

6. How many ways are there to select five unordered elements from a set with three elements when repetition is allowed?

There are $r=5$ slots and $n=3$ types to pick. The total number of ways is $C((5+2),5) = 21$

8. How many different ways are there to choose a dozen donuts from the 21 varieties at a donut shop?

There are $r=12$ slots and $n = 21$ types to choose. The total number of ways is then $C((12+20),12) = 25792840$. The same problem with out repition will have $C(21,12) = 293930$ ways.

12. How many different combinations of pennies, nickles, dimes, quarters, and half dollars can a piggy bank contain if it has 20 coins in it?

There are $r=20$ slots and $n=5$ types to pick. The total number of ways is then $C(24,20) = 10626$.

14. How many solutions are there to the equation

$x_1 + x_2 + x_3 + x_4 = 17$ where

x_1, x_2, x_3, x_4 are nonnegative integers? are nonnegative integers?

The number of slots is $r=17$ with $n=4$ types to choose. That makes the total $C(20,17) = 1140$