INFO-H-413 - Learning Dynamics: Implementation Exercise #2 The Traveling Salesman Problem with Time Windows - Stochastic Local Search Algorithms

Prof. T. Stüetzle

Jacopo De Stefani

April 22, 2013

Contents

Implementation
How to compile the program?
How to run the program?
Command-line execution
Script execution
Problem 1
Ant Colony Optimization
Problem statement
Introduction
Problem formulation
Algorithm structure
Pheromone Initialization
Solution construction
Possible heuristics
Cheng and Mao, 2007
Lopez-Ibanez and Blum, 2009
MAX-MIN Ant System (MMAS)
Results discussion
Conclusions

Jacopo De Stefani Page 2 of 14

Implementation

The heuristic solver had been written using the C++ programming language, in order to be able to take adventage of the functionalities offered by the Standard Template Library (STL).

By combining an object-oriented approach with those functionalities, I built a modular application core (*HeuristicCore*) that has been used for the two exercises required for this implementation.

The core is directly linked with the reader (*InstanceReader*) which reads the files containing all the informations to run the simulation (distance matrix, time windows vector and seeds list) and the writer (*Writer*) which outputs the results of the simulation in a CSV file.

Two different command line front-ends, sharing the same underlying structure, but having a different set of parameters, have been developed to distinguish the iterative-improvement interface from the variable neighborhood descent one.

The global program structure is depicted here:

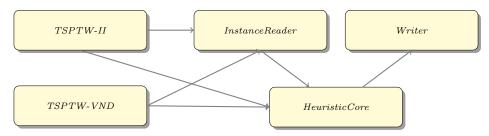


Figure 1: Simulation Code Structure

The names of the nodes corresponds to those of the implementation (.cpp) and header files for the corresponding classes. In addition to these, a class to represent the time windows (TimeWindow.h) and another one to represent the candidate solution as a user defined data type (CandidateSolution.{h,cpp}) have been implemented.

How to compile the program?

The software was developed in C++98 under Linux (Debian Wheezy), using the GNU g++ (Debian 4.7.2-5) 4.7.2 compiler and tested in this environment. The software is distributed as a compressed tar file, containing both the source code (in the src folder) and the scripts and instances (in the bin and bin\instances respectively). To install the program, first obtain the file TSPTW.V1.0.tar.gz. Unzip the file by typing:

gunzip TSPTW.V1.0.tar.gz

and then unpack it by typing:

tar -xvf TSPTW.V1.0.tar

The software will be extracted in a new folder TSPTW.V1.0 Finally, by launching

make all

the Makefile will trigger the compilation of the files, producing the executables 'TSPTW-II' and 'TSPTW-VND" in the bin folder.

Note: The code is written in C++98. Hence, the code should be reasonable portable to other Operating Systems than Linux or Unix.

Jacopo De Stefani Page 3 of 14

How to run the program?

Once the program has been compiled, two separate executable files, corresponding to the different kind of metaheuristic (i.e. Iterative Improvement and Variable Neighborhood Descent) can be either launched directly via the command line interface or using the bash script to launch.

The design choice to separate the two different kind of metaheuristic is made in order to limit the number of command line parameters to be given as input to the program.

Command-line execution

By launching¹:

```
./TSPTW-II [PARAMETERS] -i [INPUT_FILE] -s [SEEDS_FILE]
./TSPTW-VND [PARAMETERS] -i [INPUT FILE] -s [SEEDS FILE]
```

one can display the information about the meaning of the different options that can be given as input to the program.

Additional information concerning the usage of the program can be found in the README file.

The only mandatory options are "-i, -input" and "-s,-seeds", since without these components will not be possible to execute the simulation.

The argument to the input option must contain the full path to the instance file.

The seeds file must contain a number of seeds at least equal to the number of runs required, one seed per line without any additional information.

The options controlling the same parameters are mutually exclusive, with that meaning that only one option must be selected in order to run the program. If multiple options for the same parameter are chosen, the program will not run.

TSPTW-II

Parameter	Mutually exclusive options	
Initial solution	-d,-random, $-h,-heuristic$	
Neighborhood type	-t,-transpose , -e,-exchange , -n,-insert	
Pivoting rule	-f,–first-imp , -b,–best-imp	

TSPTW-VND

Parameter	Mutually exclusive options	
VND algorithm	-t,-standard , $-p,-piped$	
Neighborhood chain	-a, $-$ TEI , -b, $-$ TIE	

Output Every experiment produces a single file:

- (II) [$pivoting_rule$].[$neighborhood_type$].[$INSTANCE_NAME$] with [$pivoting_rule$] $\in \{first, best\}$ and [$neighborhood_type$] $\in \{transpose, exchange, insert\}$
- (VND) $[vnd_type]$. $[neighborhood_chain]$. $[INSTANCE_NAME]$ with $[vnd_type] \in \{standard, piped\}$ and $[neighborhood_type] \in \{tei, tie\}$

Examples:

```
exchange.best.n80w200.004.txt standard.tei.n80w20.003.txt
```

The internal structure of the file is the following: Seed CV CpuTime PRPD

For each run of the algorithm, the program writes in the file, using a tabulation as separator, the used seed, the number of constraints violations, the cpu runtime and the penalised relative percentage deviation.

Jacopo De Stefani Page 4 of 14

¹The squared-bracket notation implies that the formal parameters to the script have to be substituted by their actual value.

Script execution

By launching:

- ./launchTSPTW-II.sh [INSTANCE NAME] [RUNS] [SEEDS FILE]
- ./launchTSPTW-VND.sh [INSTANCE_NAME] [RUNS] [SEEDS_FILE]

The script will:

- 1. Create the files required by the data processing script to write statistics.
- 2. Generate a seed file, named [SEEDS_FILE] containing [RUNS] randomly generated seeds.
- 3. Launch the corresponding TSPTW program for [RUNS] using all the possible combinations of input options.
- 4. Wait for the termination of all the previously launched experiment and call the R data processing script

The script assumes that all the instances are located into the instances folder, hence it is only necessary to indicate the instance name, instead of the complete path.

Output Each execution of the script will then generate the files:

- $[INSTANCE_NAME] CpuTime.pdf$ containing the boxplots of the runtime distribution for each algorithm.
- $[INSTANCE_NAME] PRPD.pdf$ containing the boxplots of the PRPD distribution for each algorithm.
- (II) transpose.first, exchange.first, insert.first, transpose.best, exchange.best, insert.best
 - (VND) standard.tei, standard.tie, piped.tei, piped.tie

The internal structure of the file is the following:

			U
Instance	Infeasible	mean(PRDP)	mean(CpuTime)

Each line contains the instance name, the percentage of infeasible runs, the mean PRDP and the mean runtime across [RUNS] runs.

Jacopo De Stefani Page 5 of 14

Problem 1

Ant Colony Optimization

Problem statement

Implement two stochastic local search (SLS) algorithms for the traveling salesman problem with time windows (TPSTW), building on top of the perturbative local search methods from the first implementation exercise.

- 1. Run each algorithm 25 times with different random seed on each instance. Instances will be available from http://iridia.ulb.ac.be/~stuetzle/Teaching/HO/. As termination criterion, for each instance, use the maximum computation time it takes to run a full VND (implemented in the previous exercise) on the same instance and then multiply this time by 1000 (to allow for long enough runs of the SLS algorithms).
- 2. Compute the following statistics for each of the two SLS algorithms and each instance:
 - Percentage of runs with constraint violations
 - Mean penalised relative percentage deviation
- 3. Produce boxplots of penalised relative percentage deviation.
- 4. Determine, using statistical tests (in this case, the Wilcoxon test), whether there is a statistically significant difference between the quality of the solutions generated by the two algorithms.
- 5. Measure, for each of the implemented algorithms on 5 instances, the run-time distributions to reach sufficiently high quality solutions (e.g. best-known solutions available at http://iridia.ulb.ac.be/~manuel/tsptw-instances#instances). Measure the run-time distributions across 25 repetitions using a cut-off time of 10 times the termination criterion above.
- 6. Produce a written report on the implementation exercise:
 - Please make sure that each implemented SLS algorithm is appropriately described and that the computational results are carefully interpreted. Justify also the choice of the parameter settings and the choice of the iterative improvement algorithm for the hybrid SLS algorithm.
 - Present the results as in the previous implementation exercise (tables, boxplots, statistical tests).
 - Present graphically the results of the analysis of the run-time distributions.
 - Interpret appropriately the results and make conclusions on the relative performance of the algorithms across all the benchmark instances studied.

Introduction

Ant Colony Optimization is an example of population-based metaheuristic (i.e a set of algorithmic concepts that can be used to define heuristic methods) inspired by the behavior of the ant species *Iridomyrmex humilis*. To be more precise, these insects are able, by means of stigmergic communication, to choose the shortest path between their nest and a food source, when given the choice ([1]).

The communication process occurs by deposing a certain quantity of pheromone in the environment that can be sensed by the other ants and that will be used by them as an heuristic (i.e an information to guide their choice) for selecting the shortest path.

Furthermore, the pheromone quantity on a certain location decreases over time because of evaporation, thus requiring a continuous deposit process to be effective.

Jacopo De Stefani Page 6 of 14

The convergence to one of the paths will occur as a consequence of the self-reinforcing pheromone deposit mechanism. In fact the more pheromone is deposited on a path, the more ants will follow the pheromone trail on that path deposing even more pheromone.

The first application of Ant Colony Optimization method, the Ant System, has been made on the optimization version of the Travelling Salesman Problem (TSP) ([3]).

In this implementation a population of virtual agents (an ant colony) is used to explore the search space (the virtual environment).

In the same fashion as the real insects, the ants are able to deposit virtual pheromone in the environment, to signal to the other ants the presence of promising solutions.

The general outline of the implemented algorithm is the following (as in [2]):

Algorithm 1 Ant Colony Optimization - Outline

- 1: Initalize Pheromone Trail
- 2: while !(TerminationCondition) do
- 3: ConstructAntsSolutions
- 4: LocalSearch (Optional)
- 5: Update Pheromone Trails
- 6: end while

Problem formulation

An instance of the Travelling Salesman Problem with Time Windows (TSPTW) can be expressed as a tuple $\langle N, E, c, t \rangle$ where:

- $N: \{0, \cdots, n\}$ Node set
- $E: N \times N$ Edge set
- $c: E \mapsto \mathbb{R}$ Edge cost function mapping a cost c to every edge $e \in E$.
- $t: N \mapsto \mathbb{R}^2$ Time window function mapping a couple of values a_i, b_i representing respectively, the opening and closing time of the time window, such that $a_i < b_i$, to every node $i \in N$.
- A candidate solution for the problem, in this case, is represented as a permutation p of the nodes in N, where p_i represents the i^{th} solution component (node) in the sequence, such that $p_0 = 0 \forall p$.

As in [4] the formal definition of the problem is:

$$\mathbf{min} f(p) = \sum_{i=0}^{n} c(e_{p_i p_{k+i}}) (1)$$

subject to
$$\Omega(p) = \sum_{i=0}^{n+1} \omega(p_i) = 0 \tag{2}$$

(3)

where

$$\omega(p_i) \begin{cases} 1 & A_{p_i} < b_{p_i} \\ 0 & \text{otherwise} \end{cases}$$
 (4)

$$A_{p_{i+1}} = \max(A_{p_i}, a_i) + c(e_{p_i p_{k+i}})$$
(5)

As one may notice in 1 and 4, a feasible solution p for the problem is a permutation where the constraints related to the time windows are met for every node i in the permutation.

Jacopo De Stefani Page 7 of 14

Algorithm structure

The proposed algorithm is an implementation of one of the extensions to the Ant Colony Optimization metaheuristic framework, the $\mathcal{MAX} - \mathcal{MIN}$ Ant System (cf. [5]).

Algorithm 2 $\mathcal{MAX} - \mathcal{MIN}$ Ant System for TSPTW - Outline

```
1: procedure ACO(\alpha, \beta, \rho, \tau_0, n_{ants}, n_{cities}, t_{max})
                                                                                            \triangleright The main procedure
Require: N - Node set
Require: E - Edge set
Require: c - Edge cost function
Require: t - Time window function
        Initalize Pheromone Trail(\tau_0, n_{cities})
        while !TerminationCondition(t_{max}) do
 3:
           for all Ants do
 4:
               ConstructSolution(\alpha, \beta)
 5:
               IterativeImprovement(INSERT,BEST-IMPROVEMENT)
 6:
               UpdatePheromoneTrails(\rho)
 7:
           end for
 8:
 9:
        end while
        return solution
10:
11:
12: end procedure
```

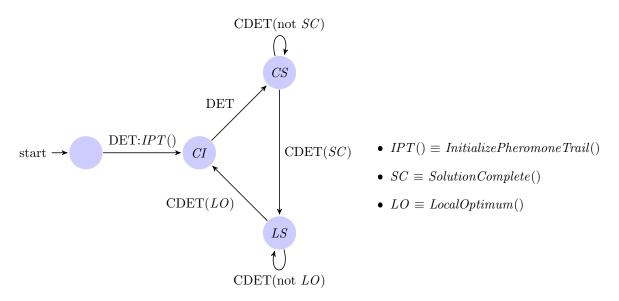


Figure 2: GLSM for the $\mathcal{MAX} - \mathcal{MIN}$ Ant System

In the implementation, an instance is completely defined by:

- Cost matrix Encapsulating information on the node set N, edge set E, and weighting of each edge c.
- Time window vector Describing the time window mapping function t for each node.

Jacopo De Stefani Page 8 of 14

Pheromone Initialization

As discussed in , the ACO methods are based on stigmergic communication among the agents by means of virtual pheromone.

While the real ants can deposit pheromone anywhere in the environment, the virtual ants may only exchange informations concerning solutions components.

For this reason, every admissible edge e_{ij} of E has an associated pheromone value τ_{ij} , that have to be initialized at the beginning of the execution of the algorithm.

The inizialization value τ_0 is a parameter of the algorithm.

Algorithm 3 Pheromone Initialization

```
1: procedure InitalizePheromoneTrail(\tau_0, n_{cities})
         i \leftarrow 0
2:
         j \leftarrow 0
 3:
         for i < n_{cities} do
 4:
              for j < i do
 5:
 6:
                   \tau_{ij} \leftarrow \tau_0
 7:
                   \tau_{ji} \leftarrow \tau_{ij}
 8:
                   j \leftarrow j + 1
              end for
9:
10:
              i \leftarrow i + 1
          end for
11:
12: end procedure
```

Solution construction

Algorithm 4 Solution Construction

```
1: procedure ConstructSolution(\alpha, \beta)
                                                                                                    ▶ The main procedure
                                                                       \triangleright s_i represes the i^{th} component of the solution
2:
        s_0 \leftarrow 0
                                                                                    ▷ Every solution starts at the depot
3:
        s_1 \leftarrow RandomCitySelection()
                                                                                   ▶ Random choice of the starting city
 4:
5:
        i \leftarrow 1
        while !SolutionComplete() do
6:
            k \leftarrow RouletteWheelSelection()
                                                              \triangleright k stochastically chosen according to the probability
7:
   distribution defined by p_k
8:
           s_i \leftarrow k
9:
            i \leftarrow i + 1
        end while
11: end procedure
```

$$p_{k} = \begin{cases} \frac{[\tau_{i-1,k}]^{\alpha} \cdot [\eta_{i-1,k}]^{\beta}}{\sum_{j \in N(s_{i-1})} [\tau_{i-1,j}]^{\alpha} \cdot [\eta_{i-1,j}]^{\beta}} & k \in N(s_{i-1}) \\ 0 & \text{otherwise} \end{cases}$$
(6)

Jacopo De Stefani Page 9 of 14

Possible heuristics

Cheng and Mao, 2007

The local heuristics used in the current algorithm are similar to that proposed by Gambardella et al. [24] in their multiple ant colony system (MACS) designed to solve the vehicle routing problem with time windows (VRPTW).

[24] L.M. Gambardella, E.D. Taillard, G. Agazzi, MACS-VRPTW: A multiple ant colony system for vehicle routing problems with time windows, in: D. Corne, M. Dorigo, F. Glover (Eds.), New Ideas in Optimization, McGraw Hill, London, UK, 1999, pp. 63–76.

$$[\eta_{i-1,k}]^{\beta} = [g_{i-1,k}]^{\beta} \cdot [h_{i-1,k}]^{\gamma} \tag{7}$$

$$g_{i-1,k} = \begin{cases} \frac{1}{1 + e^{\delta \cdot (G_{i-1,k} - \mu)}} & G_{i-1,k} = b_k - t_k \ge 0\\ 0 & \text{otherwise} \end{cases}$$
 (8)

where

- $G_{i,j} = b_j t_j$ Slack corresponding to the time window j while being in node i
- t_i Arrival time at node i
- b_i Closing time of time window i
- $G(i) = \{k \mid G_{i,k} \ge 0\}$ Set of feasible neighbors of node i (i.e. such that node k is reached earlier than its closing time)
- $\mu = \frac{1}{|G(i)|} \sum_{j \in G(i)} G_{i,j}$ Average slack
- \bullet δ Parameter to control the slope of the sigmoidal function

$$h_{i-1,k} = \begin{cases} \frac{1}{1 + e^{\lambda \cdot (H_{i-1,k} - v)}} & H_{i-1,k} = t_k - a_k \ge 0\\ 0 & \text{otherwise} \end{cases}$$
 (9)

where

- $H_{i,j} = t_j a_j$ Waiting time corresponding to the time window j while being in node i
- t_i Arrival time at node i
- a_i Opening time of time window i
- $H(i) = \{k \mid H_{i,k} \ge 0\}$ Set of non-waiting neighbors of node i (i.e such that node k is reached within the time window)
- $v = \frac{1}{|H(i)|} \sum_{j \in H(i)} H_{i,j}$ Average waiting time λ Parameter to control the slope of the sigmoidal function

Lopez-Ibanez and Blum, 2009

$$\eta_{i-1,k} = \lambda_a \cdot \frac{a_{\text{max}} - a_k}{a_{\text{max}} - a_{\text{min}}} + \lambda_b \cdot \frac{b_{\text{max}} - b_k}{b_{\text{max}} - b_{\text{min}}} + \lambda_c \cdot \frac{c_{\text{max}} - c_{i-1,k}}{c_{\text{max}} - c_{\text{min}}}$$

$$(10)$$

where

• a_i - Opening time of time window i

Jacopo De Stefani Page 10 of 14

- $a_{\max} = \max_{j \in N(i)} a_j$ Maximum time window opening time in the neighborhood of node i
- $a_{\min} = \min_{j \in N(i)} a_j$ Minimum time window opening time in the neighborhood of node i
- b_i Closing time of time window i
- $b_{\max} = \max_{j \in N(i)} b_j$ Maximum time window closing time in the neighborhood of node i
- $b_{\min} = \min_{j \in N(i)} b_j$ Minimum time window closing time in the neighborhood of node i
- $c_{i,j}$ Travelling cost from node i j
- $c_{\max} = \max_{j} c_{i,j}$ Maximum travelling cost from node i
- $c_{\min} = \min_{j} c_{i,j}$ Minimum travelling cost from node i
- $\lambda_a, \lambda_b, \lambda_c$ such that $\lambda_a + \lambda_b + \lambda_c = 1$ Randomly picked weights

Algorithm 5 Pheromone Trails Update

```
1: procedure UPDATEPHEROMONETRAILS(\rho)
                                                                                                                           ▶ The main procedure
          i \leftarrow 0
 2:
          j \leftarrow 0
 3:
          for i < n_{cities} do
 4:
               for j < i do
 5:
                    \tau_{ij} \leftarrow (1-\rho) \cdot \tau_{ij} + \Delta \tau_{i,j}
 6:
 7:
                    \tau_{ji} \leftarrow \tau_{ij}
                    j \leftarrow j + 1
 8:
               end for
 9:
               i \leftarrow i + 1
10:
          end for
11:
12: end procedure
```

MAX-MIN Ant System (MMAS)

- Only iteration best or best-so-far ants update pheromone
- $\tau_{\min} < \tau_{i,j}(t) < \tau_{\max} \forall t$ Pheromone trails have explicit upper and lower limits
- $\tau_{i,j}(0) = \tau_0 = \tau_{\text{max}} \forall t$ Pheromone trails initialized to upper limit
- Pheromone trails are re-initialized when stagnated

$$\Delta \tau_{i,j} = \begin{cases} \frac{1}{T_d} & e_{i,j} \in T^{\text{best}} \\ 0 & \text{otherwise} \end{cases}$$
 (11)

where

- $e_{i,j}$ Edge connecting node i and j
- T_d Complete tour duration
- \bullet T^{best} Best iteration

Jacopo De Stefani Page 11 of 14

An Iterative Improvement algorithm generally starts from a candidate solution, which can be either generated randomly or using an heuristic, and improves the evaluation of the solution at each step by modifying the solution structure, until a local optimum is reached.

In the previous problem, I considered different kinds of 2-opt neighborhood, and different pivoting rules.

This means that, at each step, a new solution is constructed from the current best by modifying only two solution components (with Transpose, Exchange or Insert operations) and only the first/best improving solution will become the new best solution.

The main limitation of such kind of algorithms is that they tend to get stuck in solutions that are locally optimum but not globally.

Provided that:

- A global optimum is optimal with respect to any kind of neighborhood.
- A solution that is locally optimal with respect to a neighborhood may not be optimal with respect to other kinds of neighborhood

by dynamically changing the neighborhood type an algorithm is able to escape local optima.

This section will analyse the results of the execution of two variable neighborhood descent algorithm, based on the previously analyzed iterative improvement algorithms:

- Standard Variable Neighborhood Descent (i.e. Changing neighborhood when a local optimum is encoutered, until the neighborhood chain is terminated and going back to the smallest neighborhood every time the local optimum is escaped.)
- **Piped Variable Neighborhood Descent** (i.e. Using the locally optimum solution found using one neighborhood type in the chain as the initial solution for the following type.)

The same metrics as in ?? will be used to evaluate the algorithms.

Results discussion

By looking at tables ??, ??, ??, ?? one can see that:

- For some instances (e.g. n80w20.002, n80w20.003) the algorithm are not able to converge to a feasible solution, as shown in the corresponding boxplots, since the PRPD distribution is centered around 12000-15000, thus indicating the presence of at least 1 constraint violations in most of the cases.
- For some other instances (e.g. n80w20.004, n80w20.005) the algorithms are able to converge to feasible solutions and to the best-known one, but having a right-skewed distribution towards higher values of PRPD.
- For the remaining instances, except for some outlier values, the algorithms are able to converge to the best-known solution in most of the runs, even though the average PRPD is not closer to 0. This is due to the fact that the mean of a distribution is sensible to outliers and the penalisation for a constraint violations is extremely high when compared to the mean value.
- The algorithm ordering in terms of runtimes is s.tie < p.tie < p.tie < p.tei < s.tei for the n80w20.X instances while s.tie < p.tei < s.tei < p.tie for n80w200.X ones. The choice to explore the Insert Neighborhood before the Exchange one allows to reduce the computation time for the n80w20.X instances, with a similar solution quality.
- The algorithms are more effective on the n80w200.X instances then the n80w20.X once, since they have a lower percentage of infeasible runs and a lower PRPD.

Jacopo De Stefani Page 12 of 14

- The standard variable neighborhood descent with Transpose-Insert-Exchange neighborhood chain (s.tie) outperforms all the other algorithms in terms of solution quality and runtime.
- Tables ??, ??, ??, ??, ??, ??, ??, ??, ?? contain, in any case, p-values considerably smaller than the significance level ($\alpha = 0.05$).
 - This implies that the null hypothesis corresponding to the equality of the median values of the differences of the two distributions can be rejected, hence assessing the existence of a statistically significant difference among the solution quality generated by analyzed algorithms.
- By looking at the Cpu time, one can see that the instances n80w20.X have generally lower runtimes than the n80w200.X ones. They can then be considered, with respect to the variable neighborhood descent algorithms, simpler (quickier to solve) instances with respect to the latter.

Jacopo De Stefani Page 13 of 14

Conclusions

By combining the results from the previous analysis:

- The Iterative Improvement algorithms based on Transpose and Exchange neighborhoods do not allow to find feasible solutions hence they should not be considered for a practical application.
- On the other hand, the solution quality generated by the Iterative Improvement algorithm with the Insert neighborhood is similar to those generated by the VND algorithms, regardless of the instances.
- On this set of instances, the VND algorithms have a lower runtime than the Iterative Improvement one using Insert neighborhood, hence being similar the resulting solution quality, they should be preferred to the Iterative Improvement ones.
- The algorithm that showed the best performances in terms of solution quality and runtime is the Standard Variable Neighborhood Descent with Transpose-Insert-Exchange neighborhood chain.
- The usage of average statistics as metrics to measure the quality of the algorithms is strongly biased by the presence of outliers (penalisation, in this case).

References

- [1] J-L Deneubourg, Serge Aron, Simon Goss, and Jacques Marie Pasteels. The self-organizing exploratory pattern of the argentine ant. *Journal of insect behavior*, 3(2):159–168, 1990.
- [2] Marco Dorigo, Mauro Birattari, and Thomas Stutzle. Artificial ants as a computational intelligence technique. *IEEE computational intelligence magazine*, pages 265–276, 2006.
- [3] Marco Dorigo, Vittorio Maniezzo, and Alberto Colorni. Ant system: optimization by a colony of cooperating agents. Systems, Man, and Cybernetics, Part B: Cybernetics, IEEE Transactions on, 26(1):29–41, 1996.
- [4] Manuel López-Ibáñez and Christian Blum. Beam-aco for the travelling salesman problem with time windows. Computers & operations research, 37(9):1570–1583, 2010.
- [5] Thomas Stützle and Holger H Hoos. Max-min ant system. Future Generation Computer Systems, 16(8):889–914, 2000.

Jacopo De Stefani Page 14 of 14