# Scientific Computing using python - mini project Documentation

Release

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# ONE

# **INDICES AND TABLES**

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# LORENZ SYSTEM

The Lorenz system is a system of ordinary differential equations first studied by Edward Lorenz. It has chaotic solutions for certain parameter values and initial conditions. The Lorenz attractor is a set of chaotic solutions of the Lorenz system which, when plotted, resemble a butterfly or figure eight.

The lorenz equations are as follows

$$\frac{dx}{dt} = \sigma(y - x),$$

$$\frac{dy}{dt} = x(\rho - z) - y,$$

$$\frac{dz}{dt} = xy - \beta z$$

In order to solve the differential equations it is necessary to implement a solver for the differential equations, for which the Euler approximation for first order differential equations is selected.

It is formulated as

$$\frac{x_{n+1} - x_n}{t_d} = f(x, y, z)$$
$$x_{n+1} = f(x, y, z) \cdot t_d + x_n$$

The same formulation is applied for the rest of the differential equations.

It should be noticed that the solution for a period of time of the lorenz attractor is very sensitive to initial conditions.

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4	Chapter 2.	Lorenz system

# **THREE**

# LAUNCHING THE TEST CASES FOR DIFFERENT PARAMETERS

Locate the terminal/ipython in the folder of cases. When running the script it will plot the different solutions and save all the figures, data and solutions to pdf and a hdf5 file.

You can run the test case 1 as

```
>>> python case1.py
```

## And for test case 2

```
>>> python case2.py
```

## and so on

```
>>> python case3.py
>>> python case4.py
>>> python case5.py
```



**FOUR** 

# **TESTING THE CODE**

Locate the terminal/ipython in the folder of tests. You can run the tests and it will be compared to numpy ODE solver. It should be noticed that the more chaotic the system it will fail the test.

It was observed that the Euler solver carry delays to the solution than the ODE solver inside numpy.

To run the tests you can type

>>> python test.py

It will pass the first three cases and fail the last two cases, which are compared to the ODE solver of numpy.

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**FIVE** 

# THE LORENZ PACKAGE

The package consists of the following modules and functions

# The modules and functions in the lorenz package are listed here

## Solver: lorenz attractor solver

#### Intro

It includes a basic solver for the lorenz attractor.

#### **Functions**

This is the solver for the differential equations of Lorenz attractor.

```
lorenz.solver.lorenz_solver(state, parameters, t_d)
```

Returns the array of x,y,z value after solving the ODE of the lorenz attractor using the Euler approach.

#### INPUT:

```
state: x,y,z state
parameters: sigma, rho, beta parameters
t_d: the time step for the discrete integration
```

#### OUTPUT:

```
[x+1, y+1, z+1]: The next x,y,z values
```

It is more accurate when it is close to the convergence point of the attractor.

## Example:

```
>>> state = [1.0, 1.0, 1.0]

>>> parameters = [1.0, 1.0, 1.0]

>>> t_d = 0.001

>>> lorenz_solver(state, parameters, t_d)

(1.0, 0.999, 1.0)
```

#### **Details**

**Solver** .- It solves the differential equations with a first order euler approach which explicit math is depicted below.

$$[x_{n+1}, y_{n+1}, z_{n+1}] = [t_d \sigma(y_n - x_n) + x_n, t_d(x_n(\rho - z_n) - y_n) + y_n, t_d(x_n y_n - \beta z_n) + z_n]$$

#### Code

```
This is the solver for the differential equations of Lorenz attractor.
def lorenz_solver(state, parameters, t_d):
   Returns the array of x,y,z value after solving the ODE of the lorenz
   attractor using the Euler approach.
    INPUT::
    state: x, y, z state
    parameters: sigma, rho, beta parameters
    t_d: the time step for the discrete integration
    OUTPUT::
     [x+1, y+1, z+1]: The next x, y, z values
    It is more accurate when it is close to the convergence point of the
   attractor.
   Example:
   >>> state = [1.0, 1.0, 1.0]
   >>> parameters = [1.0, 1.0, 1.0]
   >>> t_d = 0.001
   >>> lorenz_solver(state, parameters, t_d)
   (1.0, 0.999, 1.0)
   x, y, z = state # get the state
    sigma, rho, beta = parameters # get the parameters
    return t_d * sigma * (y - x) + x, t_d * (x * (rho - z) - y) + y,
          t_d * (x * y - beta * z ) + z
```

## Plot: functions for plotting

#### **Functions**

This file may contain functionalities for plotting

```
lorenz.plot.plot_2d (selection, states, save=False, fname='experimental', directory=None)
Plot the x,y and x,z and y,z coordinates of the lorenz attractor
INPUT:
```

```
selection: which to plot
states: array of [x,y,z]
save: bool value
fname: name of file
directory: route or name of folder
```

#### **OUTPUT**:

```
Plots and pdf figures
```

#### Example

```
>>> plot_2d("xy", states)
```

lorenz.plot.plot\_3d\_states (states, save=False, fname='experimental', directory=None)

Plot the x,y,z coordinates of the lorenz attractor

#### INPUT:

```
states: array of [x,y,z]
save: bool value
fname: name of file
directory: route or name of folder
```

#### **OUTPUT**:

```
Plots and pdf figures
```

#### Example

```
>>> plot_3d_states(states)
```

```
Example
   >>> plot_3d_states(states)
   fig = plt.figure()
   ax = Axes3D(fiq)
   #ax = fig.add_subplot(111, projection='3d')
   #ax = fig.gca(projection='3d')
   #ax = fig.add_subplot(111, projection = '3d')
   ax.plot(states[:,0], states[:,1], states[:,2])
   plt.title('Lorenz Attractor')
   ax.set_xlabel('X')
   ax.set_ylabel('Y')
   ax.set_zlabel('Z')
   if save:
       if directory != None:
            if not os.path.exists(directory):
                os.makedirs(directory)
           fig.savefig( directory + '/' + fname + '_3d.pdf' )
            fig.savefig( fname + '_3d.pdf' )
   plt.show()
   return
def plot_2d(selection, states, save = False, fname = 'experimental',
           directory = None):
   Plot the x,y and x,z and y,z coordinates of the lorenz attractor
   INPUT::
    selection: which to plot
    states: array of [x, y, z]
    save: bool value
    fname: name of file
    directory: route or name of folder
   OUTPUT::
    Plots and pdf figures
   Example
   >>> plot_2d("xy", states)
   plt.figure()
   if selection == "xy":
        n\ n\ n
       PLot xy graph
       plt.plot(states[:,0],states[:,1])
       plt.title("Lorenz Attractor XY")
       plt.xlabel('X')
       plt.ylabel('Y')
       plt.grid()
```

```
if save:
       if directory != None:
            if not os.path.exists(directory):
               os.makedirs(directory)
            plt.savefig( directory + '/' + fname + '_xy.pdf' )
        else:
           plt.savefig( fname + '_xy.pdf' )
   plt.show()
elif selection == "xz":
    n n n
   Plot xz graph
   plt.plot(states[:,0], states[:,2])
   plt.title("Lorenz Attractor XZ")
   plt.xlabel('X')
   plt.ylabel('Z')
   plt.grid()
    if save:
       if directory != None:
            if not os.path.exists(directory):
                os.makedirs(directory)
            plt.savefig( directory + '/' + fname + '_xz.pdf' )
        else:
            plt.savefig( fname + '_xz.pdf' )
   plt.show()
elif selection == "yz":
    Plot yz graph
   plt.plot(states[:,1], states[:,2])
   plt.title("Lorenz Attractor YZ")
   plt.xlabel('Y')
   plt.ylabel('Z')
   plt.grid()
    if save:
        if directory != None:
            if not os.path.exists(directory):
                os.makedirs(directory)
            plt.savefig( directory + '/' + fname + '_yz.pdf' )
        else:
            plt.savefig( fname + '_yz.pdf' )
    plt.show()
else:
   print ("The selection was not correct")
return
```

## File Handling: File handling for saving data for reproducible research

#### **Functions**

```
This file can contain functionalities for saving/loading data
```

```
lorenz.filehandling.load_all(fname)
Save the variables, parameters and results in a hdf5 file
INPUT:
```

```
fname: name of file
```

#### **OUTPUT**:

```
sigma: sigma parameter
rho: rho parameter
beta: beta parameter
x: x initial state
y: y initial state
z: z initial state
t_d: time differential
N: number of samples
states: array of states
```

#### Example:

```
>>> fname = "experimental"
>>> [sigma, rho, beta, x, y, z, t_d, N, states] = load_all(fname)
```

lorenz.filehandling.save\_all (fname, sigma, rho, beta, x, y, z, t\_d, N, states, directory=None) Save the variables, parameters and results in a hdf5 file

#### INPUT:

```
fname: name of file
sigma: sigma parameter
rho: rho parameter
beta: beta parameter
x: x initial state
y: y initial state
z: z initial state
t_d: time differential
N: number of samples
states: array of states
directory: directory for saving
```

#### **OUTPUT:**

```
A file with all the variables in it.
```

#### Example:

```
>>> save_all(fname, sigma, rho, beta, x, y, z, t_d, N, states)
```

```
This file can contain functionalities for saving/loading data

"""

import h5py, os

def save_all(fname, sigma, rho, beta, x, y, z, t_d, N, states, directory = None):

"""

Save the variables, parameters and results in a hdf5 file
```

```
INPUT::
    fname: name of file
    sigma: sigma parameter
    rho: rho parameter
    beta: beta parameter
    x: x initial state
    y: y initial state
    z: z initial state
    t_d: time differential
    N: number of samples
    states: array of states
    directory: directory for saving
   OUTPUT::
    A file with all the variables in it.
   Example:
   >>> save_all(fname, sigma, rho, beta, x, y, z, t_d, N, states)
   ......
   if directory != None:
       if not os.path.exists(directory):
           os.makedirs(directory)
       f = h5py.File( directory + '/' + fname + '.hdf5', 'w')
   else:
       f = h5py.File( fname + '.hdf5', 'w')
   f.create_dataset( 'sigma', data = sigma)
   f.create_dataset( 'rho', data = rho)
   f.create_dataset( 'beta', data = beta)
   f.create_dataset( 'x', data = x)
   f.create_dataset( 'y', data = y)
   f.create_dataset( 'z', data = z)
   f.create_dataset( 't_d', data = t_d)
   f.create_dataset( 'N', data = N)
   f.create_dataset( 'states', data = states)
   f.close()
def load_all(fname):
   Save the variables, parameters and results in a hdf5 file
   INPUT::
    fname:
            name of file
   OUTPUT::
    rho: rho parameter beta: beta r
             sigma parameter
            beta parameter
    x: x initial state
    y: y initial state
    z: z initial state
```

```
t_d: time differential
 N: number of samples
 states: array of states
Example:
>>> fname = "experimental"
>>> [sigma, rho, beta, x, y, z, t_d, N, states] = load_all(fname)
f = h5py.File( fname + '.hdf5', 'r')
sigma = f [ 'sigma' ]
sigma = sigma [...]
rho = f [ 'rho' ]
rho = rho [...]
beta = f [ 'beta' ]
beta = beta [...]
x = f [ 'x']
x = x [...]
y = f ['y']
y = y [...]
z = f ['z']
z = z [...]
t_d = f [ 't_d' ]
t_d = t_d [...]
N = f [ 'N' ]
N = N [...]
states = f [ 'states' ]
states = states [...]
return sigma, rho, beta, x, y, z, t_d, N, states
```

## Run: Code for running all together

## **Functions**

This file may contain a convenient interface/function for

1: computing a trajectory using an ODE solver from solver.py 2: save data to file 3: plot data and possible another function that

2: load data from file 3: plot data

```
lorenz.run.load_lorenz(fname='Test', plot=True)
```

This function will load the lorenz and plot it

#### INPUT:

```
fname: the name of the file to open
plot: bool to plot or not
```

#### **OUTPUT**:

```
Nothing, just plots
```

#### Example:

```
>>> load_lorenz('Test', True)
```

lorenz.run.run\_lorenz (parameters, ini\_state=[0.1, 0.1, 0.1], t\_d=0.001, N=50000, plot=False, save=False, fname='Test', directory=None)

Return the states, save the variables, plots and save the plots using the auxiliary functions provided.

#### INPUT:

```
parameters: the parameters of the lorenz attractor ini_state: initial state of the lorenz attractor t_d: the time differential N: number of samples plot: bool to plot save: bool for saving fname: name of file directory: directory to save
```

#### OUTPUT:

```
states: the states of the lorenz attractor in the span of the differential time and number of samples
```

#### Example:

```
>>> param = [10, 2, 6]
>>> run_lorenz(param)
```

```
This file may contain a convenient interface/function for
1: computing a trajectory using an ODE solver from solver.py
2: save data to file
3: plot data
and possible another function that
2: load data from file
3: plot data
import numpy as np
import sys, os
sys.path.append(os.path.join(os.path.dirname(__file__), ".."))
import lorenz.plot as pl
import lorenz.solver as sol
import lorenz.filehandling as fh
import lorenz.util as ut
import matplotlib.pyplot as plt
def run_lorenz(parameters, ini_state = [0.1, 0.1, 0.1], t_d = 1e-3,
               N = 50000, plot = False, save = False, fname = 'Test',
               directory = None):
```

```
Return the states, save the variables, plots and save the plots
   using the auxiliary functions provided.
   INPUT::
    parameters: the parameters of the lorenz attractor
    ini_state: initial state of the lorenz attractor
    t_d: the time differential
    N: number of samples
    plot: bool to plot
    save: bool for saving
    fname: name of file
    directory: directory to save
    OUTPUT::
              the states of the lorenz attractor in the span of
    states:
               the differential time and number of samples
   Example:
   >>> param = [10, 2, 6]
   >>> run_lorenz(param)
   sigma, rho, beta = parameters
   x, y, z = ini_state
   \#t_d = t/N
   #time = [i*t_d for i in range(N)] #get each discrete time
   states = np.array([[x,y,z]]) #create the array
   t = t_d * N
   ti = np.arange(0.0, t, t_d)
   cntr = 1
   for i in ti[:-1]:
       states = np.concatenate((states,
            [sol.lorenz_solver(states[cntr-1,:], parameters, t_d)]))
       cntr = cntr + 1
        #states = np.concatenate((states,
       # [sol.lorenz_solver(states[i-1,:], parameters, t_d)]))
    if plot:
       pl.plot_3d_states(states, save, fname, directory) #plot x,y,z
       pl.plot_2d("xy", states, save, fname, directory) #plot xy
       pl.plot_2d("xz", states, save, fname, directory) #plot xz
       pl.plot_2d("yz", states, save, fname, directory) #plot yz
    if save:
       fh.save_all(fname, sigma, rho, beta, x, y, z, t_d, N, states,
                   directory)
   return states
def load_lorenz(fname = 'Test', plot = True):
    This function will load the lorenz and plot it
    INPUT::
             the name of the file to open
    fname:
    plot: bool to plot or not
```

```
OUTPUT::
    Nothing, just plots
   Example:
   >>> load_lorenz('Test', True)
    [s2, r3, b2, x2, y2, z2, t_d2, N2, st2] = fh.load_all(fname)
   if plot:
        pl.plot_3d_states(st2)
    return
if __name__ == '__main__':
    11 11 11
    This is just debugging code
#print("This is a convenient interface for running the simulation \setminus
     of a lorenz attractor")
    #sigma = ut.my_input_float("sigma") #input all parameters
    #rho = ut.my_input_float("rho")
    #beta = ut.my_input_float("beta")
    #x = ut.my_input_float("x") #input initial conditions
    #y = ut.my_input_float("y")
    #z = ut.my_input_float("z")
    #ini\_state = x, y, z
   sigma = 10
   rho = 6
   beta = 8/3
   ini_state = [1.0, 1.0, 1.0]
   t_d = 0.01
   #t = ut.my_input_int("time in seconds")
   parameters = (sigma, rho, beta)
   N = 80000 #assign 50000 steps as suggested
   t = t_d * N #timestep calculated from simulation time
    \#states = np.array([[x,y,z]]) \#create the array
    states = np.array([ini_state])
    for i in range (0, N-1):
        states = np.concatenate((states,
            [sol.lorenz_solver(states[i-1,:], parameters, t_d)]))
    pl.plot_3d_states(states) #plot x,y,z
    #pl.plot_2d("xy", states) #plot xy
    #pl.plot_2d("xz", states) #plot xz
    #pl.plot_2d("yz", states) #plot yz
    #fh.save_all('testo', sigma, rho, beta, x, y, z, t, t_d, states)
    #[s2,r3,b2,x2,y2,z2,t2,t_d2,st2] = fh.load_all('testo')
    #pl.plot_3d_states(st2)
    This is for testing. For testing the function.
   w_states = ut.wikipedia_lorenz([sigma, rho, beta], ini_state, t_d, N, plot = True)
    fig = plt.figure()
```

```
ax = fig.gca(projection='3d')
   ax.plot(w_states[0000:70000,0], w_states[0000:70000,1], w_states[0000:70000,2])
   plt.legend(['wiki'])
   plt.title('Wikipedia')
   plt.show()
  fig = plt.figure()
   ax = fig.gca(projection='3d')
   ax.plot(states[0000:70000,0], states[0000:70000,1], states[0000:70000,2])
   plt.legend(['my'])
   plt.title(' mine')
   plt.show()
   fig = plt.figure()
   ax = fig.gca(projection='3d')
   ax.plot(states[:,0], states[:,1], states[:,2])
   ax.plot(w_states[:,0], w_states[:,1], w_states[:,2])
   plt.legend(['my','wiki'])
   plt.title('Wikipedia vs mine')
   plt.show()
   ss = states - w_states
   fig = plt.figure()
   ax = fig.gca(projection='3d')
   ax.plot(ss[:,0], ss[:,1], ss[:,2])
   plt.legend(['my'])
   plt.title('diff Wikipedia vs mine')
   plt.show()
#
#
#
    import numpy as np
#
    import matplotlib.pyplot as plt
#
    from scipy.integrate import odeint
#
    from mpl_toolkits.mplot3d import Axes3D
#
#
    rho = 28.0
    sigma = 10.0
    beta = 8.0 / 3.0
#
    def f(state, t):
        x, y, z = state # unpack the state vector
        return sigma * (y - x), x * (rho - z) - y, x * y - beta * z # derivatives
#
    state0 = [1.0, 1.0, 1.0]
#
    t = np.arange(0.0, 40.0, 0.01)
#
#
    states = odeint(f, state0, t)
#
    fig = plt.figure()
    ax = fig.gca(projection='3d')
#
    ax.plot(states[:,0], states[:,1], states[:,2])
    plt.show()
```

## **Util: Utility code**

#### **Functions**

This file may contain utility functionalities.

```
lorenz.util.my_input_float(var)
```

This function is for validation of entering a float value.

#### **INPUT:**

```
var: name of variable to display.
```

#### **OUTPUT:**

```
variable: float input variable
```

#### Example:

```
>>> a = my_input_float("a")
```

```
lorenz.util.my_input_int(var)
```

This function is for validation of entering an int value.

#### INPUT:

```
var: name of variable to display.
```

#### **OUTPUT**:

```
variable: int input variable
```

## Example:

```
>>> a = my_input_int("a")
```

lorenz.util.wikipedia\_lorenz(parameters,  $ini_state=[1.0, 1.0, 1.0]$ ,  $t_d=0.0008$ , N=50000, plot=False)

This is a Lorenz attractor taken from the wikipedia page It will solve the lorenz attractor with a built-in solver odeint of numpy

#### INPUT:

```
parameters: array of parameters of the lorenz attractor ini_state: initial state t_d: time difference N: number of samples plot: bool value for ploting
```

#### **OUTPUT**:

```
states: array of states
```

#### Example:

```
>>> state = [1.0, 1.0, 1.0]

>>> parameters = [1.0, 1.0, 1.0]

>>> t_d = 0.001

>>> states = lorenz_solver(parameters, state, t_d, plot = True)
```

```
This file may contain utility functionalities.
import numpy as np
import matplotlib.pyplot as plt
from scipy.integrate import odeint
from mpl_toolkits.mplot3d import Axes3D
def my_input_float(var):
   This function is for validation of entering a float value.
    INPUT::
    var: name of variable to display.
   OUTPUT::
    variable: float input variable
   Example:
   >>> a = my_input_float("a")
   while True:
       try:
           variable = float(input("Please enter "+ var +": "))
       except ValueError:
           print("Sorry, I didn't understand that.")
           continue
       else:
           break
   return variable
def my_input_int(var):
    This function is for validation of entering an int value.
   INPUT::
    var: name of variable to display.
   OUTPUT::
    variable: int input variable
   Example:
   >>> a = my_input_int("a")
   while True:
```

```
try:
           variable = int(input("Please enter "+ var +": "))
       except ValueError:
           print("Sorry, I didn't understand that.")
           continue
       else:
           break
   return variable
def wikipedia_lorenz(parameters, ini_state = [1.0, 1.0, 1.0],
                    t_d = 8e-4, N = 50000, plot = False):
   This is a Lorenz attractor taken from the wikipedia page
    It will solve the lorenz attractor with a built-in solver
   odeint of numpy
   INPUT::
    parameters: array of parameters of the lorenz attractor
    ini_state:
                 initial state
    t_d: time difference
    N: number of samples
    plot: bool value for ploting
    OUTPUT::
    states:
              array of states
   Example:
   >>> state = [1.0, 1.0, 1.0]
   >>> parameters = [1.0, 1.0, 1.0]
   >>> t_d = 0.001
   >>> states = lorenz_solver(parameters, state, t_d, plot = True)
   sigma, rho, beta = parameters
   x, y, z = ini_state
    \#t\_d = t/N
   def f(state, t):
       x, y, z = state # unpack the state vector
       return sigma * (y - x), x * (rho - z) - y, x * y - beta * z # derivatives
   t_t = t_d * N
   t = np.arange(0.0, t_t, t_d)
   states = odeint(f, ini_state, t)
   if plot:
       fig = plt.figure()
       ax = fig.gca(projection='3d')
       ax.plot(states[:,0], states[:,1], states[:,2])
       plt.title('Wikipedia Lorenz Attractor')
       plt.show()
   return states
```

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