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MAE 273A Project Script

```
clear all

List =
    ["FirstOrderTruth_BASELINE_linear.mat","FirstOrderTruth_R0_25_linear.mat","FirstO
NameList = ["Linear Baseline", "R0:25% Linear", "RC:25%
    Linear","CC:25% Linear","R0:50% Linear","RC:50% Linear","CC:50%
    Linear","R0:20% RC: 20%Linear","Nonlinear Baseline ","R0:25%
    Nonlinear","RC:25% Nonlinear","CC:25% Nonlinear","R0:50%
    Nonlinear","RC:50% Nonlinear","CC:50% Nonlinear", "R0:20% RC:20%
    Nonlinear" ];

for k = 1:length(List)
    load(List(k))

s = tf('s');

%battery model parameters
Rc = 0.015;      %Ohms
Cc = 2400;      %F
Cbat = 5*3600;
alpha =0.65;
R0 = 0.01;      %Ohms
Vocv0 = 3.435; %V

%tunning parameters
K = 1;          %gain
% zeta = 0.707; %damping ratio
zeta = 0.5;     %damping ratio

wn = 75;        %natural frequency

%continuous time ss model
A = [-1/(Rc*Cc) 0; 0 0];
B = [1/Cc; -1/Cbat];
C = [-1 alpha];
D = -R0;

A1 = A(1,1);
B1 = B(1,1);
A2 = A(2,2);
```

```

B2 = B(2,1);
C2 = alpha;

SI = [s 0;0 s];
Gp = C*(inv(SI-A))*B+D;           %plant
T = minreal(K*wn^2/(s^2+2*zeta*wn*s+wn^2)); %complimentary
Y = minreal(T/Gp);               %youla
S = minreal(1-T);                 %sensitivity
Gc = minreal(Y/S);               %controller
L = minreal(Gc*Gp);               %open loop TF
sysTF = minreal(Gc*Gp/(1+Gc*Gp)); %actual sys TF
[num, den] = tfdata(Gc, 'v'); %get numerator and denominator of Gc tf

out = sim('Estimator_Simulink_trial1') ; %run simulink model

est_soc = out.SOC_est;
tout = out.tout;

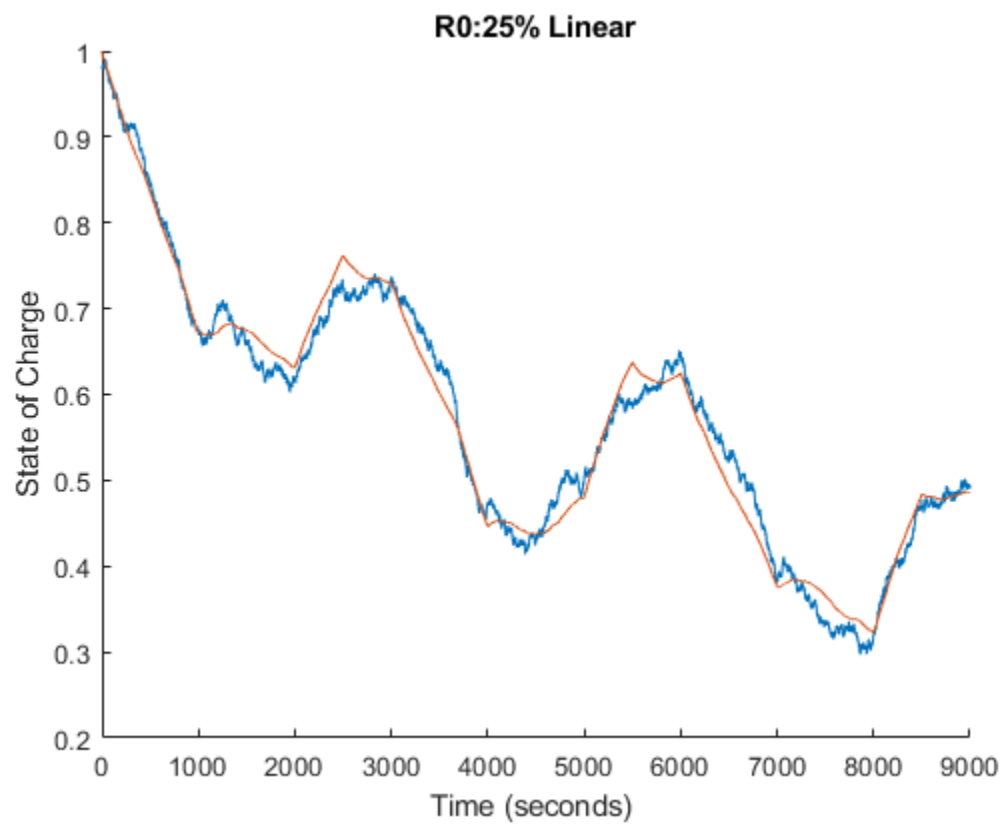
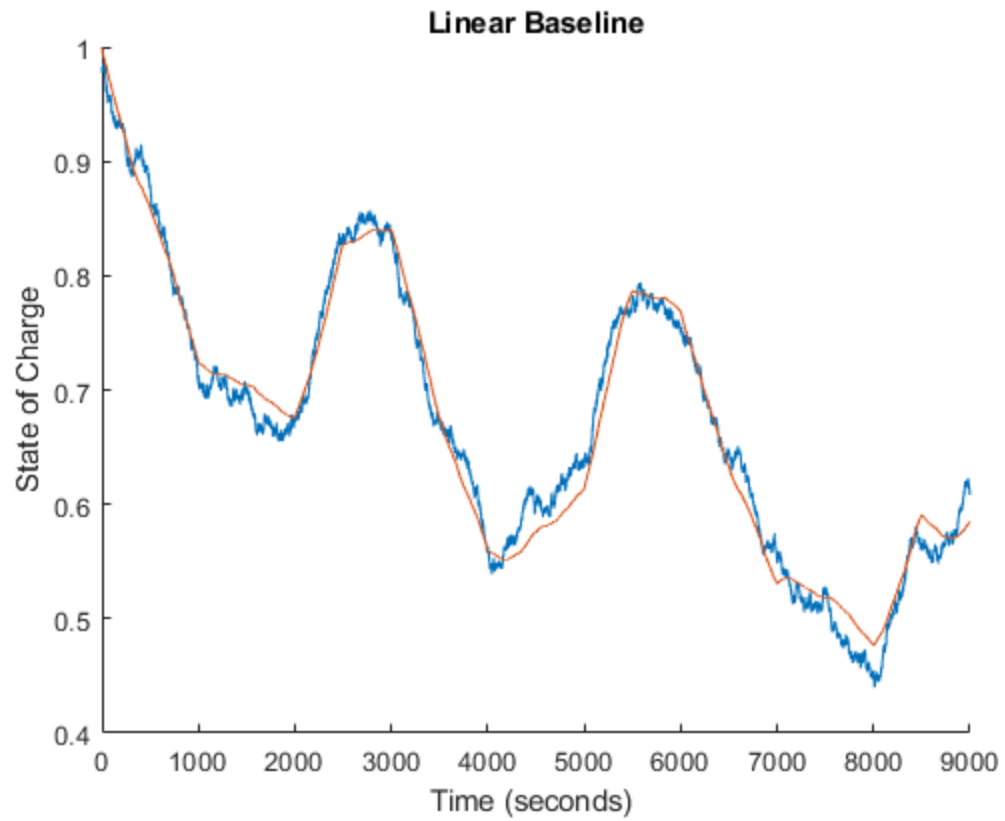
YOULA_ACTUAL(:,k) = SOC_act;
YOULA_ESTIMATED(:,k) = est_soc;

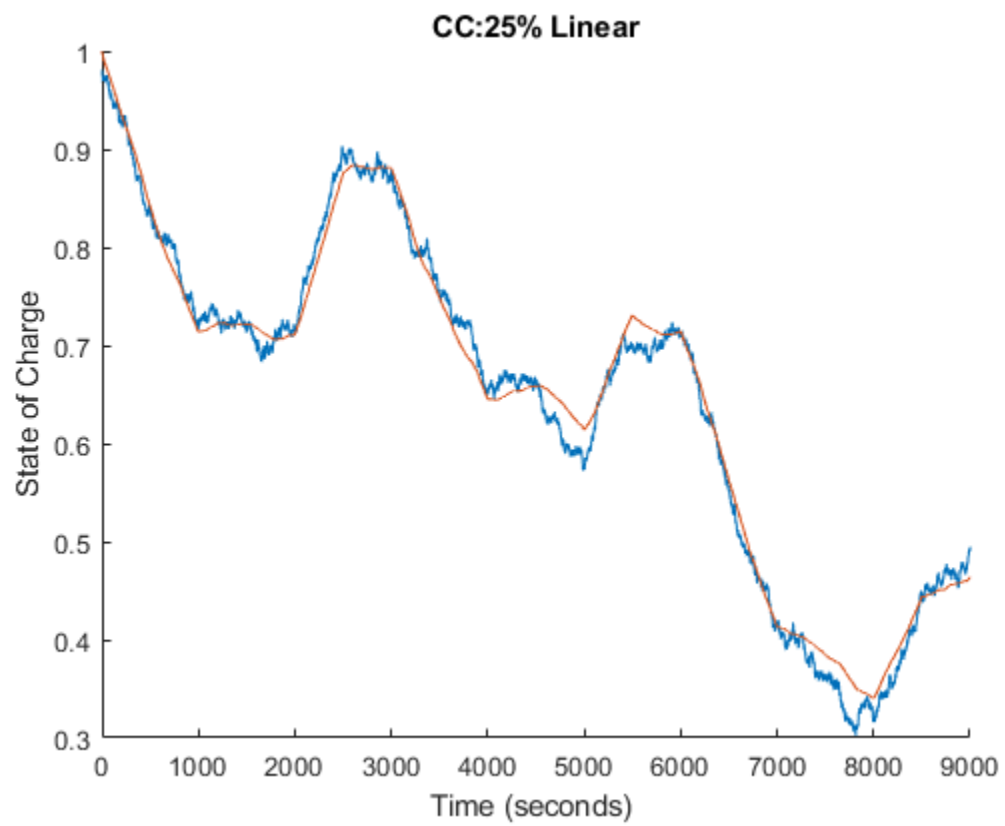
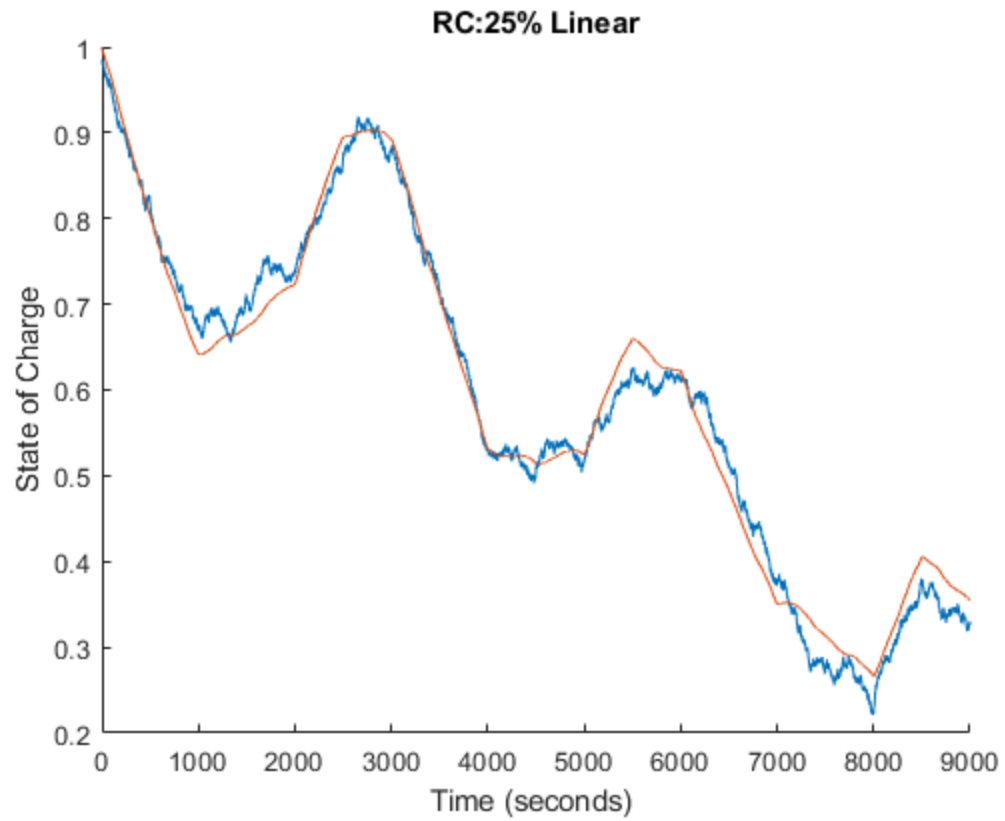
figure()
hold on
plot(t,SOC_act);
plot(tout,est_soc);

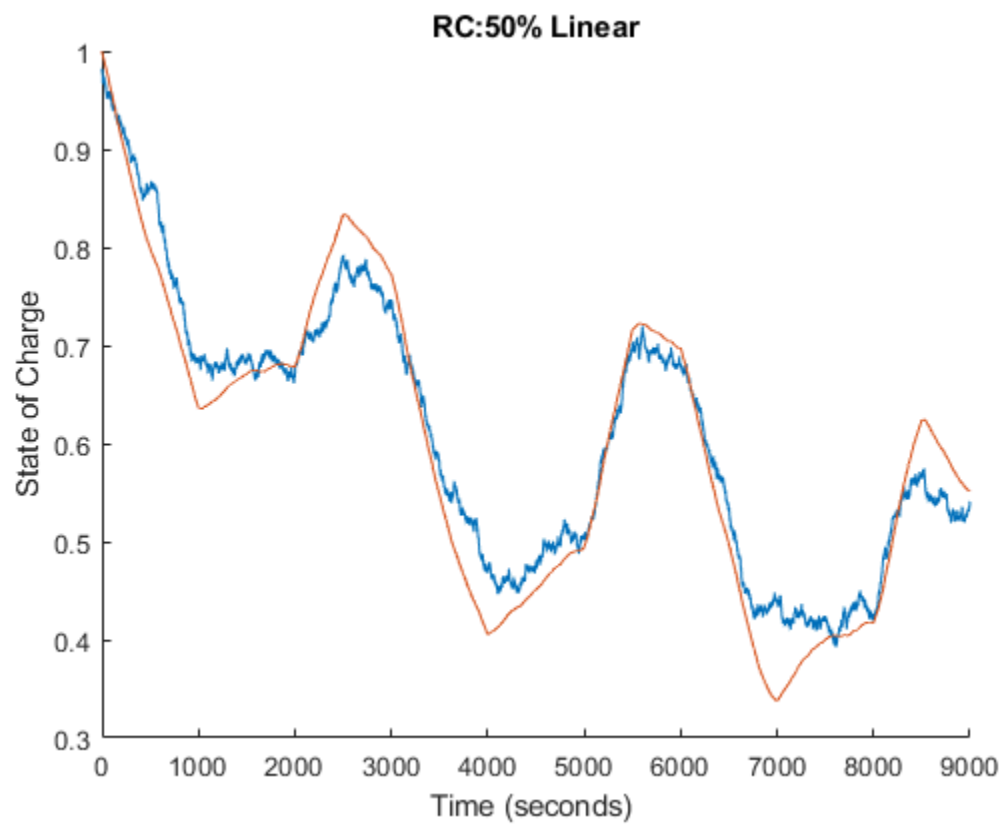
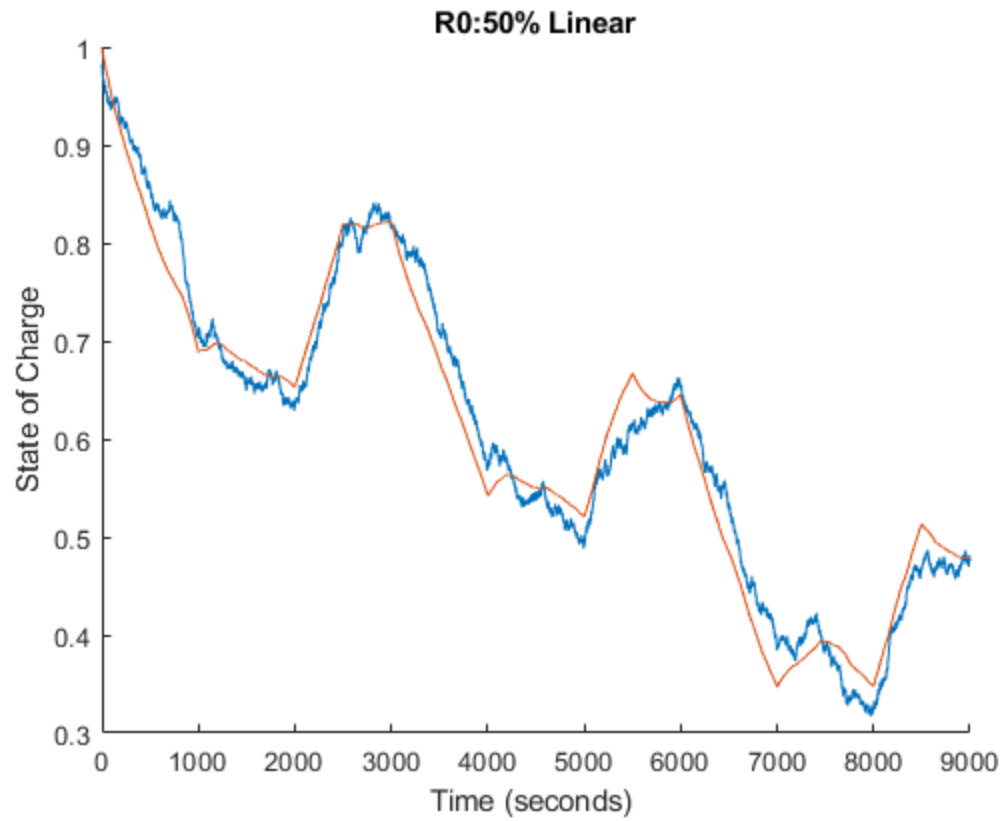
title(NameList(k))
xlabel('Time (seconds) ')
ylabel('State of Charge')

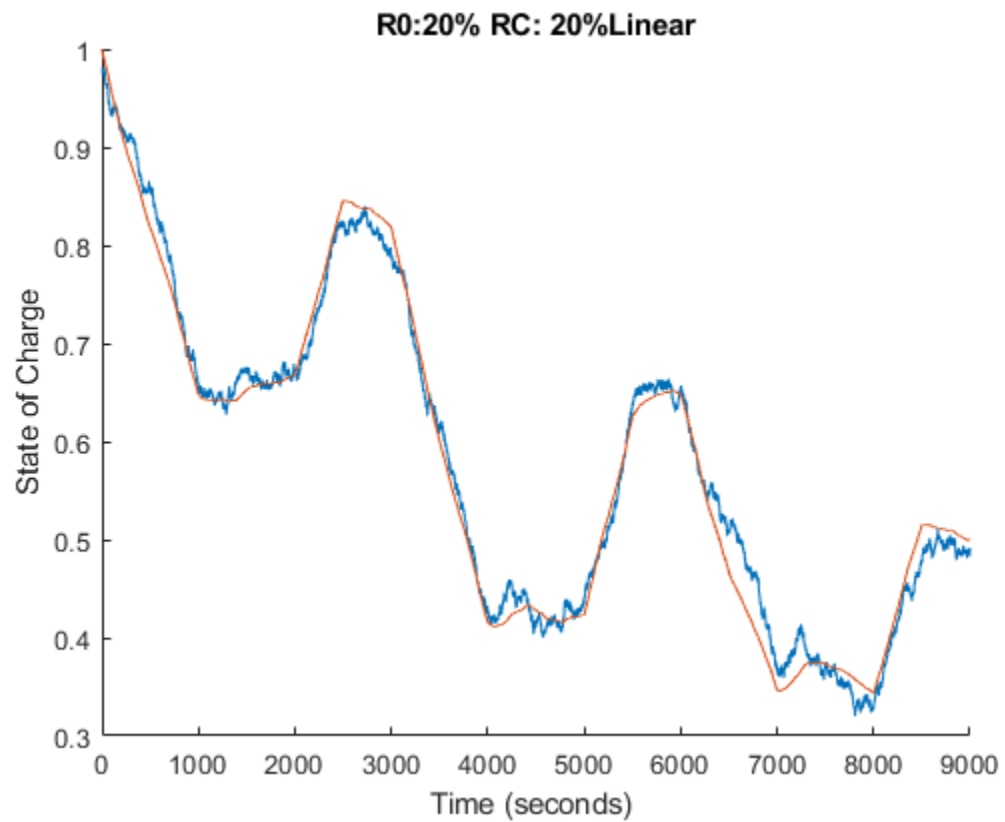
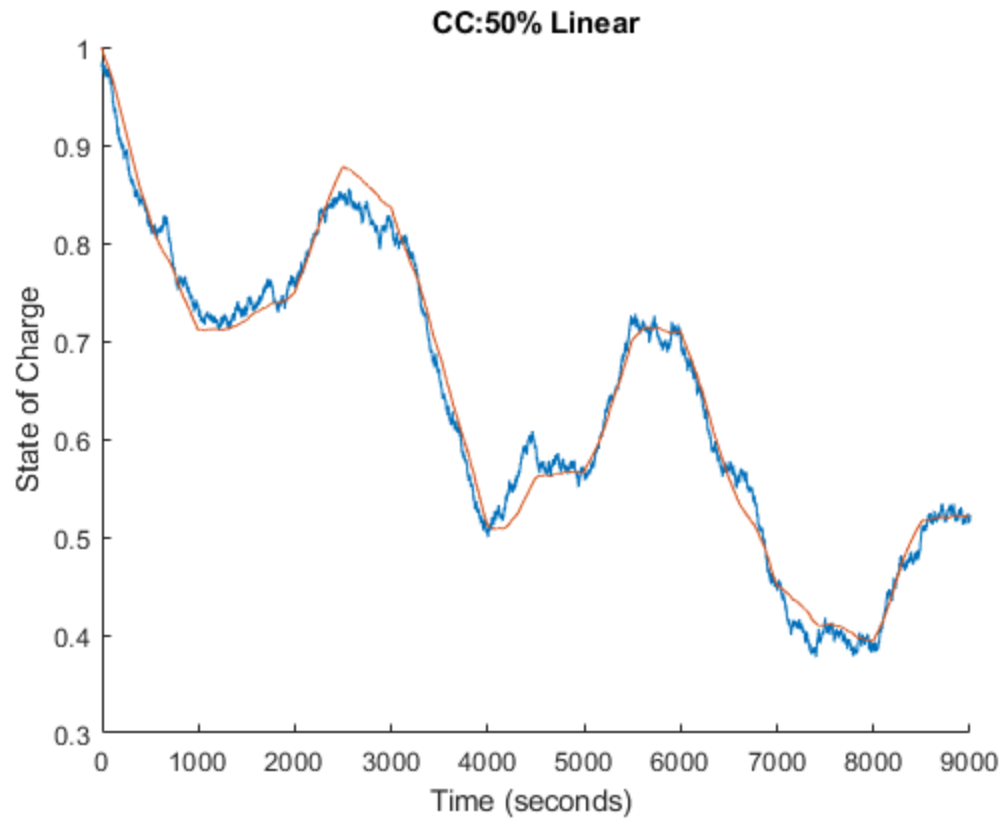
end

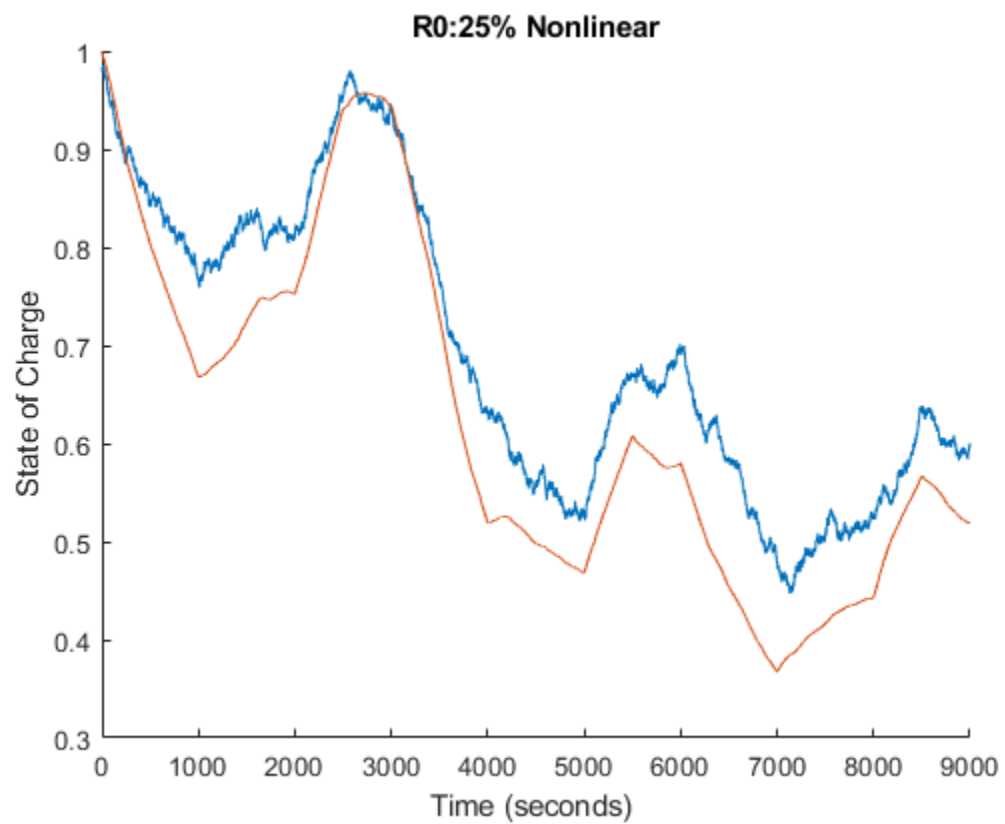
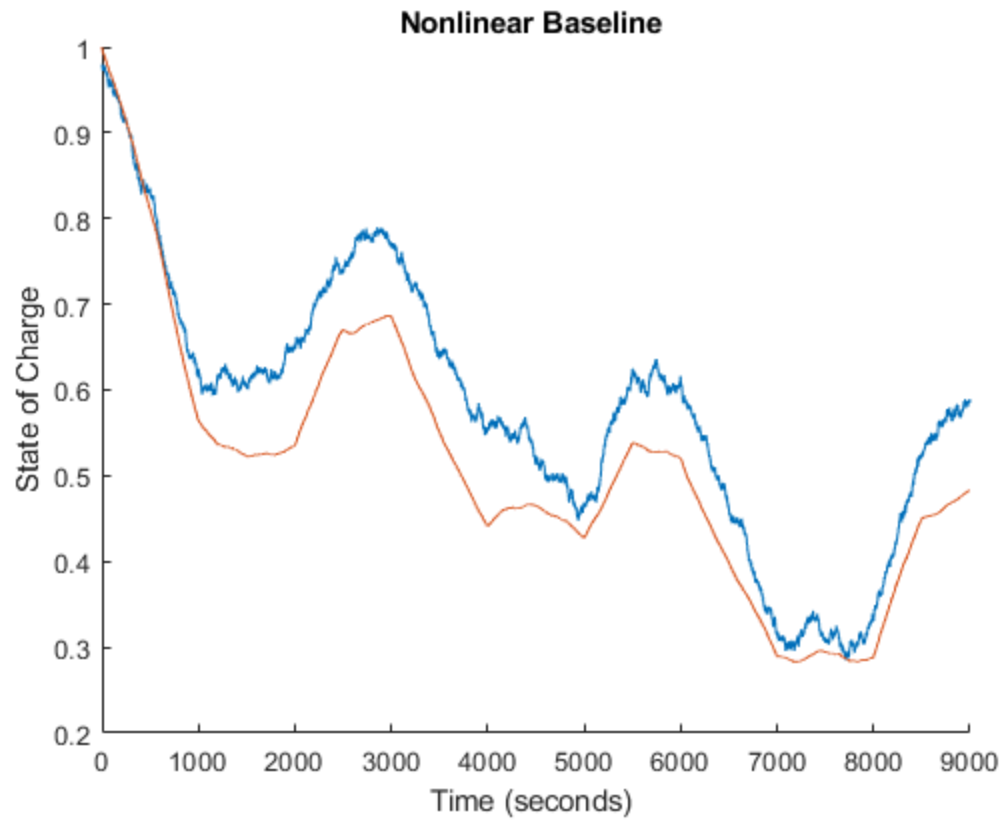
```

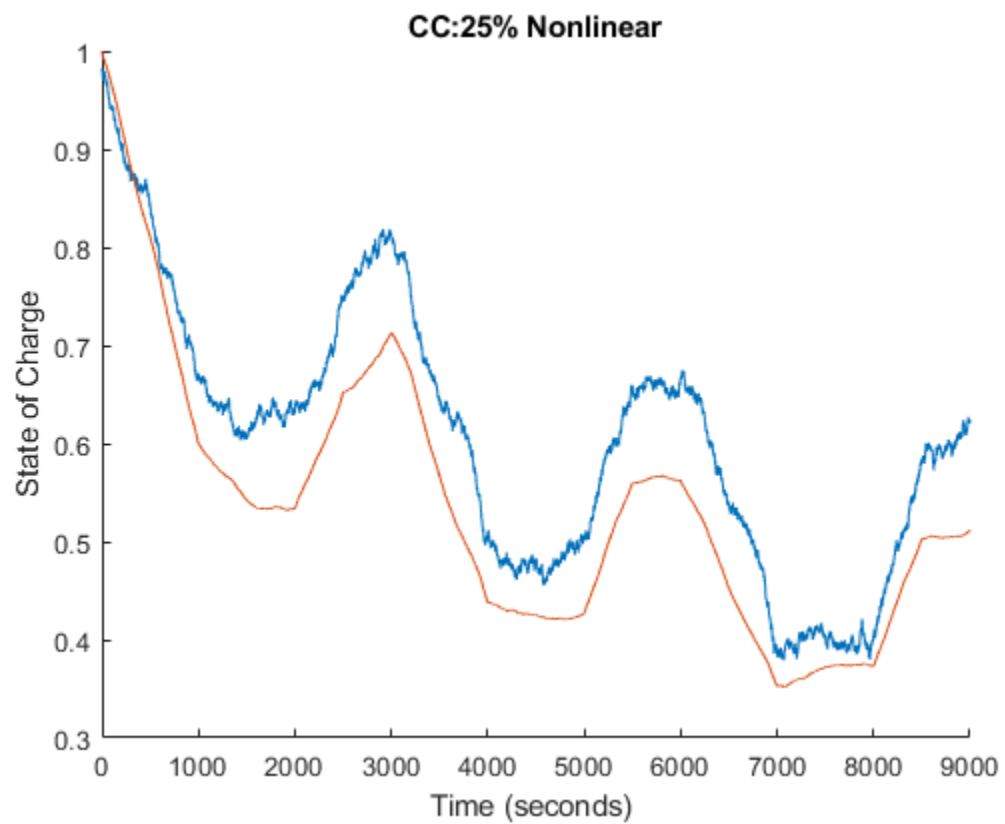
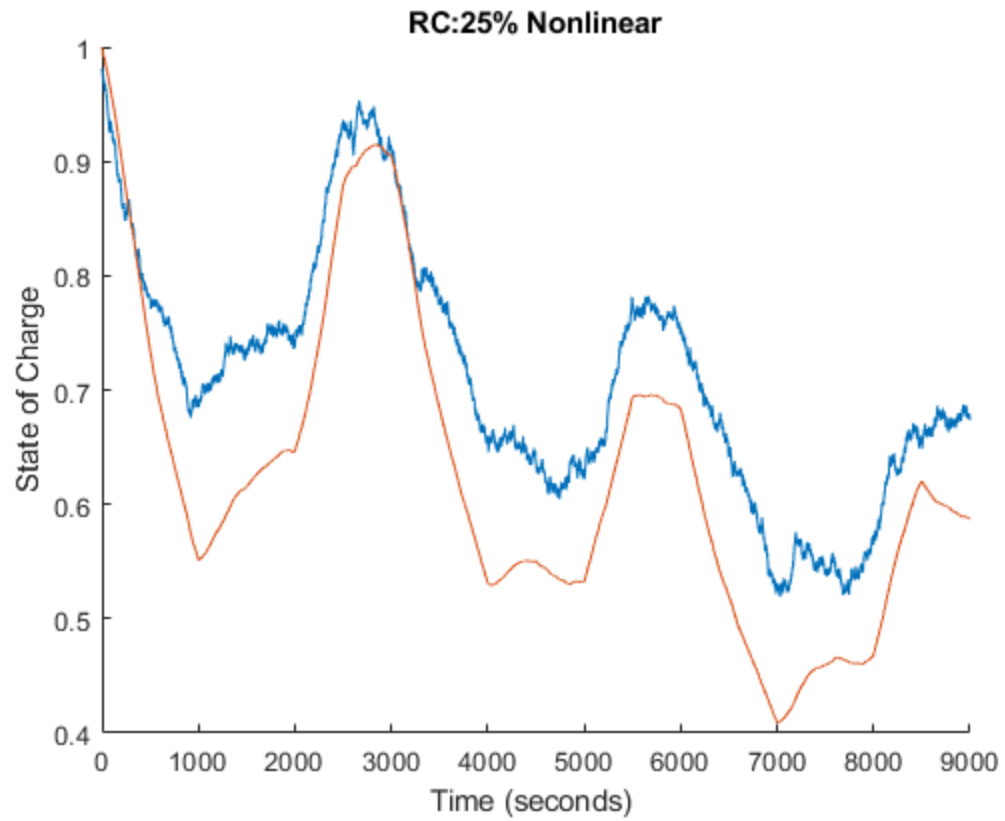


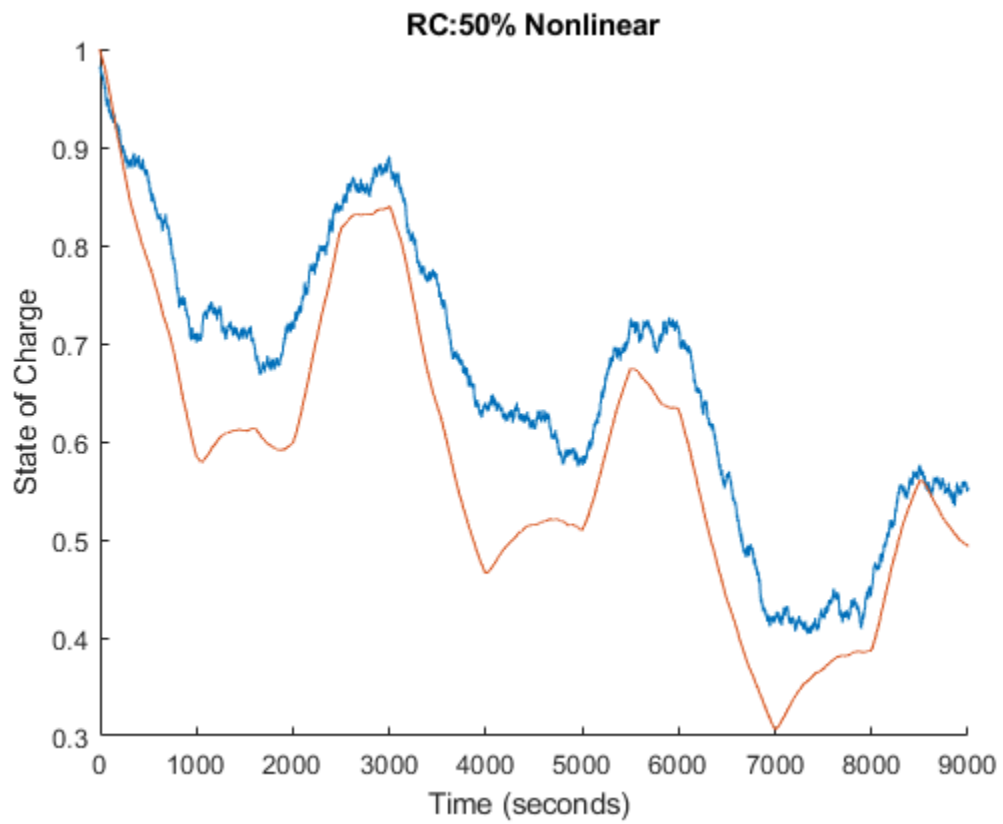
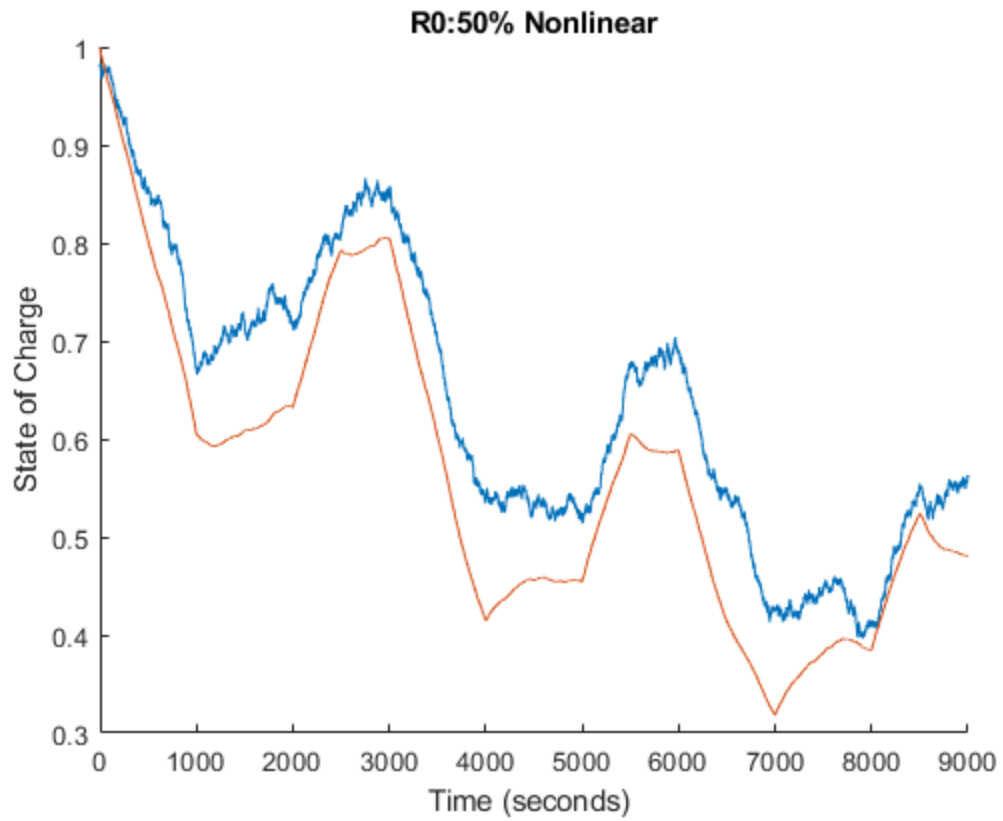


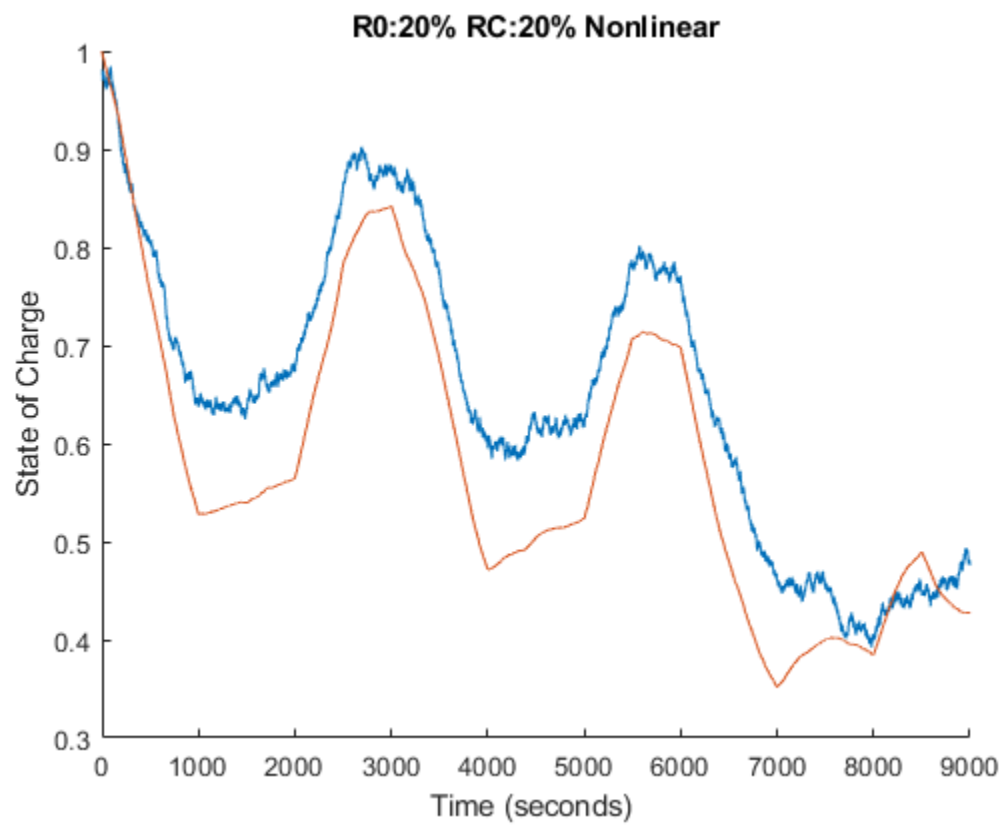
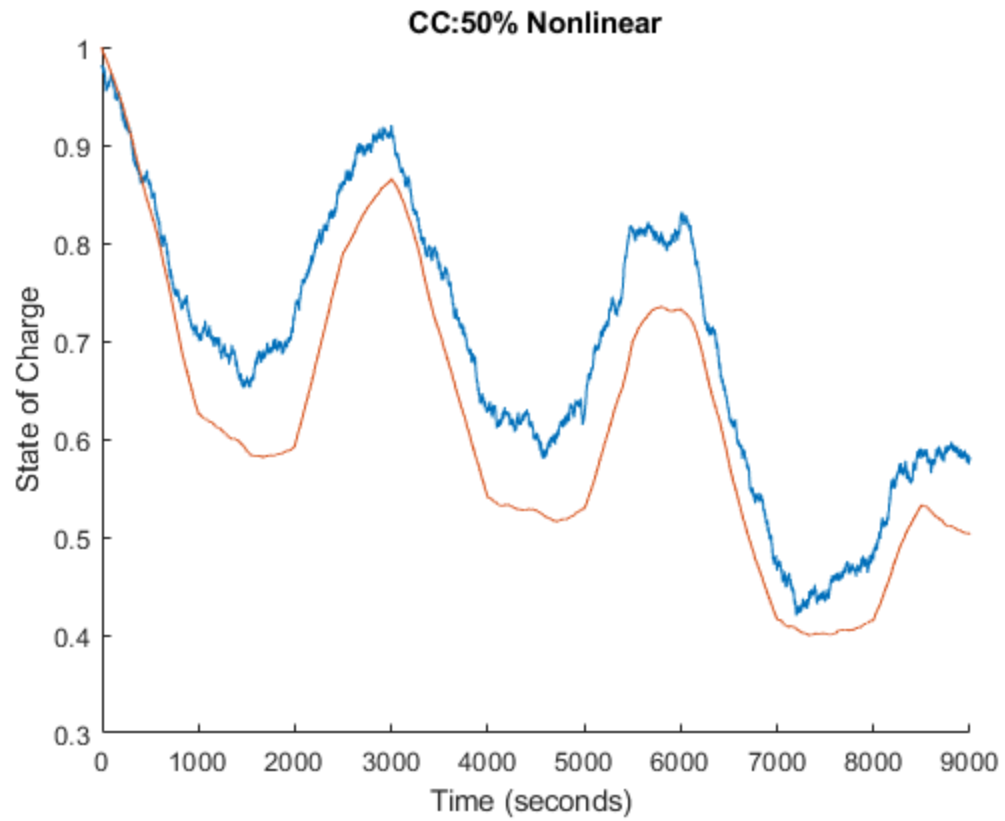












Nonlinear Estimator Plant with Nonlinear BASELINE data

```
List =  
    ["FirstOrderTruth_BASELINE_linear.mat", "FirstOrderTruth_R0_25_linear.mat", "FirstO  
  
load('OCV_table.mat')  
load('OCV_slope_table.mat')  
load(List(9));  
  
s = tf('s');  
  
%battery model parameters  
Rc = 0.015;      %Ohms  
Cc = 2400;       %F  
Cbat = 5*3600;  
alpha = 0.65;  
R0 = 0.01;       %Ohms  
Vocv0 = 3.435; %V  
  
%tunning parameters  
K = 1;           %gain  
% zeta = 0.707; %damping ratio  
zeta = 0.5;      %damping ratio  
  
wn = 75;         %natural frequency  
  
%continuous time ss model  
A = [-1/(Rc*Cc) 0; 0 0];  
B = [1/Cc; -1/Cbat];  
C = [-1 alpha];  
D = -R0;  
  
A1 = A(1,1);  
B1 = B(1,1);  
A2 = A(2,2);  
B2 = B(2,1);  
C2 = alpha;  
  
SI = [s 0; 0 s];  
Gp = C*(inv(SI-A))*B+D;      %plant  
T = minreal(K*wn^2/(s^2+2*zeta*wn*s+wn^2)); %complimentary  
Y = minreal(T/Gp);          %youla  
S = minreal(1-T);           %sensitivity  
Gc = minreal(Y/S);          %controller  
L = minreal(Gc*Gp);          %open loop TF  
sysTF = minreal(Gc*Gp/(1+Gc*Gp)); %actual sys TF  
[num, den] = tfdata(Gc, 'v'); %get numerator and denominator of Gc tf  
  
out = sim('Estimator_Simulink_trial2') ; %run simulink model
```

```

est_soc = out.SOC_est;
tout = out.tout;

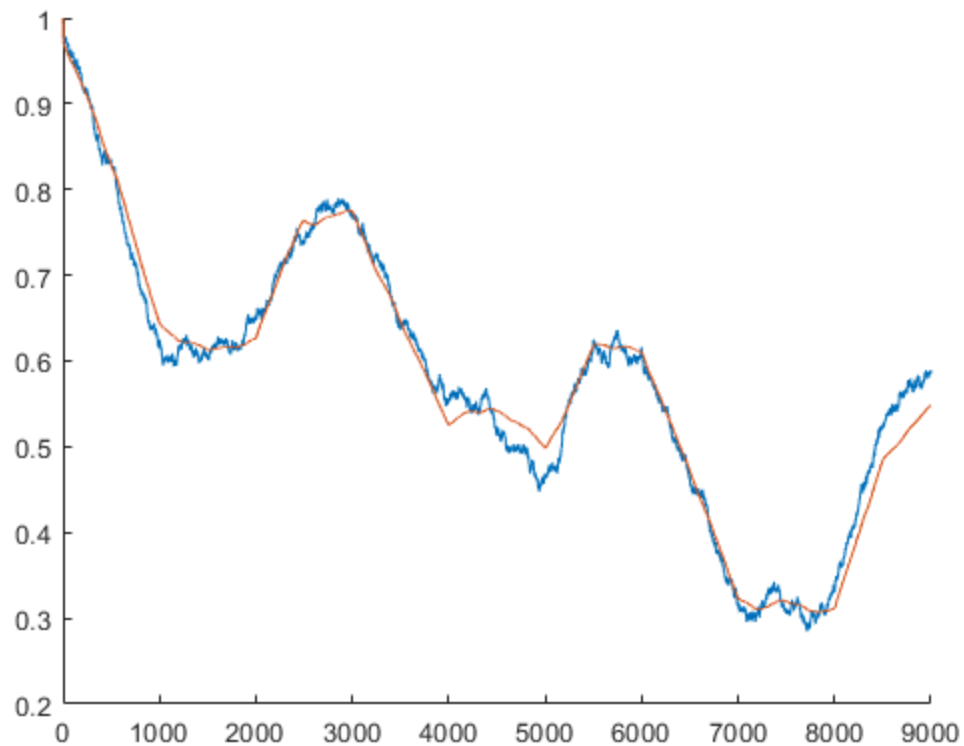
figure()
hold on
plot(t,SOC_act);
plot(tout,est_soc);
% %% Hinf Optimization Based Controller
%
%
% List =
% ["FirstOrderTruth_BASELINE_linear.mat","FirstOrderTruth_R0_25_linear.mat","FirstO
% NameList = ["Linear Baseline", "R0:25% Linear", "RC:25%
% Linear","CC:25% Linear","R0:50% Linear","RC:50% Linear","CC:50%
% Linear","R0:20% RC: 20%Linear","Nonlinear Baseline ","R0:25%
% Nonlinear","RC:25% Nonlinear","CC:25% Nonlinear","R0:50%
% Nonlinear","RC:50% Nonlinear","CC:50% Nonlinear", "R0:20% RC:20%
% Nonlinear" ];
%
%
% for k = 1:length(List)
%     load(List(k))
%     s=tf('s');
%
% Rc = 0.015;      %Ohms
% Cc = 2400;      %F
% Cbat = 5*3600;
% alpha =0.65;
% R0 = 0.01;      %Ohms
% Vocv0 = 3.435; %V
%
% %tunning parameters
% K = 1;          %gain
% % zeta = 0.707; %damping ratio
% zeta = 0.87; %damping ratio
%
% wn = 60;        %natural frequency
%
% %continuous time ss model
% A = [-1/(Rc*Cc) 0; 0 0];
% B = [1/Cc; -1/Cbat];
% C = [-1 alpha];
% D = -R0;
%
% A1 = A(1,1);
% B1 = B(1,1);
% A2 = A(2,2);
% B2 = B(2,1);
% C2 = alpha;
%
%
% Gp = (-64800*s^2 - 2093.4*s - 0.65)/(18000*s*(36*s+1)); %plant
% sysg=ss(Gp);
% [Ag,Bg,Cg,Dg]=ssdata(sysg);

```

```

%
% Ag=Ag-0.08*eye(1); % slightly shift A to avoid poles on jw axis
%
% [num,den]=ss2tf(Ag,Bg,Cg,Dg);
% Gpn=tf(num,den); % perturbed plant
%
% % Hinf shaping filter
% W1=(s+43)/(2*s+0.01); %(BW >= 65rad/s(CL at -6dB) so step input resp
%   shows tracking at high freq) *input data at 10Hz
% W2=0.05;
% % W3=0.5;
% W3 = makeweight(1/2,43,50); %(low freq gain, cross over freq, high
%   freq gain)
%
%                               %^^to make it look like a
%   differentiator!
%
% %Hinf Controller Computation
% ssga_=augtf(Gpn,W1,W2,W3);
% [sys3,sscl,GAM]=hinfsyn(ssga_); %sys3=controller, sscl=CL tf (w/z),
%
% % Hinf Controller
% Gc=minreal(tf(sys3));
%
% [num, den] = tfdata(Gc, 'v'); %get numerator and denominator of Gc
%   tf
%
% out = sim('Estimator_Simulink_trial1') ; %run simulink model
%
% est_soc = out.SOC_est;
% tout = out.tout;
%
% figure()
% hold on
% plot(t,SOC_act);
% plot(tout,est_soc);
%
% end

```



Kalman Filter

```
List =
    ["FirstOrderTruth_BASELINE_linear.mat", "FirstOrderTruth_R0_25_linear.mat", "FirstO
NameList = ["Linear Baseline", "R0:25% Linear", "RC:25%
    Linear", "CC:25% Linear", "R0:50% Linear", "RC:50% Linear", "CC:50%
    Linear", "R0:20% RC: 20%Linear", "Nonlinear Baseline ", "R0:25%
    Nonlinear", "RC:25% Nonlinear", "CC:25% Nonlinear", "R0:50%
    Nonlinear", "RC:50% Nonlinear", "CC:50% Nonlinear", "R0:20% RC:20%
    Nonlinear" ];

for i = 1:length(List)

    load(List(i));

    R0 = 0.01;
    Rc = 0.015;
    Cc = 2400;
    Cbat = (5*3600);
    alpha = .65;
    Voc_0 = 3.435;
    SOC0 = 1;

    dt = .1;
```

```

%System Dynamics
%Linear Model
A = [1 0 ; 0 (1-(dt/(Rc*Cc)))];
B = [-(dt/Cbat) ; (dt/Cc)];
C = [alpha -1];
D = [-R0];

%Kalman Model
Ak = [1];
Bk = [-(dt/Cbat)];
Ck=[alpha];
Dk=[R0];

% Kalman Filter

wk_mean = 0;
Q = 2.5*10^-7;
vk_mean = 0;
R = 1*10^-4;
P0 = 0;

Q = 2.5*10^-9;

% Set Initial Conditions
P(1) = P0;
x1(1) = .98; % SOC
x2(1) = 0; % Vc
x1_hat(1) = .98;

for k = 2:1:length(t)
    %State Equations:
    x1(k) = x1(k-1)-(dt/Cbat)*I(k-1); %normrnd(0,Q); % SOC
    x2(k) = (1-(dt/(Rc*Cc)))*x2(k-1)+(dt/Cc)*I(k-1); % Vc

    % Open Loop:
    x1_ol(k) = Ak*x1(k-1)+Bk*I(k-1);

    % Model Prediction:
    x1_hat_prev(k) = Ak*x1_hat(k-1)+ Bk*I(k-1);
    P_prev = Ak*P(k-1)*Ak' + Q;

    %Estimated Output:
    V_hat = alpha*x1_hat_prev(k)-x2(k)- R0*I(k)+ Voc_0;

    % Measurement Update:
    x1_hat(k) = x1_hat_prev(k) +
    P_prev*Ck'*inv(Ck*P_prev*Ck'+R)*(V(k)-V_hat);
    P(k) = P_prev -P_prev*Ck'*inv(Ck*P_prev*Ck'+R)*Ck*P_prev;

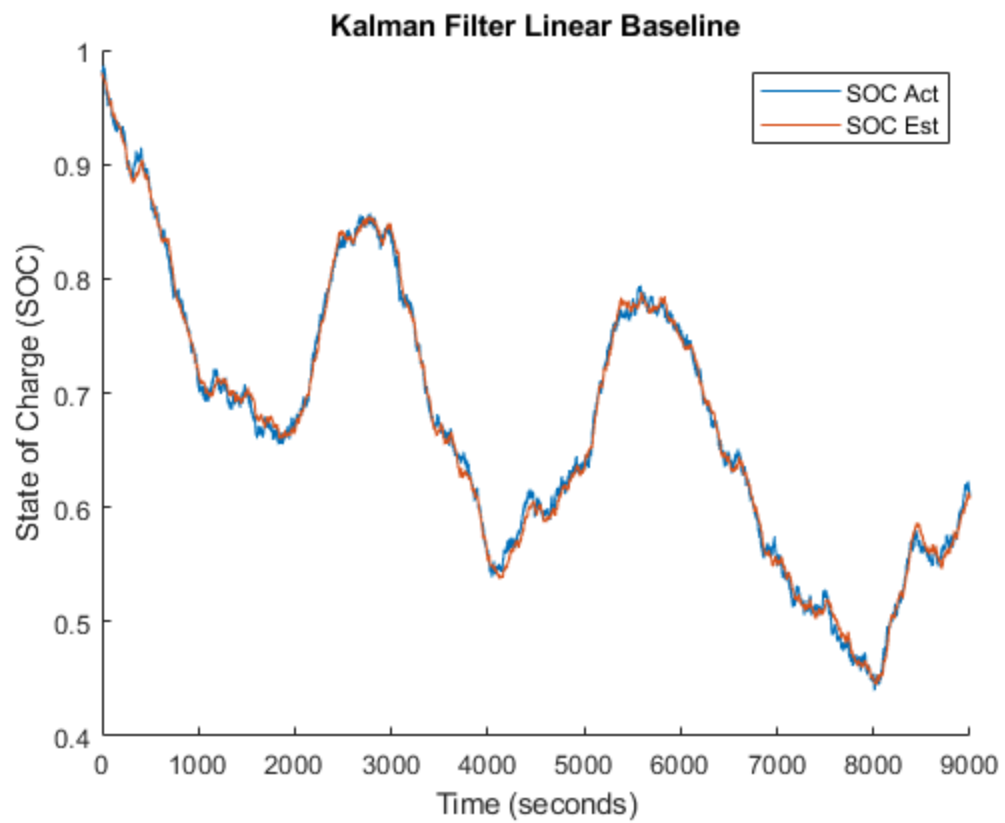
end

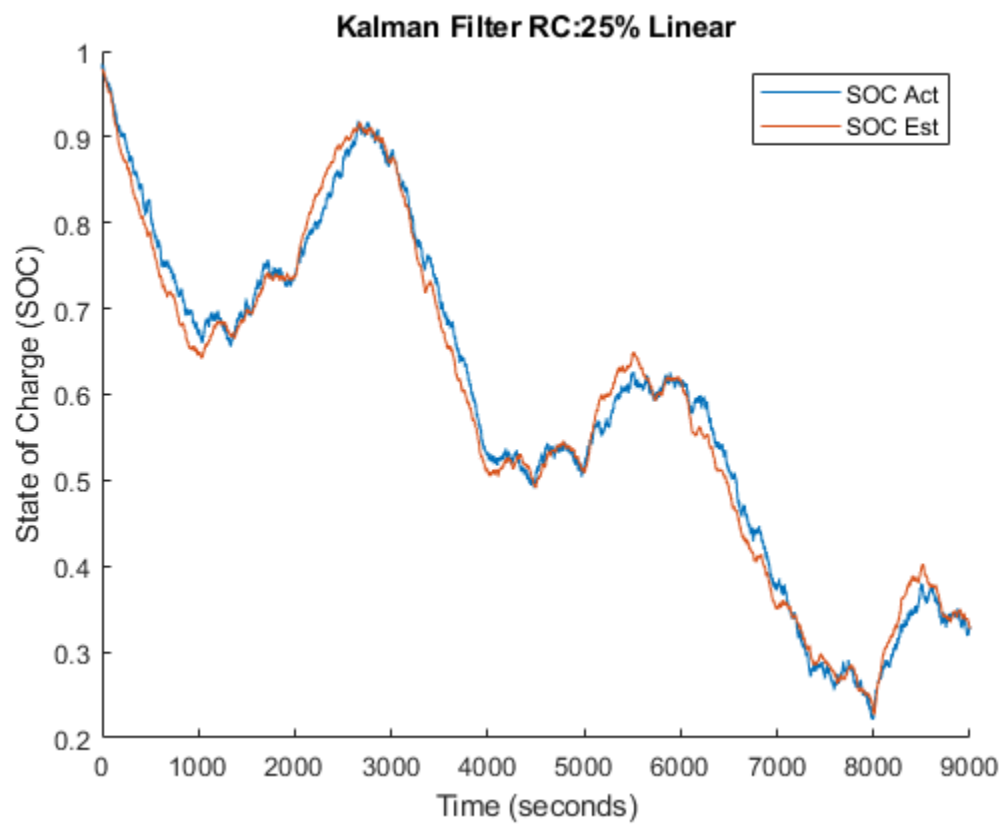
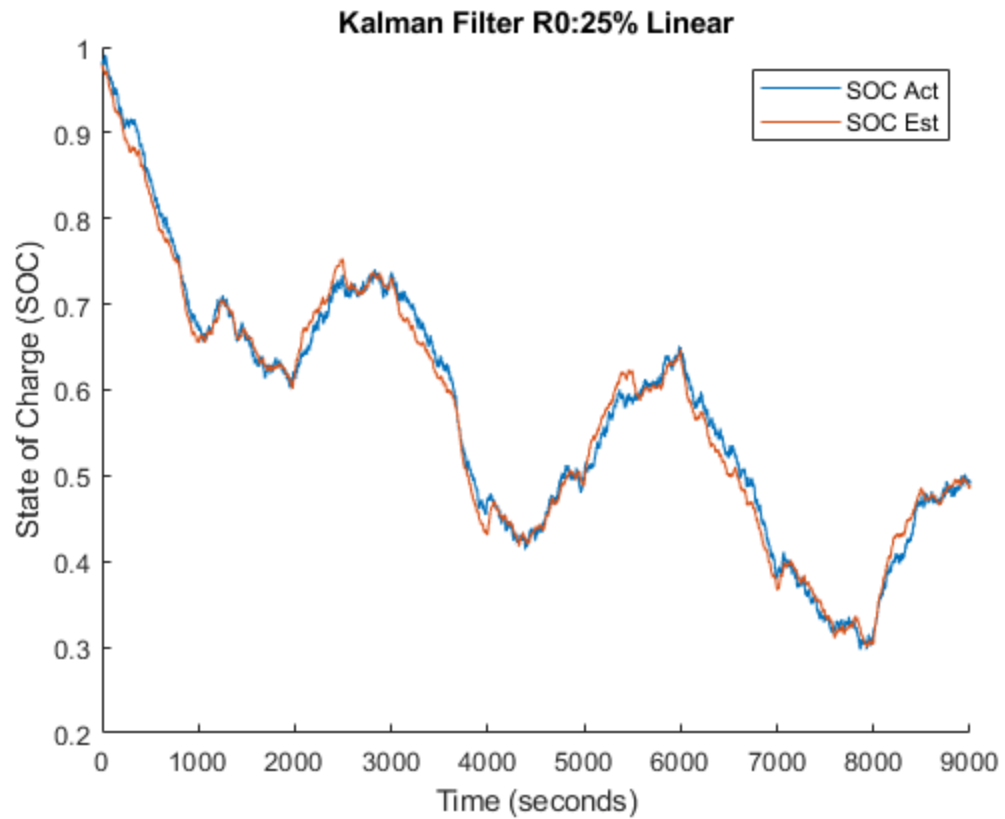
```

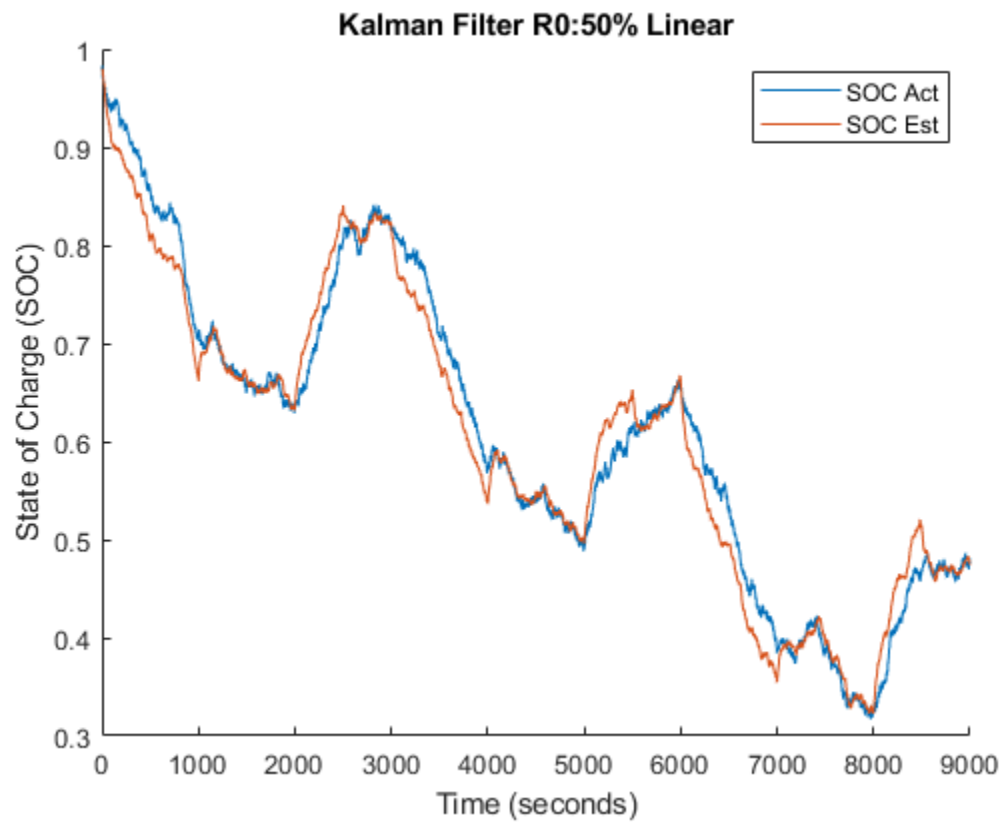
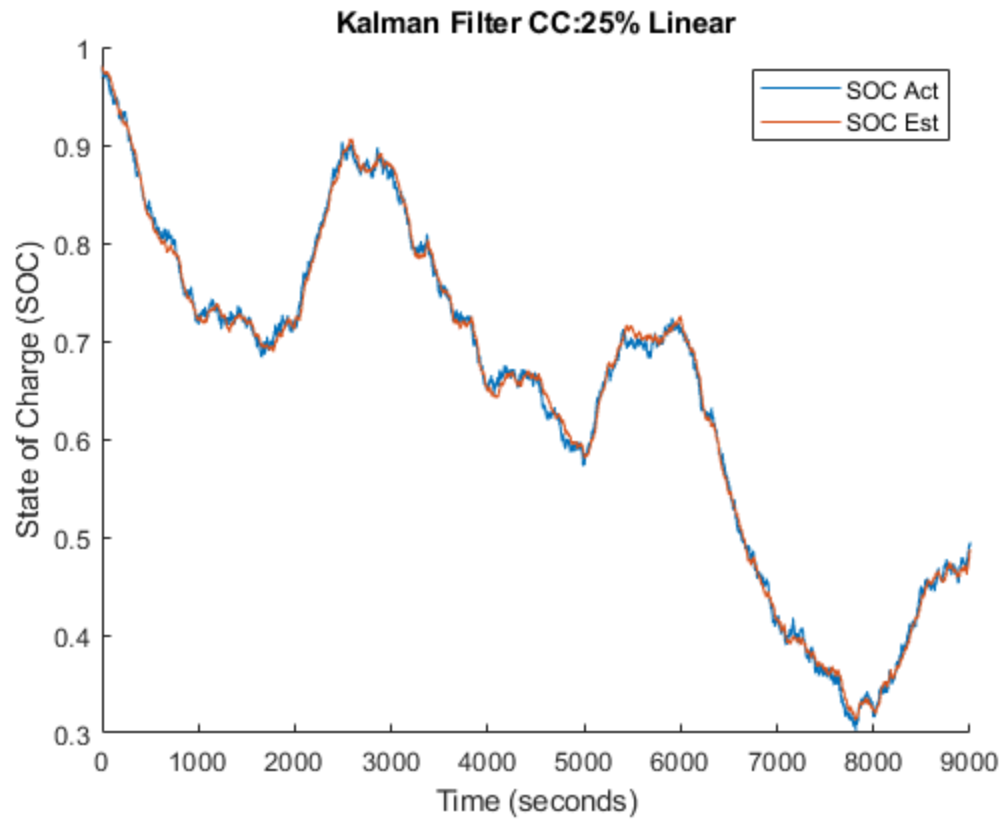
```
KALMAN_ACTUAL(:,i)= SOC_act;
KALMAN_ESTIMATED(:,i)=x1_hat;

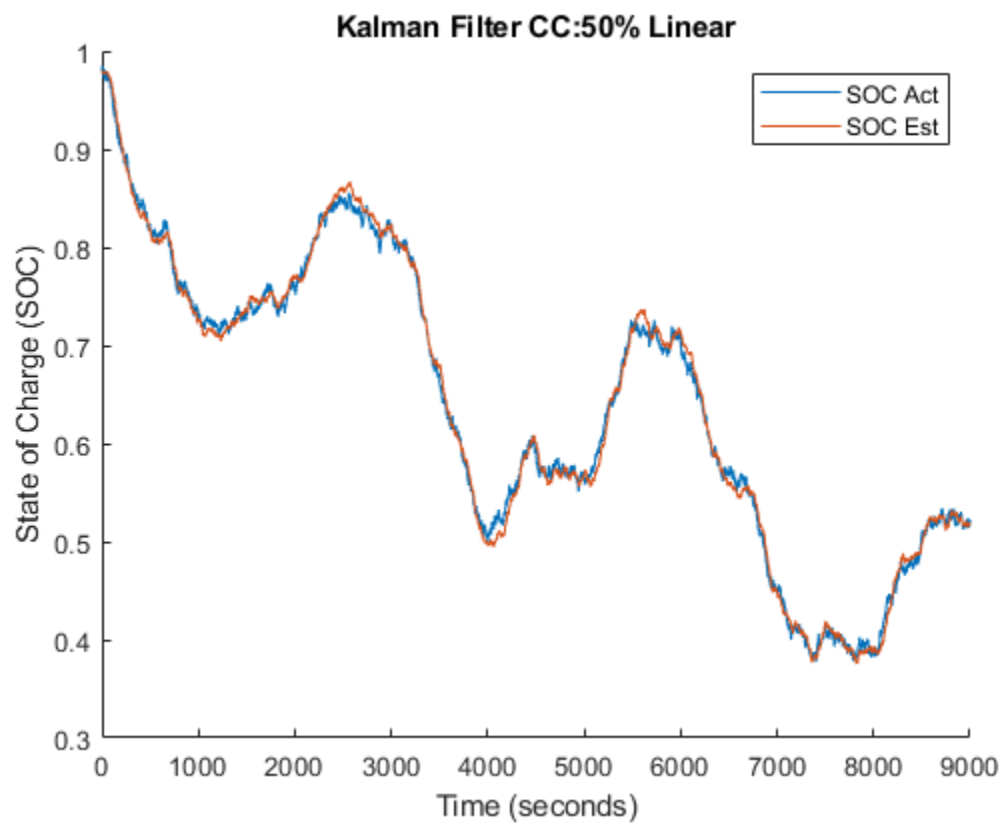
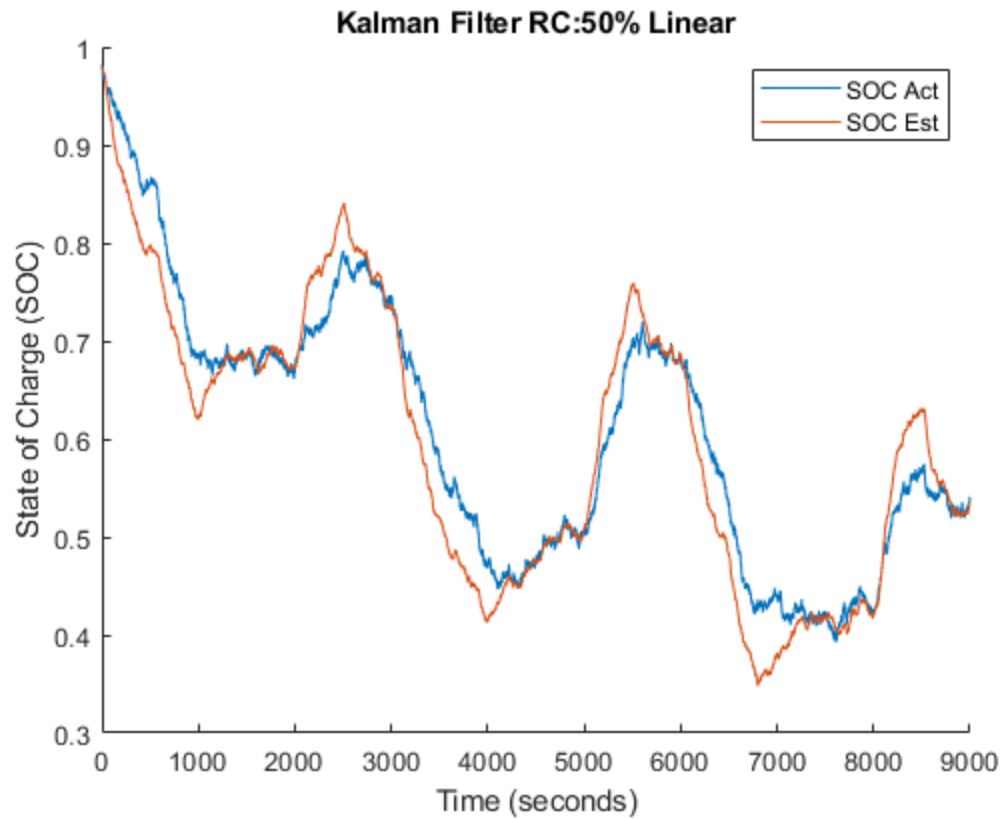
figure();
hold on
plot(t,SOC_act)
plot(t,x1_hat)
title('Kalman Filter '+ NameList(i));
xlabel('Time (seconds)');
ylabel('State of Charge (SOC)');
legend('SOC Act','SOC Est');

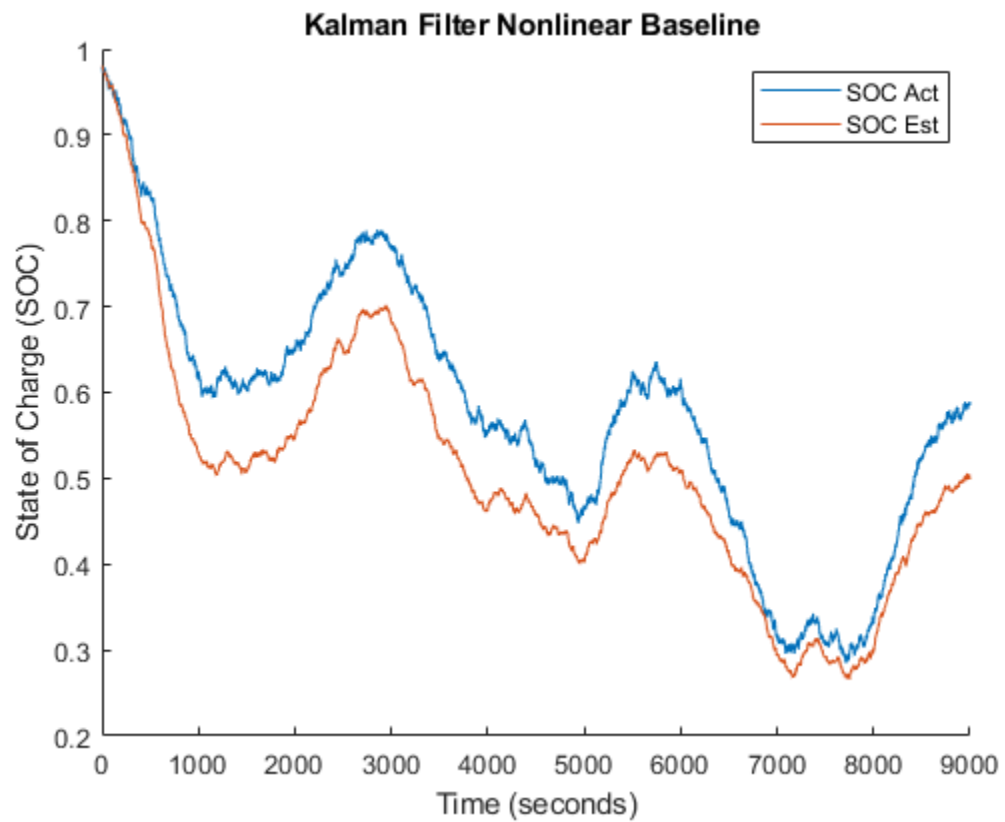
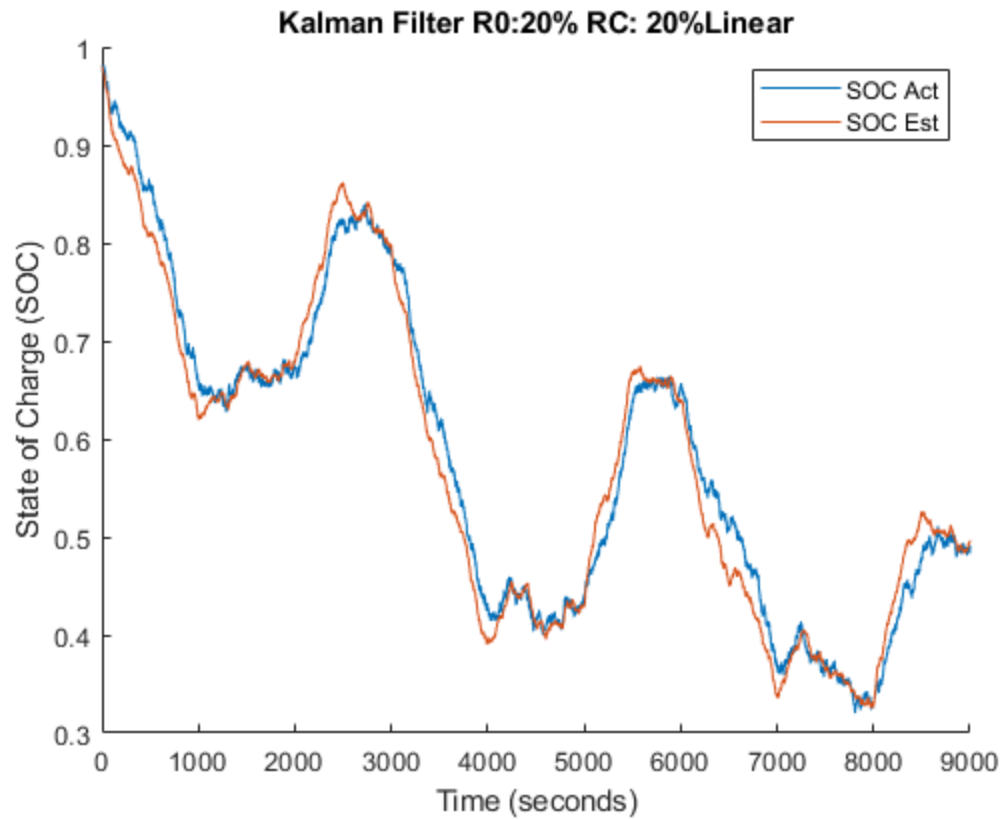
end
```

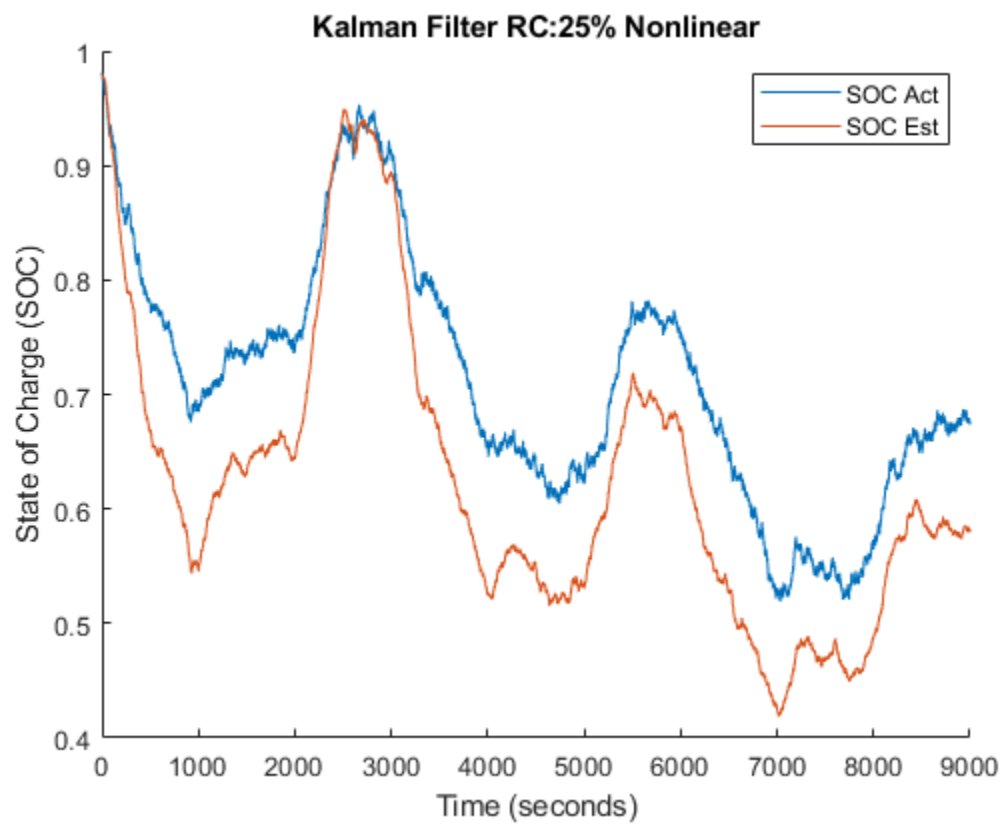
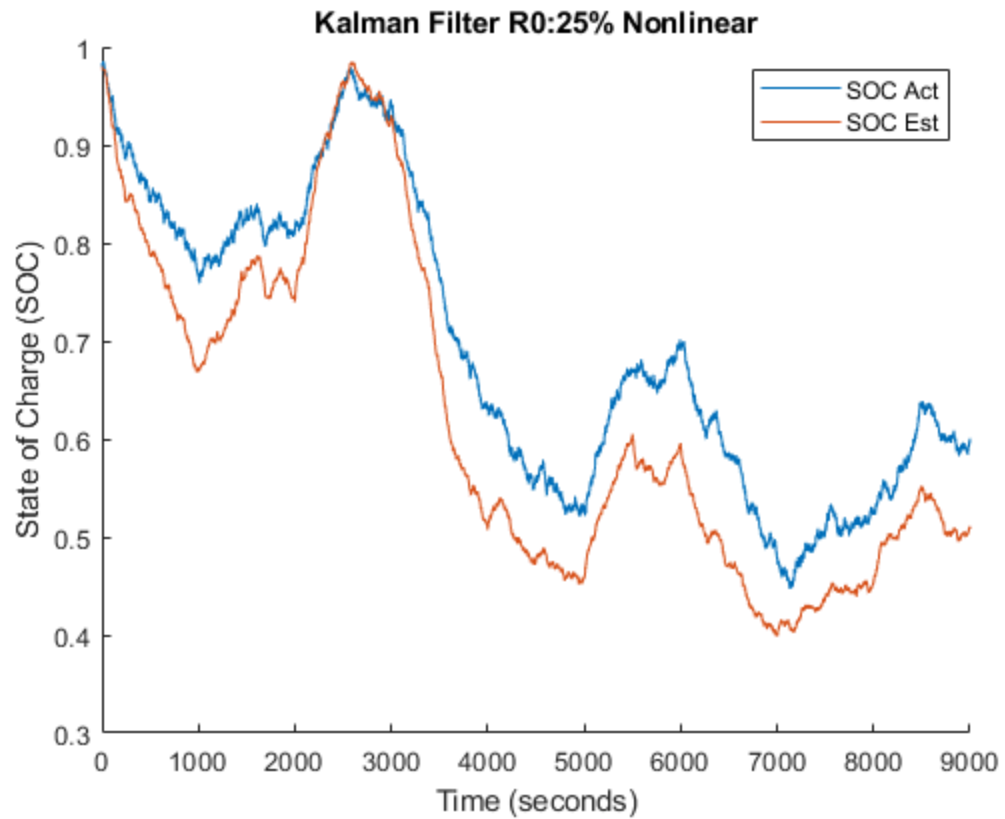


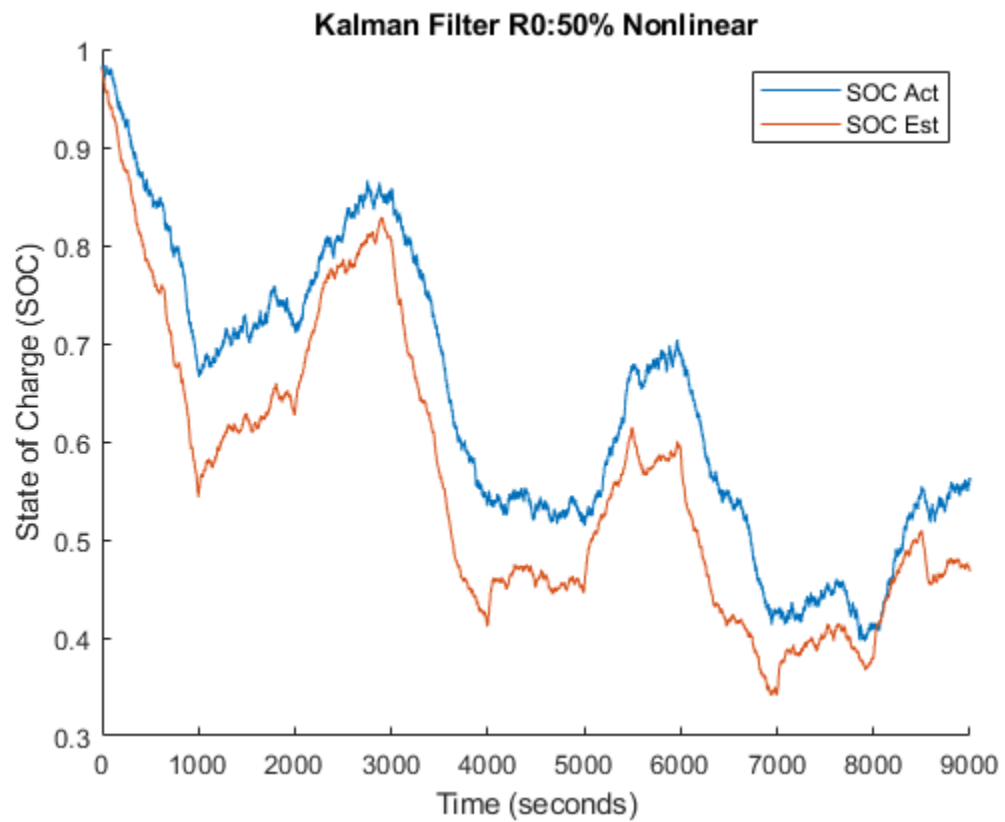
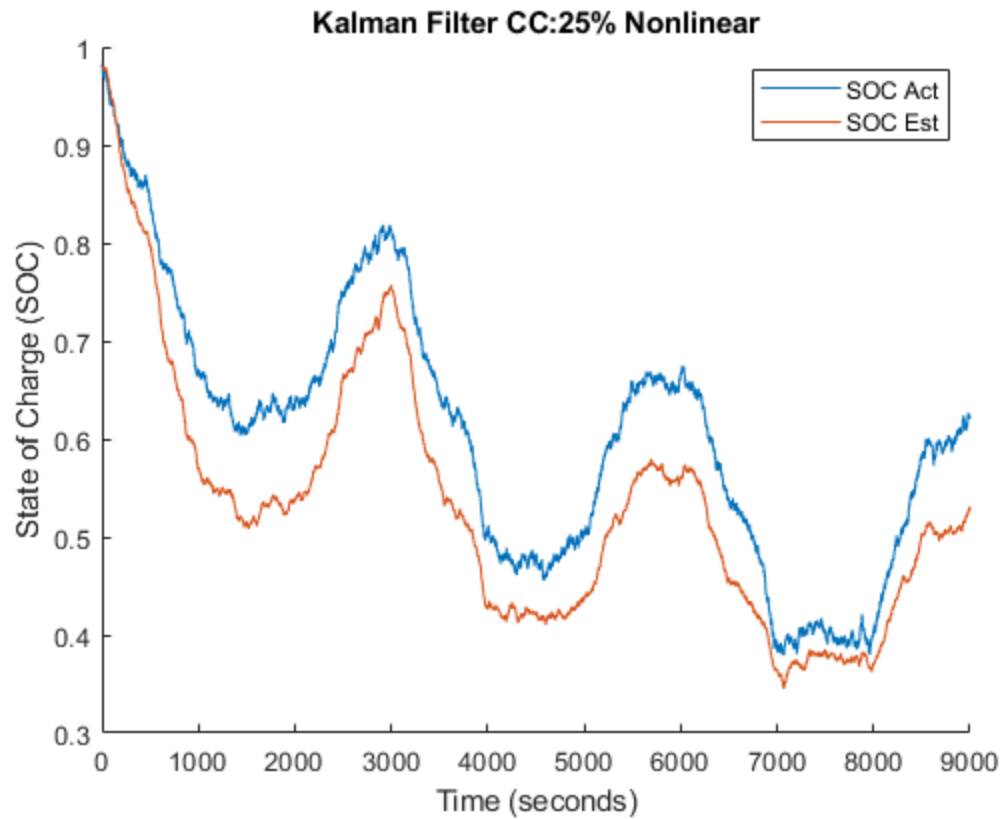


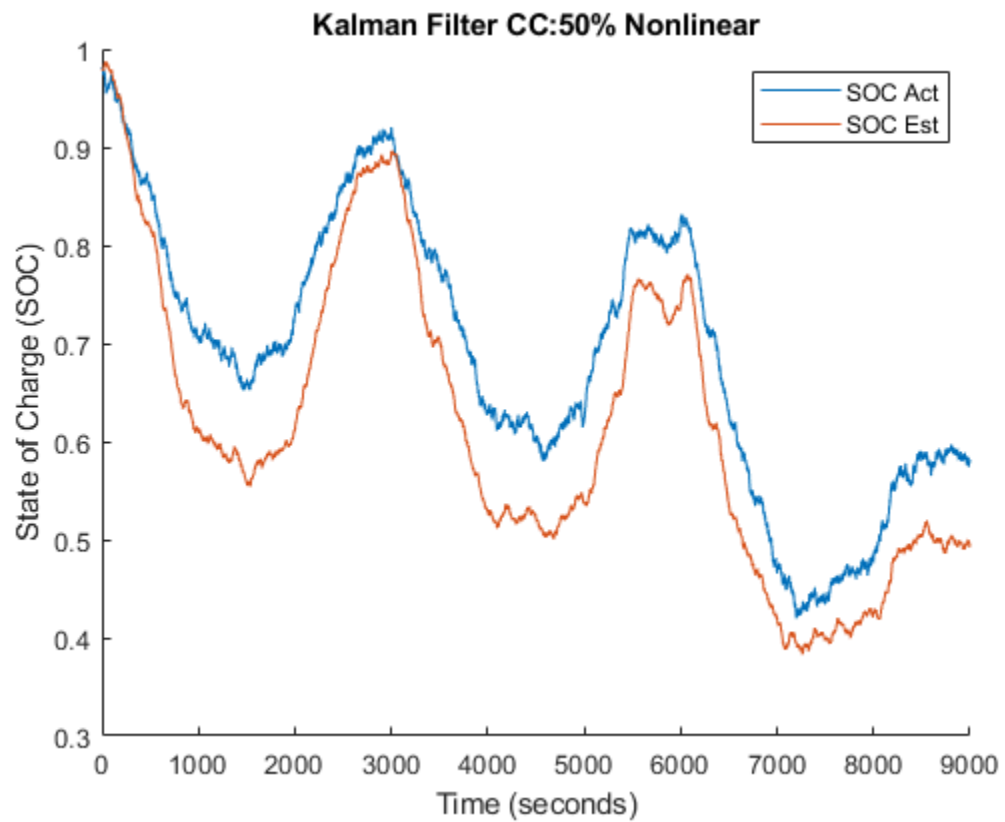
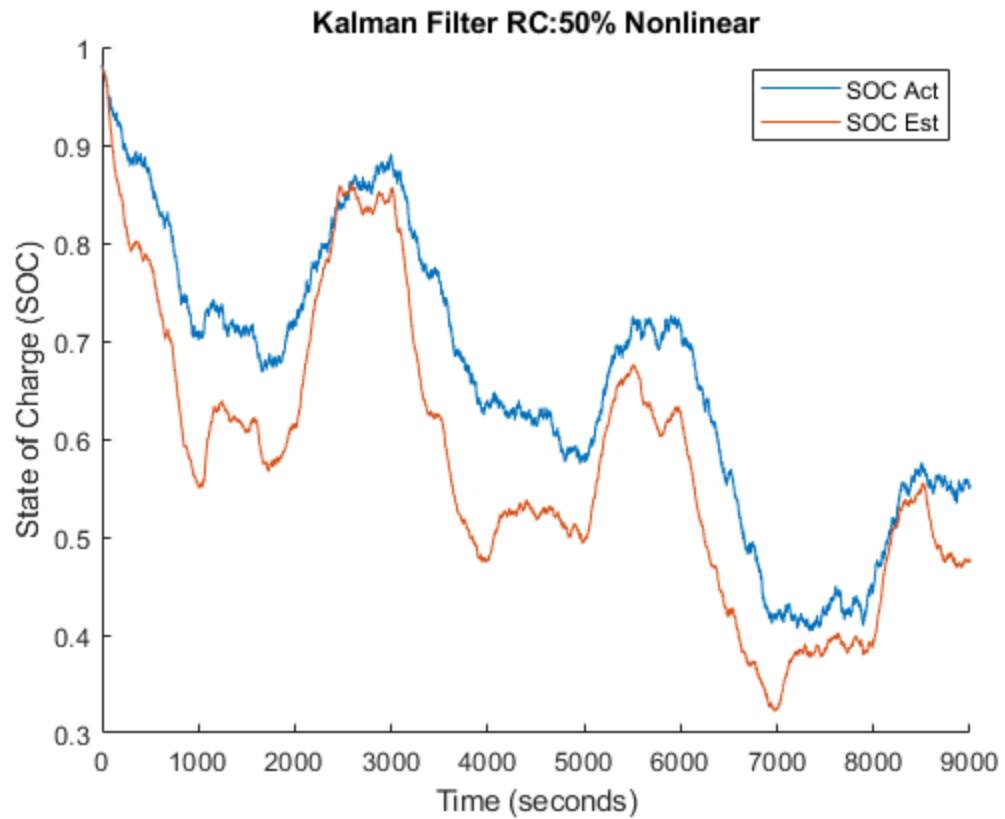


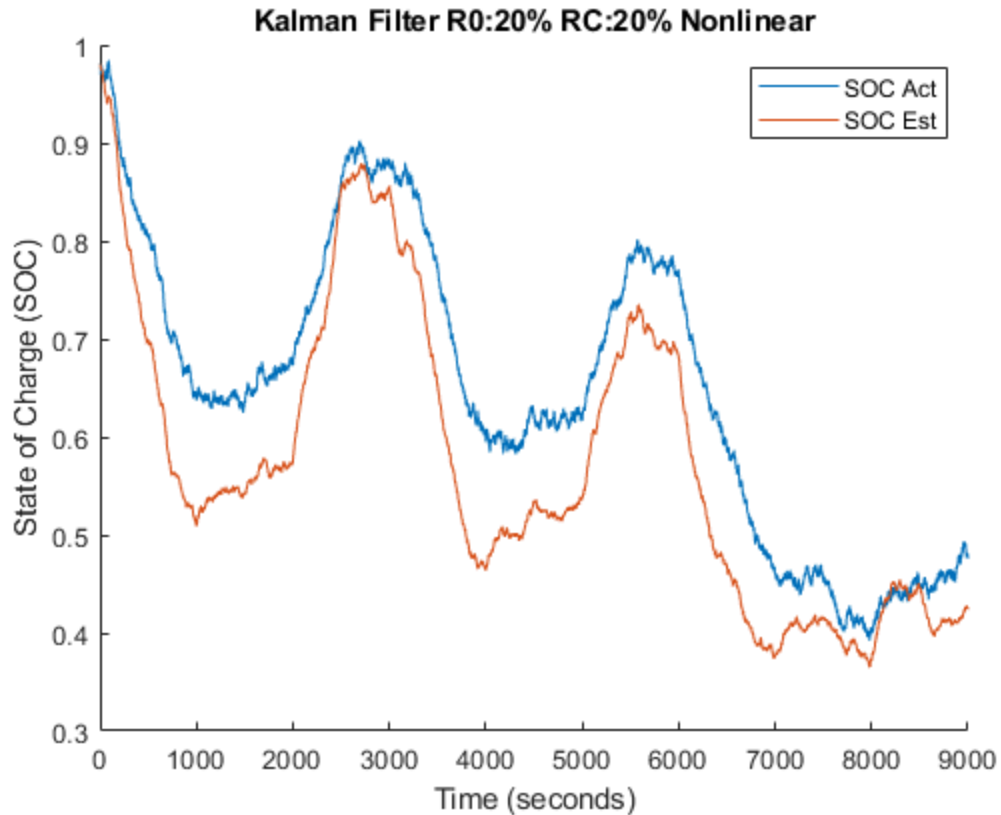












Extended Kalman Filter

```
List =
    ["FirstOrderTruth_BASELINE_linear.mat", "FirstOrderTruth_R0_25_linear.mat", "FirstO
NameList = ["Linear Baseline", "R0:25% Linear", "RC:25%
    Linear", "CC:25% Linear", "R0:50% Linear", "RC:50% Linear", "CC:50%
    Linear", "R0:20% RC: 20%Linear", "Nonlinear Baseline ", "R0:25%
    Nonlinear", "RC:25% Nonlinear", "CC:25% Nonlinear", "R0:50%
    Nonlinear", "RC:50% Nonlinear", "CC:50% Nonlinear", "R0:20% RC:20%
    Nonlinear" ];

for i = 1:length(List)

    load(List(i));

    R0 = 0.01;
    Rc = 0.015;
    Cc = 2400;
    Cbat = (5*3600);
    alpha = .65;
    Voc_0 = 3.435;
    SOC0 = 1;

    dt = .1;
```

```

wk_mean = 0;
Q = 2.5*10^-7;
vk_mean = 0;
R = 1*10^-4;
P0 = 0;

A_ek = 1 ;

% function val = C_ek(SOC_hat)
% val = interp1(soc_intpts_OCV_slope,OCV_slope_intpts,SOC_hat);
% end
E_ek = 1;
F_ek = 1;

Ak = 1;
Bk = -dt/Cbat;

load('OCV_table.mat')
load('OCV_slope_table.mat')
% load('IV_data_nonlinear')

R = 1*10^-4;
Q = 2.5*10^-9;

% Set Initial Conditions
P(1) = P0;
x1(1) = .98; % SOC
x2(1) = 0; % Vc
x1_hat(1) = .98;

for k = 2:length(t)
    x1(k) = x1(k-1)-(dt/Cbat)*I(k-1); %normrnd(0,Q); % SOC - Coulomb
    Counting
    x2(k) = (1-(dt/(Rc*Cc)))*x2(k-1)+(dt/Cc)*I(k-1); % Vc

    C_ek =
    interp1(soc_intpts_OCV_slope' ,OCV_slope_intpts,x1_hat(k-1));

    % Model Prediction:
    x1_hat_prev = Ak*x1_hat(k-1)+Bk*I(k-1);
    P_prev = A_ek*P(k-1)*A_ek'+E_ek*Q*E_ek';

    % Measurement Update:
    V_hat = interp1(soc_intpts_OCV' ,OCV_intpts,x1_hat(k-1)) -I(k)*R0-
x2(k);
    L = P_prev*C_ek'*inv(C_ek*P_prev*C_ek'+F_ek*R*F_ek');

    x1_hat(k) = x1_hat_prev + L*(V(k)-V_hat);
    P(k) = P_prev -L*C_ek*P_prev;

end

```

```

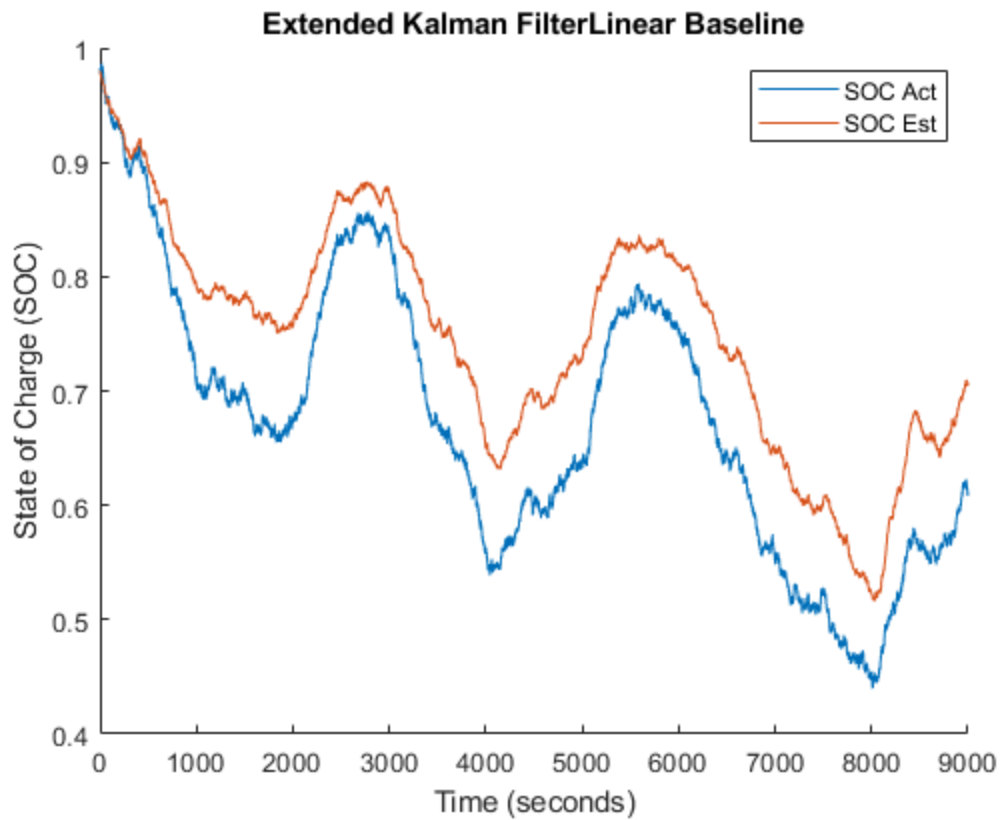
EXTENDED_KALMAN_ACTUAL(:,i)= SOC_act;
EXTENDED_KALMAN_ESTIMATED(:,i)=x1_hat;

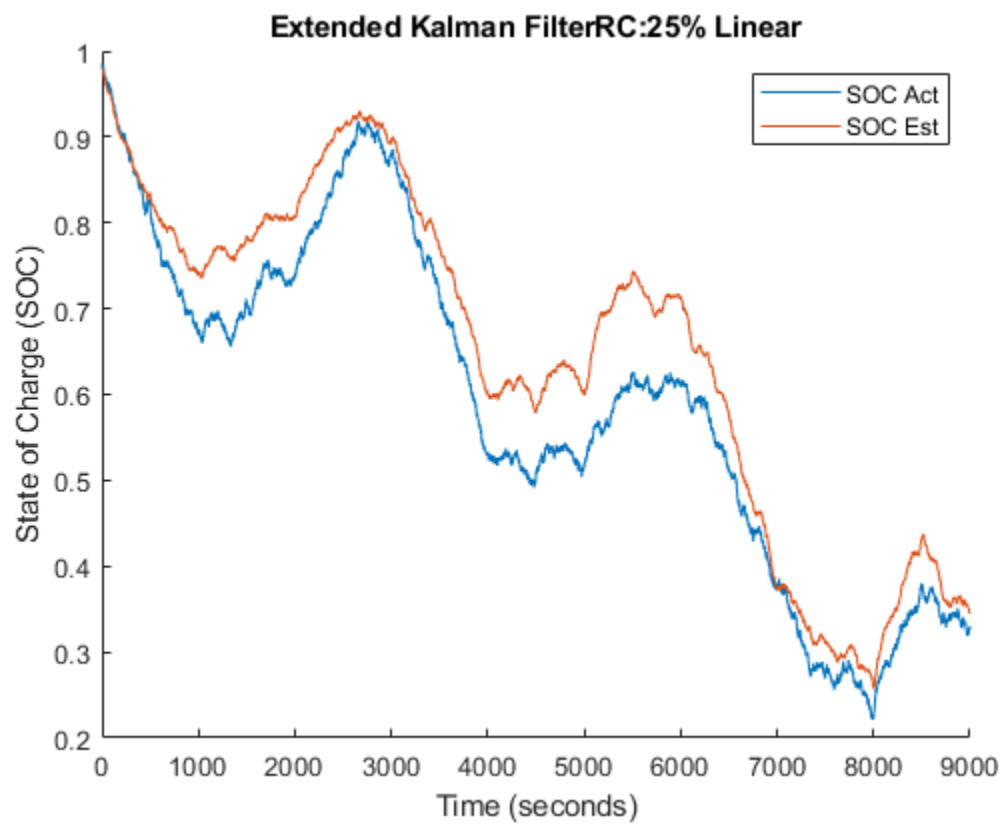
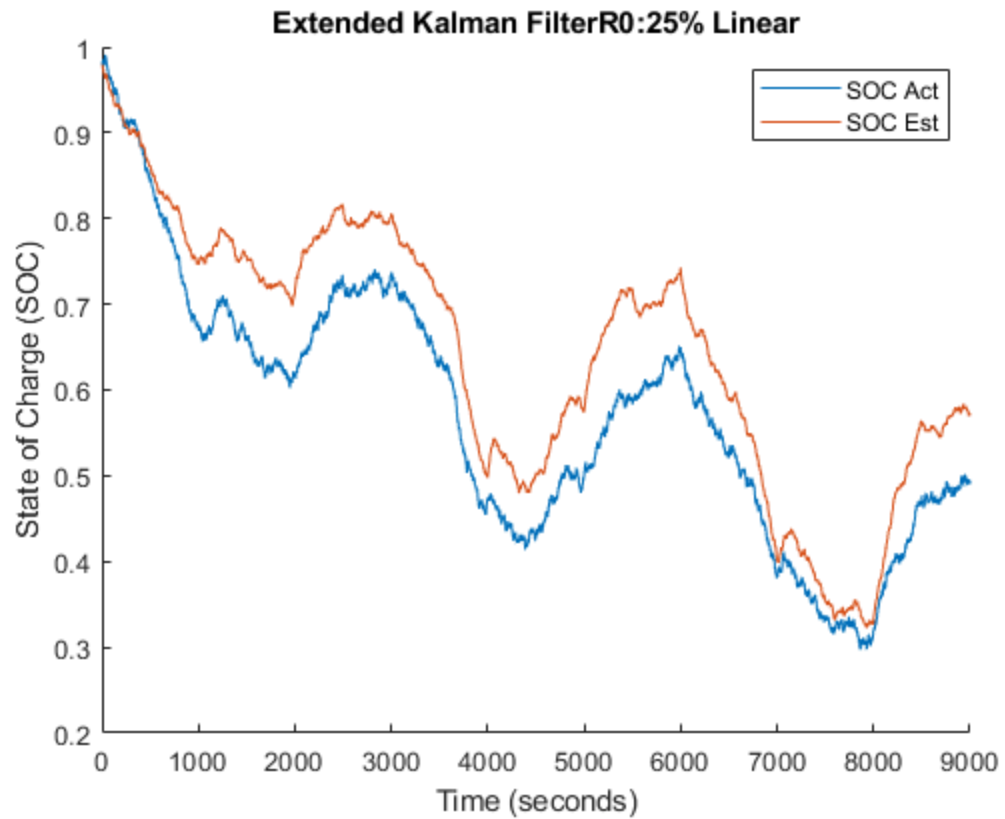
figure();
hold on
plot(t,SOC_act)
plot(t,x1_hat)
title('Extended Kalman Filter' + NameList(i));
xlabel('Time (seconds)');
ylabel('State of Charge (SOC)');

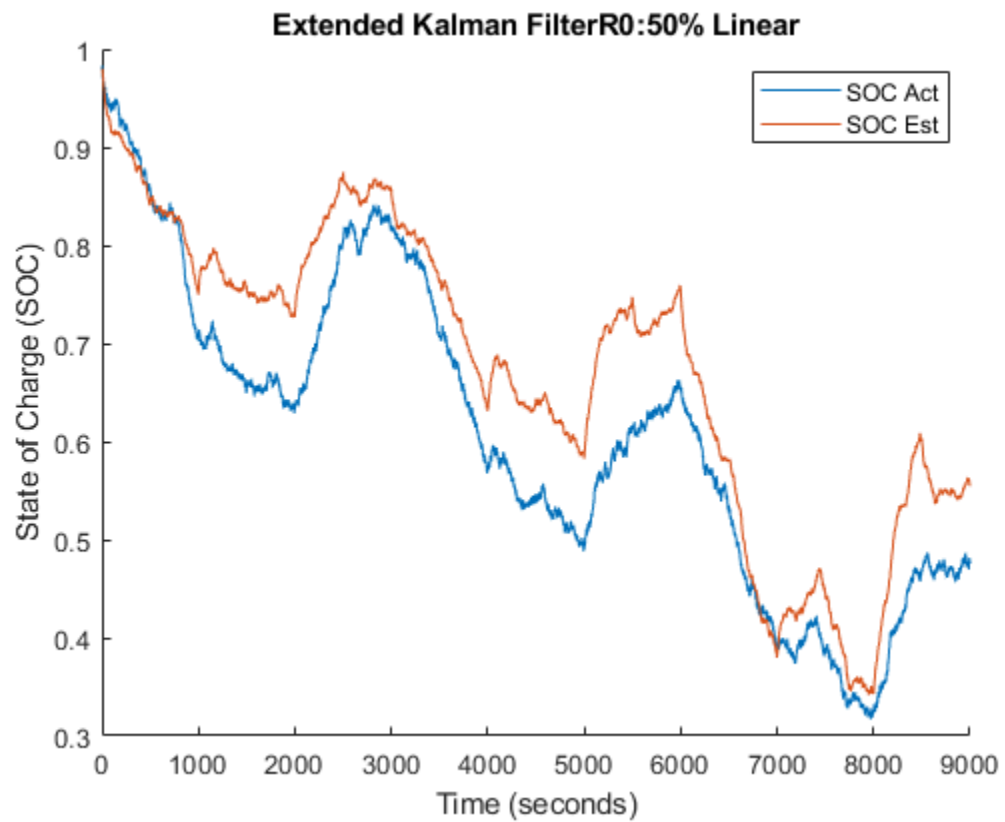
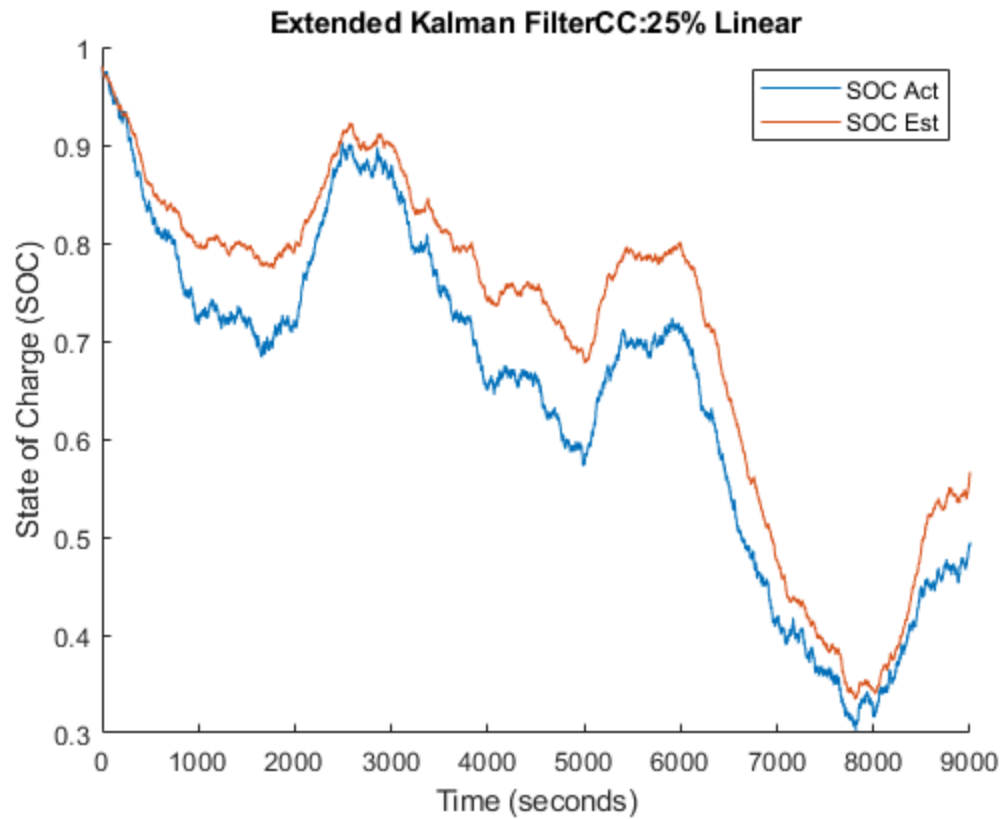
legend('SOC Act','SOC Est');

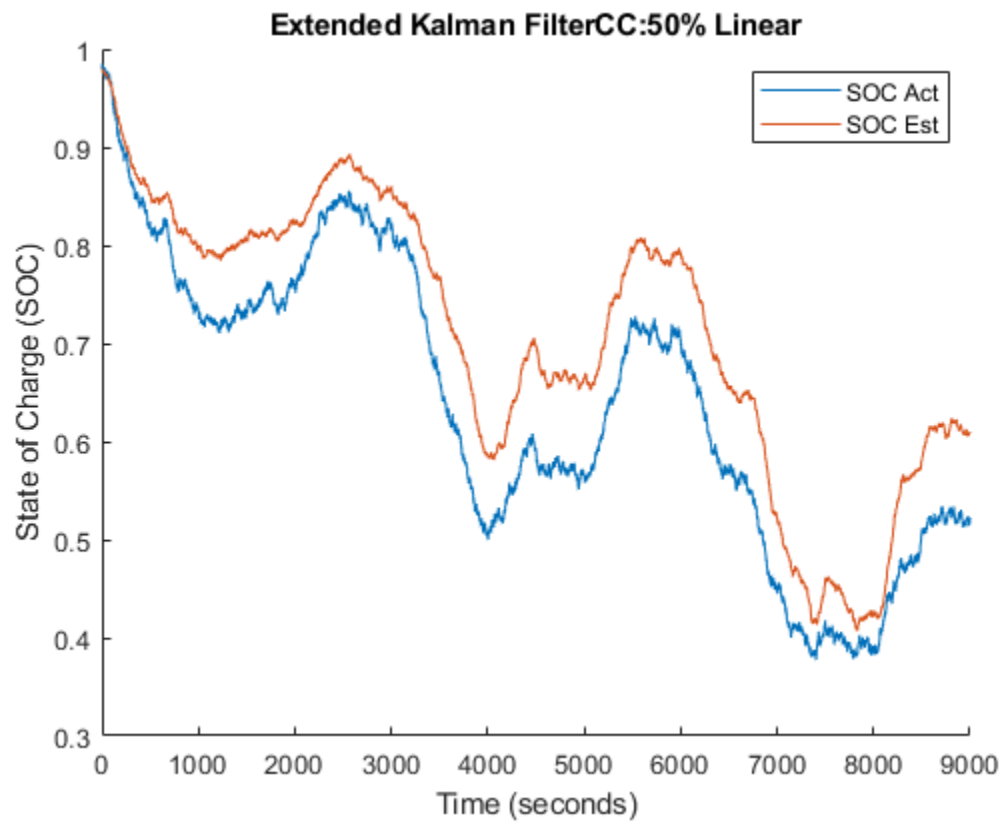
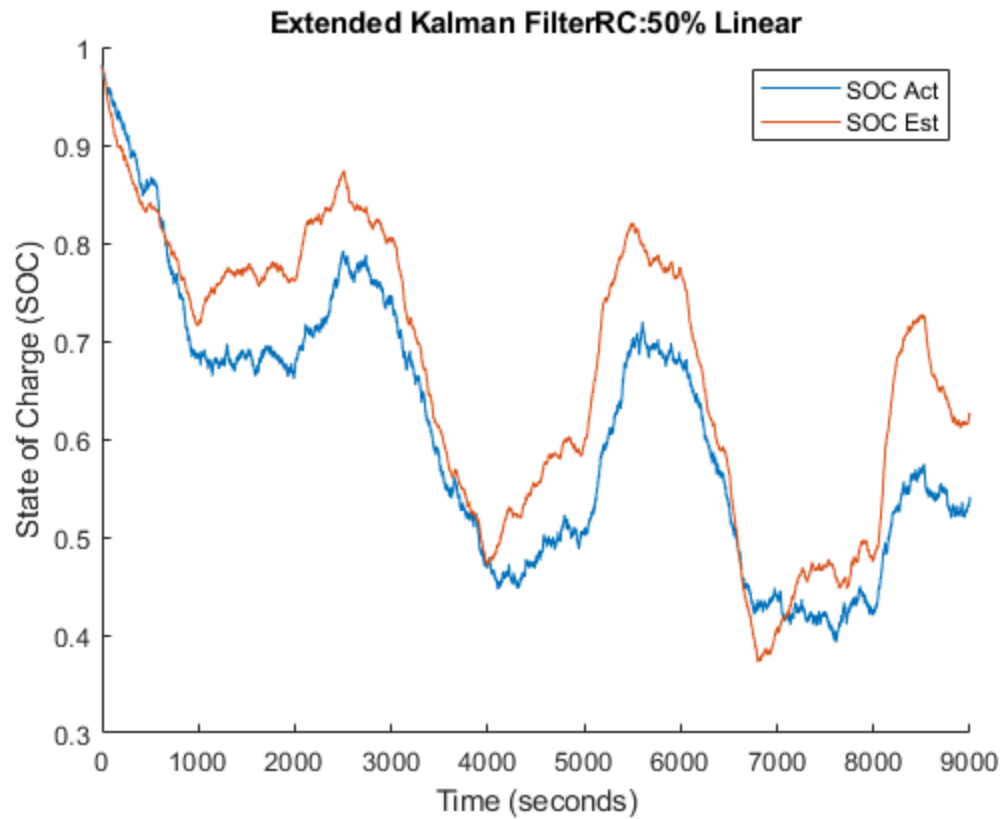
end

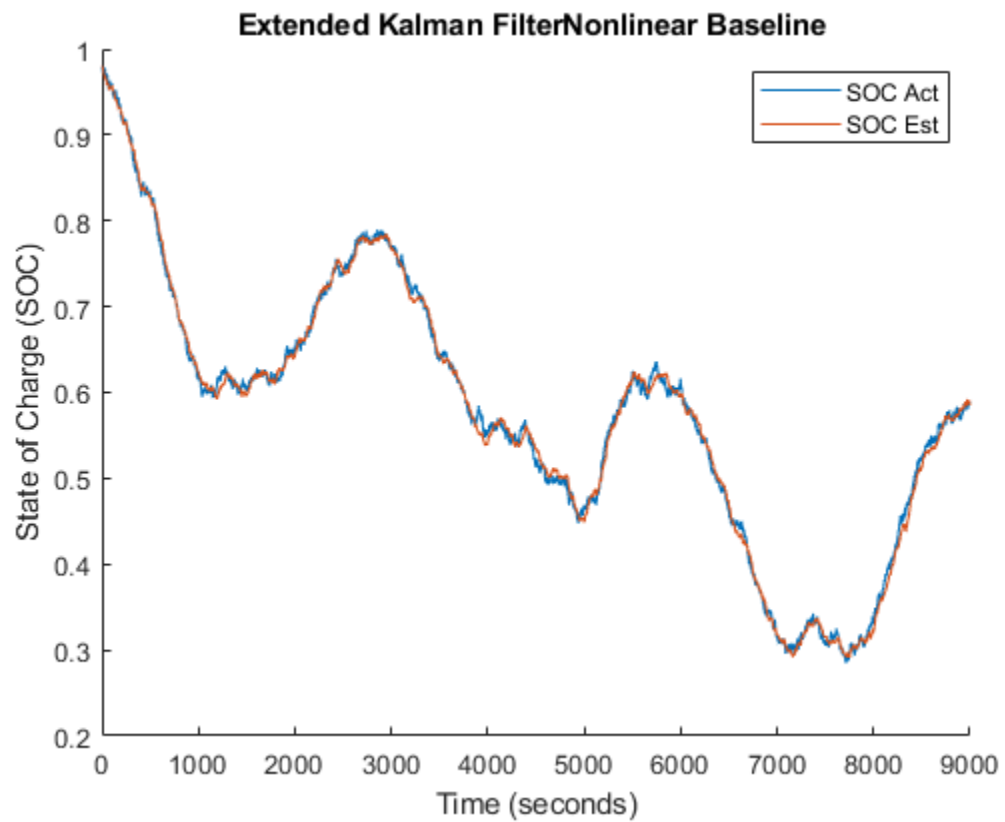
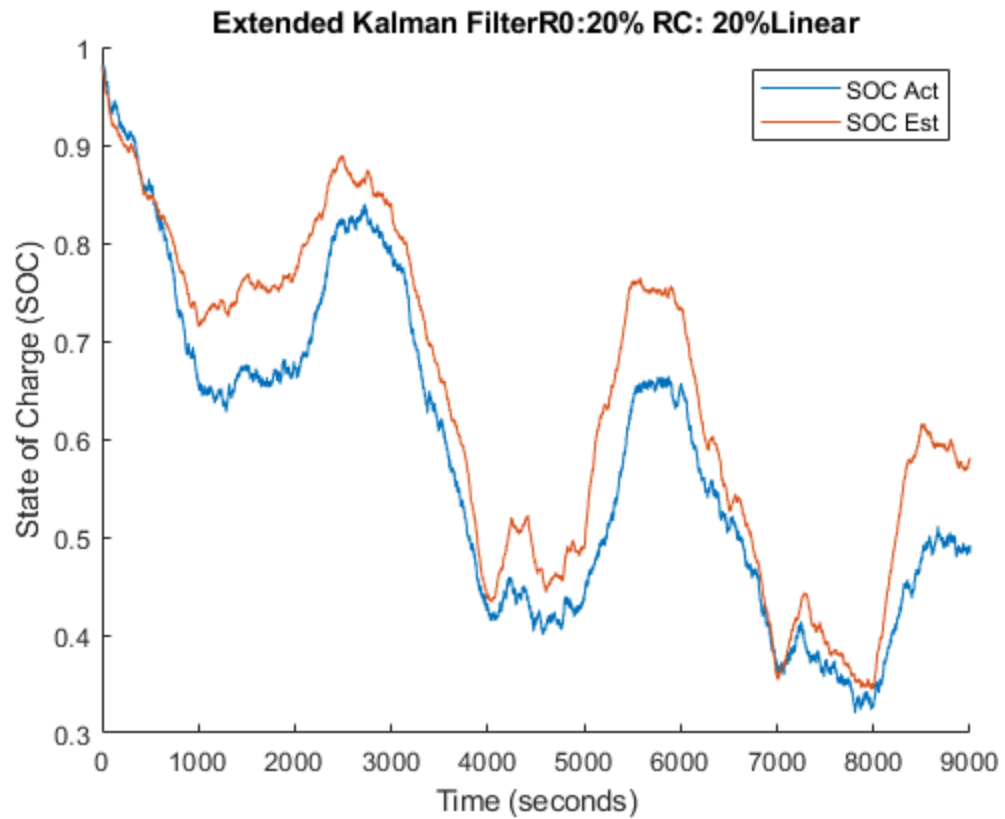
```

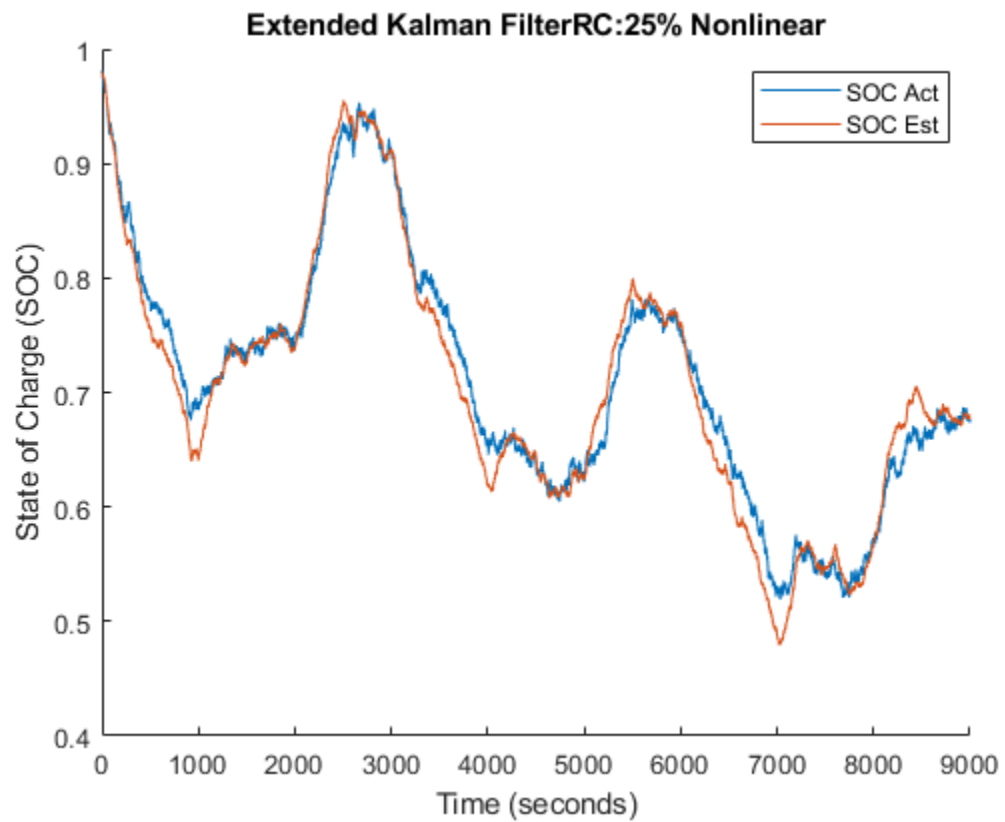
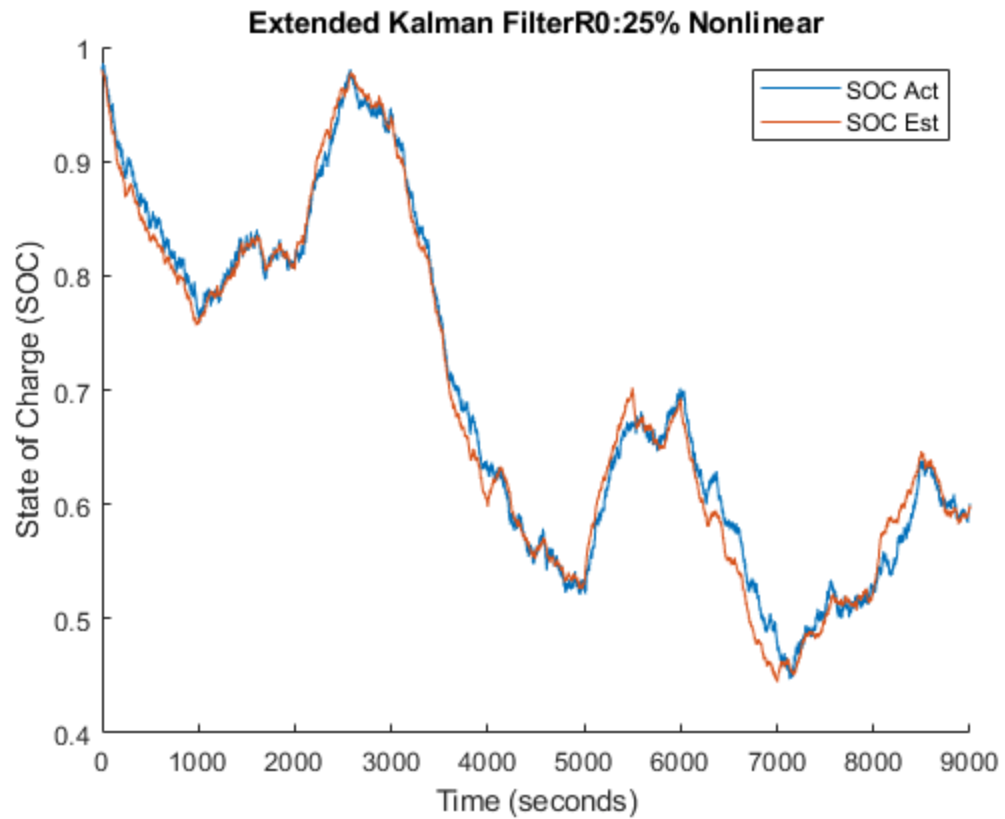


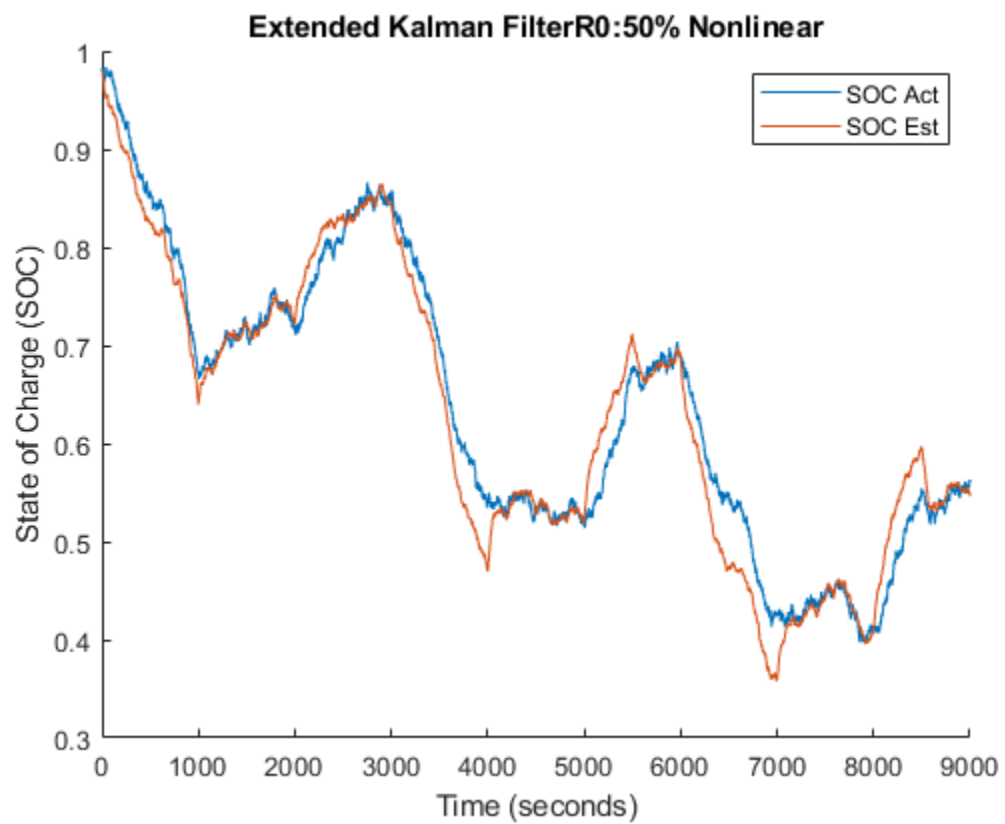
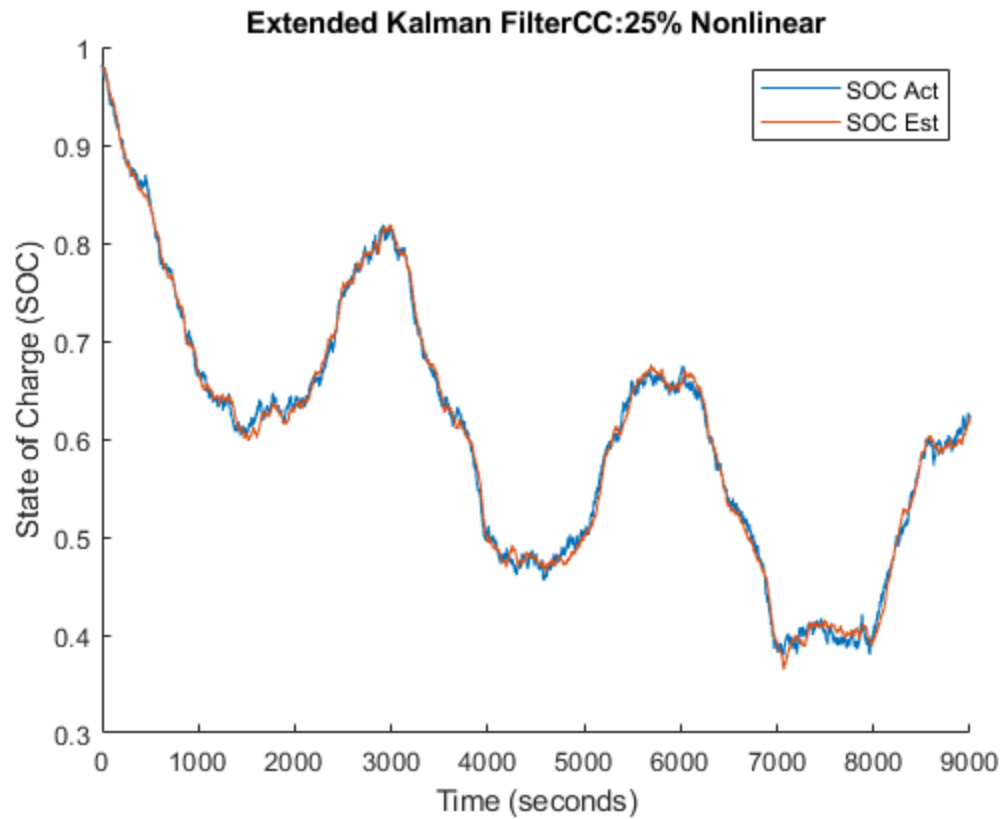


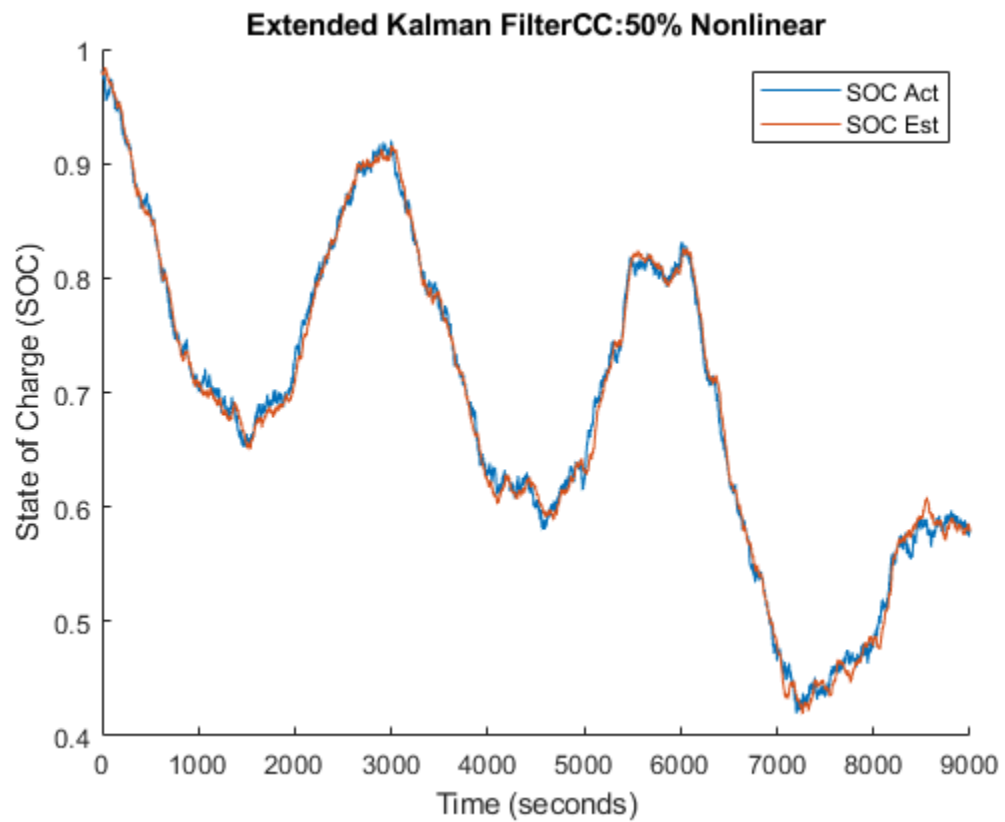
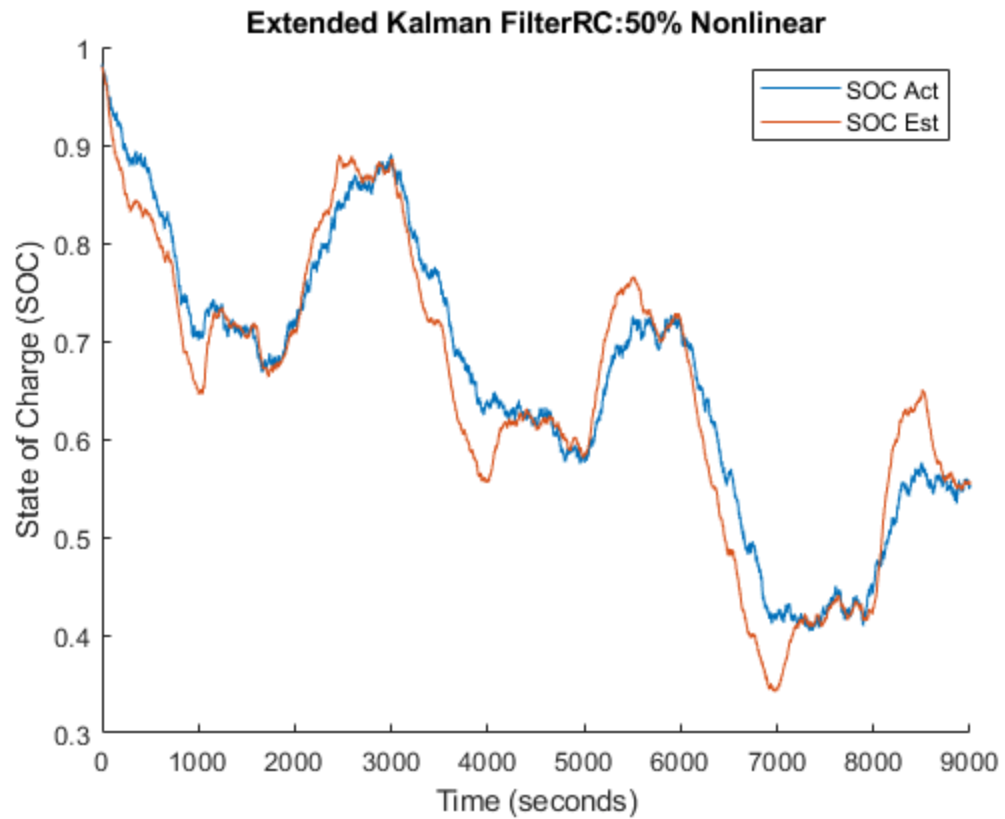


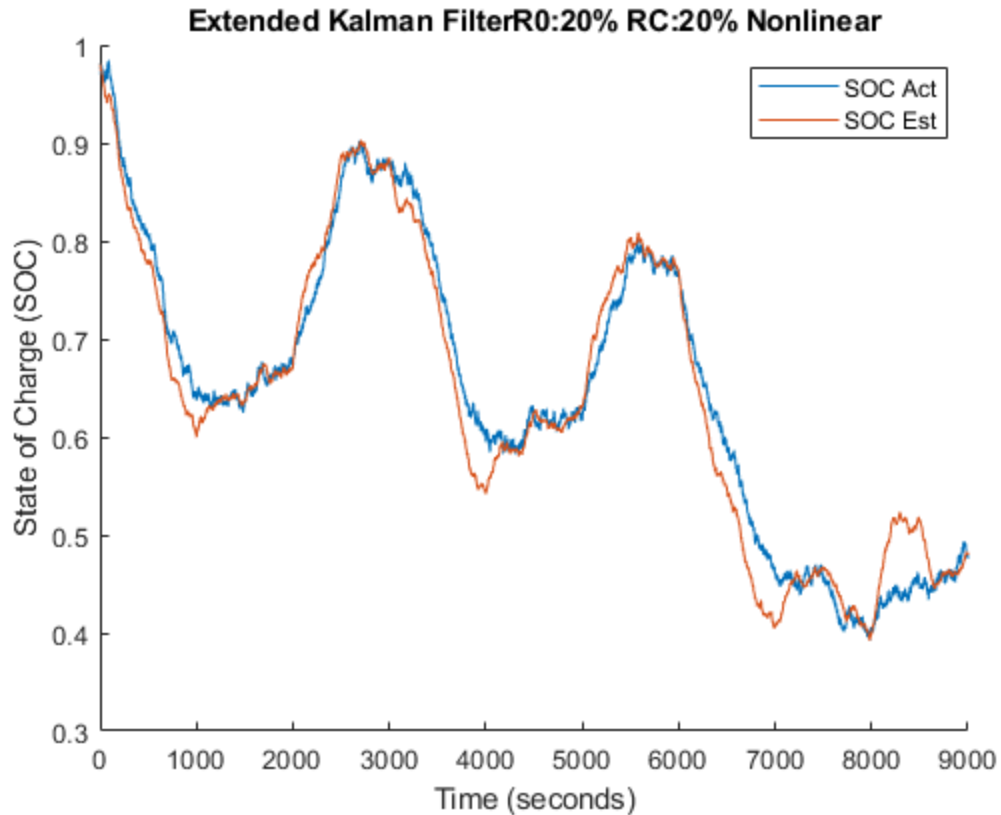












RMS Tabulation

```
NameList = [ "Linear Baseline", "R0:25% Linear", "RC:25%
Linear", "CC:25% Linear", "R0:50% Linear", "RC:50% Linear", "CC:50%
Linear", "R0:20% RC: 20%Linear", "Nonlinear Baseline ", "R0:25%
Nonlinear", "RC:25% Nonlinear", "CC:25% Nonlinear", "R0:50%
Nonlinear", "RC:50% Nonlinear", "CC:50% Nonlinear", "R0:20% RC:20%
Nonlinear" ];
```

```
for i = 1:length(List)
```

```
    Youla_act_rms(1,i) = rms(YOULA_ACTUAL(:,i));
    Youla_est_rms(1,i) = rms(YOULA_ESTIMATED(:,i));
```

```
    Kalman_act_rms(1,i) = rms(KALMAN_ACTUAL(:,i));
    Kalman_est_rms(1,i) = rms(KALMAN_ESTIMATED(:,i));
```

```
    EKF_act_rms(1,i) = rms(EXTENDED_KALMAN_ACTUAL(:,1));
    EKF_est_rms(1,i) = rms(EXTENDED_KALMAN_ESTIMATED(:,1));
end
```

```
table = [ " ", NameList;...
          "Youla Actual RMS", Youla_act_rms;...
```

```

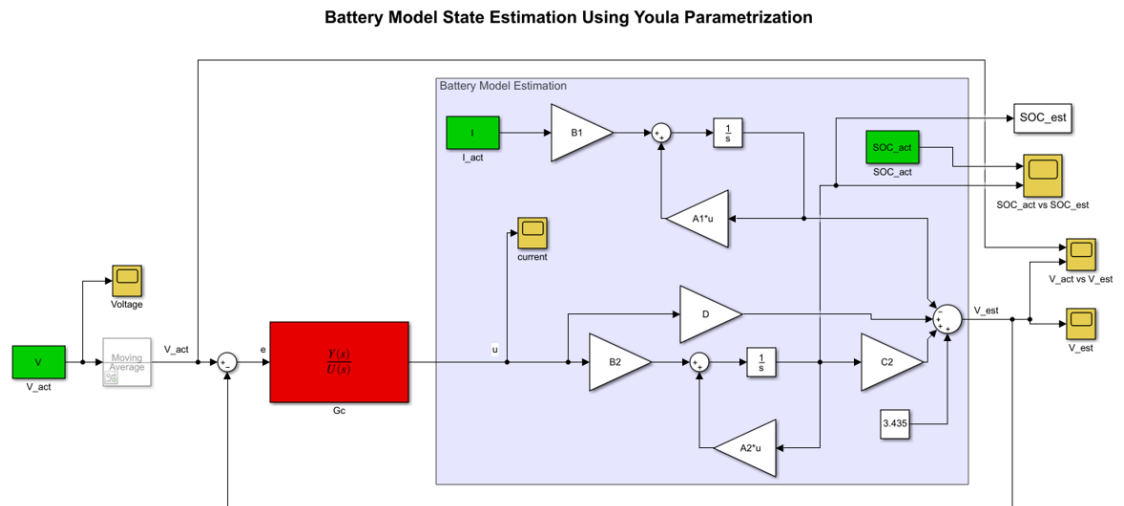
"Youla Estimated RMS", Youla_est_rms;...
"Youla RMS Error", (Youla_act_rms-Youla_est_rms);...

"Kalman Filter Actual RMS", Kalman_act_rms;...
"Kalman Filter Estimated RMS",Kalman_est_rms;...
"Kalman RMS Error", (Kalman_act_rms-Kalman_est_rms);...

"EKF Actual RMS", EKF_act_rms; ...
"EKF Estimated RMS", EKF_est_rms;...
"EKF RMS Error", (EKF_act_rms-EKF_est_rms)];

open_system('Estimator_Simulink_trial1')

```



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