The Skeleton Assembly Line

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Abstract

Optimized routines to transform the skeletons and joints for a skeletal animation system are presented. The Intel Streaming SIMD Extensions are used to exploit parallelism with a compressed calculation. The optimized routines are well over two times faster than the implementation in C on a Pentium 4.

1. Introduction

Transformation matrices are often used when many points in space need to be transformed like the vertices of the mesh of an animated model. Matrices are typically more efficient on today's hardware when many positions in space need to be transformed. Skeletal animation systems often use row major 3x4 matrices for the joints of a skeleton. These joints are usually stored and animated in local space, relative to a parent joint, because of several advantageous properties. However, when the skeleton is used to transform the vertices of an animating mesh the joint matrices need to be transformed to global (object or world) space first.

1.1 Previous Work

Interpolating between vertex positions of two animation frames is simple and cheap. However, storing all the vertex positions for every animation frame consumes a lot of memory. The use of skeletons is more efficient when high detail polygonal meshes need to be animated. The vertex positions are only stored once and they are transformed with the joints of a skeleton. Such skeletal animation systems are not new [2, 3] and are used in many applications.

1.2 Layout

Section 2 shows some properties of the skeletons often used in skeletal animation systems. Section 3 describes how the joint matrices of a skeleton can be transformed from local space to global space. The opposite transformation from global space to local space is presented in section 4. General joint matrix multiplication as often used for matrix palette skinning is described in section 5. The results of the optimizations are presented in section 6 and several conclusions are drawn in section 7.

2. Skeletons

Transformation matrices are often used when many points in space need to be transformed like the vertices of the mesh of an animated model. Matrices are typically more efficient on today's hardware when many positions in space need to be transformed. A skeletal animation system often uses row major 3x4 matrices for the joints of a skeleton. These 3x4 matrices consist of a 3x3 orthonormal rotation matrix and a 3D translation vector.

```
struct JointMat {
    float mat[3*4];
};
```

The first three elements of each row are from the 3x3 rotation matrix and the last element of each row is a translation along one of the coordinate axes.

Each joint of a skeleton is usually stored and animated relative to a parent joint. Storing and animating joints in local space has several advantages. Some joints hardly or never change relative to their parents during certain animations which allows for better compression when joints are stored relative to their parent. Joint orientations and translations from multiple animations can also be blended together locally when joints are animated in local space. Furthermore specifying joints relative to their parents allows joints to be modified locally for instance for game controlled effects and Inverse Kinematics.

When a skeleton is used to transform the vertices of an animating mesh the joints of the skeleton need to be specified in global (object or world) space. The following section presents and optimizes a routine to transform joints matrices from local space to global space.

3. Transforming a Skeleton

The following routine transforms local joint matrices (relative to parent joints) to global joint matrices (object or world space). The joint matrices are stored in an ordered array where the parent joints come first. The routine works on this array and transforms the joint matrices in place. The parent for each joint is specified with an array with integers where each integer specifies the index of the parent joint in the array with joint matrices. Furthermore the index of the first and last joint of a sequence of joints that need to be transformed are specified. This allows the complete skeleton to be split up in multiple sequences of joints that are transformed. Joints inbetween such sequences can then be transformed separately and additional modifications can be applied where necessary.

```
void TransformJoint( JointMat &a, const idJointMat &b ) {
    float tmp[3];

    tmp[0] = a.mat[0 * 4 + 0] * b.mat[0 * 4 + 0] + a.mat[1 * 4 + 0] * b.mat[0 * 4 + 1] + a.mat[2 * 4 + 0] * b.mat[0 * 4 + 2];
    tmp[1] = a.mat[0 * 4 + 0] * b.mat[1 * 4 + 0] + a.mat[1 * 4 + 0] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 0] * b.mat[1 * 4 + 2];
    tmp[2] = a.mat[0 * 4 + 0] * b.mat[2 * 4 + 0] + a.mat[1 * 4 + 0] * b.mat[2 * 4 + 1] + a.mat[2 * 4 + 0] * b.mat[2 * 4 + 2];
    a.mat[0 * 4 + 0] = tmp[0];
    a.mat[1 * 4 + 0] = tmp[1];
    a.mat[2 * 4 + 0] = tmp[2];

    tmp[0] = a.mat[0 * 4 + 1] * b.mat[0 * 4 + 0] + a.mat[1 * 4 + 1] * b.mat[0 * 4 + 1] + a.mat[2 * 4 + 1] * b.mat[0 * 4 + 2];
    tmp[1] = a.mat[0 * 4 + 1] * b.mat[1 * 4 + 0] + a.mat[1 * 4 + 1] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 1] * b.mat[2 * 4 + 2];
    a.mat[0 * 4 + 1] = tmp[0];
    a.mat[0 * 4 + 1] = tmp[0];
    a.mat[0 * 4 + 1] = tmp[1];
    a.mat[0 * 4 + 1] = tmp[2];

    tmp[0] = a.mat[0 * 4 + 2] * b.mat[0 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[0 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[0 * 4 + 2];
    tmp[1] = a.mat[0 * 4 + 2] * b.mat[1 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[1 * 4 + 2];
    tmp[1] = a.mat[0 * 4 + 2] * b.mat[1 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[1 * 4 + 2];
    tmp[2] = a.mat[0 * 4 + 2] * b.mat[2 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 2];
    tmp[2] = a.mat[0 * 4 + 2] * b.mat[2 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[2 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 2];
    tmp[2] = a.mat[0 * 4 + 2] * b.mat[2 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[2 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 2];
    tmp[2] = a.mat[0 * 4 + 2] * b.mat[2 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[2 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 2];
    tmp[2] = a.mat[0 * 4 + 2] * b.mat[2 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[2 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[2 * 4
```

```
a.mat[0 * 4 + 2] = tmp[0];
a.mat[1 * 4 + 2] = tmp[1];
a.mat[2 * 4 + 2] = tmp[2];

tmp[0] = a.mat[0 * 4 + 3] * b.mat[0 * 4 + 0] + a.mat[1 * 4 + 3] * b.mat[0 * 4 + 1] + a.mat[2 * 4 + 3] * b.mat[0 * 4 + 2];
tmp[1] = a.mat[0 * 4 + 3] * b.mat[1 * 4 + 0] + a.mat[1 * 4 + 3] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 3] * b.mat[1 * 4 + 2];
tmp[2] = a.mat[0 * 4 + 3] * b.mat[2 * 4 + 0] + a.mat[1 * 4 + 3] * b.mat[2 * 4 + 1] + a.mat[2 * 4 + 3] * b.mat[2 * 4 + 2];
a.mat[0 * 4 + 3] = tmp[0];
a.mat[1 * 4 + 3] = tmp[1];
a.mat[2 * 4 + 3] = tmp[2];

a.mat[0 * 4 + 3] += b.mat[0 * 4 + 3];
a.mat[1 * 4 + 3] += b.mat[1 * 4 + 3];
a.mat[2 * 4 + 3] += b.mat[2 * 4 + 3];
}

void TransformSkeleton( JointMat *jointMats, const int *parents, const int firstJoint, const int lastJoint ) {
    int i;

    for( i = firstJoint; i <= lastJoint; i++ ) {
        TransformJoint( jointMats[i], jointMats[parents[i]] );
    }
}</pre>
```

Transforming the joints of a skeleton as shown above is a typical example of a loop with a lot of mathematical operations which should be ideal for taking advantage of parallelism using SIMD code. However, there is no guarentee that the individual iterations are independent from each other. One iteration may transform the joint which is the parent of the joint transformed in the next iteration. As such parallelism cannot be exploited through increased throughput. Fortunately the transformation is ideal for exploiting parallelism with a compressed calculation. The multiplication of two 3x4 matrices involves many independent multiplications and additions that can be executed in parallel.

When multiplying matrices in SSE code it is common practice to load a single scalar from one matrix and shuffle it into all four elements of an SSE register. This register is then multiplied with a row of the other matrix. The following code shows how four scalars are loaded in this manner.

```
movss xmm0, [esi+edx+ 0] shufps xmm0, xmm0, R_SHUFFLE_D( 0, 0, 0, 0 ) movss xmm1, [esi+edx+ 4] shufps xmm1, xmm1, R_SHUFFLE_D( 0, 0, 0, 0 ) movss xmm2, [esi+edx+ 8] shufps xmm2, xmm2, R_SHUFFLE_D( 0, 0, 0, 0 ) movss xmm3, [esi+edx+12] shufps xmm3, xmm3, R_SHUFFLE_D( 0, 0, 0, 0 )
```

Instead of using the above code it can be advantageous to use the SSE2 instruction 'pshufd' to load the scalars into SSE registers. Four scalars are loaded with a single move into a temporary register and then the 'pshufd' instruction is used to copy and spread the individual scalars to the other registers. The 'pshufd' instruction is meant to be used for double word integer data. However, since every 32 bits floating point bit pattern represents a valid integer this instruction can be used on floating point data without problems.

```
movaps xmm7, [esi+edx+ 0] xmm7, [esi+edx+ 0] xmm0, xmm7, R_SHUFFLE_D( 0, 0, 0, 0 ) yshufd xmm1, xmm7, R_SHUFFLE_D( 1, 1, 1, 1 ) yshufd xmm2, xmm7, R_SHUFFLE_D( 2, 2, 2, 2 ) yshufd xmm3, xmm7, R_SHUFFLE_D( 3, 3, 3, 3 )
```

Obviously when using the 'pshufd' instruction the total number of instructions required is less. However, a dependency is introduced on the temporary register into which the four scalars are loaded and on a Pentium 4 the 'pshufd' instruction trades latency for throughput. Whether or not using the 'pshufd' instruction provides an advantage depends on the

surrounding instructions and the processor type. However, it is usually worthwhile to try both variants for loading scalars into SSE registers and time the results.

The SSE code for the above routine uses the 'pshufd' instruction to copy and spread scalars from one of the matrices into SSE registers. The complete SSE optimized code for transforming the joints in a skeleton can be found in appendix A.

4. Untransforming a Skeleton

In some cases it may be desired to transform the joints of a skeleton from global space back to local space. The following routine is basically the opposite of the routine presented in the previous section.

```
void UntransformJoint( JointMat &a, const idJointMat &b ) {
               float tmp[3];
               a.mat[0 * 4 + 3] -= b.mat[0 * 4 + 3];
               a.mat[1 * 4 + 3] -= b.mat[1 * 4 + 3];
               a.mat[2 * 4 + 3] -= b.mat[2 * 4 + 3];
                \begin{split} & \text{tmp[0] = a.mat[0 * 4 + 0] * b.mat[0 * 4 + 0] * b.mat[1 * 4 + 0] * b.mat[1 * 4 + 0] * b.mat[2 * 4 + 0] * b.mat[2 * 4 + 0] * b.mat[2 * 4 + 0] * b.mat[1] = a.mat[0 * 4 + 0] * b.mat[0 * 4 + 1] + a.mat[1 * 4 + 0] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 0] * b.mat[2 * 4 + 1]; } \end{split}
                tmp[2] = a.mat[0 * 4 + 0] * b.mat[0 * 4 + 2] + a.mat[1 * 4 + 0] * b.mat[1 * 4 + 2] + a.mat[2 * 4 + 0] * b.mat[2 * 4 + 2];
               a.mat[0 * 4 + 0] = tmp[0];
a.mat[1 * 4 + 0] = tmp[1];
               a.mat[2 * 4 + 0] = tmp[2];
                \begin{split} & \text{tmp[0] = a.mat[0 * 4 + 1] * b.mat[0 * 4 + 0] + a.mat[1 * 4 + 1] * b.mat[1 * 4 + 0] + a.mat[2 * 4 + 1] * b.mat[2 * 4 + 1] * b.mat[2 * 4 + 1] * b.mat[2 * 4 + 1] * b.mat[1 * 4 + 1] * b.mat[1 * 4 + 1] * b.mat[2 * 4 + 2] * b.mat[2 * 4 + 
               a.mat[0 * 4 + 1] = tmp[0];
a.mat[1 * 4 + 1] = tmp[1];
               a.mat[2 * 4 + 1] = tmp[2];
                \texttt{tmp[0]} = \texttt{a.mat[0 * 4 + 2] * b.mat[0 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[1 * 4 + 0] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 0]; \\ \texttt{tmp[1]} = \texttt{a.mat[0 * 4 + 2] * b.mat[0 * 4 + 1] + a.mat[1 * 4 + 2] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 2] * b.mat[2 * 4 + 1]; \\ \texttt{tmp[1]} = \texttt{a.mat[0 * 4 + 2] * b.mat[0 * 4 + 1] + a.mat[1 * 4 + 2] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 1]; } 
                tmp[2] = a.mat[0 * 4 + 2] * b.mat[0 * 4 + 2] + a.mat[1 * 4 + 2] * b.mat[1 * 4 + 2] * a.mat[2 * 4 + 2] * b.mat[2 * 4 + 2] * b.ma
               a.mat[0 * 4 + 2] = tmp[0];
               a.mat[1 * 4 + 2] = tmp[1];
               a.mat[2 * 4 + 2] = tmp[2];
                tmp[0] = a.mat[0 * 4 + 3] * b.mat[0 * 4 + 0] + a.mat[1 * 4 + 3] * b.mat[1 * 4 + 0] + a.mat[2 * 4 + 3] * b.mat[2 * 4 + 0];
               tmp[1] = a.mat[0 * 4 + 3] * b.mat[0 * 4 + 1] + a.mat[1 * 4 + 3] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 3] * b.mat[2 * 4 + 1];

tmp[2] = a.mat[0 * 4 + 3] * b.mat[0 * 4 + 2] + a.mat[1 * 4 + 3] * b.mat[1 * 4 + 2] + a.mat[2 * 4 + 3] * b.mat[2 * 4 + 3] * b.mat[2 * 4 + 2];
               a.mat[0 * 4 + 3] = tmp[0];
a.mat[1 * 4 + 3] = tmp[1];
               a.mat[2 * 4 + 3] = tmp[2];
void UntransformSkeleton( JointMat *jointMats, const int *parents, const int firstJoint, const int lastJoint ) {
               int i;
               for( i = lastJoint; i >= firstJoint; i-- ) {
                               UntransformJoint( jointMats[i], jointMats[parents[i]] );
```

The exact same approach is used for the implementation of the SSE optimized code for the above routine and the routine specified in the previous section. The complete SSE optimized code for the above routine can be found in appendix B.

5. Transforming Joints

One approach to matrix palette skinning involves transforming a base pose of a mesh. The vertices for this base pose are stored in model space. These vertices are not transformed directly by the joint matrices of the animated skeleton but the joint matrices are first

multiplied with the inverse joint matrices for the base pose. These inverse joint matrices can be precalculated because the same base pose is used during all animations. The following routine can be used to multiply the joint matrices of the animated skeleton with the precalculated inverse joint matrices of the base pose. The routine multiplies two arrays with joint matrices and stores the result in another array.

```
void MultiplyJoints( JointMat & result, const JointMat &a, const JointMat &b) {
    result.mat[0 * 4 + 0] = a.mat[0 * 4 + 0] * b.mat[0 * 4 + 0] + a.mat[0 * 4 + 1] * b.mat[1 * 4 + 0] + a.mat[0 * 4 + 2] * b.mat[2 * 4 + 0];
    result.mat[0 * 4 + 1] = a.mat[0 * 4 + 0] * b.mat[0 * 4 + 1] + a.mat[0 * 4 + 1] * b.mat[1 * 4 + 1] + a.mat[0 * 4 + 2] * b.mat[2 * 4 + 1];
    result.mat[0 * 4 + 2] = a.mat[0 * 4 + 0] * b.mat[0 * 4 + 2] + a.mat[0 * 4 + 1] * b.mat[1 * 4 + 2] + a.mat[0 * 4 + 2] * b.mat[2 * 4 + 2];
    result.mat[0 * 4 + 3] = a.mat[0 * 4 + 0] * b.mat[0 * 4 + 3] + a.mat[0 * 4 + 1] * b.mat[1 * 4 + 2] + a.mat[0 * 4 + 2] * b.mat[2 * 4 + 2];
    result.mat[1 * 4 + 0] = a.mat[1 * 4 + 0] * b.mat[0 * 4 + 0] + a.mat[1 * 4 + 1] * b.mat[1 * 4 + 0] + a.mat[1 * 4 + 2] * b.mat[2 * 4 + 0];
    result.mat[1 * 4 + 1] = a.mat[1 * 4 + 0] * b.mat[0 * 4 + 2] + a.mat[1 * 4 + 1] * b.mat[1 * 4 + 1] + a.mat[1 * 4 + 2] * b.mat[2 * 4 + 1];
    result.mat[1 * 4 + 3] = a.mat[1 * 4 + 0] * b.mat[0 * 4 + 3] + a.mat[1 * 4 + 1] * b.mat[1 * 4 + 3] + a.mat[1 * 4 + 2] * b.mat[2 * 4 + 3];

    result.mat[2 * 4 + 0] = a.mat[2 * 4 + 0] * b.mat[0 * 4 + 3] + a.mat[2 * 4 + 1] * b.mat[1 * 4 + 3] + a.mat[1 * 4 + 2] * b.mat[2 * 4 + 3] + a.mat[1 * 4 + 3];

    result.mat[2 * 4 + 0] = a.mat[2 * 4 + 0] * b.mat[0 * 4 + 1] + a.mat[2 * 4 + 1] * b.mat[1 * 4 + 1] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 3] + a.mat[2 * 4 + 2] * b.mat[2 * 4 + 3] + a.mat[2 * 4 + 3] + a.mat
```

Although this routine has no dependencies between iterations, the best way to exploit parallelism is still through a compressed calculation. It is easy to spot the independent multiplications and additions that can be executed in parallel. The same approach to SIMD as used for the previous routines can be used for this routine. The complete SSE optimized code for the above routine can be found in appendix B.

6. Results

The various routines have been tested on an Intel® Pentium® 4 Processor on 130nm Technology and an Intel® Pentium® 4 Processor on 90nm Technology. The routines operated on a list of 1024 joints. The total number of clock cycles and the number of clock cycles per joint for each routine on the different CPUs are listed in the following table.

Hot Cache Clock Cycle Counts				
Routine	P4 130nm total clock cycles	P4 130nm clock cycles per element	P4 90nm total clock cycles	P4 90nm clock cycles per element
TransformSkeleton (C)	132224	130	166176	163
TransformSkeleton (SSE)	53580	53	54297	53
UntransformSkeleton (C)	133680	131	157104	154
UntransformSkeleton (SSE)	55488	55	57285	56
TransformJoints (C)	137980	135	151587	148
TransformJoints (SSE)	36520	36	48906	48

7. Conclusion

Transforming the joints of a skeleton involves the multiplication of 3x4 matrices. The transformations involve many independent multiplications and additions that can be executed in parallel and this parallelism can be exploited with a compressed calculation using the Intel Streaming SIMD Extensions.

The SSE optimized implementations are significantly faster than their C counterparts. In all cases the transformations are at least two times faster and in some cases close to three times faster.

8. References

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Appendix A

```
SSE Optimized Skeleton Transform for Skeletal Animation Systems
       Copyright (C) 2005 Id Software, Inc.
       Written by J.M.P. van Waveren
       This code is free software; you can redistribute it and/or
       modify it under the terms of the GNU Lesser General Public
       License as published by the Free Software Foundation; either
       version 2.1 of the License, or (at your option) any later version.
       This code is distributed in the hope that it will be useful,
       but WITHOUT ANY WARRANTY; without even the implied warranty of
       MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
       Lesser General Public License for more details.
#define assert_16_byte_aligned( pointer ) assert( (((UINT_PTR)(pointer))&15) == 0 );
#define ALIGN16( x )
                                                                                 __declspec(align(16)) x
#define ALIGN16( x )
#define ALIGN4_INIT4( X, I0, I1, I2, I3 )
#define R_SHUFFLE_D( x, y, z, w )
ALIGN4_INIT4( unsigned long SIMD_SP_clearFirstThree, 0x00000000, 0x00000000, 0x00000000, 0xFFFFFFFF);
struct JointMat {
                             mat[3*4];
      float
#define JOINTMAT_SIZE
                                                        (4*3*4)
void TransformSkeleton( JointMat *jointMats, const int *parents, const int firstJoint, const int lastJoint ) {
       assert_16_byte_aligned( jointMats );
       __asm {
                                    ecx, firstJoint
                                    eax, lastJoint
              sub
                                    eax, ecx
                                    done
              shl
                                    ecx, 2
                                                                                                            // ecx = firstJoint * 4
              mov
                                    edi, parents
              add
                                                                                                             // edx = &parents[firstJoint]
                                    edi, ecx
               lea
                                    ecx, [ecx+ecx*2]
                                                                                                              // ecx = firstJoint * JOINTMAT_SIZE
              shl
                                    ecx, 2
                                                                                                               // esi = jointMats
              mov
                                    esi, jointMats
              shl
                                    eax, 2
                                                                                                              // eax = ( lastJoint - firstJoint ) * 4
                                    edi, eax
              add
              neg
                                    eax
       loopJoint:
                                    edx, [edi+eax]
                                    xmm0, [esi+ecx+ 0]
                                                                                                             // xmm0 = m0, m1, m2, t0
              movaps
              lea
                                    edx, [edx+edx*2]
              movaps
                                    xmm1, [esi+ecx+16]
                                                                                                              // xmm1 = m2, m3, m4, t1
                                                                                                               // edx = parents[i] * JOINTMAT_SIZE
                                    edx, 4
              movaps
                                    xmm2, [esi+ecx+32]
                                                                                                               // \text{xmm2} = \text{m5}, \text{m6}, \text{m7}, \text{t2}
                                    xmm7, [esi+edx+ 0]
              movaps
              pshufd
                                    xmm4, xmm7, R_SHUFFLE_D( 0, 0, 0, 0 )
              mulps
                                    xmm4, xmm0
              pshufd
                                   xmm5, xmm7, R_SHUFFLE_D( 1, 1, 1, 1 )
              mulps
                                    xmm5, xmm1
              addps
                                   xmm4, xmm5
```

```
ecx, JOINTMAT_SIZE
    add
    add
                eax, 4
    pshufd
                xmm6, xmm7, R_SHUFFLE_D( 2, 2, 2, 2)
    mulps
                xmm6, xmm2
    addps
                xmm4, xmm6
    andps
                xmm7, SIMD_SP_clearFirstThree
   addps
                xmm4, xmm7
                [esi+ecx-JOINTMAT_SIZE+ 0], xmm4
   movaps
   movaps
                xmm3, [esi+edx+16]
                xmm5, xmm3, R_SHUFFLE_D( 0, 0, 0, 0)
    pshufd
    mulps
                xmm5, xmm0
    pshufd
                xmm6, xmm3, R_SHUFFLE_D( 1, 1, 1, 1 )
    mulps
                {\tt xmm6}, {\tt xmm1}
   addps
                xmm5, xmm6
   pshufd
                xmm4, xmm3, R_SHUFFLE_D(2, 2, 2, 2)
    mulps
                xmm4, xmm2
    addps
                {\tt xmm5}, {\tt xmm4}
    andps
                {\tt xmm3, SIMD\_SP\_clearFirstThree}
   addps
                xmm5, xmm3
                [esi+ecx-JOINTMAT_SIZE+16], xmm5
   movaps
   movaps
               xmm7, [esi+edx+32]
   pshufd
                xmm6, xmm7, R_SHUFFLE_D(0,0,0,0)
    mulps
                xmm6, xmm0
    pshufd
                xmm4, xmm7, R_SHUFFLE_D( 1, 1, 1, 1 )
    mulps
                {\tt xmm4}, {\tt xmm1}
   addps
                xmm6, xmm4
   pshufd
                xmm3, xmm7, R_SHUFFLE_D(2, 2, 2, 2)
    mulps
                xmm3, xmm2
   addps
                xmm6, xmm3
    andps
                xmm7, SIMD_SP_clearFirstThree
   addps
                xmm6, xmm7
   movaps
                [esi+ecx-JOINTMAT_SIZE+32], xmm6
    jle
                loopJoint
done:
```

Appendix B

```
SSE Optimized Skeleton Untransform for Skeletal Animation Systems
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    Written by J.M.P. van Waveren
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void UntransformSkeleton( JointMat *jointMats, const int *parents, const int firstJoint, const int lastJoint ) {
   assert_16_byte_aligned( jointMats );
    __asm {
                    edx, firstJoint
       mov
                    eax, lastJoint
       mov
                    ecx, eax
       mov
       sub
                    eax, edx
       jl
                    done
                    esi, jointMats
       mov
                                                            // esi = jointMats
        lea
                    ecx, [ecx+ecx*2]
                                                            // ecx = lastJoint * JOINTMAT_SIZE
                    ecx, 4
       shl
                    edx, 2
       shl
                    edi, parents
       mov
                                                            // edi = &parents[firstJoint]
        add
                    edi, edx
```

```
shl
                eax, 2
                                                           // eax = ( lastJoint - firstJoint ) * 4
loopJoint:
                edx, [edi+eax]
    mov
                xmm0, [esi+ecx+ 0]
                                                          // xmm0 = m0, m1, m2, t0
    movaps
    lea
                edx, [edx+edx*2]
                                                          // xmm1 = m2, m3, m4, t1
// edx = parents[i] * JOINTMAT_SIZE
// xmm2 = m5, m6, m7, t2
    movaps
                xmm1, [esi+ecx+16]
    shl
                \operatorname{edx}, 4
                xmm2, [esi+ecx+32]
    movaps
    movss
                xmm7, [esi+edx+12]
                xmm7, xmm7, R_SHUFFLE_D(1, 2, 3, 0)
    pshufd
    subps
                xmm0, xmm7
                xmm6, [esi+edx+28]
    movss
    pshufd
                xmm6, xmm6, R_SHUFFLE_D(1, 2, 3, 0)
    subps
                xmm1, xmm6
    movss
                xmm5, [esi+edx+44]
    pshufd
                xmm5, xmm5, R_SHUFFLE_D(1, 2, 3, 0)
    subps
                xmm2, xmm5
                ecx, JOINTMAT_SIZE
    sub
    sub
                eax, 4
                xmm7, [esi+edx+ 0]
    movaps
    pshufd
                xmm3, xmm7, R_SHUFFLE_D( 0, 0, 0, 0 )
    mulps
                xmm3, xmm0
                xmm4, xmm7, R_SHUFFLE_D( 1, 1, 1, 1 )
    pshufd
    mulps
                xmm4, xmm0
                xmm5, xmm7, R_SHUFFLE_D( 2, 2, 2, 2)
    pshufd
    mulps
                xmm5, xmm0
    movaps
                xmm7, [esi+edx+16]
    pshufd
                xmm0, xmm7, R_SHUFFLE_D( 0, 0, 0, 0 )
    mulps
                xmm0, xmm1
    addps
                xmm3, xmm0
    pshufd
                xmm6, xmm7, R_SHUFFLE_D(1, 1, 1, 1)
    mulps
                xmm6, xmm1
    addps
                xmm4, xmm6
    pshufd
                xmm0, xmm7, R_SHUFFLE_D( 2, 2, 2, 2)
    mulps
                {\tt xmm0} , {\tt xmm1}
    addps
                xmm5, xmm0
    movaps
                xmm7, [esi+edx+32]
   pshufd
                xmm6, xmm7, R_SHUFFLE_D( 0, 0, 0, 0)
    mulps
                xmm6, xmm2
    addps
                xmm3, xmm6
    movaps
                [esi+ecx+JOINTMAT_SIZE+ 0], xmm3
    pshufd
                xmm1, xmm7, R_SHUFFLE_D( 1, 1, 1, 1 )
    mulps
                xmm1, xmm2
    addps
                xmm4, xmm1
    movaps
                [esi+ecx+JOINTMAT_SIZE+16], xmm4
   pshufd
                xmm6, xmm7, R_SHUFFLE_D( 2, 2, 2, 2)
    mulps
                xmm6, xmm2
    addps
                xmm5, xmm6
    movaps
                 [esi+ecx+JOINTMAT_SIZE+32], xmm5
                loopJoint
done:
```

Appendix C

```
SSE Optimized Joint Transform for Skeletal Animation Systems
    Copyright (C) 2005 Id Software, Inc.
    Written by J.M.P. van Waveren
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    Lesser General Public License for more details.
void TransformJoints( JointMat *result, const JointMat *joints1, const JointMat *joints2, const int numJoints ) {
    assert_16_byte_aligned( result );
    assert_16_byte_aligned( joints1 );
    assert_16_byte_aligned( joints2 );
    __asm {
        mov
                    eax, numJoints
        test
                    eax, eax
        jz
                    done
        mov
                    ecx, joints1
        mov
                    edx, joints2
        mov
                    edi, result
                    eax, JOINTMAT_SIZE
        imul
        add
                    ecx, eax
        add
                    edx, eax
        add
                    edi, eax
        neg
                    eax
    loopJoint:
        movaps
                    xmm0, [edx+eax+ 0]
        movaps
                    xmm1, [edx+eax+16]
        movaps
                   xmm2, [edx+eax+32]
        movaps
                    xmm7, [ecx+eax+ 0]
        pshufd
                    xmm3, xmm7, R_SHUFFLE_D( 0, 0, 0, 0 )
        mulps
                    xmm3, xmm0
        pshufd
                    xmm4, xmm7, R_SHUFFLE_D( 1, 1, 1, 1 )
        mulps
                    xmm4, xmm1
        addps
                    xmm3, xmm4
                    eax, JOINTMAT_SIZE
        add
                    xmm5, xmm7, R_SHUFFLE_D( 2, 2, 2, 2)
        pshufd
        mulps
                    xmm5, xmm2
        addps
                    xmm3, xmm5
        andps
                    xmm7, SIMD_SP_clearFirstThree
        addps
                    xmm3, xmm7
        movaps
                    [edi+eax-JOINTMAT_SIZE+0], xmm3
        movaps
                    xmm7, [ecx+eax-JOINTMAT_SIZE+16]
        pshufd
                    xmm3, xmm7, R_SHUFFLE_D(0,0,0,0)
        mulps
                    xmm3, xmm0
        pshufd
                    xmm4, xmm7, R_SHUFFLE_D(1, 1, 1, 1)
        mulps
                    xmm4, xmm1
        addps
                    {\tt xmm3}, {\tt xmm4}
                    xmm5, xmm7, R_SHUFFLE_D(2, 2, 2, 2)
        pshufd
        mulps
                    {\tt xmm5}, {\tt xmm2}
        addps
                    xmm3, xmm5
        andps
                    xmm7, SIMD_SP_clearFirstThree
        addps
                    xmm3, xmm7
        movaps
                    [edi+eax-JOINTMAT_SIZE+16], xmm3
                    xmm7, [ecx+eax-JOINTMAT_SIZE+32]
        pshufd
                    xmm3, xmm7, R_SHUFFLE_D( 0, 0, 0, 0 )
        mulps
                    xmm3, xmm0
        pshufd
                    xmm4\,,\ xmm7\,,\ R\_SHUFFLE\_D(\ 1,\ 1,\ 1,\ 1\ )
        mulps
                    xmm4, xmm1
```