

CS 577: Final Project

Addernets - Reformulating CNNs without Multiplications

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Abstract

A discussion and implementation of AdderNet [1], an architecture that replicates the behavior of convolutional neural networks via matrix addition rather than multiplication.

Team Member Responsibilities

Code

- Jane: Adder Layer, Flatten Layer, Fully Connected Layer, Max Pool Layer, Model Class.
- Quin: Batch Norm Layer, Minibatch, Plots, Training
- Both: Collaborative debugging/testing/plotting

Paper/Presentation

- Jane: Proposed Solution, Results and Discussion
- Quin: Problem Statement, Implementation Details, Presentation

Problem statement

Multiplications in neural networks are computationally expensive and slow the training process. This makes it difficult to train deep and complex networks, particularly with CNNs, and prevents improvements in efficiency. Multiplication of tensors in neural networks makes it impractical not to train on GPU or TPU; these devices are not as ubiquitous as other chip architectures, are power intensive, and expensive. AdderNet [1] thus relieves the dependence on such devices and opens up opportunities for applications in edge devices.

Proposed Solution

AdderNet proposes several modifications to the traditional convolutional neural network.

1. Abandoning convolution in favor of addition-based operations. AdderNet proposes using $l1$ -distance as a similarity measure between windows and filters.

$$l1(a, y) = \sum_{i=1}^n |x_i - y_i| \quad \text{Eq. 1}$$

2. Update filters using full-precision gradients, which the paper's authors argue more frequently take the direction of steepest descent and are more suitable for networks with many parameters.

$$\frac{\partial Y(i, m, n, t)}{\partial F(i, j, k, t)} = X(m + i, n + j, k) - F(i, j, k, t) \quad \text{Eq. 2}$$

- Also use the full-precision gradient for network inputs, but clipped to range (-1,1) since it affects all prior layers via the chain rule.

$$\frac{\partial Y(i,m,n,t)}{\partial X(m+i,n+j,k)} = HT(F(i,j,k,t) - X(m+i,n+j,k)) \quad \text{Eq. 3}$$

Where

$$H(x) = \begin{cases} x & \text{if } -1 < x < 1 \\ 1 & \text{if } x \geq 1 \\ 0 & \text{otherwise} \end{cases} \quad \text{Eq. 4}$$

- The nature of the addition-based operations results in larger variance for layer outputs. AdderNet uses batch normalization to “promote more effective activations”. Batch-normalized output can be calculated by:

$$y = \frac{\gamma x - \mu_B}{\sigma_B} \beta \quad \text{Eq. 5}$$

where B denotes a batch and γ and β are learnable parameters.

- The larger variance mentioned above can yield smaller gradient norms. To counteract this, AdderNet introduces the concept of an additional, adaptive gradient rate for each network layer l , defined as:

$$\alpha_l = \frac{\eta \sqrt{k}}{\|\Delta L(F_l)\|_2} \quad \text{Eq. 6}$$

Where k is the number of elements in filter F_l , $\Delta L(F_l)$ is the change in loss with respect to filter F_l , and η is a hyper-parameter. The update rule for the filter is thus

$$\Delta F_l = \gamma \times \alpha_l \times \Delta L(F_l) \quad \text{Eq. 7}$$

Implementation Details

Our entire network implementation was done from scratch without the use of any deep learning libraries. NumPy was used for higher level numerical calculations that could be handled by Python and for speeding up computation. Similarly SciPy was used for additional functionality. The main functionality lies in model.py and layers.py where the model class and the layers classes were respectively defined. A data loader was defined in data.py and the rest of smaller functions fell under util.py.

Utils

We implemented a number of layer classes to form the backbone of our model.

- L1()** - returns the L1 distance between two points by taking the difference between its two inputs and returning the absolute value of that difference using `np.abs()`. See Eq 1.
- hard_tanh()** - hard tangent function is implemented using `np.clip()` and specifying the upper and lower bounds to clip at as 1 and -1 respectively. See Eq 4.
- eps()** - returns a small value (epsilon) from a uniform distribution with a lower bound of 1e-7 and an upper bound of 1e-6. This function is used repeatedly to allow use of natural logs, and division where zeros would make the operations undefined..
- cat_cross_entropy()** - computes the categorical cross entropy between the true one hot encoded label and a prediction. It does so by using numpy to compute the log of prediction array with an added epsilon, then multiplying the result with the ground truth array, and summing over the results and dividing to take the average value over all the examples in the batch.
- cat_cross_entropy_prime()** - computes the local gradient of the categorical cross entropy function with respect to its input. This is done by returning an array of the negative ratio between the ground truth and the prediction using list comprehension.

- `get_mini_batches()` - takes as its arguments, input data, target data, and the `batch_size` to split this data up into. The function operates through a loop that generates upper and lower indices used to split the input and target data and append them to a list of batches and is returned.

Data

A function `load_cifar_data` is written to aid in downloading, importing, and preprocessing CIFAR-10 data. It includes options to specify the folder the data is stored in, whether to download the data and store it to a folder, and whether to return the full dataset, or a smaller subset of the dataset. If the option is selected to download the dataset the `wget` package is used to download the `.tar` file, which is then unzipped and moved into a folder using the `tarfile` and `os` packages. The data is stored in multiple pickle files which are loaded and appended with functionality of the pickle package. The final option to return a smaller dataset works by slicing the data arrays and returning them, otherwise the full arrays are returned.

Layers

We implemented a number of layer classes to form the backbone of our model.

- `Layer()` – the parent class that defines the structure of more specific layers. All layers include forward and backward methods and store the inputs to the layer and the outputs of the layer. The forward takes as its arguments the input to the layer, and a boolean value: `init_weights` which is specified to only be true on the first forward pass through the network and tells the forward function to initialize weights for that layer.
- `adder_layer()` – takes number of output channels, kernel size, stride, padding, and η (see Eq. 6) as hyperparameters. Includes the following methods:
 - `__init__()` - initializes variable passed in the object declaration, additionally it initializes the filters and bias variables using `np.ones()` and `np.zeros()` respectively.
 - `get_adaptive_learning_rate()` - computes the adaptive learning rate according to Eq. 6
 - `forward()` - iterates over image tensor in ‘sliding-window’ fashion, computing the dot product between the filter and the input window and entering the result into the output tensor.
 - `backward()` - takes an upstream gradient and learning rate as input. Slides window across image tensor, computing the gradients with respect to the image, weights, and biases. Computes the gradient with respect to the weights and images according to Eq. 2 and Eq. 3, respectively. After iterating over the image tensor, `self.get_adaptive_learning_rate()` is called. Updates filters and biases with the below rule, and returns the gradient with respect to the input.

Update rules:

```
self.filters -= learning_rate*adaptive_lr*dfilters
self.bias    -= learning_rate*dbias
```

- `FullyConnected()` – standard ‘dense’ layer. Initialized with number of output channels.
 - `forward()` - Performs a single matrix multiplication (image tensor times weight tensor), adds bias, and returns result.
 - `backward()` - takes upstream gradient and learning rate as input. Calculates gradients with respect to X , W , and bias with the below formulas:

```
dX = np.dot(upstream_g, self.weights.T)
dW = np.dot(self.input.T, upstream_g)
```

```
dbias = np.mean(upstream_g)
```

And updates weights and bias with the following rules:

```
self.weights -= learning_rate*dW
self.bias    -= learning_rate*dbias
```

- Returns gradient with respect to X.
- Flatten() - while technically a layer, mainly serves to reshape X into an array-like output. Gradient and individual elements do not change with forward or backward pass.
- batch_norm_layer() - normalizes a four-dimensional 'batch' of images during training, with learnable scale and shift parameters.
 - forward() - computes mean and standard deviation of inputs and normalizes the data. Scales by 'gamma' and shifts by 'beta', which are instantiated to ones and zeros so as to not have any effect unless the model updates them in the backward pass.
 - backward() - takes upstream gradient and learning rate as input. Computes the gradients with respect to gamma, beta and inputs via the following equation:

```
for i in range(m):
    for j in range(m):
        dX[i] += (upstream_g[i] - upstream_g[j]*(1 +
(X[i]-X[j])*(X[j]-mean)/std))
dX *= self.gamma/((m**2)*std)
```

And updates the gradients:

```
self.gamma = self.gamma - learning_rate*dGamma
self.beta  = self.beta  - learning_rate*dBeta
```

Returns gradients with respect to the input.

- MaxPool() – takes max pool filter size and stride as hyperparameter inputs.
 - forward() - performs a sliding window search over image tensor and computes the maximum at each location. Populates a smaller tensor with these values and outputs the result. Keeps track of locations of maxima for use in backward pass.
 - backward() - outputs a gradient the shape of the original tensor which is 1 at the locations of the maxima, and 0 otherwise.
- Activation() -takes 'relu' and 'softmax' as options.
 - forward() - performs non-linear transformation on output of previous layer.
 - 'Relu':
 - Changes any negative elements to zero and outputs result.
 - 'Softmax':
 - Takes the output of a fully-connected layer, which has 10 output channels (one per class). Converts the 10 elements in each example into 'probabilities' via the following formula and outputs the result.
 - backward() - takes upstream gradient and learning rate as input, computes gradients with respect to input, and returns result
 - 'Relu':
 - Computes gradient by converting the positive values of the upstream gradient to 1, and the negatives to 0.
 - 'Softmax'

```
exp_ = np.exp(x - np.max(x))
return exp_ / (np.sum(exp_) + eps())
```

- Instantiates a matrix of zeros in the shape of `softmax(input)`. Sets each element `(i, j)` of the matrix equal to:

$$J[i][j] = s[i][j] * (\text{indicator_ij} - s[i][j])$$
- Where `indicator_ij` is equal to one if `i==j`, else 0.

Model

The model class allows for building of sequential models. It takes as it's input only the name of the name of the loss function to use with the model.

- `add()` - appends layer input to the `self.layers`.
- `predict()` - returns a prediction for the input passed to the function. It works by calling looping the layers in `self.layer` and calling forward on each of the layers, successively pushing the input through the network and finally it returns the result of the network.

```
Z = input_data
for layer in self.layers:
    Z = layer.forward(Z, init_weight=False)
```

- `fit()` - this function does the training on the model for the specified number of epochs, with minibatch. The function works through two main loops, the first of which iterates over the number of epochs it is training for, before the second loop starts `get_mini_batches` is called and the result stored so that the second loop can iterate over the batches in the dataset. Within the second loop the batch first pushed through the network in the same way a single example in `predict()` was. Then the loss on this batch is calculated and the backwards pass is started be executing:

```
error = -y/(np.argmax(y_pred,axis=1) + util.eps())
for layer in (self.layers)[::-1]:
    Error = layer.backward(error, learning_rate)
```

Once the forwards and backwards pass is completed for every batch then the accuracy is computed and the loss and the accuracy are appended to the history variable and the validation loss and accuracy is computed in the same way and printed out. Once all the epochs are complete the function returns the history.

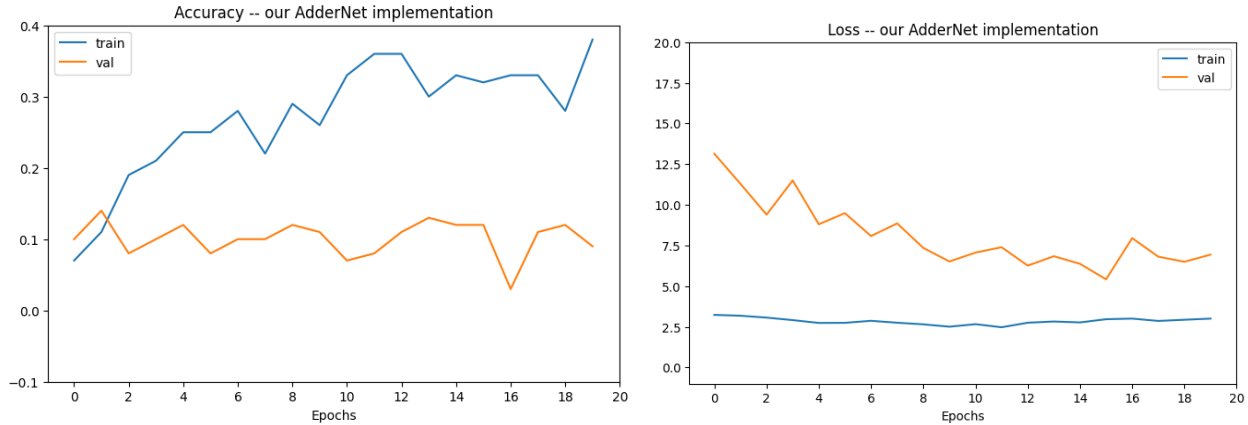
Results and Discussion

Part I. Our Implementation

The most straightforward way to assess the performance of our implementation is to train the model on image data and plot the resulting accuracy and loss. This proved to be a difficult task, first, because of the computational expenditure required by the sliding window addition – in our implementation, this involved a nested loop that traversed every dimension of the input. As we mention below, the problem with speed was not unique to our implementation, and we faced these issues with the original AdderNet as well. As a result, we often trained with a small dataset to monitor performance progress. Below is the result of one such training loop.

Training set: 100 images

Validation set: 100 images
Epochs: 20
Batch size: 16
Learning rate: 1e-05



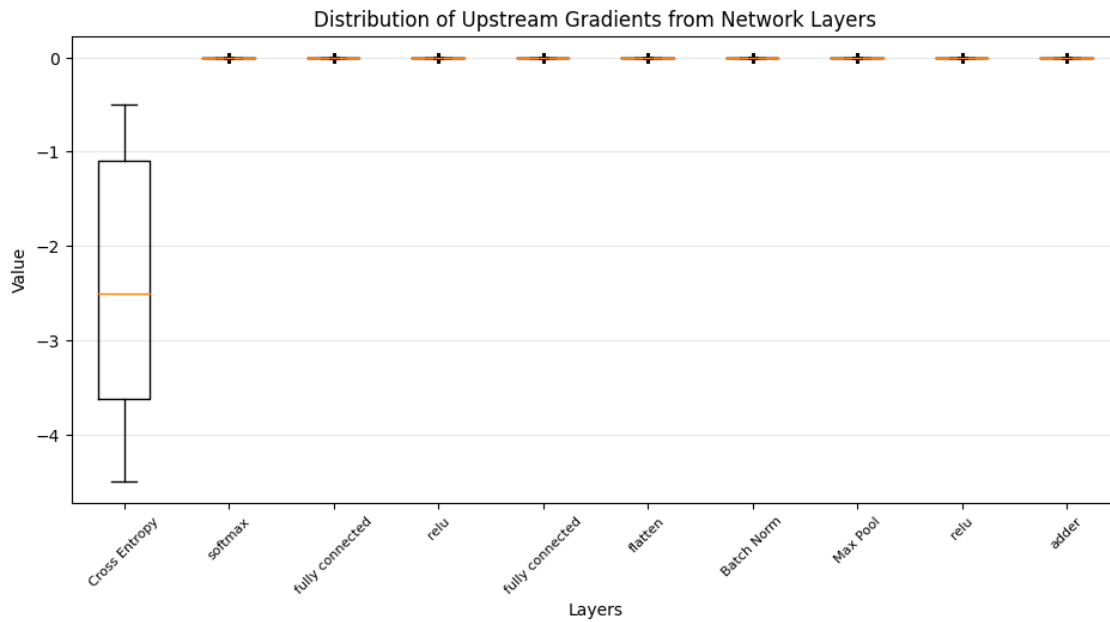
Test loss: 12.814556466007623

After a lot of troubleshooting, we were able to get our model to learn – albeit slowly. There were a number of issues that we encountered that required correction prior to this. A few mistakes that we found, and corrected:

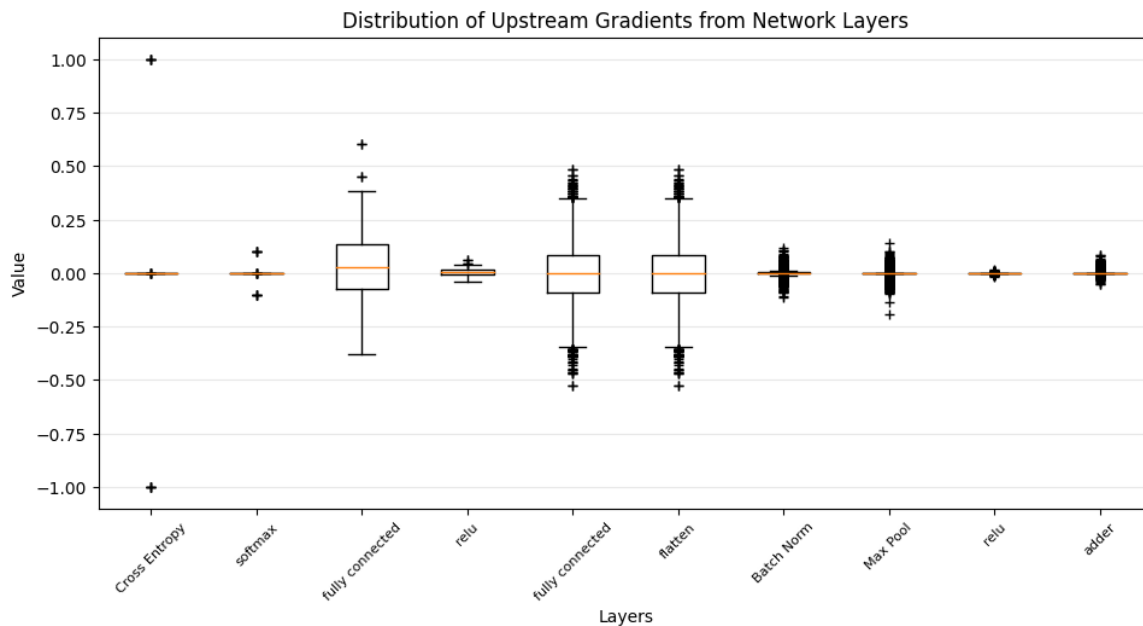
- The equations for gradients with respect to weights and inputs (Eq. 2 and Eq. 3) were reversed – this was corrected
- Weights were re-initialized within each forward pass – corrected
- `np.log()` and division operations were being called on 0 – corrected by adding small value, `eps()` (discussed above)
- Softmax function was unstable – corrected by including the `np.max()` term below:
$$\frac{\exp(x - \max(x))}{\sum(\exp_) + \text{eps}()}$$
- Local gradients in the softmax backward function included an extra subtraction that reduced gradients to zero – corrected.

While troubleshooting our code, we found the gradients to be a helpful tool for diagnosing problems.

Below are the gradients prior to achieving a working model.

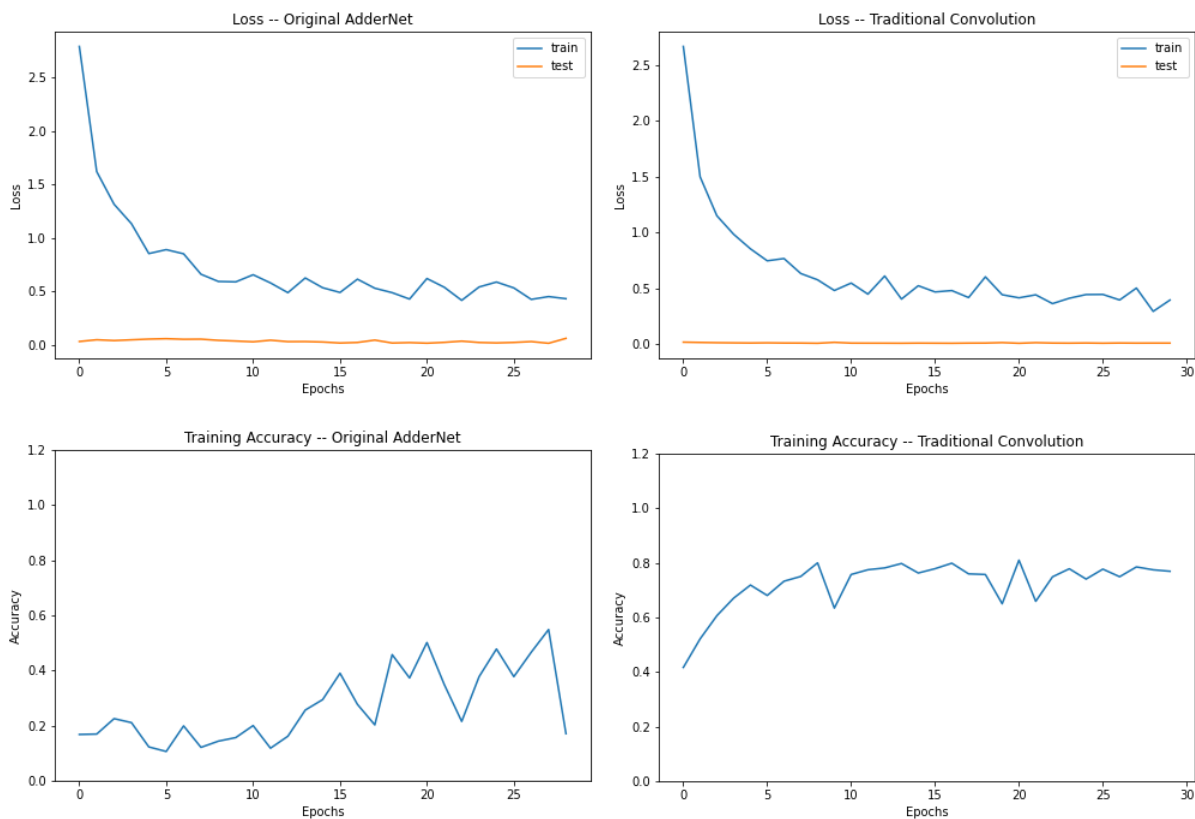


Alternatively, here are the results once the model began to work.



Part II. Original Addernet

A purported benefit of AdderNet is its alleged speed over regular convolution. The Addernet repository includes a model with its own “adder2d” layers, which replace convolution. By substituting these layers for `tf.keras.Conv2D` layers, we can easily compare performance against a traditional, convolution-based model. Below are the results:



After 30 epochs:

Original AdderNet:

Train Loss: 0.514889 Accuracy: 0.378600 Test Loss: 0.041237 time spent: 64 minutes and 2 seconds

Replacing 'adder' layers with traditional convolution:

Train Loss: 0.392941 Accuracy: 0.768900 Test Loss: 0.007318
time spent: 3 minutes and 55 seconds

We were surprised to find that, despite the reported benefits of AdderNet, we did not find improvement in speed or accuracy. In fact, a traditional convolution-based network trained over 10 times as fast, and with far superior accuracy. We expected accuracy to suffer slightly, which is acknowledged in the paper, but had the assumption that it would be made up for with time and efficiency. Unfortunately this was not the case.

Future Improvements

Given more time, we would like to troubleshoot any issues that are slowing down the learning in our model. We would also like to test against our own implementation of a convolution-based network, by substituting the adder layers in our network, as we did with the network from the original AdderNet repository. We would also like to test the runtime of various functions within the original AdderNet code to find the source of the slowdown.

References

[1] Hanting Chen, Yunhe Wang, Chunjing Xu, Boxin Shi, Chao Xu, Qi Tian, and Chang Xu. Addernet:

Do we really need multiplications in deep learning? CVPR, 2020.

https://openaccess.thecvf.com/content_CVPR_2020/papers/Chen_AdderNet_Do_We_Really_Need_Multiplications_in_Deep_Learning_CVPR_2020_paper.pdf

[2] Alex Krizhevsky, Vinod Nair, and Georey Hinton. Cifar-10 (Canadian Institute for Advanced Research). <https://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz>