

Now it is your turn, you will want to write this down, with steps showing how you found the value so that we can give you lab credit:

i. 1111

$$8 + 4 + 2 + 1 = 15_{10}$$

ii. 1000

$$8 + 0 + 0 + 0 = 8_{10}$$

iii. 1000 1000 (a much bigger number, but remember to just keep doubling the place values as you move to the right)

$$128 + 8 = 136_{10}$$

iv. 11 1010 (while not all people or programs do this, notice how I have the bits in groups of four? This will be to help us with a shortcut when I get to hexadecimal)

$$32 + 16 + 8 + 0 + 2 + 0 = 58_{10}$$

g. Now it is your turn, be sure to write these down in a file along with the other values for this lab to get credit (please show your binary values grouped into groups of four, grouping them starting from the right, so 73 would be 100 1001, grouped starting from the right)

i. 127

$$\begin{array}{r} 127-64 \\ \hline 1 \\ 64 \end{array} \quad \begin{array}{r} 63-32 \\ \hline 1 \\ 32 \end{array} \quad \begin{array}{r} 31-16 \\ \hline 1 \\ 16 \end{array} \quad \begin{array}{r} 15-8 \\ \hline 1 \\ 8 \end{array} \quad \begin{array}{r} 7-4 \\ \hline 1 \\ 4 \end{array} \quad \begin{array}{r} 3-2 \\ \hline 1 \\ 2 \end{array} \quad \begin{array}{r} 1-1 \\ \hline 1 \\ 1 \end{array} = \boxed{1111111_2}$$

ii. 63

$$\begin{array}{r} 63-32 \\ \hline 1 \\ 32 \end{array} \quad \begin{array}{r} 31-16 \\ \hline 1 \\ 16 \end{array} \quad \begin{array}{r} 15-8 \\ \hline 1 \\ 8 \end{array} \quad \begin{array}{r} 7-4 \\ \hline 1 \\ 4 \end{array} \quad \begin{array}{r} 3-2 \\ \hline 1 \\ 2 \end{array} \quad \begin{array}{r} 1-1 \\ \hline 1 \\ 1 \end{array} = \boxed{11111_2}$$

iii. 15

(these first three should show you something about the relationship between the powers of two and the value one less than that)

$$\begin{array}{r} 15-8 \\ \hline 1 \\ 8 \end{array} \quad \begin{array}{r} 7-4 \\ \hline 1 \\ 4 \end{array} \quad \begin{array}{r} 3-2 \\ \hline 1 \\ 2 \end{array} \quad \begin{array}{r} 1-1 \\ \hline 1 \\ 1 \end{array} = \boxed{1111_2}$$

iv. 72 (this value should be somehow closely related to the 73 we did up above as an example)

$$\begin{array}{r} 72-64=8 \\ 1 \quad 0 \quad 0 \quad 1 \quad 0 \quad 0 \quad 0 \\ 64 \quad 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \end{array} \quad \begin{array}{r} 8-8=0 \\ 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \end{array} = \boxed{1001000_2}$$

v.

65 (this value should also be related to the example of 73 up above... what is it?)

$$\begin{array}{r}
 65-64 \\
 \begin{array}{ccccccc}
 1 & 0 & 0 & 0 & 0 & 0 & 1 \\
 64 & 32 & 16 & 8 & 4 & 2 & 1
 \end{array}
 \end{array}
 = \boxed{1000001_2}$$

$$73 - 65 = 8 = 1000_2 \text{ so.. } \begin{array}{r} 1000001 \\ + 1000 \\ \hline 1001001 = 73 \end{array}$$

Now it is your turn, convert the following into decimal assuming that they are hexadecimal to start with

i.
5

5

ii.
8

8

iii.
14

(the above are not trick questions, but should show you that small numbers are easy)

E

iv.
AA

$$10 \cdot 16 + 10 = 170$$

v.
CAD

$$12(256) + 10(16) + 13 = 3245$$

K. Now your turn

i. 53

$$53-32$$

$$\begin{array}{r}
 1 & 1 & 0 & 1 & 0 \\
 32 & 16 & 8 & 4 & 2
 \end{array}
 \begin{array}{r}
 110101_2 \\
 \begin{array}{cc}
 \parallel & \parallel \\
 3 & 5
 \end{array}
 \end{array}
 = \boxed{0x35}$$

ii. 187

$$187-128$$

$$59-32 \quad 27-16 \quad 11-8$$

$$\begin{array}{r}
 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 \\
 128 & 64 & 32 & 16 & 8 & 4 & 2 & 1
 \end{array}
 = \begin{array}{r}
 10111011 \\
 \parallel \quad \parallel
 \end{array} = \boxed{0xBB}$$

c.

Now without much more demonstration, how about you try it! Write the following in two's complement with 4-bit numbers

i.
3

$$\begin{array}{r} 0011 \\ 2+1 = 3 \end{array}$$

ii.
7

$$\begin{array}{r} 0111 \\ 4+2+1 = 7 \end{array}$$

iii.
-4

$$\begin{array}{r} 1100 \\ -4 \end{array}$$

d.

Now do something more than just using a table, show the work on some addition for lab credit

i.
3 + 4

$$\begin{array}{r} 0011 \\ + 0100 \\ \hline 0111 = 7 \end{array}$$

ii.
-2 + 2

$$\begin{array}{r} 11 \\ 1110 \\ + 0010 \\ \hline 0000 = 0 \end{array}$$

iii.
-2 + -6

$$\begin{array}{r} 11 \\ 1110 \\ 1010 \\ \hline 1000 = -8 \end{array}$$

iv.

3 + 5 (notice that this one does something strange... and to find out what it might be, try looking up a concept called overflow)

$$\begin{array}{r} 111 \\ 0011 \\ 0101 \\ \hline 1000 = -8, \text{ should be } 8 \text{ but overflows.} \end{array}$$