

$$\frac{dE}{dt} = \beta S(t) \frac{I(t)}{N} - \sigma E(t) - \frac{V I i + V I e}{N} E(t)$$