Report 2. SRS.

Group #1

Predicting Mean Maximum Rainfall in Mount Ginini

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• The true parameter (the mean max temperature):
μ = 19.1129 degrees celsius

The population size $N = 745$

• Calculate sample size n for 90% and 95% confidence levels and couple different d's. Use true σ^2 for these calculations.

Here is an idea on how to choose d. It is based on relative error. Take $r = .05$, $r = .01$ and $r = .10$. Since $r = \left|\frac{\hat{\theta} - \theta}{\theta}\right| = \left|\frac{d}{\theta}\right|$, we get $d = |r\theta|$.

r value	Approximate d value
.05	0.9556
.01	0.1911
.10	1.9112

Confidence Interval	Approximate d Value	Rounded Sample Size, n
90%	0.9556	60
	0.1911	510
	1.911	16
95%	0.9556	82
	0.1911	563
	1.911	23

- Estimate your parameter of interest using SRS with *n*'s which you calculated above.
- Estimate variance of your estimator for these *n*'s.

Confidence Interval	Rounded Sample Size, n	Sample Mean for Daily High Temperatures	Variance for Sample Mean
90%	60	19.4150	0.4108
	510	19.3967	0.0132
	16	20.03125	1.0621
95%	82	19.6402	0.2277
	563	19.1274	0.0096
	23	19.7783	1.0538

• Calculate confidence intervals for these estimators.

Confidence Interval	Rounded Sample Size, n	Sample Mean for Daily High Temperatures	Confidence Interval for Sample Mean
90%	60	19.4150	[18.3608, 20.4692]
	511	19.3967	[19.2076, 19.5858]
	16	20.03125	[18.3361, 21.7264]
95%	82	19.6402	[18.7050, 20.5755]
	564	19.1274	[18.9355, 19.3192]
	23	19.7783	[17.7663, 21.7903]

- Choose the optimal sample size n among the ones calculated above. The best sample size should be between 10% − 20%. Definitely it should be a 'large sample' size $n > 40$. If you have several such n, choose the one which produces the smaller CI or has a smaller α level.

  We chose the sample size n=82~=80 for the 95% confidence interval. This falls nicely in between the 10% and 20% guidelines and provides a smaller CI than 60. And this uses the 95% CI, which gives a smaller alpha.

  A sample size greater than 500 is unrealistic in the real world and samples far too large of a proportion of our population. The sample sizes 16 and 23 are too low to give an accurate estimate.

- Does your choice of best estimator guarantee the nominal confidence level? To answer this question, take 100 samples of size n where n has been selected above. For each sample, compute the difference between the parameter and its estimator. Compare these differences with d. How many samples have the difference less than d? Does it agree with the nominal confidence level? Justify your answer.

  Out of the 100 samples taken, 95 of the samples had a difference between the parameter and its estimator less than our d value of 0.9556. This does agree with the nominal confidence level because we had 95 samples with a d less than our d-value of .95556 for a 95% confidence interval. The proportion of samples with d less than the d-value matches the expected proportion.

The code used for this assignment is included in the following pages.