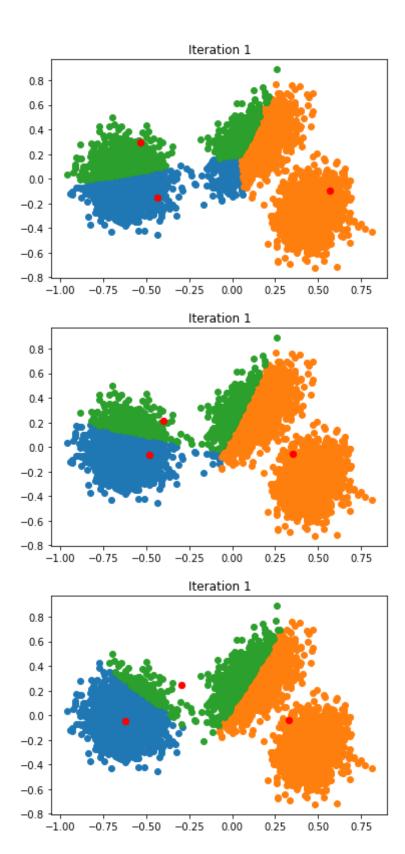
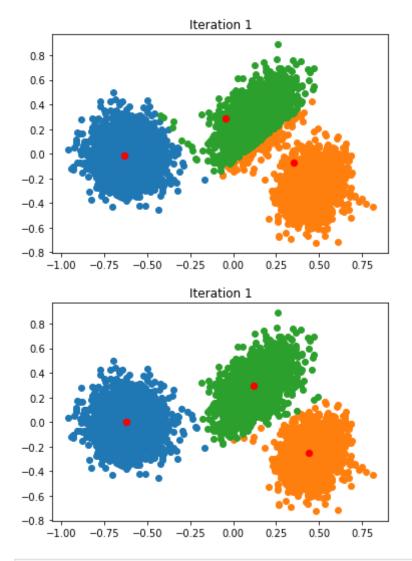
Question '4' (final question)

```
In [343...
          import pandas as pd
          import csv
          import matplotlib.pyplot as plt
          import random
          import numpy as np
          import itertools
In [296...
          with open("X.dat", "r") as f:
              lines = f.readlines()
          Xs, Ys = [], []
          for 1 in lines:
              l = l.split()
              Xs.append(float(1[0]))
              Ys.append(float(l[1]))
          with open("X.dat", "r") as f2:
              12 = f2.readlines()
          data = pd.DataFrame({'X': Xs, 'Y': Ys})
In [516...
          def distance(element_1,element_2):
              x1,y1,x2,y2 = element 1[0],element 1[1],element 2[0],element 2[1]
              d = np.sqrt((x1-x2)**2 + (y1-y2)**2)
              return d
          def denom(a,b):
              d = 0.001 if max(a,b) == 0 else max(a,b)
              return d
          def percent_change(element_1,element_2):
              x1,y1,x2,y2 = element 1[0], element 1[1], element 2[0], element 2[1]
              change_x = np.abs((x1-x2)/(denom(x1,x2)))
              change y = np.abs((y1-y2)/(denom(y1,y2)))
              return (change_x+change_y)/2
          def best centroid index(element, centroids):
              dist dict = {}
              for i in range(len(centroids)):
                  d = distance(centroids[i],element)
                  dist dict[d] = i
              min d = min(dist dict.keys())
              min index = list(dist dict.keys()).index(min d)
              return min index
          def assign(X,centroids):
              clusters = dict(zip(range(len(centroids)), [[] for c in centroids] ))
              for element in X:
                  best i = best centroid index(element,centroids)
                  clusters[best_i].append(element.tolist())
```

```
new centroids = []
    for cluster in list(clusters.values()):
        xs,ys = [c[0] for c in cluster], [c[1] for c in cluster]
        x_new,y_new = np.average(xs),np.average(ys)
        new_centroids.append([x_new,y_new])
    change = 0
    for (c1,c2) in list(zip(centroids, new centroids)):
        change += percent_change(c1,c2)
    return clusters, new_centroids, change
def show_clusters(clusters,centroids,iteration):
    for c in clusters.items():
        c_ = [[item[0] for item in list(c[1])],[item[1] for item in list(c[1])]]
        plt.scatter(x=c_[0],y=c_[1])
        plt.title('Iteration {}'.format(iteration))
    for c in centroids:
        plt.scatter(x=c[0],y=c[1],color='red',s=40)
   plt.show()
def k means(X,k):
    good_count = 0
    centroids = None
   while good_count < 3:</pre>
        good count = 0
        indices = random.choices(population=range(len(X)), k=k)
        if len(set(indices)) == len(indices):
            candidates = X[indices]
            paired_candidates = itertools.combinations(candidates,2)
            for p in paired candidates:
                if distance(p[0],p[1]) > 0.1:
                    good count += 1
   centroids = X[indices].tolist()
   plt.scatter([c[0] for c in centroids],[c[1] for c in centroids],color='red',
   change = 1
    iteration = 0
   while change > 0.4:
        clusters = dict(zip(range(len(centroids)),[[c] for c in centroids]))
        clusters, centroids new, change = assign(X,centroids)
        show clusters(clusters,centroids,1)
        centroids = centroids new
   return clusters, centroids
```

```
In [517... clusters3, centroids3 = k_means(X,3)
```





In [518... clusters4, centroids4 = k_means(X,4)

