# My title

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#### 1 Introduction

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### 2 Methods

#### 2.1 The Model

Let  $s_i \in \mathbb{R}^2$  for each i = 1, ..., n denote a spatial location for which we have collected data, and  $\mathbf{s} = (s_1, ..., s_n)^{\top}$  be the vector of all such locations. Then  $Y(\mathbf{s})$  are univariate dependent variables and  $\mathbf{X}(\mathbf{s}) = (X_1(\mathbf{s}), ..., X_p(\mathbf{s}))^{\top}$  are  $p \times 1$  vectors of covariates. A linear regression model with spatially varying coefficients assumes  $Y(\mathbf{s})$  are dependent on  $\mathbf{X}(\mathbf{s})$  as follows:

$$Y(s) = \sum_{j=1}^{p} X_r(s) w_r(s) + w_0(s) + \epsilon(s),$$

where  $w_r(s)$  are the regression coefficients corresponding to  $X_r(s)$ ,  $w_0(s)$  are spatial random effects, and  $\epsilon(s)$  are independently and identically distributed multivariate normal (MVN) measurement errors, i.e.

$$\epsilon(s) \sim \text{MVN}(0, \tau^2 I_n).$$

For convenience, we will treat  $w_0(s)$  as the regression coefficients corresponding to  $X_0(s) = \mathbf{1}_n$ , a vector of length n with every element equal to 1.

For each  $w_r(s)$ , we assign a Gaussian process (GP) prior with squared exponential covariance, i.e.

$$w_r \sim GP(0, C(s, s'))$$
, where

$$C(s, s') = \sigma_r^2 \exp \phi_r^{-1} ||s - s'||^2.$$

We refer to  $C(\cdot, \cdot)$  as the covariance function, which calculates the covariance between two locations s and s'. Squared exponential covariance is a commonly used covariance function due to useful properties such as infinite smoothness and gradual decrease in covariance with distance. The parameter  $\sigma_r^2$  is the spatial variance and  $\phi_r$  is the spatial decay, which indicates how quickly correlation decreases with the squared distance.

We assign inverse-gamma conjugate priors for the variance parameters  $\tau^2$  and each  $\sigma_r^2$ . In addition, each  $phi_r$  is assigned a uniform prior. In summary,

$$au^2 \sim \text{Inv.Gamma}(\alpha_\tau, \beta_\tau),$$

$$\sigma_r^2 \sim \text{Inv.Gamma}(\alpha_r, \beta_r), \text{ and}$$

$$\phi_r \sim \text{Uniform}(l_r, u_r).$$

## 3 Conclusion

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