


Introduction to Robotics

[Introduction to Robotics book PDF](#), Third Edition. John J. Craig,

 **Youtube** : 고려대학교 송재복 교수님

Chapter 2. Manipulator kinematics

2-1. Introduction

- **Kinematics**
 - The relationship between position, velocity, acceleration and time of the arm links.
 - The forces which cause motion are not included in kinematics.
- **Roles of kinematics in the robot arm**
 - The relationship between the end-effector pose(position, orientation) and the joint variables can be obtained by studying kinematics.
- **Joint space(관절 공간)**

- Joint vector : a vector consisting of n joint variables of arm

$$q = \begin{bmatrix} q_1 \\ \vdots \\ q_n \end{bmatrix}, \text{ where } q_i : \text{joint variable}(i = 1, \dots, n)$$

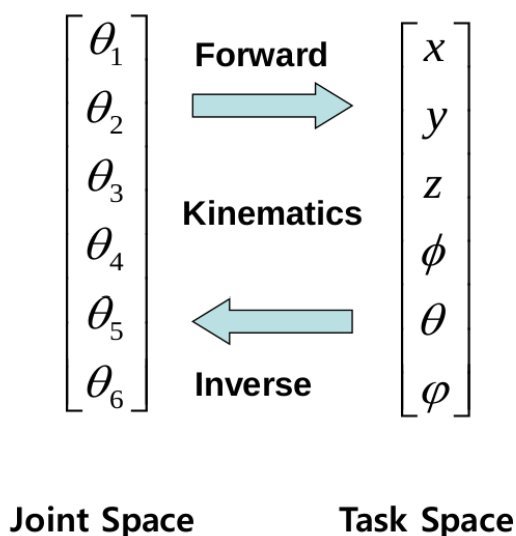
- Joint space : a space consisting of all joint vectors

- **Cartesian space (직교 공간) (or operational, task space)**

- End-effector pose vector

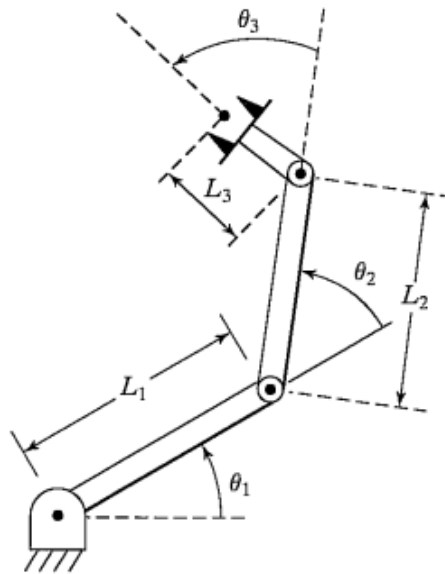
$$x = \begin{bmatrix} P \\ - \\ \alpha \end{bmatrix} \in \mathbb{R}^{m \times 1}, \text{ where } p : \text{end-effector position} \ \& \ \alpha : \text{end-effector orientation}$$

- A space in which the end-effector pose is measured in the Cartesian coordinate system.



2-2. Forward kinematics

- Joint space \rightarrow Cartesian space



2-3. Inverse kinematics

- Cartesian space \rightarrow Joint space

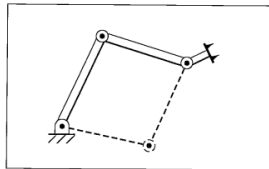


FIGURE 4.2: Three-link manipulator. Dashed lines indicate a second solution.

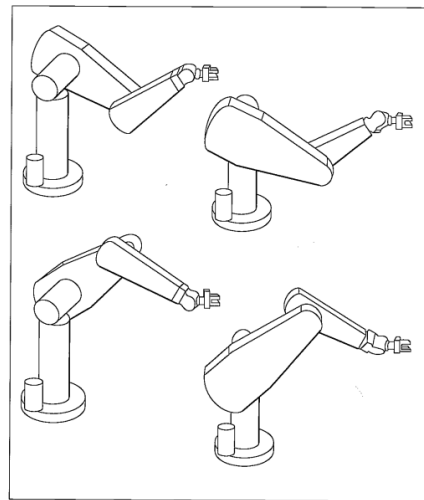


FIGURE 4.4: Four solutions of the PUMA 560.

next  [jacobian matrix](#)