Research Plan for Matching in Multi Agent Pathfinding using M*

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Title:	Matching in Multi Agent Pathfinding using M*
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Contents

1 Background of the research

1.1 Definition of Multi agent pathfinding

Stern (2019) [1] defines a multi agent pathfinding (in this plan abbreviated to *MAPF*) as a problem of n so-called agents [1] and the following tuple:

$$\langle G, s, t \rangle$$

- G is a graph $\langle V, E \rangle$

- V is a set of vertices

- E is a set of edges between vertices

- s is a list of n vertices where every s_i is a starting position for an agent a_i

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[1] Agents can be thought of as robots travelling through a graph

- t is a list of n vertices where every t_i is a target position for an agent a_i

An algorithm to solve $MAPF$ finds solutions such that each agent moves from their starting position to their target position. Each agent a_i has a path π_i. Each path π_i is a list of positions, defining where each agent a_i is at a moment x (referred to as $pi_i[x]$). The cost of a path π_i is it's length.
However, while moving, there are a number of conflicts that are to be avoided by the agents.

- Edge conflict: two agents are on the same edge E at a timestep x ($\pi_i[x] = \pi_j[x]$ and $\pi_i[x+1] = \pi_j[x+1]$)

- Vertex conflict: two agents are on the same vertex V at a timestep x ($\pi_i[x] = \pi_j[x]$)

- Swapping: two agents swap vertices at a timestep x ($\pi_i[x] = \pi_j[x+1]$ and $\pi_i[x+1] = \pi_j[x]$)

- Following conflict: an agent travels to a vertex from which another agent leaves in the same timestep ($\pi_i[x+1] = \pi_j[x]$)

- Cycle conflict: a number of agents larger than 2 all swap vertices such that each of the agents lands on a vertex another agent in the set just left.

Summarised, these conflicts define that in $MAPF$ it's not allowed for agents to collide in any way. Notable is that some definitions of $MAPF$ allow for some of the conflicts defined above to be broken. For example, in previous research that attempted to add waypoints to $MAPF$, the following and cycle constraint were dropped. Their reasoning for this was that when seeing agents as being point-like, and are following each other, they are never actually colliding.

Algorithms solving $MAPF$ are minimising either the *makespan*, which is the cost of the longest single path, or the *sum of costs* which is the combined cost of all agent's paths.

1.2 Matching

Matching in a bipartite graph is the problem of finding a set of connections between two parts of a graph. No vertex in one part of the graph may be connected to another part of the graph by two edges in the matching. Adding matching to $MAPF$ (in this plan referred to as $MMAPF$) alters the original problem definition in the following way:

$$\langle G, s, t, sc, tc \rangle$$

Two variables are added to the definition of this problem:

- sc is an array of colours sc_i for each starting vertex s_i

- tc is an array of colours tc_i for each target vertex t_i

For a solution to $MMAPF$, it does not matter which agent a_i travels to which target t_i. In stead, an agent a_i can travel to any t_i as long as $sc_i = tc_i$.
However, $MMAPF$ is not yet fully defined. For example, is it allowed for there to be more target positions than there are agents? Or conversely, is it allowed for there to be fewer target positions than there are agents.

1.3 Algorithms

A number of algorithms exist to solve the $MAPF$ problem. These include A* with operator decomposition and independence detection ($A*+OD+ID$) [2], $M*$ [3], *Conflict based search* [4] and *Branch and cut and price* [5].
However, to solve the $MMAPF$, no algorithm currently exists. Planned is that through this research, and other similar research by peers, each of these algorithms will be adapted to be able to solve $MMAPF$.

M*

M^*, as previously described, is an algorithm designed to solve $MAPF$. I will briefly outline it's workings as this is the algorithm I will be proposing to adapt to be able to use matching.

M^* solves MAPF by planning paths for each agent individually using A^* pathfinding. However, when it detects that two agents will be in conflict with each other, it will for a short time, plan the paths of these two agents together in such a way that the conflict is resolved. This is very similar to what $(A^*+OD+ID)$ does. But in $(A^*+OD+ID)$, when two agents are in conflict their entire path will be planned together, while in M^*, paths can be planned independently again after the conflict.

M^* without extensions, guarantees to generate optimal paths for $MAPF$. However, in previous research extending $MAPF$ to allow for waypoints to be added to paths, optimality could no longer be guaranteed (in certain cases). [6]

1.4 Applications and related problems

$MAPF$ is a problem which very naturally applies to railways. Trains moving around shunting yards are like agents. They can not collide or move past each other as they are bound to the tracks they ride on. But in shunting yards, it's usually less important which exact train moves where, and more important what type of train moves somewhere. For example, if trains are the same length, then it does not matter very much which one goes where in the shunting yard as long as they both end up somewhere with enough space.

When trains are stored and serviced in shunting yard, they need to be moved around. From their parking space, to servicing stations, and back to service to transport people. The scheduling problem that arises is called the Train unit Shunting problem (here abbreviated as $TUSP$). To find relaxations to the $TUSP$ problem, Mulderij used $MAPF$ [7]. In his work he describes that extensions to $MAPF$ (such as matching) are necessary to make this viable. That is in fact the root of this planned research.

Research Question

During this research, I will be answering the following question:

Can M^* be adapted to efficiently find optimal solutions to the $MMAPF$ problem?

To answer this question, I think I will need to answer the following sub questions. However, while researching, it is possible that more of these will arise. If so, and if they fall in the scope of the project, they may be added to these.

- Can M^* be adapted to do matching

- Are M^* solutions still optimal with matching?

- How does the runtime cost of adding matching to M^* compare to adding matching to other base algorithms?

- Are there heuristics which can improve the runtime of M^* with matching?

- What happens when the number of agents is no longer equal to the number of target locations?

The last subquestion I find especially interesting as real life scenarios (with for example shunting yards) will certainly have situations in which the number of agents is not equal to the number of target locations.

From now on, I will call the algorithm I will be developing to solve $MMAPF$ using M^* as base algorithm M^*MMAPF

2 Method

In chronological order, this is how I intend to go about researching the previously stated subquestions:

- Implement *M** for plain *MAPF* problems to get a starting point from which can be extended.

- Extend this *MAPF* solver to also solve *MMAPF*.

- Create a number of benchmarks to quantitatively evaluate the performance of this algorithm.

- Compare *M** to the algorithms developed by peers by running them on these same benchmarks.

- Research ways to improve the runtime of *M*MMAPF*, for example by using better heuristics.

- Research possibilities to allow for a different number of agents than there are

To fairly compare benchmarks, I will be working on an online system to compare *MMAPF* algorithms, adapted from a similar website used in 2020 by a group researching waypoints in multi agent pathfinding. This will not be a part of the research, but I believe that it will be very valuable when comparing our algorithms.

3 Planning of the research project

Planning	
week 1	- Kick off - Lecture Research methods - Create planning for week 1 (Monday) - Assignment Information literacy (Tuesday) - Distribute base algorithms - Create research plan - Benchmarking website - Meeting with supervisor (Thursday)
week 2	- Prepare presentation of research plan. - Presentation of research plan (Thursday) - Start implementing base algorithm - Lecture responsible research - Meeting with supervisor (Thursday)
week 3	- Lecture Academic communication skills (Friday) - Implement base algorithm - Research extending to *MMAPF* - Meeting with supervisor (Thursday)

week 4	• Session responsible research (Monday) • Meeting with supervisor (Thursday) • Extend the algorithm to be able to solve *MMAPF*.
week 5	• Session Academic communication skills (Monday) • Prepare midterm presentation (before Wednesday) • Midterm presentation (Wednesday) • Meeting with supervisor (Thursday) • Create benchmarks and start comparing to other algorithms (made by peers).
week 6	• Meeting with supervisor (Thursday) • Session Academic communication skills (Friday) • Find ways to improve runtime performance of *M*MAPF* • Start working on the basics of the final paper.
week 7	• Quantitative evaluation and comparison with other algorithms. • Possibly extend to solve *MMAPF* with a different number of agents than targets. • Work on paper for draft deadline. • Meeting with supervisor (Thursday)
week 8	• Paper draft v1 (Monday) • Peer review paper draft v1 (Thursday) • Meeting with supervisor (Thursday) • Improve paper for draft 2. • Find more ways to improve *M*MMAPF*
week 9	• Paper draft v2 (Wednesday) • Final work on paper.
week 10	• Submit final paper version (day tbd?) • Create poster and work on poster presentation. • Meeting with supervisor (Thursday)

week 11	- Session Academic communication skills (Monday) - submission poster (Tuesday) - poster presentation (Thursday or Friday) - Meeting with examiner

References

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[6] J. van Dijk, "Solving the multi-agent path finding with waypoints problem using subdimensional expansion," 2020.

[7] J. Mulderij, B. Huisman, D. Tönissen, K. van der Linden, and M. de Weerdt, "Train unit shunting and servicing: A real-life application of multi-agent path finding," *arXiv preprint arXiv:2006.10422*, 2020.