \gamma_y - p_z \gamma_z + (-E + m) \gamma_w \\ & - p_z \gamma_1 \gamma_z - p_z \gamma_1 \gamma_y - p_z \gamma_1 \gamma_z + p_z \gamma_1 \gamma_z + p_z \gamma_1 \gamma_z + (-E + m) \gamma_1 \gamma_w - p_z \gamma_2 \gamma_w - p_y \gamma_2 \gamma_w - p_z \gamma_2 \gamma_w \\ & - p_z \gamma_1 \gamma_z - p_z \gamma_1 \gamma_y - p_z \gamma_1 \gamma_z + p_z \gamma_1 \gamma_z \gamma_z - p_z \gamma_1 \gamma_2 \gamma_w - p_y \gamma_1 \gamma_2 \gamma_w + p_z \gamma_1 \gamma_2 \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w - p_z \gamma_2 \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w + p_z \gamma_1 \gamma_2 \gamma_y \gamma_z \gamma_w + (E + m) \gamma_1 \gamma_2 \gamma_2 \gamma_z \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w + p_z \gamma_1 \gamma_2 \gamma_y \gamma_z \gamma_w + (E + m) \gamma_1 \gamma_2 \gamma_2 \gamma_z \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w + p_z \gamma_1 \gamma_2 \gamma_y \gamma_2 \gamma_w + (E + m) \gamma_1 \gamma_2 \gamma_2 \gamma_z \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w - p_z \gamma_1 \gamma_2 \gamma_w + (E + m) \gamma_1 \gamma_2 \gamma_2 \gamma_2 \gamma_w + p_z \gamma_1 \gamma_2 \gamma_2 \gamma_z \gamma_w + p_z \gamma_1 \gamma_2 \gamma_2 \gamma_w + p_z \gamma_1 \gamma_2 \gamma_2 \gamma_w + p_z \gamma_1 \gamma_2 \gamma_2 \gamma_z \gamma_w + p_z \gamma_1 \gamma_2 \gamma_2 \gamma_z \gamma_w + p_z \gamma_1 \gamma_2 \gamma_2 \gamma_w + p_z \gamma_1 \gamma_2 \gamma_2 \gamma_z \gamma_w + p_z \gamma_1 \gamma_2 \gamma_2 \gamma_z \gamma_z$$

$$\begin{split} &\psi_1^{13}K_1 = 0 \\ &\psi_1^{14} = (A_1^2 - iA_1^3) = +K_1 + K_4 \mathbf{i} + K_3 \mathbf{j} + K_2 \mathbf{k} - i(-K_1 + K_4 \mathbf{i} - K_3 \mathbf{j} + K_2 \mathbf{k}) \\ &\psi_1^{14} = E - m \\ &\quad + (-E + m)\gamma_1 - p_2\gamma_2 - p_3\gamma_3 - p_2\gamma_2 + (E + m)\gamma_6 \\ &\quad + p_2\gamma_1\gamma_2 + p_3\gamma_1\gamma_2 + p_2\gamma_1\gamma_3 + p_2\gamma_1\gamma_2 - p_3\gamma_2\gamma_3 + p_2\gamma_3\gamma_3 + p_2\gamma_1\gamma_2 + p_2\gamma_1\gamma_2 + p_3\gamma_1\gamma_3 - p_2\gamma_1\gamma_3 + p_3\gamma_1\gamma_2 - p_3\gamma_1\gamma_3 + p_3\gamma_1\gamma_2 - p_3\gamma_1\gamma_2 + p_3\gamma_1\gamma_2 - p_3\gamma_1\gamma_2 + p_3\gamma_1\gamma_2 - p$$

$$\begin{split} &\psi_1^{20} K_1 = 0 \\ &\psi_1^{20} = L(A_1^2 - iA_1^3) = -K_1 - K_2\mathbf{i} + K_3\mathbf{j} + K_2\mathbf{k} - i(-K_1 + K_4\mathbf{i} - K_3\mathbf{j} + K_2\mathbf{k}) \\ &\psi_1^{20} = E - m \\ &\quad + (-E + m)\gamma_t - p_x\gamma_x - p_y\gamma_y - p_z\gamma_z + (-E - m)\gamma_w \\ &\quad + p_y\gamma_t\gamma_x + p_y\gamma_t\gamma_y + p_z\gamma_z\gamma_y + p_z\gamma_t\gamma_z - p_y\gamma_z\gamma_z + p_z\gamma_y\gamma_z + (E + m)\gamma_t\gamma_w + p_x\gamma_x\gamma_w + p_y\gamma_y\gamma_w + p_z\gamma_z\gamma_w \\ &\quad - p_z\gamma_t\gamma_z\gamma_y + p_y\gamma_t\gamma_x\gamma_z - p_z\gamma_t\gamma_y\gamma_z + (-E - m)\gamma_x\gamma_y\gamma_z - p_z\gamma_t\gamma_y\gamma_x + (-E + m)\gamma_x\gamma_y\gamma_z\gamma_w + p_y\gamma_x\gamma_x\gamma_w + p_x\gamma_y\gamma_z\gamma_w \\ &\quad + (E + m)\gamma_t\gamma_x\gamma_y\gamma_z - p_z\gamma_t\gamma_y\gamma_y\gamma_w + p_y\gamma_t\gamma_z\gamma_z\gamma_w - p_z\gamma_t\gamma_y\gamma_z\gamma_w + (-E + m)\gamma_x\gamma_y\gamma_z\gamma_w \\ &\quad + (E - m)\gamma_t\gamma_x\gamma_y\gamma_z - p_z\gamma_t\gamma_z\gamma_w + p_y\gamma_t\gamma_z\gamma_z\gamma_w - p_z\gamma_t\gamma_y\gamma_z\gamma_w + (-E + m)\gamma_x\gamma_y\gamma_z\gamma_w \\ &\quad + (E + m)\gamma_t\gamma_x\gamma_y\gamma_z - p_z\gamma_t\gamma_z + (-E - m)\gamma_w \\ &\quad + (E + m)\gamma_t + p_x\gamma_x + p_y\gamma_y + p_z\gamma_z + (-E - m)\gamma_w \\ &\quad + (E + m)\gamma_t + p_x\gamma_x + p_y\gamma_y + p_z\gamma_z + (-E - m)\gamma_w \\ &\quad + (E + m)\gamma_t + p_x\gamma_x + p_y\gamma_y + p_z\gamma_z + (-E - m)\gamma_w \\ &\quad + p_x\gamma_t\gamma_x + p_y\gamma_t\gamma_y - p_z\gamma_t\gamma_y + p_y\gamma_t\gamma_z + p_y\gamma_z - p_z\gamma_y\gamma_z + (E + m)\gamma_t\gamma_w + p_x\gamma_w\gamma_w + p_y\gamma_y\gamma_w + p_z\gamma_z\gamma_w \\ &\quad - p_z\gamma_t\gamma_x\gamma_y + p_y\gamma_t\gamma_x\gamma_z - p_z\gamma_t\gamma_y\gamma_z + (-E + m)\gamma_x\gamma_y\gamma_z - p_x\gamma_t\gamma_y\gamma_w - p_y\gamma_t\gamma_y\gamma_w + (-E + m)\gamma_x\gamma_y\gamma_w - p_z\gamma_t\gamma_z\gamma_w - p_y\gamma_x\gamma_z\gamma_w + p_y\gamma_y\gamma_z\gamma_w \\ &\quad + (E - m)\gamma_t\gamma_x\gamma_y\gamma_z\gamma_w - p_z\gamma_t\gamma_x\gamma_y\gamma_w + p_y\gamma_t\gamma_x\gamma_x\gamma_w - p_y\gamma_y\gamma_y\gamma_w + (-E + m)\gamma_x\gamma_y\gamma_z\gamma_w \\ &\quad + (E - m)\gamma_t\gamma_x\gamma_y\gamma_z\gamma_w - p_z\gamma_t\gamma_z\gamma_y\gamma_w + p_y\gamma_t\gamma_x\gamma_x\gamma_w + p_x\gamma_y\gamma_y\gamma_w + p_z\gamma_z\gamma_w + p_z\gamma_t\gamma_w\gamma_y\gamma_y\gamma_w + p_z\gamma_z\gamma_w + p_y\gamma_t\gamma_x\gamma_x\gamma_w + p_z\gamma_t\gamma_x\gamma_w + p_z\gamma_t\gamma_x\gamma_w + p_z\gamma_t\gamma_x\gamma_y\gamma_x\gamma_w + p_z\gamma_t\gamma_x\gamma_x\gamma_w + p_z\gamma_t\gamma_x\gamma_w + p_z\gamma_t\gamma_x\gamma$$

 $+(-E+m)\gamma_t\gamma_x\gamma_y\gamma_z-p_z\gamma_t\gamma_x\gamma_y\gamma_w+p_y\gamma_t\gamma_x\gamma_z\gamma_w-p_x\gamma_t\gamma_y\gamma_z\gamma_w+(E-m)\gamma_x\gamma_y\gamma_z\gamma_w$

 ψ_2

 $+ (E-m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w$

$$\begin{split} & \psi_2^2 \, K_2 = 0 \\ & \psi_2^2 = (A_2^1 - iA_3^2) = + K_2 - K_3 \mathbf{i} - K_4 \mathbf{j} + K_1 \mathbf{k} - i(-K_2 + K_3 \mathbf{i} - K_4 \mathbf{j} + K_1 \mathbf{k}) \\ & \psi_2^0 = E + m \\ & + (-E - m) \gamma_t + p_x \gamma_x + p_y \gamma_y + p_x \gamma_z + p_x \gamma_t \gamma_z + p_y \gamma_t \gamma_z + (-E - m) \gamma_w \\ & + p_x \gamma_t \gamma_x - p_y \gamma_t \gamma_y - p_x \gamma_z \gamma_z - p_x \gamma_t \gamma_z + p_y \gamma_t \gamma_z + (-E - m) \gamma_w \\ & + p_x \gamma_t \gamma_x - p_y \gamma_t \gamma_y - p_x \gamma_t \gamma_z + p_x \gamma_t \gamma_y \gamma_z + (-E + m) \gamma_x \gamma_y \gamma_z + p_x \gamma_t \gamma_x \gamma_w + p_y \gamma_t \gamma_y \gamma_w + p_x \gamma_x \gamma_w + p_y \gamma_t \gamma_x \gamma_w + p_y \gamma_t \gamma_y \gamma_w + p_x \gamma_t \gamma_x \gamma_w + p_y \gamma_t \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_y \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_x \gamma_x \gamma_y \gamma_x \gamma_x \gamma_x \gamma_x \gamma_x$$

$$\begin{split} & \psi_2^{21} K_2 = 0 \\ & \psi_2^{22} = (A_3^2 - iA_3^2) = -K_2 + K_3 \mathbf{i} - K_4 \mathbf{j} + K_1 \mathbf{k} - i(-K_2 + K_3 \mathbf{i} - K_4 \mathbf{j} + K_1 \mathbf{k}) \\ & \psi_2^{22} = E + m \\ & + (-E - m) \gamma_1 + p_x \gamma_x + p_y \gamma_y + p_z \gamma_z + (E + m) \gamma_w \\ & - p_z \gamma_1 \gamma_x - p_y \gamma_1 \gamma_y + p_z \gamma_2 \gamma_y - p_z \gamma_1 \gamma_z + p_y \gamma_z \gamma_z - p_z \gamma_y \gamma_z + (E + m) \gamma_t \gamma_w - p_z \gamma_x \gamma_w - p_y \gamma_t \gamma_w - p_z \gamma_t \gamma_z \gamma_w \\ & + p_z \gamma_t \gamma_x \gamma_y - p_x \gamma_t \gamma_z \gamma_y + p_z \gamma_t \gamma_z \gamma_y + (E + m) \gamma_z \gamma_y - p_z \gamma_t \gamma_z \gamma_w - p_y \gamma_t \gamma_y \gamma_w - p_z \gamma_t \gamma_z \gamma_w + p_y \gamma_z \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_y \gamma_z \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_z \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_z \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_z \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_z \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_z \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_z \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E - m) \gamma_t \gamma_x \gamma_y \gamma_x \gamma_w \\ & + (E$$

$$\begin{split} &\psi_2^{20}K_2 = 0 \\ &\psi_2^{20} = (A_3^2 - iA_3^2) = -K_2 - K_3\mathbf{i} + K_4\mathbf{j} + K_1\mathbf{k} - i(-K_2 + K_3\mathbf{i} - K_4\mathbf{j} + K_1\mathbf{k}) \\ &\psi_2^{20} = E + m \\ &\quad + (-E - m)\gamma_t + p_x\gamma_x + p_y\gamma_y + p_z\gamma_z + (-E + m)\gamma_w \\ &\quad - p_x\gamma_t\gamma_w - p_y\gamma_t\gamma_w - p_z\gamma_z\gamma_y - p_z\gamma_t\gamma_z + p_x\gamma_t\gamma_z + p_y\gamma_z\gamma_z + p_x\gamma_y\gamma_z + p_x\gamma_t\gamma_y + p_y\gamma_z\gamma_x + p_x\gamma_t\gamma_y\gamma_y + p_z\gamma_t\gamma_y\gamma_y + p_z\gamma_t\gamma_y\gamma_z\gamma_w + (-E - m)\gamma_x\gamma_y\gamma_z\gamma_w + p_z\gamma_t\gamma_y\gamma_x\gamma_w + p_z\gamma_t\gamma_y\gamma_y\gamma_y + p_z\gamma_t\gamma_z\gamma_w + p_z\gamma_t\gamma_y\gamma_y\gamma_y + (-E - m)\gamma_x\gamma_y\gamma_z\gamma_w + p_z\gamma_t\gamma_z\gamma_w +$$

 $+(-E+m)\gamma_t\gamma_x\gamma_y\gamma_z+p_z\gamma_t\gamma_x\gamma_y\gamma_w-p_y\gamma_t\gamma_x\gamma_z\gamma_w+p_x\gamma_t\gamma_y\gamma_z\gamma_w+(E-m)\gamma_x\gamma_y\gamma_z\gamma_w$

 ψ_3

 $+(E-m)\gamma_t\gamma_r\gamma_u\gamma_s\gamma_w$

$$\begin{split} & \psi_3^3 K_3 = 0 \\ & \psi_3^{30} = (A_3^2 - iA_3^1) = +K_3 + K_2 \mathbf{i} + K_1 \mathbf{j} + K_4 \mathbf{k} - i(+K_3 - K_2 \mathbf{i} - K_1 \mathbf{j} + K_4 \mathbf{k}) \\ & \psi_3^{30} = -E - m \\ & + (E + m) \gamma_1 + p_2 \gamma_2 + p_2 \gamma_3 + p_2 \gamma_3 \gamma_2 + (E - m) \gamma_2 \\ & - p_2 \gamma_1 \gamma_2 - p_3 \gamma_2 \gamma_3 + p_2 \gamma_3 \gamma_3 + p_2 \gamma_3 \gamma_2 + p_2 \gamma_3 \gamma_2 + (-E + m) \gamma_1 \gamma_2 - p_2 \gamma_2 \gamma_2 - p_3 \gamma_2 \gamma_3 - p_2 \gamma_1 \gamma_2 \gamma_3 + p_2 \gamma_1 \gamma_2 \gamma_2 + p_2 \gamma_1 \gamma_2 \gamma_3 + p_2 \gamma_1 \gamma_2 \gamma_2 + (-E - m) \gamma_2 \gamma_2 \gamma_2 + p_2 \gamma_1 \gamma_2 \gamma_3 + p_2 \gamma_1 \gamma_2 \gamma_2 + (-E - m) \gamma_2 \gamma_2 \gamma_2 \gamma_3 + p_2 \gamma_1 \gamma_2 \gamma_2 \gamma_3 + p_2 \gamma_2 \gamma_2 \gamma_3 + (-E - m) \gamma_2 \gamma_2 \gamma_2 \gamma_3 + p_2 \gamma_2 \gamma_2 \gamma_3 + p_2 \gamma_2 \gamma_2 \gamma_3 + (-E - m) \gamma_1 \gamma_3 - p_2 \gamma_2 \gamma_3 - p_2 \gamma_2 \gamma_2 + (-E - m) \gamma_2 \gamma_2 + (-E + m) \gamma_1 \gamma_3 - p_2 \gamma_2 \gamma_3 - p_2 \gamma_2 \gamma_2 \gamma_2 + (-E - m) \gamma_2 \gamma_2 \gamma_2 + p_2 \gamma_2 \gamma_3 \gamma_3 + p_2 \gamma_2 \gamma_2 \gamma_2 \gamma_2 + p_2 \gamma_2 \gamma_2 \gamma_2 +$$

$$\begin{split} & \psi_3^{25} K_3 = 0 \\ & \psi_3^{25} = (A_3^4 - iA_3^4) = -K_3 - K_2 \mathbf{i} + K_1 \mathbf{j} + K_4 \mathbf{k} - i(+K_3 - K_2 \mathbf{i} - K_1 \mathbf{j} + K_4 \mathbf{k}) \\ & \psi_3^{25} = -E - m \\ & + (E + m) \gamma_1 + p_2 \gamma_2 + p_3 \gamma_3 + p_2 \gamma_2 + (-E + m) \gamma_w \\ & - p_2 \gamma_1 \gamma_2 - p_3 \gamma_1 \gamma_2 + p_2 \gamma_2 \gamma_2 - p_3 \gamma_2 \gamma_2 + p_2 \gamma_3 \gamma_2 + (E - m) \gamma_1 \gamma_2 \gamma_w + p_2 \gamma_2 \gamma_w + p_3 \gamma_3 \gamma_w + p_2 \gamma_1 \gamma_2 \gamma_w \\ & - p_2 \gamma_1 \gamma_2 \gamma_2 + p_3 \gamma_1 \gamma_2 \gamma_2 - p_2 \gamma_1 \gamma_2 \gamma_3 + (-E + m) \gamma_2 \gamma_2 - p_3 \gamma_1 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_w + p_2 \gamma_3 \gamma_3 \gamma_w + p_2 \gamma_1 \gamma_2 \gamma_w \\ & + (E - m) \gamma_1 \gamma_2 \gamma_3 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_2 + p_3 \gamma_1 \gamma_2 \gamma_w + (-E - m) \gamma_2 \gamma_3 \gamma_2 \gamma_w \\ & + (E + m) \gamma_1 \gamma_2 \gamma_3 \gamma_2 \gamma_w \\ & + (E + m) \gamma_1 \gamma_2 \gamma_3 \gamma_2 \gamma_w \\ & \psi_3^{25} K_3 = 0 \\ & \psi_3^{25} = (A_3^4 + iA_3^2) = -K_3 - K_2 \mathbf{i} + K_1 \mathbf{j} + K_4 \mathbf{k} + i(+K_3 + K_2 \mathbf{i} + K_1 \mathbf{j} + K_4 \mathbf{k}) \\ & \psi_3^{27} = -E + m \\ & + (-E + m) \gamma_1 - p_2 \gamma_2 - p_3 \gamma_3 - p_2 \gamma_1 \gamma_2 + (-E + m) \gamma_w \\ & - p_2 \gamma_1 \gamma_2 - p_3 \gamma_1 \gamma_3 - p_2 \gamma_1 \gamma_2 - p_2 \gamma_1 \gamma_2 + p_3 \gamma_2 \gamma_2 - p_2 \gamma_2 \gamma_2 + (E - m) \gamma_1 \gamma_w + p_2 \gamma_2 \gamma_w + p_3 \gamma_3 \gamma_w + p_2 \gamma_2 \gamma_w \\ & - p_2 \gamma_1 \gamma_2 - p_3 \gamma_1 \gamma_3 - p_2 \gamma_1 \gamma_2 \gamma_3 \gamma_2 + (-E - m) \gamma_2 \gamma_3 - p_2 \gamma_1 \gamma_2 \gamma_w + p_3 \gamma_3 \gamma_w + p_3 \gamma_2 \gamma_w + p_2 \gamma_2 \gamma_w \\ & + (E + m) \gamma_1 \gamma_2 - p_2 \gamma_2 \gamma_2 \gamma_2 + p_3 \gamma_1 \gamma_2 + (-E - m) \gamma_2 \gamma_3 - p_2 \gamma_1 \gamma_2 \gamma_w + p_3 \gamma_3 \gamma_3 \gamma_w + p_2 \gamma_2 \gamma_2 \gamma_w + p_3 \gamma_3 \gamma_2 \gamma_w \\ & + (E + m) \gamma_1 \gamma_2 \gamma_3 \gamma_3 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_3 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_3 \gamma_2 \gamma_2 + (E - m) \gamma_1 \gamma_3 \gamma_3 \gamma_3 \gamma_w + (-E - m) \gamma_2 \gamma_3 \gamma_2 \gamma_w \\ & + (E + m) \gamma_1 \gamma_2 \gamma_3 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_3 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_3 \gamma_3 \gamma_4 + (-E - m) \gamma_2 \gamma_3 \gamma_3 \gamma_w + p_2 \gamma_1 \gamma_2 \gamma_w - p_3 \gamma_2 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_w \\ & + (E + m) \gamma_1 \gamma_2 \gamma_3 \gamma_3 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_3 \gamma_3 \gamma_4 + (-E + m) \gamma_4 \gamma_3 \gamma_3 \gamma_4 + (-E - m) \gamma_2 \gamma_3 \gamma_3 \gamma_w + p_2 \gamma_1 \gamma_2 \gamma_w + p_3 \gamma_2 \gamma_2 \gamma_w + p_3 \gamma_3 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_w - p_3 \gamma_2 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_w \\ & + (E + m) \gamma_1 \gamma_2 \gamma_3 \gamma_3 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_1 \gamma_2 \gamma_w - p_3 \gamma_2 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_w - p_3 \gamma_1 \gamma_2 \gamma_w - p_3 \gamma_2 \gamma_2 \gamma_w + p_3 \gamma_1 \gamma_2 \gamma_w - p_3 \gamma_1 \gamma_2 \gamma_w + p_3$$

$$\begin{split} & \frac{4}{3}^{30}K_{3} = 0 \\ & \frac{4}{3}^{30} = (A_{3}^{4} - iA_{3}^{4}) = -K_{3} - K_{2}\mathbf{i} + K_{1}\mathbf{j} + K_{4}\mathbf{k} - i(-K_{3} + K_{2}\mathbf{i} - K_{1}\mathbf{j} + K_{4}\mathbf{k}) \\ & \frac{2}{3}^{30} = E + m \\ & + (-E - m)\gamma_{1} - p_{x}\gamma_{x} - p_{y}\gamma_{y} - p_{z}\gamma_{z} + (-E + m)\gamma_{w} \\ & + p_{x}\gamma_{x}\gamma_{x} + p_{y}\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{z} + p_{x}\gamma_{y}\gamma_{z} + (E - m)\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{w} + p_{y}\gamma_{x}\gamma_{w} - p_{y}\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{w} - p_{y}\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{y} + p_{x}\gamma_{x}\gamma_{y}\gamma_{w} + p_{x}\gamma_{x}\gamma_{y}\gamma_{w} + p_{x}\gamma_{x}\gamma_{y}\gamma_{w} + p_{x}\gamma_{x}\gamma_{y}\gamma_{w} + p_{x}\gamma_{x}\gamma_{x}\gamma_{w} - p_{x}\gamma_{1}\gamma_{y}\gamma_{x}\gamma_{w} + (E - m)\gamma_{x}\gamma_{y}\gamma_{x}\gamma_{w} - p_{x}\gamma_{1}\gamma_{x}\gamma_{w} + p_{x}\gamma_{x}\gamma_{y}\gamma_{w} + p_{x}\gamma_{x}\gamma_{y}\gamma_{w} - p_{x}\gamma_{1}\gamma_{y}\gamma_{x}\gamma_{w} + p_{x}\gamma_{x}\gamma_{y}\gamma_{w} - p_{x}\gamma_{1}\gamma_{y}\gamma_{x}\gamma_{w} + p_{x}\gamma_{x}\gamma_{y}\gamma_{w} - p_{x}\gamma_{1}\gamma_{x}\gamma_{w} + p_{x}\gamma_{x}\gamma_{x}\gamma_{w} + p_{x}\gamma_{x$$

 ψ_4

$$\begin{split} & \psi_{1}^{2}K_{4} = 0 \\ & \psi_{1}^{2} = (A_{1}^{1} - iA_{1}^{1}) = +K_{4} - K_{1}\mathbf{i} - K_{2}\mathbf{j} + K_{3}\mathbf{k} - i(+K_{4} - K_{1}\mathbf{i} - K_{2}\mathbf{j} + K_{3}\mathbf{k}) \\ & \psi_{2}^{2} = -E + m \\ & + (E - m) \gamma_{1} - p_{2}\gamma_{2} - p_{3}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} + (-E + m) \gamma_{w} \\ & + p_{2}\gamma_{1}\gamma_{2} + p_{3}\gamma_{1}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} + p_{2}\gamma_{1}\gamma_{2} + p_{2}\gamma_{1}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} + (-E + m) \gamma_{1}w + p_{2}\gamma_{2}\gamma_{w} + p_{3}\gamma_{1}\gamma_{w} + p_{2}\gamma_{1}\gamma_{x} + p_{3}\gamma_{1}\gamma_{w} + p_{3}\gamma_{1}\gamma_{x} + p_{3}\gamma_{1}\gamma_{w} + p_{2}\gamma_{1}\gamma_{2}\gamma_{w} + p_{3}\gamma_{2}\gamma_{w} + p_{3}\gamma_{2}\gamma_{2}\gamma_{w} + p_{3}\gamma_{2}\gamma_{2}\gamma_{w} + p_{3}\gamma_{3}\gamma_{w} + p_{2}\gamma_{2}\gamma_{w} + p_{3}\gamma_{3}\gamma_{w} + p_{2}\gamma_{2}\gamma_{w} + p_{3}\gamma_{3}\gamma_{w} + p_{2}\gamma_{2}\gamma_{w} + p_{3}\gamma_{3}\gamma_{w} + p_{2}\gamma_{2}\gamma_{2}\gamma_{w} + p_{3}\gamma_{3}\gamma_{3}\gamma_{w} + p_{2}\gamma_{2}\gamma_{3}\gamma_{w} + p_{2}\gamma_{2}\gamma_{3}\gamma_{w} + p_{2}\gamma_{2}\gamma_{2}\gamma_{w} + p_{2}\gamma_{2}\gamma_{2}\gamma_{w}$$

$$\begin{split} &\psi_{2}^{25}K_{4} = 0 \\ &\psi_{1}^{26} = (A_{1}^{4} - iA_{1}^{4}) = -K_{4} - K_{1}\mathbf{i} + K_{2}\mathbf{j} + K_{3}\mathbf{k} - i(+K_{4} - K_{1}\mathbf{i} - K_{2}\mathbf{j} + K_{3}\mathbf{k}) \\ &\psi_{2}^{26} = -E + m \\ &+ (E - m)\gamma_{1} - p_{2}\gamma_{2} - p_{3}\gamma_{1} - p_{2}\gamma_{2} + (-E - m)\gamma_{10} \\ &+ p_{2}\gamma_{1}\gamma_{2} - p_{3}\gamma_{1}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} + p_{2}\gamma_{1}\gamma_{2} + p_{3}\gamma_{3}\gamma_{2} - p_{2}\gamma_{3}\gamma_{2} + (E + m)\gamma_{1}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} + (E + m)\gamma_{1}\gamma_{2}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2} + (E + m)\gamma_{1}\gamma_{2}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2}\gamma_{2} + p_{2}\gamma_{1}\gamma_{2}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2}\gamma_{2} - p_{2}\gamma_{2}\gamma_{2}\gamma_{2} + p_{2}\gamma_{1}\gamma_{2}\gamma_{2}\gamma_{2} + p_$$

$$\begin{split} &\psi_4^{20} K_4 = 0 \\ &\psi_4^{30} = (A_4^4 - iA_4^3) = -K_4 - K_1 \mathbf{i} + K_2 \mathbf{j} + K_3 \mathbf{k} - i(-K_4 + K_1 \mathbf{i} - K_2 \mathbf{j} + K_3 \mathbf{k}) \end{split}$$

$$&\psi_4^{30} = E - m \\ &\quad + (-E + m) \gamma_{l} + p_x \gamma_{x} + p_y \gamma_{y} + p_z \gamma_{z} + (-E - m) \gamma_{w} \\ &\quad - p_x \gamma_{l} \gamma_{x} - p_y \gamma_{l} \gamma_{y} - p_z \gamma_{x} \gamma_{y} - p_z \gamma_{l} \gamma_{z} + p_y \gamma_{z} \gamma_{z} - p_z \gamma_{y} \gamma_{z} + (E + m) \gamma_{l} \gamma_{w} - p_z \gamma_{x} \gamma_{w} - p_y \gamma_{y} \gamma_{w} - p_z \gamma_{z} \gamma_{w} \\ &\quad + p_z \gamma_{l} \gamma_{x} \gamma_{y} - p_y \gamma_{l} \gamma_{x} z + p_x \gamma_{l} \gamma_{y} \gamma_{z} + (-E - m) \gamma_{x} \gamma_{y} \gamma_{z} + p_x \gamma_{l} \gamma_{y} \gamma_{w} + p_z \gamma_{l} \gamma_{y} \gamma_{w} - p_z \gamma_{x} \gamma_{w} - p_y \gamma_{y} \gamma_{w} - p_z \gamma_{x} \gamma_{w} - p_x \gamma_{y} \gamma_{z} \gamma_{w} \\ &\quad + (E + m) \gamma_{l} \gamma_{x} \gamma_{y} \gamma_{z} \gamma_{w} - p_y \gamma_{l} \gamma_{x} \gamma_{z} \gamma_{w} + p_x \gamma_{l} \gamma_{y} \gamma_{z} \gamma_{w} + (-E + m) \gamma_{x} \gamma_{y} \gamma_{z} \gamma_{w} + p_z \gamma_{l} \gamma_{z} \gamma_{y} \gamma_{z} \gamma_{w} + (-E + m) \gamma_{x} \gamma_{y} \gamma_{z} \gamma_{w} \\ &\quad + (E - m) \gamma_{t} \gamma_{x} \gamma_{y} \gamma_{z} \gamma_{w} \\ &\quad + (E - m) \gamma_{t} \gamma_{x} \gamma_{y} \gamma_{z} \gamma_{w} - p_y \gamma_{t} \gamma_{x} \gamma_{z} \gamma_{w} + p_x \gamma_{t} \gamma_{y} \gamma_{z} \gamma_{w} + (-E + m) \gamma_{x} \gamma_{y} \gamma_{z} \gamma_{w} \\ &\quad + (E + m) \gamma_{t} - p_{x} \gamma_{x} - p_{y} \gamma_{y} - p_{z} \gamma_{z} + (-E - m) \gamma_{w} \\ &\quad - p_{x} \gamma_{t} \gamma_{x} - p_{y} \gamma_{y} \gamma_{y} - p_{x} \gamma_{x} \gamma_{z} + p_{x} \gamma_{y} \gamma_{z} + (-E - m) \gamma_{w} \\ &\quad - p_{x} \gamma_{t} \gamma_{x} - p_{y} \gamma_{t} \gamma_{x} \gamma_{z} + p_{x} \gamma_{t} \gamma_{y} \gamma_{z} + (-E - m) \gamma_{w} \\ &\quad + p_{x} \gamma_{t} \gamma_{x} \gamma_{y} - p_{y} \gamma_{t} \gamma_{x} \gamma_{z} + p_{x} \gamma_{t} \gamma_{z} - p_{y} \gamma_{x} \gamma_{z} + p_{x} \gamma_{t} \gamma_{x} \gamma_{w} + p_{y} \gamma_{t} \gamma_{y} \gamma_{w} - p_{x} \gamma_{x} \gamma_{w} + p_{y} \gamma_{x} \gamma_{x} \gamma_{w} + p_{y} \gamma_{x} \gamma_{y} \gamma_{w} + p_{x} \gamma_{t} \gamma_{x} \gamma_{w} + p_{y} \gamma_{x} \gamma_{y} \gamma_{w} + p_{x} \gamma_{t} \gamma_{x} \gamma_{w} + p_{y} \gamma_{x} \gamma_{y} \gamma_{w} + p_{x} \gamma_{t} \gamma_{x} \gamma_{w} + p_{y} \gamma_{x} \gamma_{y} \gamma_{w} + p_{x} \gamma_{t} \gamma_{x} \gamma_{w} + p_{y} \gamma_{x} \gamma_{x} \gamma_{w} + p_{x} \gamma_{t} \gamma_{x} \gamma_{w} + p_{x} \gamma$$

Symmetry with ψ_1 solutions [1, 2, 3, 4, 9, 10, 11, 12]

$$i\psi_1^1 + \psi_1^2 = 0$$

$$i\psi_1^{11} + \psi_1^{12} = 0$$

$$i\psi_1^3 + \psi_1^{10} = 0$$

$$i\psi_1^9 + \psi_1^4 = 0$$

$$\mathbf{i}\psi_1^1 - \psi_1^2 = 0$$

$$\mathbf{j}\psi_1^1 + \psi_1^{11} = 0$$

$$\mathbf{k}\psi_1^1 - \psi_1^{12} = 0$$

[3, 10]

$$\mathbf{i}\psi_1^3 - \psi_1^3 = 0$$

$$\mathbf{j}\psi_1^3 + \psi_1^{10} = 0$$

$$\mathbf{k}\psi_1^3 - \psi_1^{10} = 0$$

[4, 9]

$$\mathbf{i}\psi_1^4 - \psi_1^4 = 0$$

$$\mathbf{j}\psi_1^4 + \psi_1^9 = 0$$

$$\mathbf{k}\psi_1^4 - \psi_1^9 = 0$$

[5, 6, 15, 16, 17, 18, 27, 28]

$$i\psi_1^5 + \psi_1^{18} = 0$$

$$i\psi_1^{17} + \psi_1^6 = 0$$

$$i\psi_1^{15} + \psi_1^{28} = 0$$

$$i\psi_1^{27} + \psi_1^{16} = 0$$

[7, 8, 13, 14, 19, 20, 25, 26]

$$i\psi_1^7 + \psi_1^{26} = 0$$

$$i\psi_1^{25} + \psi_1^8 = 0$$

$$i\psi_1^{13} + \psi_1^{20} = 0$$

$$i\psi_1^{19} + \psi_1^{14} = 0$$

[5, 6, 16, 15]

$$\mathbf{i}\psi_1^5 - \psi_1^6 = 0$$

$$\mathbf{j}\psi_1^5 + \psi_1^{16} = 0$$

$$\mathbf{k}\psi_1^5 - \psi_1^{15} = 0$$

[7, 13]

$$\mathbf{i}\psi_1^7 - \psi_1^7 = 0$$

$$\mathbf{j}\psi_1^7 + \psi_1^{13} = 0$$
$$\mathbf{k}\psi_1^7 - \psi_1^{13} = 0$$

[8, 14]

$$\mathbf{i}\psi_1^8 - \psi_1^8 = 0$$

$$\mathbf{j}\psi_1^8 + \psi_1^{14} = 0$$

$$\mathbf{k}\psi_1^8 - \psi_1^{14} = 0$$

[17, 18, 28, 27]

$$\mathbf{i}\psi_1^{17} - \psi_1^{18} = 0$$

$$\mathbf{j}\psi_1^{17} - \psi_1^{28} = 0$$

$$\mathbf{k}\psi_1^{17} + \psi_1^{27} = 0$$

[19, 25]

$$\mathbf{i}\psi_1^{19} - \psi_1^{19} = 0$$

$$\mathbf{j}\psi_1^{19} - \psi_1^{25} = 0$$

$$\mathbf{k}\psi_1^{19} + \psi_1^{25} = 0$$

[20, 26]

$$\mathbf{i}\psi_1^{20} - \psi_1^{20} = 0$$

$$\mathbf{j}\psi_1^{20} - \psi_1^{26} = 0$$

$$\mathbf{k}\psi_1^{20} + \psi_1^{26} = 0$$

[21, 22, 23, 24, 29, 30, 31, 32]

$$i\psi_1^{21} + \psi_1^{22} = 0$$

$$i\psi_1^{31} + \psi_1^{32} = 0$$

$$i\psi_1^{23} + \psi_1^{30} = 0$$

$$i\psi_1^{29} + \psi_1^{24} = 0$$

[21, 22, 31, 32]

$$\mathbf{i}\psi_1^{21} - \psi_1^{22} = 0$$

$$\mathbf{j}\psi_1^{21} - \psi_1^{31} = 0$$

$$\mathbf{k}\psi_1^{21} + \psi_1^{32} = 0$$

[23, 30]

$$\mathbf{i}\psi_1^{23} - \psi_1^{23} = 0$$

$$\mathbf{j}\psi_1^{23} - \psi_1^{30} = 0$$

$$\mathbf{k}\psi_1^{23} + \psi_1^{30} = 0$$

[24, 29]

$$\mathbf{i}\psi_1^{24} - \psi_1^{24} = 0$$

$$\mathbf{j}\psi_1^{24} - \psi_1^{29} = 0$$

$$\mathbf{k}\psi_1^{24} + \psi_1^{29} = 0$$

Rotations ψ_1

$$\mathbf{i}\psi_1^1\mathbf{i} - \psi_4^{22} = 0$$

$$\mathbf{j}\psi_1^1\mathbf{j} + \psi_3^{31} = 0$$

$$\mathbf{k}\psi_1^1\mathbf{k} - \psi_2^{12} = 0$$

$$\mathbf{i}\psi_1^2\mathbf{i} - \psi_4^{21} = 0$$

$$\mathbf{j}\psi_1^2\mathbf{j} + \psi_3^{32} = 0$$

$$\mathbf{k}\psi_1^2\mathbf{k} - \psi_2^{11} = 0$$

$$\mathbf{i}\psi_1^3\mathbf{i} - \psi_4^{24} = 0$$

$$\mathbf{j}\psi_1^3\mathbf{j} + \psi_3^{29} = 0$$

$$\mathbf{k}\psi_1^3\mathbf{k} - \psi_2^{10} = 0$$

$$\mathbf{i}\psi_1^4\mathbf{i} - \psi_4^{23} = 0$$

$$\mathbf{j}\psi_1^4\mathbf{j} + \psi_3^{30} = 0$$

$$\mathbf{k}\psi_1^4\mathbf{k} - \psi_2^9 = 0$$

$$\mathbf{i}\psi_1^5\mathbf{i} - \psi_4^{18} = 0$$

$$\mathbf{j}\psi_1^5\mathbf{j} + \psi_3^{27} = 0$$

$$\mathbf{k}\psi_1^5\mathbf{k} - \psi_2^{16} = 0$$

$$\mathbf{i}\psi_1^6\mathbf{i} - \psi_4^{17} = 0$$

$$\mathbf{j}\psi_1^6\mathbf{j} + \psi_3^{28} = 0$$

$$\mathbf{k}\psi_1^6\mathbf{k} - \psi_2^{15} = 0$$

$$\mathbf{i}\psi_1^7\mathbf{i} - \psi_4^{20} = 0$$

$$\mathbf{j}\psi_1^7\mathbf{j} + \psi_3^{25} = 0$$

$$\mathbf{k}\psi_1^7\mathbf{k} - \psi_2^{14} = 0$$

$$\mathbf{i}\psi_1^8\mathbf{i} - \psi_4^{19} = 0$$

$$\mathbf{j}\psi_1^8\mathbf{j} + \psi_3^{26} = 0$$

$$\mathbf{k}\psi_1^8\mathbf{k} - \psi_2^{13} = 0$$

$$\mathbf{i}\psi_1^9\mathbf{i} - \psi_4^{30} = 0$$

$$\mathbf{j}\psi_1^9 \mathbf{j} + \psi_3^{23} = 0$$

$$\mathbf{k}\psi_1^9\mathbf{k} - \psi_2^4 = 0$$

$$\mathbf{i}\psi_1^{10}\mathbf{i} - \psi_4^{29} = 0$$

$$\mathbf{j}\psi_1^{10}\mathbf{j} + \psi_3^{24} = 0$$

$$\mathbf{k}\psi_1^{10}\mathbf{k} - \psi_2^3 = 0$$

$$\mathbf{i}\psi_1^{11}\mathbf{i} - \psi_4^{32} = 0$$

$$\mathbf{j}\psi_1^{11}\mathbf{j} + \psi_3^{21} = 0$$

$$\mathbf{k}\psi_1^{11}\mathbf{k} - \psi_2^2 = 0$$

$$\mathbf{i}\psi_1^{12}\mathbf{i} - \psi_4^{31} = 0$$

$$\mathbf{j}\psi_1^{12}\mathbf{j} + \psi_3^{22} = 0$$

$$\mathbf{k}\psi_1^{12}\mathbf{k} - \psi_2^1 = 0$$

$$\mathbf{i}\psi_1^{13}\mathbf{i} - \psi_4^{26} = 0$$

$$\mathbf{j}\psi_1^{13}\mathbf{j} + \psi_3^{19} = 0$$

$$\mathbf{k}\psi_1^{13}\mathbf{k} - \psi_2^8 = 0$$

$$\mathbf{i}\psi_1^{14}\mathbf{i} - \psi_4^{25} = 0$$

$$\mathbf{j}\psi_1^{14}\mathbf{j} + \psi_3^{20} = 0$$

$$\mathbf{k}\psi_1^{14}\mathbf{k} - \psi_2^7 = 0$$

$$\mathbf{i}\psi_1^{15}\mathbf{i} - \psi_4^{28} = 0$$

$$\mathbf{j}\psi_1^{15}\mathbf{j} + \psi_3^{17} = 0$$

$$\mathbf{k}\psi_1^{15}\mathbf{k} - \psi_2^6 = 0$$

$$\mathbf{i}\psi_1^{16}\mathbf{i} - \psi_4^{27} = 0$$

$$\mathbf{j}\psi_1^{16}\mathbf{j} + \psi_3^{18} = 0$$

$$\mathbf{k}\psi_1^{16}\mathbf{k} - \psi_2^5 = 0$$

$$\mathbf{i}\psi_1^{17}\mathbf{i} - \psi_4^6 = 0$$

$$\mathbf{j}\psi_1^{17}\mathbf{j} + \psi_3^{15} = 0$$

$$\mathbf{k}\psi_1^{17}\mathbf{k} - \psi_2^{28} = 0$$

$$\mathbf{i}\psi_1^{18}\mathbf{i} - \psi_4^5 = 0$$

$$\mathbf{j}\psi_1^{18}\mathbf{j} + \psi_3^{16} = 0$$

$$\mathbf{k}\psi_1^{18}\mathbf{k} - \psi_2^{27} = 0$$

$$\mathbf{i}\psi_1^{19}\mathbf{i} - \psi_4^8 = 0$$

$$\mathbf{j}\psi_1^{19}\mathbf{j} + \psi_3^{13} = 0$$

$$\mathbf{k}\psi_1^{19}\mathbf{k} - \psi_2^{26} = 0$$

$$\mathbf{i}\psi_1^{20}\mathbf{i} - \psi_4^7 = 0$$

$$\mathbf{j}\psi_1^{20}\mathbf{j} + \psi_3^{14} = 0$$

$$\mathbf{k}\psi_1^{20}\mathbf{k} - \psi_2^{25} = 0$$

$$\mathbf{i}\psi_1^{21}\mathbf{i} - \psi_4^2 = 0$$

$$\mathbf{j}\psi_1^{21}\mathbf{j} + \psi_3^{11} = 0$$

$$\mathbf{k}\psi_1^{21}\mathbf{k} - \psi_2^{32} = 0$$

$$\mathbf{i}\psi_1^{22}\mathbf{i} - \psi_4^1 = 0$$

$$\mathbf{j}\psi_1^{22}\mathbf{j} + \psi_3^{12} = 0$$

$$\mathbf{k}\psi_1^{22}\mathbf{k} - \psi_2^{31} = 0$$

$$\mathbf{i}\psi_1^{23}\mathbf{i} - \psi_4^4 = 0$$

$$\mathbf{j}\psi_1^{23}\mathbf{j} + \psi_3^9 = 0$$

$$\mathbf{k}\psi_1^{23}\mathbf{k} - \psi_2^{30} = 0$$

$$\mathbf{i}\psi_1^{24}\mathbf{i} - \psi_4^3 = 0$$

$$\mathbf{j}\psi_1^{24}\mathbf{j} + \psi_3^{10} = 0$$

$$\mathbf{k}\psi_1^{24}\mathbf{k} - \psi_2^{29} = 0$$

$$\mathbf{i}\psi_1^{25}\mathbf{i} - \psi_4^{14} = 0$$

$$\mathbf{j}\psi_1^{25}\mathbf{j} + \psi_3^7 = 0$$

$$\mathbf{k}\psi_1^{25}\mathbf{k} - \psi_2^{20} = 0$$

$$\mathbf{i}\psi_1^{26}\mathbf{i} - \psi_4^{13} = 0$$

$$\mathbf{j}\psi_1^{26}\mathbf{j} + \psi_3^8 = 0$$

$$\mathbf{k}\psi_1^{26}\mathbf{k} - \psi_2^{19} = 0$$

$$\mathbf{i}\psi_1^{27}\mathbf{i} - \psi_4^{16} = 0$$

$$\mathbf{j}\psi_1^{27}\mathbf{j} + \psi_3^5 = 0$$

$$\mathbf{k}\psi_1^{27}\mathbf{k} - \psi_2^{18} = 0$$

$$\mathbf{i}\psi_1^{28}\mathbf{i} - \psi_4^{15} = 0$$

$$\mathbf{j}\psi_1^{28}\mathbf{j} + \psi_3^6 = 0$$

$$\mathbf{k}\psi_1^{28}\mathbf{k} - \psi_2^{17} = 0$$

$$\mathbf{i}\psi_1^{29}\mathbf{i} - \psi_4^{10} = 0$$

$$\mathbf{j}\psi_1^{29}\mathbf{j} + \psi_3^3 = 0$$

$$\mathbf{k}\psi_1^{29}\mathbf{k} - \psi_2^{24} = 0$$

$$\mathbf{i}\psi_1^{30}\mathbf{i} - \psi_4^9 = 0$$

$$\mathbf{j}\psi_1^{30}\mathbf{j} + \psi_3^4 = 0$$

$$\mathbf{k}\psi_1^{30}\mathbf{k} - \psi_2^{23} = 0$$

$$\mathbf{i}\psi_1^{31}\mathbf{i} - \psi_4^{12} = 0$$

$$\mathbf{j}\psi_1^{31}\mathbf{j} + \psi_3^1 = 0$$

$$\mathbf{k}\psi_1^{31}\mathbf{k} - \psi_2^{22} = 0$$

$$\mathbf{i}\psi_1^{32}\mathbf{i} - \psi_4^{11} = 0$$

$$\mathbf{j}\psi_1^{32}\mathbf{j} + \psi_3^2 = 0$$

$$\mathbf{k}\psi_1^{32}\mathbf{k} - \psi_2^{21} = 0$$