

Introduction to Natural Language Processing and Text Classification

Goal: discuss how to build a spam filter.

documents come in and we decide $\begin{cases} \text{spam?} \\ \text{ham?} \end{cases}$

We will see how to train a classifier using prelabeled documents.
(in this case, emails w/ 'spam' or 'ham' labels)

To do this requires knowing:

1. How to preprocess text

2. How to turn text data into features

(the X in the equation $Y = f(X) + \epsilon$)

3. Probability theory to build a classifier.

- Bayes theorem
- Laplace smoothing, log-probabilities (implementation details)

Processing text

We've done this in the past (homeworks). But it is a key step to NLP (Natural Language Processing).

Terminology:

Token - words, punctuation, numbers, etc.

Sentence - ordered sequence of tokens

Tokenization - process of segmenting a sentence into tokens. Whitespace makes tokenizing English, say, easy. But other languages, such as Chinese, are hard to tokenize.

Corpus - A body of text, usually w/ a large number of sentences.

Documents - Many corpora are broken down into smaller bodies of text called documents. For example, each ^{individual} email is a document in an email corpus.

Parts-of-Speech Tag (POS) - Words may be nouns, verbs, adjectives, etc. POS tags are symbols representing those categories:

NN - Noun
VB - Verb
JJ - adjective
AT - article
etc....

Stop words - common, low meaning words "the", "that", etc. which are often, but not always removed from a text.

POS tagging - labelling the tokens in a sentence

The ball is red.
AT NN VB JJ

Stemming - breaking words down to root morphemes by, among other things, removing suffixes.

cats, catlike, catty \Rightarrow cat.

argue, argues, arguing, argued, \Rightarrow argu (not a word)

Lemmatization - grouping together the different inflected forms of a word.

- walk, walks, walked, walking \Rightarrow walk (lemma (same as stem))
- better \Rightarrow good (lemma not matched by stemming)
- "meeting" may be a noun ^(lemma: meetings) or a verb (lemma: meet). Context required.

Stemming and Lemmatization are common text preprocessing steps. \Rightarrow Normalize the words.

Turning text into features:

The simplest feature transform for a tokenized text is the Bag-of-words model.

→ throw out any structure/order to the text and assume all the data is with the counts: i.e. the number of times each unique word occurred.

→ each document becomes a count vector

$v_d(\text{"foo"}) = 7 \rightarrow$ "foo" appeared in document d a total of 7 times.

→ dimensionality of v 's \rightarrow # unique words in the corpus.

(notice the effects stemming/lemmatization may have.)

→ unigrams \Rightarrow n-grams.

Text classification \rightarrow spam filtering

Given a document d what is the probability it is or is not spam?

We want $\Pr(\text{spam} | d)$. We can generalize to more than two categories/classes.

$\Pr(c | d)$ where, for now, $c \in \{\text{spam}, \text{ham}\}$.

If we can compute this probability for each c , we can decide which class the document belongs to.

$c_{\text{MAP}} = \underset{c}{\text{argmax}} \Pr(c | d)$ (MAP = maximum a posteriori, most likely)

But, how to compute $\Pr(c | d)$?

First ingredient we need: Bayes Theorem

$$Pr(A \text{ and } B) = Pr(B \text{ and } A), \quad Pr(A \text{ and } B) = P(A|B) \cdot P(B)$$

$$P(A|B)P(B) = Pr(B|A)P(A) \quad \leftarrow \text{plug in}$$

$$P(A|B) = \frac{Pr(B|A)P(A)}{Pr(B)} \quad \text{that's it!}$$

Bayes thm lets us "Flip around" conditional probabilities.

In the text classifier it is easier to ~~measure~~ $Pr(d|c)$ than $Pr(c|d)$.

$$\begin{aligned} c_{MAP} &= \operatorname{argmax}_c Pr(c|d) \\ &= \operatorname{argmax}_c \frac{Pr(d|c)Pr(c)}{Pr(d)} \end{aligned}$$

Now, to find a way to calculate c_{MAP} we need to make some simplifications.

I. The document we want to classify is constant, this means that $Pr(d)$ is the same regardless of $c \Rightarrow$ it won't change what c_{MAP} is:

$$c_{MAP} = \operatorname{argmax}_c Pr(d|c)Pr(c)$$

Next, the document d is a collection of words:

$$Pr(d|c) = Pr(w_1, w_2, \dots, w_n|c)$$

this is not the bag of words (BOW) model.

Assume Bag-of-Words \Rightarrow position/order of words doesn't matter.

Assume conditional independence \Rightarrow probabilities of different words appearing together are independent given the document class.

$$Pr(d|c) = Pr(w_1, \dots, w_n|c) = Pr(w_1|c) \cdot Pr(w_2|c) \cdots Pr(w_n|c)$$

Note these last two assumptions are certainly not true for a real text!

Put these together and you have constructed a (text) classifier called Naive Bayes

$$C_{MAP} = \arg \max_c \Pr(d|c) \Pr(c)$$

\Downarrow

$$C_{NB} = \arg \max_c \Pr(c) \prod_{i=1}^n \Pr(w_i|c)$$

Learning Naive Bayes

How to compute these probabilities...

Training corpus N_{docs} documents, each labeled w/ $c = \text{spam or ham}$.

Estimate probabilities: $\hat{P}(c) = \frac{\# \text{ docs labeled } c}{N_{\text{docs}}}$

$$\hat{P}(w_i|c) = \frac{\text{count}(w_i, c)}{\sum_j \text{count}(w_j, c)}$$

fraction of the words among all c documents which are word i .

Problem! what if we use this \hat{P} estimator and then, when we attempt to classify a new document we see a new word we have never seen before, ?

→ word will have a count of zero → $\hat{P}(w|c) = 0$
plug into C_{NB} and it becomes zero:

$$C_{NB} = \arg \max_c \hat{P}(c) \prod_{i=1}^n \hat{P}(w_i|c)$$

↑ one of those is now zero!

The fix is madness → Laplace (or additive) smoothing!

assume: $\hat{P}(w_i|c) = \frac{\text{count}(w_i, c) + 1}{\sum_{j=1}^n (\text{count}(w_j, c) + 1)} = \frac{\text{count}(w_i, c) + 1}{\sum_{j=1}^n \text{count}(w_j, c) + |V|}$

"n"