Analyzing air quality, providing lowpollution bicycle routing in Stuttgart, Germany

Seminar: GIS Analyses with Free and Open-Source Software

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0. Abstract

Airborne particulate matter (PM) is in the focus of public health concern. In 2016, the city of Stuttgart, Germany introduced measures to reduce the PM levels within the city.

In this study, two sources of air pollution data to analyse the PM-concentration were used:

Citizen-science data from Luftdaten.info project using low-cost, self-built sensors; and official air quality sensor data by the State Office for the Environment, Measurements and Nature Conservation of the Federal State of Baden-Württemberg (LUBW).

The hourly data was automatically downloaded from the respective API, ingested into a database, filtered for outliers, then passed to a raster-interpolation process and a bicycle routing application.

An in-short analysis of comparability between the two datasets showed overall agreement in terms of general PM-concentration trends, yet considerable discrepancies (#how much?) on daily concentration levels.

A comparison of raster interpolation methods showed comparable outputs for inverse distance weighted, B-Splines and regularized splines with tension methods. The latter produced the output most fitting for this study.

Based on the resulting data, a bicycle routing application was developed, allowing users to avoid areas of high average PM-concentration for different hours of the day.

1. Introduction

Since the introduction of a public alert for high particulate matter (PM) concentrations ("Feinstaubalarm") in 2016, the issue of air quality in the city of Stuttgart, Germany, has been in the focus of media and scientific interest due to increased levels of particulate matter.

Atmospheric particulate matter (PM) is solid or liquid matter suspended in the atmosphere with diameters of under 10 μ m (coarse-particle matter) or under 2.5 μ m (fine-particle matter) (FUZZI ET AL. 2015 pp. 8228). In the past years, there has been a high interest in particulate matter and its effects on human health (FUZZI ET AL. 2015 p. 8217).

Short-term exposure to particulate matter can cause inflammation of the respiratory system, immune response and oxidative stress to the affected cells (RISTOVSKI, Z. ET AL. 2005, p. 205).

Long term exposure to elevated levels of particulate matter can lead to increased mortiality due to nonallergic respiratory morbidity, allergic illness and symptoms (such as asthma), cardiovascular morbidity, cancer, and effects pregnancy, birth outcomes and male fertility (HEINRICH ET AL 2005, pp. 132).

It is also the area of interest of an ongoing project by the German Federal Ministry of Transport and Digital Infrastructure (BMVI): The Satellite-based system for displaying, predicting and simulating air pollutants for sustainable urban and regional development ("Satellitenbasiertes System zur Anzeige, Prognose und Simulation von Luftschadstoffen für eine nachhaltige Stadt- und Regionalentwicklung - SAUBER").

At the same time, while cycling has no direct adverse effect on the air quality - cyclists themselves are directly subjected to air pollution within a city, as cycle paths are usually in immediate proximity to roads. Analyzing and mapping this concentration and distribution of particulate matter - and to map a 'least-polluted' route through particularly affected areas - is a step towards informing about - and protecting users from - air pollution in the city of Stuttgart.

It is also a step towards informing decision-making processes e.g. for guiding the traffic of combustion engine vehicles and possibly enforce restrictions on it in order to reduce air pollution.

It is vital for the analysis to combine official datasets with more extensive open source data, as a recent study on the impact of driving bans in Stuttgart states that "The sparsity [of the sensor network] introduces uncertainty which cannot be modeled correctly or can not be modeled at all" (WOLFMANN ET AL. 2019, pp. 295)

The goal of this analysis is thus to provide a small-scale geographic analysis of the particulate matter concentration in the city of Stuttgart; comparing official and *citizen-science* data quality; making the resulting map available on a user-interface; and allowing users to combine the results with a routing service informed by the result of the analysis.

2. Literature research

Using PM monitoring site data, LI ET AL. (2017) offer a literature review of interpolation methods (LI ET AL. 2017, pp. 9103) and identify the Inverse Distance Weight (IDW) method as most widely used in epidemiological studies on air pollution (LI ET AL. 2017, p. 9104).

In an early approach of mapping air pollution using data from low-cost sensors, BRIGGS ET AL. mention Kriging as standard method of geographic interpolation; but developed a multiple regression model fitted for different cities individually (BRIGGS ET AL. 1997, p. 701). The use using weighted land cover instead of simple distance weight (BRIGGS ET AL. 1997, p. 707) appears useful for inner-city mapping. For modelling air pollution, MATĚJÍČEK ET AL. (2006) used a simple Inverse Distance Weighting method and ordinary Kriging with estimates of variability (MATĚJÍČEK ET AL. 2006, p. 266).

AL-HAMDAN ET AL. (2009) coupled PM 2.5 air pollution data with Moderate Resolution Imaging Spectrometer data to reduce errors and explored both IDW and B-Spline surface-fitting techniques.

The Office for the Environment, Measurements and Nature Conservation of the Federal State of Baden-Württemberg (LUBW) has conducted research into the comparability of the Nova Fitness SDS011 sensor used by Luftdaten.info (see 3.1), and a calibrated sensor by Grimm GmbH. The SDS011 sensor performs comparable to sensors used by the LUBW in conditions of 50-70% air humidity and below 20µg/m3 PM concentration. Above these thresholds, or under changing atmospheric conditions, the SDS011 data significantly higher values (LUBW 2017, pp.17). The tests were conducted under 'laboratory' conditions and direct comparison between one LUBW measuring station and one nearby SDS011 (LUBW 2017, pp. 17).

3. Data

3.1 Particulate matter sensor data

Air quality measurements in Stuttgart and the State of Baden-Württemberg is conducted by the State Office for the Environment, Measurements and Nature Conservation of the Federal State of Baden-Württemberg (LUBW). The LUBW operates 44 measuring stations within the State of Baden-Württemberg, with 5 stations located within Stuttgart itself. Upon request, direct access to the measuring station data was not provided by the LUBW. Thus, the first goal of the project will be to access and automatically download the output of the LUBW's publicly available data at https://www.lubw.baden-wuerttemberg.de/luft/messwerte-immissionswerte. The site provides an hourly average of Ozone (O3) and Nitrogen dioxide (NO2); and a moving 24-hour average of particulate matter (PM2.5, PM10). The data is provided in the GeoJSON format.

To supplement these measurements, the Stuttgart-based project Luftdaten.info was brought into life. As a 'Citizen Science'-project, it offers shopping and building instructions for inexpensive particulate matter sensors (mainly the Nova Fitness Co., Ltd. SDS011), and multiple APIs at https://github.com/opendata-stuttgart/meta/wiki/APIs to access the recorded data, which are queryable for e.g. geographic bounding boxes, and with a temporal resolution of down to 5 minutes. The Luftdaten.info-data is provided in JSON formatting.

The strength of the project is the relatively very high density of sensors - especially within the city of Stuttgart. A simple bounding-box query of all active sensor around in the greater area of Stuttgart has yielded 1350 sensors. Apart from the non-standarized installation of the sensor, the accuracy of measurements of the SDS011 sensor was investigated by the LUBW (2017) and discussed in BLON (2017).

Direct comparisons of the accuracy of the PM-measuring devices used in the Luftdaten.info project has shown that while the SDS011 perform measurements comparable to the calibrated, high-accuracy sensors used by the LUBW in conditions of 50-70% air humidity and below 20µg/m3 PM concentration. Above these thresholds, or under changing atmospheric conditions respectively, the reported concentrations by the SDS011 show significant discrepancies (LUBW 2017, p.5).

Since the smallest temporal resolution offered by the LUBW is one hour, and the accuracy of the SDS011 data seems to benefit from using aggregate data, the project's aim is to use hourly data from the Luftdaten.info project. Additionally, subsequent analyses based on this project can utilize different queries on Luftdaten.info APIs in terms of geographical area, temporal resolution, etc. with little effort.

The hourly data can be categorized by using the *European Air Quality Index* (EAQI) which was was developed jointly by the European Commission's Directorate General for Environment and the European Environment Agency to inform citizens and public

authorities about the recent air quality status across Europe₁. The classification is explained in chapter 4.6.

3.2 OpenStreetMap Data

Data from the collaborative OpenStreetMap (OSM) project is used both for the analysis as well as internally by the Openrouteservice.

OpenStreetMap was founded back in 2004 because of the often legal and technical restrictions of most maps. The data is available to everyone without charge under the condition of appropriate attribution. Furthermore, corrections and improvements of the data can be shared back with the project by using online or standalone editors.

Although the data quality is a controversial issue, OSM data is widely used and produces results comparable with proprietary map providers. Especially in developed countries the coverage of way data is very good and often surpasses traditional data sets that fail to capture smaller tracks and paths.

Apart from the available geodata and possible contributions, OSM additionally offers map tiles that are used as background map for a lot of web applications.

The Openrouteservice offers calculation of shortest and fastest routes for different vehicle-, bicycle- and pedestrian-profiles. The graph needed for calculating the solution of the shortest-path-problem is built from OSM data. Only appropriate ways are extracted from a global dataset to build the way network which is updated currently about once a month.

For the analysis the boundaries of the administrative area of Stuttgart and the areas of different districts are pulled from the OSM database to generate the extent of the GRASS location and visualize the area of Stuttgart in the web application.

4. Methodology

4.1 Data model

In order to organize the stream of relevant input sensor data, a time-series data model for low redundancy and disk usage was developed:

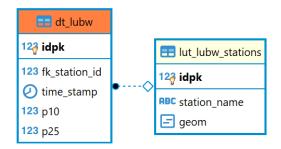


Figure 1: Entity relationship data model

The E-R diagram shows the data model. The actual sensor data is stored in a data table containing each hourly data point as one row. The columns consist of

- idpk: an individual primary key / ID
- fk_station_id: the station ID, which is assigned during parsing
- time_stamp: the time stamp of the measurement
- p10: the PM10 value
- p25: the PM25 value

To prevent having to store non-changing values such as the name and location of the associated sensor on disk, the data tables for both API data contain a column "fk_station_id" to reference this information once for each sensor in a lookup-table as a foreign key.

4.2 Data download

To store the expected numerous datapoints, a database, including a fitting data-model was developed. PostGIS, an extension to the Free and Open Source relational Database Management System PostgreSQL, offers support of geographic data types and simple geographical analyses.

In order to obtain a complete, 24-hour dataset from the respective APIs, automated download scripts were developed to access, download and ingest the data, which were run by the task scheduler *cron*. For these hourly values, both APIs did not offer any filter on retrieval. Thus, the "global" datasets from each API for each hour were downloaded.

This was realized via the two *shell*-scripts *dl_lubw.sh* and *dl_luftdaten.sh*. The scripts download the data using the *cURL*-library. In case of a failed download due to temporary connectivity problems, the scripts will reattempt downloading the dataset every 30 seconds.

On success, the files are stored on the host system under given a unique name based on the time of download.

As the LUBW API already provided valid GeoJSON data, the *ogr2ogr* command of the GDAL library was used to insert each file into a temporary database table. Afterwards, a parser function is invoked by the script. Since the input data contains the name of each sensor location, the function finds all values matching the name "Stuttgart", then distributes the values according to the data model described in #4.1.

The Luftdaten.info data is similarly ingested into a temporary database table. Due to the structure of the data, first the geographical location of each sensor is built from lat/lon values, then a geographical filter is applied by intersecting the values with a reference polygon for the area of interest. Lastly, due to apparent non-valid values for the PM-concentration, a preliminary filter discarding values higher than 200µg/m³ is applied before the values are ingested into the persistent data- and lookup-tables.

The OSM data used for the GRASS location and visualization are extracted by the download_osm_data.py script. It is the only script that was run in a Python 3 environment due to complications between the request package and the Python version used by the GRASS shell. The script automatically downloads the geometries from OSM using the Overpass API2 and converts the response to a GeoJSON with the osmtogeojson command line tool3.

4.3 Data pre-processing

Access to the stored data was realized within the database via stored SQL queries ("views").

While LUBW data showed no obvious outliers, Luftdaten.api data was filtered for extreme PM-values during ingestion into the database (see 4.2). The remaining dataset still contained outlying measurements of several hundred percent above the city-wide mean value of the same timeframe.

In order to provide additional filtering for outliers, the database views on Luftdaten.info data calculates the 99_{th} percentile of PM-concentration for the requested timeframe, then discards any value above it. Trials with this method showed that for timeframes without extreme values, the 99_{th} percentile will fall directly on the highest recorded value, which in consequence is not discarded from the query.

For the bicycle routing application, a set of 24 views for each hour of the day were created via a batch script. Each view combines all filtered Luftdaten.info and LUBW sensors with their respective, average PM-concentration of the queried hour.

In respect to the scope of the project and the therefore limited time, instead of directly connecting the GRASS workflow with the database to always interpolate the most

² https://overpass-api.de/api/interpreter

³ https://www.npmjs.com/package/osmtogeojson

recent data, the average aggregated values for every hour of the day were used from the 02.01.2020 to the 29.02.2020.

After creating a new GRASS Location, the *interpolation_setup.py* script is used to import needed files to the GRASS database for further processing and also remove some stations, that were reporting unreasonable values during most hours, from the hourly aggregated data. The script additionally creates the classification files needed for the categorization as well as a *eaqi_colors.txt* file, which enables the GRASS user interface to display classified raster in the original colors used on the EAQI website.

4.4 Comparing official and crowd-sourced data

Based on the findings concerning measurement accuracy of Luftdaten.info data in chapter 4.4, a simple comparison of both datasets regarding their comparability was performed.

Using an SQL-query, the PM-concentration recorded by the three LUBW stations was compared to the average of all Luftdaten.info sensors within a radius of 1000 meters for each timestep. The resulting line graph is shown in chapter #5.

4.5 Interpolation

Air quality and air pollution are spatio-temporal ('4-D') data. Meanwhile, the measurements of air pollution by official or distributed measuring stations are point-data.

An analysis of the concentration of particulate matter within the city of Stuttgart needs to interpolate the measured concentration of particulate matter at one station with its surrounding environment. (move somewhere else? Intro?)

As by course specification the free and Open Source GIS *GRASS* was used to perform the interpolation of the pollution point data. For the installed GRASS version three interpolation algorithms are available which were tested with different parameters and analyzed for suitability by means of calculating a normalized difference raster for categorized (EAQI see 4.6) raster of various input combinations. The tests were executed by the *{method}_tests.py* scripts with the data for the 11th hour of the day.

The directly accessible interpolation methods were *v.surf.idw* (IDW method), *v.surf.bspline* that is using bilinear splines (B-Splines) for 2D interpolation and *v.surf.rst* which uses regularized splines with adjustable tension (RST).

Although Kriging is supported by GRASS through the *v.kriging* extension it was not possible to enable it due to failing installation.

To explore their capabilities, each of the methods was run with parameter configurations where one parameter changed while the other ones were static. By creating a difference raster of the categorized output of the lowest and highest parameter value using *r.mapcalc*, the impact of the parameter became apparent. The insights were used to choose a fitting parameter configuration for each method.

After classification of the interpolated raster, all of the methods produced comparable result with some minor differences. The RST algorithm was best suited for the use case and therefore utilized for the final interpolation (see chapter 5). It is used with a *smooth* factor of 0.1 and a high *tension* of 100. Apart from hardcoded 10 and 50 for *segmax* and *npmin* values respectively, to minimize interfering artefacts, the default values were used.

4.6 Categorization

To facilitate the identification and graphical representation of polluted areas, the interpolated data is further categorized using the EAQI (see 3.1).

The index is specifically developed for short-term air quality situations and is therefore the appropriate choice for the calculated hourly mean data set. The basis for the calculation of the EAQI are the concentration values of up to five key pollutants, namely particulate matter (PM10), fine particulate matter (PM2.5), ozone (O3), nitrogen dioxide (NO2) and sulphur dioxide (SO2).

The poorest level in any of the pollutants is decisive for the index level and it can therefore be used for single pollutants as well.

The driver of the index is the relative risks associated to short-term exposure to PM2.5 as defined by the Health Risk of Air Pollution in Europe project (WHO 2013).

According to the report for an increase of 10 μ g/m³ in PM2.5, a higher daily mortality of up to 1.23% is estimated for different urban agglomerations in developed countries (WHO 2013).

The index levels are derived from this factor and the PM2.5 concentration values correspond to index values shown in table 1.

Table 1: EAQI index level assignment

PM 2.5 μg/m ³	0 - 10	10 - 20	20 - 25	25 - 50	50 - 75	75 - 800
EAQI	Good	Fair	Moderate	Poor	Very poor	Extremely poor

These categories are applied to the interpolated concentration raster using the *r.reclass* method with the *pm25.txt* config file. The output is subsequently converted to a vector layer by the *r.to.vect* function using *area* as *type*.

At this point the edges of the vector geometry follow the pixel borders. As we are working with interpolated values pixel-perfect precision is not required. Therefore the vector geometries is simplified using *v.generalize* using the douglas-peucker algorithm with threshold value of 20, reducing also the output file size significantly.

After removing the redundant polygons of the *Good* index level with the *v.edit* method, the remaining areas are exported as GeoJSON using *v.out.ogr* and transformed to EPSG:4326 projection with *ogr2ogr* to enable "avoid routing" in the webapp.

4.7 Routing Web Application

The Application for generating cycling routes was realized using the Vue.js framework for Single Page Applications (SPA). All dependencies are managed by Node.js which needs to be installed on the operation system to run the solution locally.

The main advantage of SPAs over static websites is the dynamic rendering and updating of specific website components.

The map interface uses the vue2leaflet plugin for simple communication between Vue and Leaflet and easy creation of map objects. The actual route generation is done using the openrouteservice-js software development kit, which only needs a few parameters as well as an API key (which is free) to calculate routes avoiding areas of a specific air quality index.

The *format* parameter is obligatory and is specified to return a GeoJSON output which can be directly fed to the map by using the LGeoJson component. The *profile* needs to specified as well and should be *cycling-regular* for our use case. Start- and endpoint are defined by the user by means of right-clicking on the map and are passed in the *coordinates* parameter.

Depending on the current setting of the *time of the day* and the selected *air quality level*, which default to *9AM* and *moderate* respectively, the matching areas are passed in GeoJSON format to the *avoid_polygons* property of the *options* parameter.

5. Results

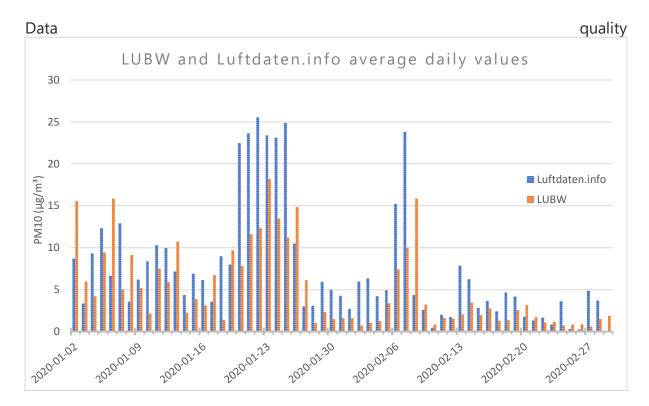


Figure 2: Comparison of Luftdaten.info and LUBW daily average PM10 values.

Figure 3 shows the average daily values of PM10 for all LUBW stations and Luftdaten.info sensors within 1000 meters distance of each station in $\mu g/m^3$.

The timeframe starts at 2020-01-02 to account for the large influx of particulate matter from fireworks on New Year's Eve. The timeframe ends on 2020-02-30 due to the Luftdaten.info API being unresponsive during several days in March 2020. The time axis is parted in weekly increments from the starting date.

The figure shows that the aggregated Luftdaten.info sensor values are higher for most days of the timeframe. Out of a total 59 days, the Luftdaten.info network returned higher values than the LUBW for 47 days.

The two datasets display the largest discrepancy around 2020-01-23, but appear generally in agreement with another. On average, the absolute difference of PM10 values within the timeframe was $\sim 3.1 \, \mu g/m^3$.

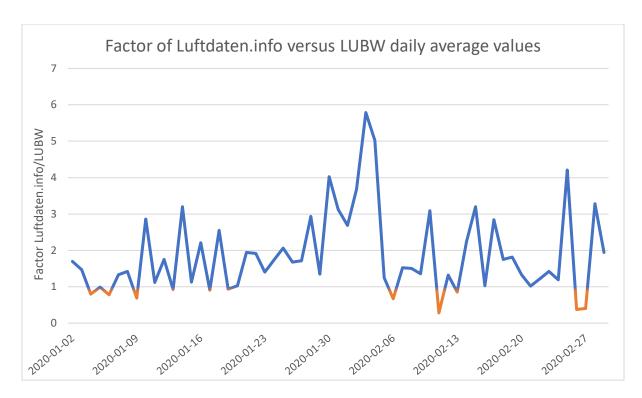


Figure 3: Factor of Lufdaten.info vs LUBW daily average values.

Figure 3 shows the collected data during the same timeframe in a single graph as a factor of the Lufdaten.info daily average divided by the LUBW daily average.

While the previous figure shows the highest absolute discrepancies to lie around 2020-01-23, figure 3 shows the largest relative difference in the week between 2020-01-30



Figure 4: IDW interpolation (default) at 9:00

and 2020-02-06, where the Luftdaten.info network returned values up to 5.8 times higher than the LUBW stations. The average factorized difference between both datasets in the timeframe was approximately 2.8.

Although the IDW method was deemed fitting in past studies, in this use case accuracy was only playing a minor role due to classification and using average values. The IDW method was in many cases creating rather angular and complex polygons (Fig. 4) which is obstructive when passing them to the routing API and doesn't fit well with average values.

The B-Splines method produced better results in terms of smoother polygons (Fig. 5) but was topped by the highly customizable RST which in addition to smoother polygons can also interpolate values outside of the input value range.

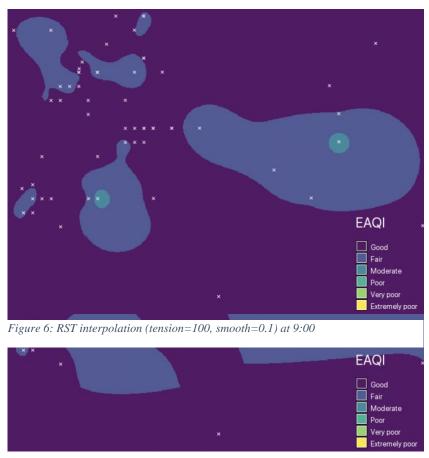


Figure 5: B-Spline interpolation (ns_step=50, ew_step=50, lambda_i=0.01) at 9:00

By using *v.surf.rst* with a low *smooth* factor and a high *tension*, the resulting polygons were closer the input data points in sparsely filled areas (Fig. 6). This is another advantage over the B-Splines method, as the interpolation of higher values further into data-empty areas is not desirable.

The routing web application was working as designed and displays the relevant areas above a given EAQI value for the selected hour of the day. Interacting with the map by means of right-clicking produces fastest routes from the first to the second point that

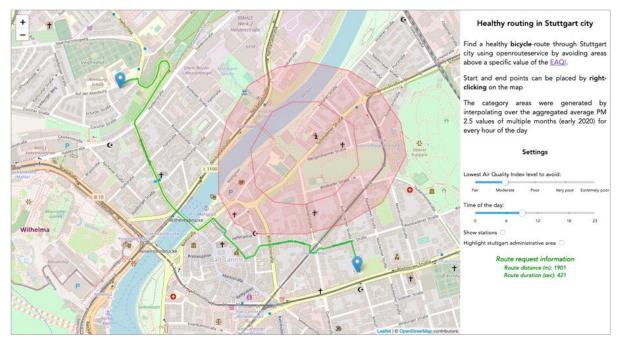


Figure 7: Route (green line) avoiding Moderate EAQI values at 9:00 (red polygon)

avoid areas with PM 2.5 values of the selected EAQI index level or higher (Fig. 7). The duration as well as the distance of the generated route is displayed at the bottom of the sidebar.

In addition to the adjustable hour of the day, which results in different areas for the index categories, the administrative area of Stuttgart and moreover the positions of the stations used for the current hour can be visualized (Fig. 8).

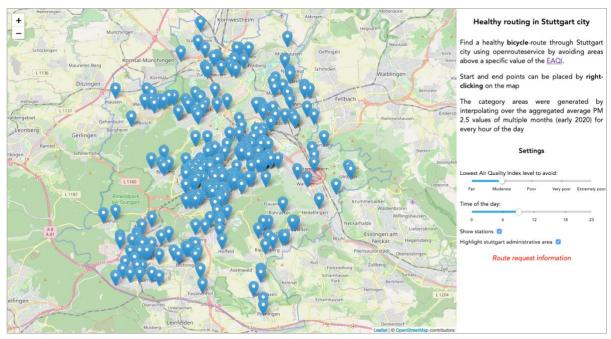


Figure 8: Overview of stations used to generate index areas at 9:00

6. Discussion

The following chapter critically discusses the results of this study shown in the previous chapter. The reliability of the analysis depends on two main factors: Data quality, and data processing.

The analysis of the relationship between LUBW and Luftdaten.info sensors has shown that by using *citizen-science* data, the amount and density of measurements of air quality can be greatly extended; both of which are crucial for attempts to model the air pollution of an area.

On the other hand, the comparison of both sensor networks, coinciding with results from field-laboratory tests in the literature, has shown that there is a noticeable, non-systemic discrepancy of Luftdaten.info data towards the reference LUBW data.

Using simple statistical methods, obvious outliers from the Ludtdaten.info dataset could already be excluded from the analysis and data quality significantly improved.

By incorporating known factors influencing the deviation of Lufdaten.info sensors and reference networks, such as temperature, wind speed and humidity, future studies using this sensor data should attempt to model and reduce the discrepancies between both networks; and enrich the resulting models with these additional atmospheric factors.

In summary, while the Lufdaten.info sensor network could not measure PM-levels in Stuttgart with enough accuracy to allow for the prediction of exact pollution levels, the network was capable of capturing the overall trend of PM-pollution.

In accordance with the conclusions of the data quality analysis that the combined sensor network is able to return the general trend of PM-pollution in Stuttgart, the resulting interpolated maps were categorized according to EAQI air quality classification. Within this classification schema, the particulate matter pollution in Stuttgart can be modeled with comparable certainty, as opposed to giving the exact predicted PM-values for each location – creating a false sense of accuracy.

The comparison of different GRASS interpolation methods yielded the RST algorithm as best suited for the study which might be not appropriate for use cases where the interpolation should represent exact values as accurate as possible.

Due to connectivity problems between the GeoServer⁴ connected to the database and the website, the web application is currently limited to the average values. Thus, the generated polygons can only be seen as a general assumption of where higher PM 2.5

concentrations might occur. In the current state the generated routes might still traverse areas of higher air pollution, as the newest data is not reflected.

A wider coverage of stations would be beneficial for the accuracy of the interpolation as well.

7. Conclusion

The aim of the project was to automatically download and store both official and citizen citizen-science data, perform a comparison of usability of both datasets, create maps showing areas of high particulate matter pollution and develop a routing app to avoid high-concentration areas.

The automatic download and ingestion were realized successfully. Database views were developed to filter outliers from the Luftdaten.info dataset. The comparison of both datasets shows discrepancies both in absolute and relative values, yet overall comparability over time.

Based on the results of the data-preprocessing, the one-dimensional point data was interpolated into classified raster maps in order to model the two-dimensional distribution of air pollution.

Finally, a Vue.js application was developed, providing cyclists with the ability to find a route avoiding areas of high particulate matter concentration.

If a connection between a GeoServer running the created data base and the web application is established the interpolation and therefore the routing results will be more relevant.

The whole workflow can be easily transferred to other regions of interest in a short amount of time by doing adjustments in few places. This might help people in more contaminated cities to evade air pollution and increase their life expectancy.

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