#### WSABI Summer Research Lab

**Summer 2025** 

Lab 9: The Bootstrap

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## 9.1 Skittles Demo

You have an Skittles bag with n total Skittles and r red ones. Suppose the color of each Skittle is drawn independently from some distribution.

### 9.1.1 Your Task

- Construct a 95% Wald and Agresti-Coull confidence interval for the true probability Mars, Inc. makes a Skittle red.
- 2. Use the bootstrap to construct a 95% confidence interval. Compare the width of the bootstrap interval to the Wald and Agresti-Coull intervals. What does this tell you about the relative coverage of the three intervals?

# 9.2 NBA Free Throws

Yesterday, you constructed 95% confidence intervals for the true free throw percentage of NBA players. You also performed a simulation study to see how well the Wald and Agresti-Coull intervals performed. Now, you will use the bootstrap to do the same.

### 9.2.1 Your Task

- 1. Use the bootstrap to construct a 95% confidence interval for the true free throw percentage of NBA players.
- 2. Overlay the bootstrap confidence interval on the plot you made in Task 8.2.1. Rank the three intervals in terms of width.
- 3. Use the bootstrap to construct a 95% confidence interval for the simulation study you performed in Task 8.2.2.
- 4. Add a plot of the coverage probability for the bootstrap confidence interval. How does it compare to the Wald and Agresti-Coull intervals?

We will be working with the bootstrap more in the Machine Learning unit.