Shapley values

Aprendizaje automático

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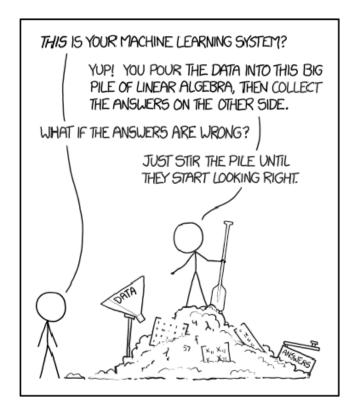


Agenda

- ML interpretable
- SHapley Additive exPlanations



Estado actual de ML







Usos



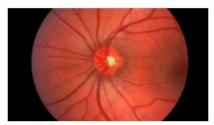
https://www.tesla.com/videos/autopilot-selfdriving-hardware-neighborhood-long



NYPost



MIT Technology Review



DeepMind



DeepMind

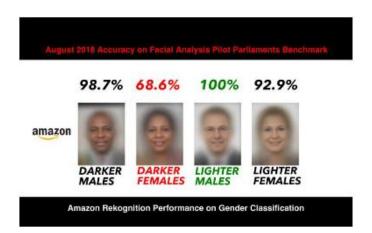






Problemas

Sesgos de los algoritmos



https://medium.com/@Joy.Buolamwini/response-racial-andgender-bias-in-amazon-rekognitioncommercial-ai-system-for-analyzing-facesa289222eeced

Machine Learning can amplify bias.



- · Data set: 67% of people cooking are women
- · Algorithm predicts: 84% of people cooking are women

https://www.infoq.com/presentations/unconscious-bias-machine-learning/

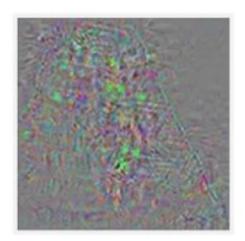


Problemas

Ejemplos adversarios



Original image Temple (97%)



Perturbations



Adversarial example
Ostrich (98%)



ML interpretable

Tenemos varios problemas:

- No confiamos en los modelos
- No sabemos qué pasa en casos extremos
- Los errores pueden ser costosos/nocivos
- ¿Los modelos cometen errores similares a los de los humanos?
- ¿Cómo cambiamos el modelo si no da los resultados esperados?

Una forma de lidiar con estos problemas es a través de la interpretabilidad



Shapley Additve exPlanations - SHAP

A Unified Approach to Interpreting Model Predictions

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Shapley Additve exPlanations - SHAP

$$\phi_{i} = \sum_{S \subseteq \{1,\dots,p\}\{i\}} \frac{|S|!(p-|S|-1)!}{p!} [val(S \cup \{i\}) - val(S)]$$



Shapley values para juego de 2 participantes



$$C_{12} = 10,000$$
 $C_{1} = 7,500$
 $C_{2} = 5,000$
 $C_{0} = 0$

Valores de las coaliciones



Contribución marginal esperada = Shapley values



$$C_{12} = 10,000$$
 $C_{1} = 7,500$
 $C_{2} = 5,000$
 $C_{0} = 0$



$$C_{12} - C_{2} = 5,000$$

 $C_{1} - C_{0} = 7,500$

$$(5,000+7,500)/2 = $6,250$$

$$C_{12} - C_{1} = 2500$$

 $C_{2} - C_{0} = 5000$

$$(2500+5000)/2 = $3,750$$



Shapley values para juego de 3 participantes

$$\mathbf{C}_{123} = 10,000$$
 $\mathbf{C}_{12} = 7,500$
 $\mathbf{C}_{1} = 5,000$
 $\mathbf{C}_{0} = 0$
 $\mathbf{C}_{13} = 7,500$
 $\mathbf{C}_{23} = 5,000$
 $\mathbf{C}_{3} = 0$



Shapley values para juego de 3 participantes

Contribución marginal esperada P1

$$C_{123} - C_{23} = 5,000$$
 5,000*(1/3) + 2,500*(1/6)
 $C_{12} - C_{2} = 2,500$ + 7,500*(1/6) + 5,000*(1/3)
 $C_{13} - C_{3} = 7,500$ = \$5,000
 $C_{1} - C_{0} = 5,000$



Shapley values para juego de 3 participantes

de formas en las que se puede crear una coalición de 3 participantes

3!

de formas en las que P1 se puede unir a una coalición de P2 y P3

2!*1!



Shapley Additve exPlanations - SHAP

$$\Phi_i = \sum_{S \subseteq \{1,\dots,p\}\{i\}} \frac{|S|!(p-|S|-1)!}{p!} [val(S \cup \{i\}) - val(S)]$$
Weight

Marginal contribution of player i to coalition S

|S|! ⇒ number of ways players can join S before player i

(p - |S| - 1)! ⇒ number of ways players can join coalition

after player i joins

p! ⇒ number of ways to form coalition of p players



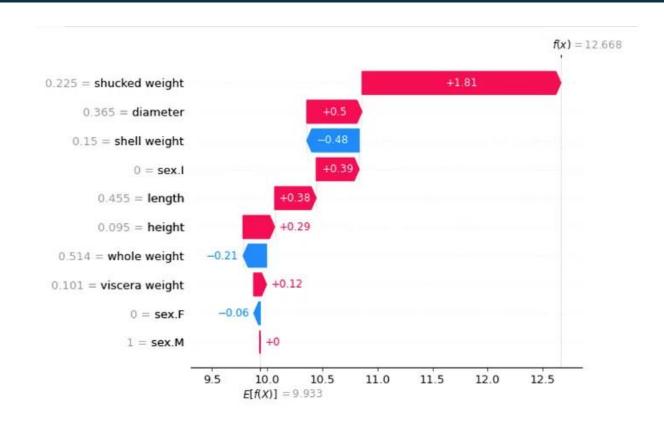
Shapley values - propiedades

Symmetry Two players are considered interchangeable if they make the same contributions to all coalitions. If two players are interchangeable then they must be given an equal share of the game's total value.

Null player property If a player makes zero marginal contribution to all coalitions then they get none of the total value.

Additivity If we combine two games, then a player's overall contribution is the sum of the contributions for the two individual games. This axiom makes the assumption that any games played are independent.







$$val_x(S) = \int f(x_1,...,x_p) dP_{x \notin S}$$

El valor de la coalición S es la predicción del modelo marginalizada sobre todas las características que no están en S



Predicción del salario

$$f(x_{1}, x_{2}) = 200x_{1} + 1000x_{2}$$

$$age \rightarrow x_{1} \in [18, 60]$$

$$degree \rightarrow x_{2} \in \{0, 1\}$$

Persona de 20 años con título

$$val_x(\{1,2\}) = f(20,1)$$

= 200(20) + 1000(1)
= 5000



$$val_{x}(\{1\}) = \int f(20, x_{2}) dP_{x_{2}}$$

$$= \sum_{i=0}^{1} f(20, i) P(x_{2} = i)$$

$$= (200(20) + 1000(0))(0.5) + (200(20) + 1000(1))(0.5)$$

$$= 4500$$

Contribución marginal de x_2 a $S = \{1\}$

$$val_{x}(\{1,2\}) - val_{x}(\{1\}) = 500$$



Para calcular la contribución marginal de x_2 debemos calcular también la contribución marginal de esta característica a $S = \{\}$. Esto requiere marginalizar sobre la distribución de ambas características.



Aproximación de los Shapley values

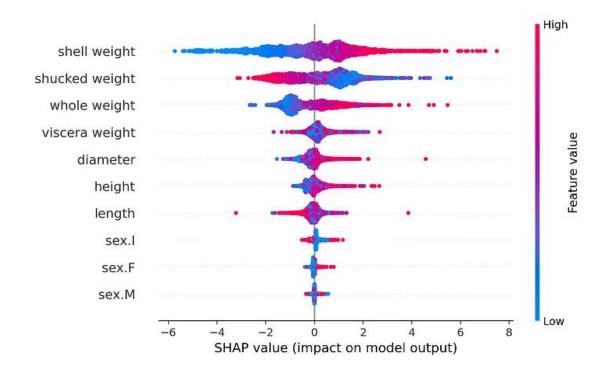
Monte-Carlo sampling

$$\widehat{\Phi}_{i} = \frac{1}{M} \sum_{m=1}^{M} (f(x_{+i}^{m}) - f(x_{-i}^{m}))$$

$$f(x) = \sum_{i=1}^{p} \phi_i + E_X[f(X)]$$



SHAP values - gráficas





Referencias

https://christophm.github.io/interpretable-ml-book/shapley.html

https://towardsdatascience.com/from-shapley-to-shap-understanding-the-math-e7155414213b

