

# On the Topic of Jets

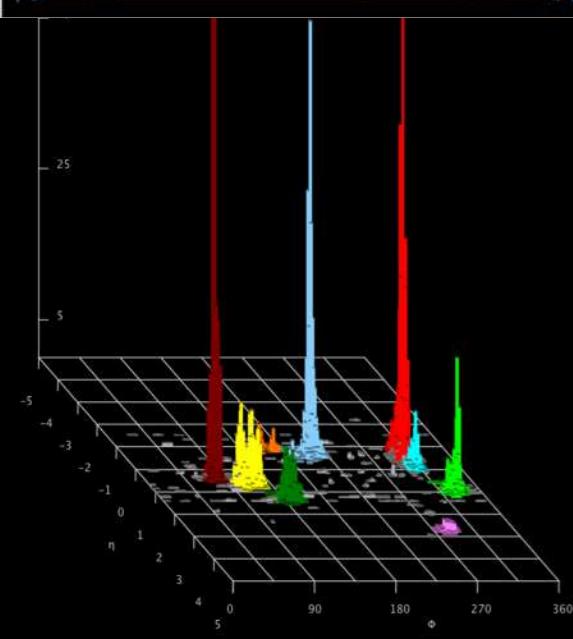
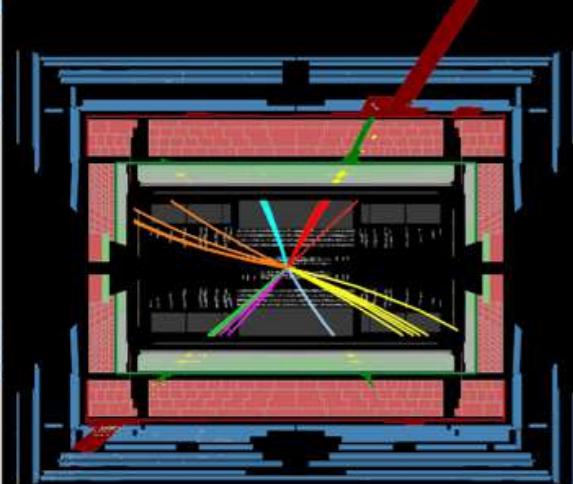
Jesse Thaler



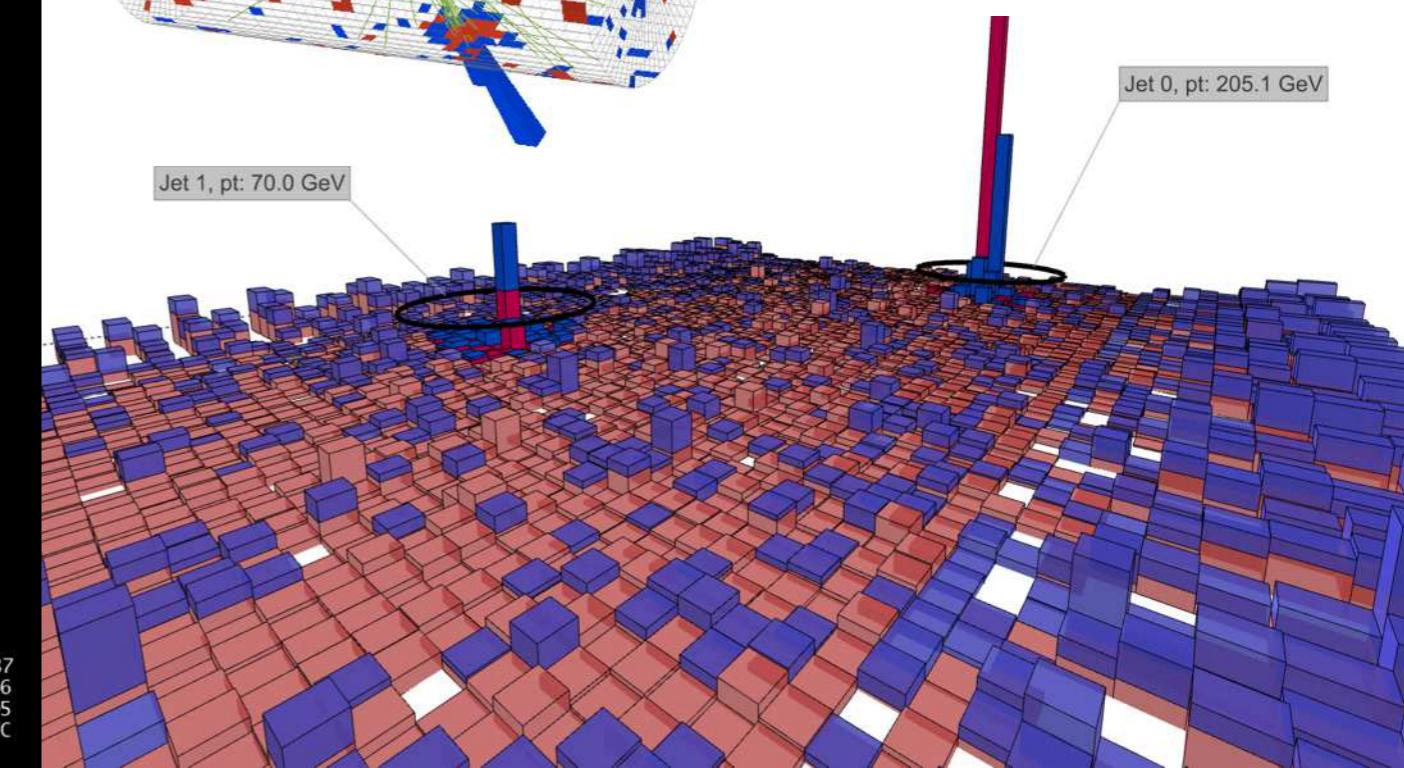
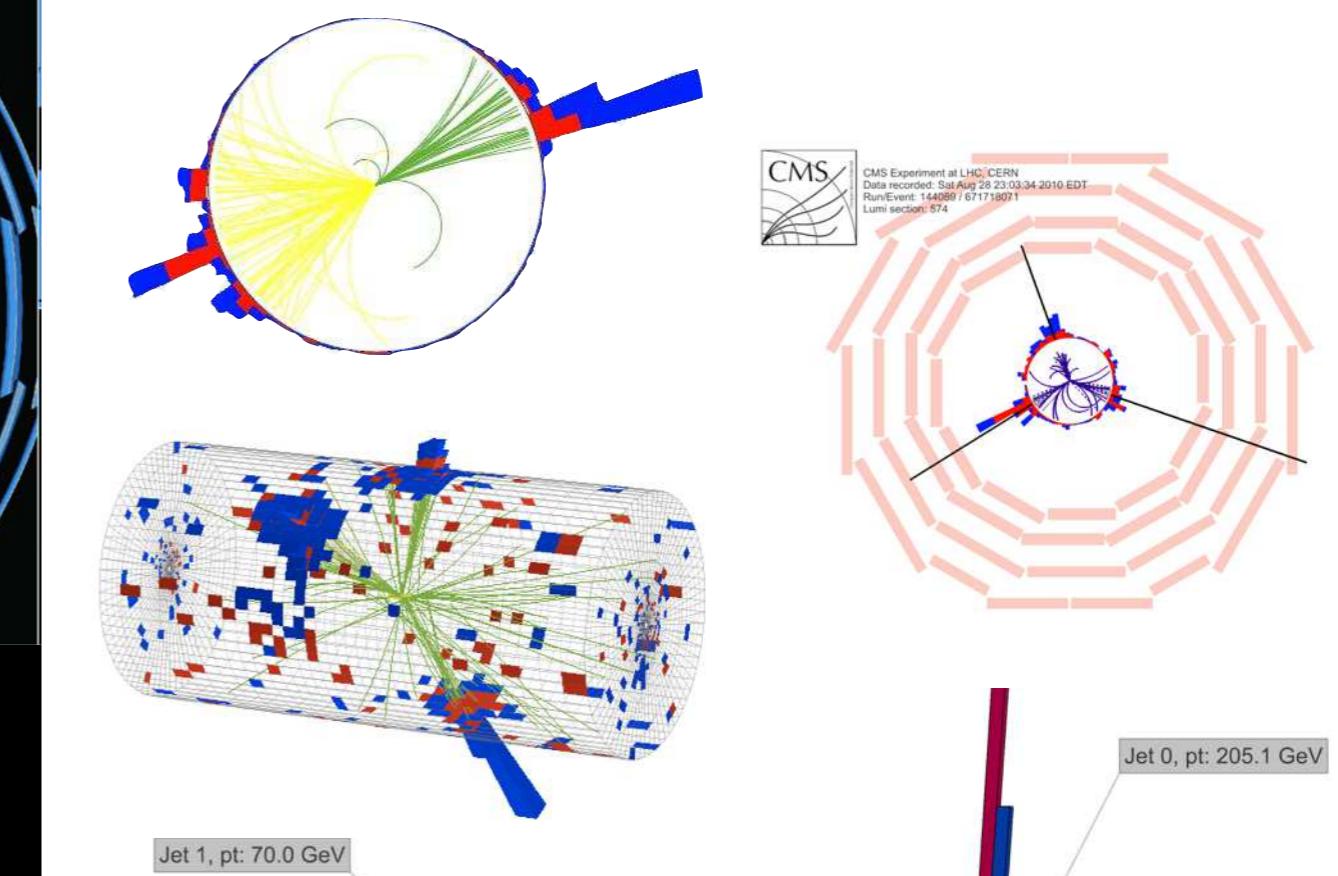
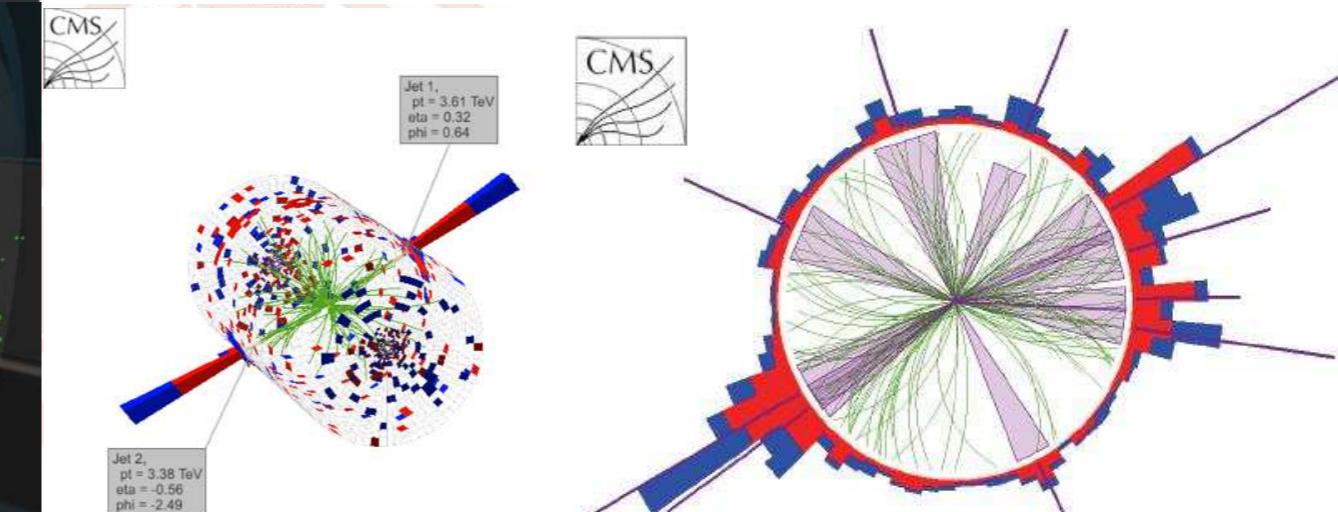
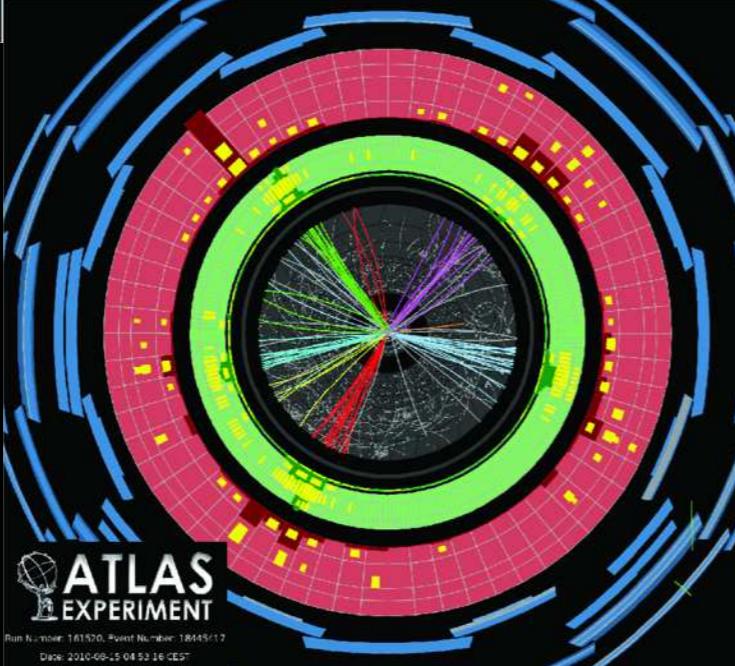
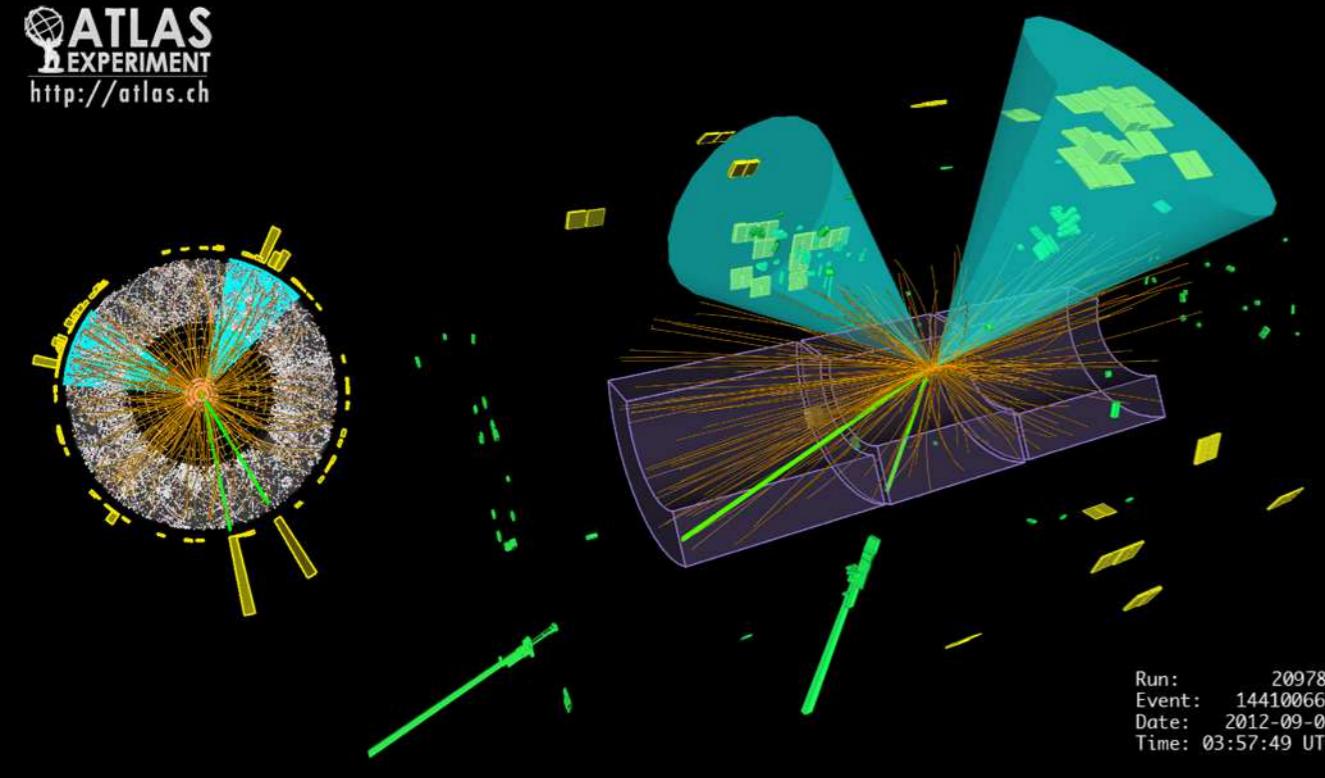
Self-Invited Seminar, DAMTP Cambridge — May 1, 2018

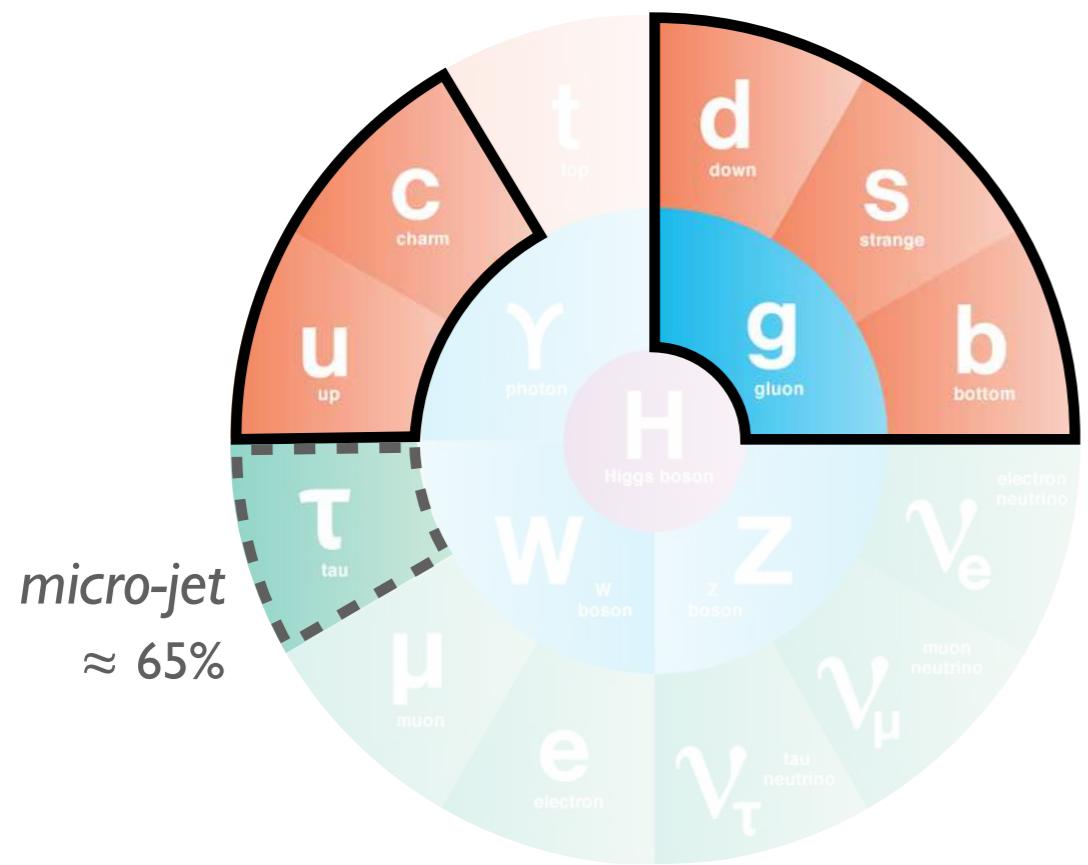
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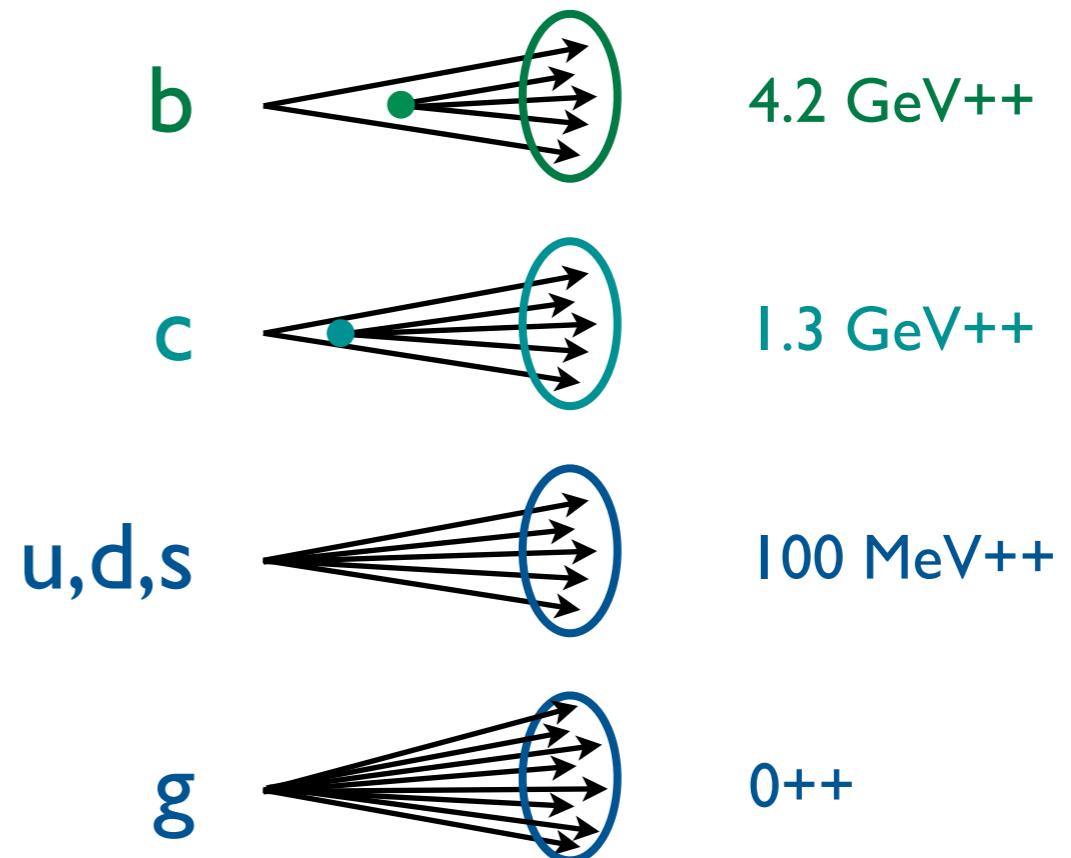
**ATLAS**  
EXPERIMENT  
<http://atlas.ch>

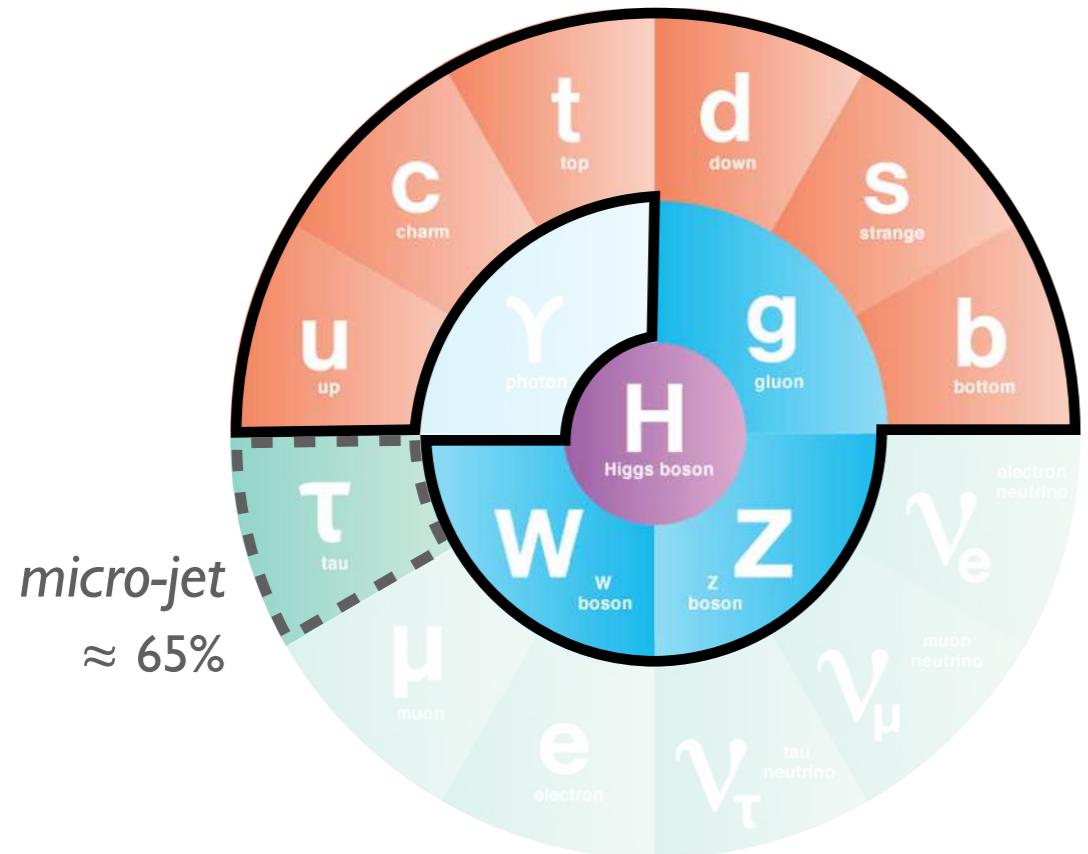




## *Jets from the Standard Model*

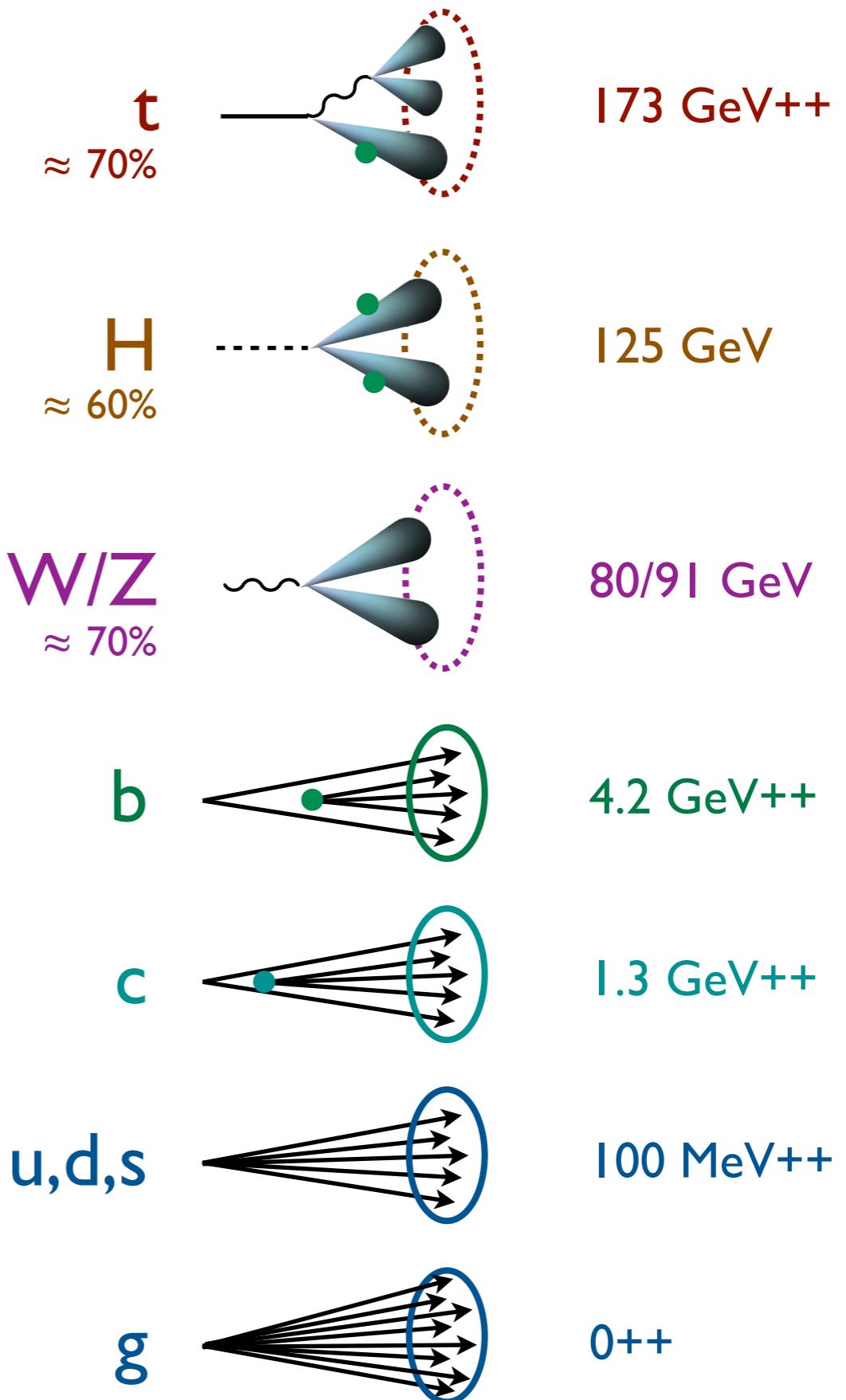
$\text{++}$  = Mass from QCD Radiation

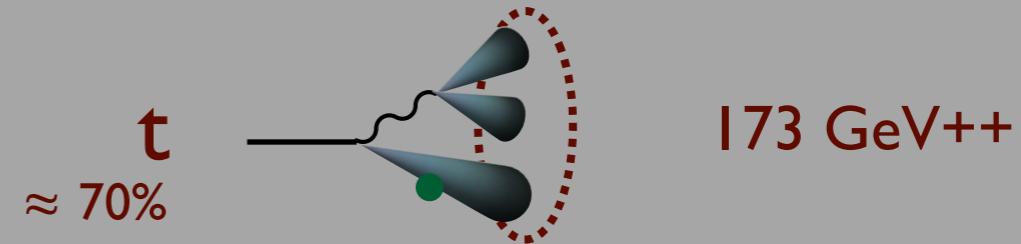




## *Jets from the Standard Model*

$\text{++}$  = Mass from QCD Radiation



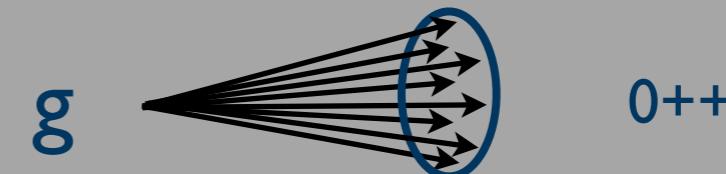


# Bottom Line: Jet Classification is “Solved”

*Trustable training samples?*  
*Well-defined categories?*  
*Controlled systematics?*

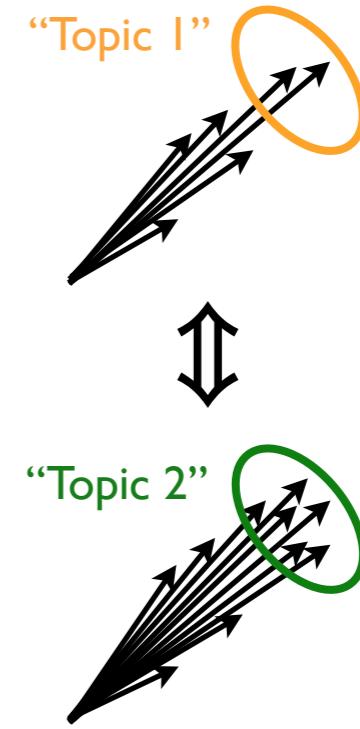
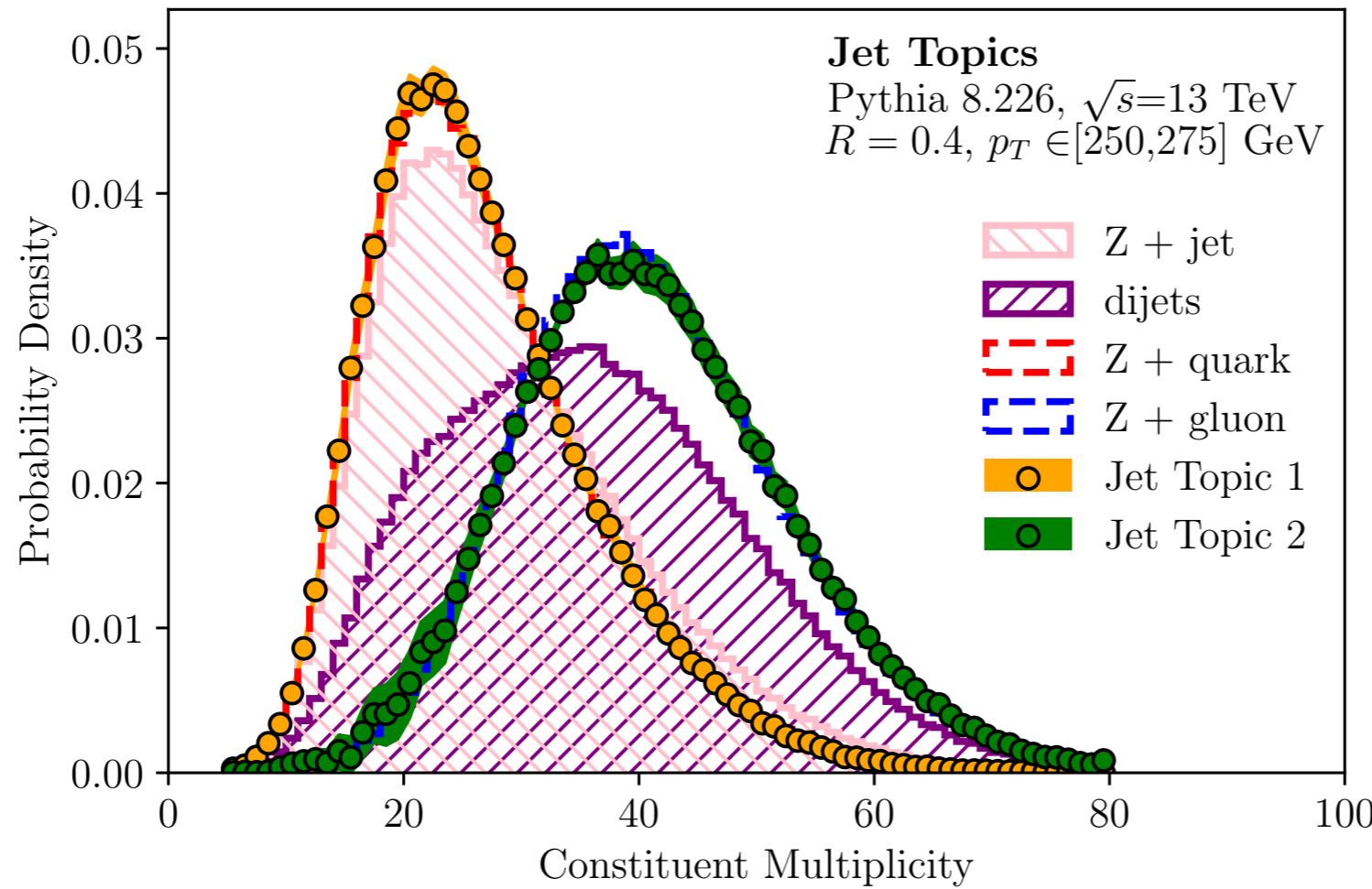
micro-jets  
 $\approx 65^\circ$

$++$  = Mass from QCD Radiation



# Jet Topics

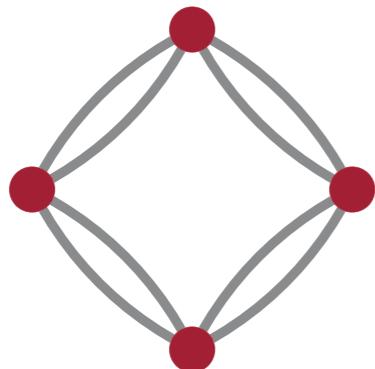
Extract jet categories from data...



...solely\* from the assumption they exist

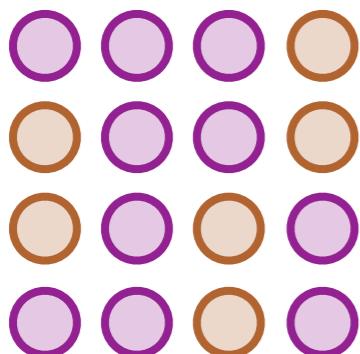
[Metodiev, JDT, 1802.00008]

# Outline



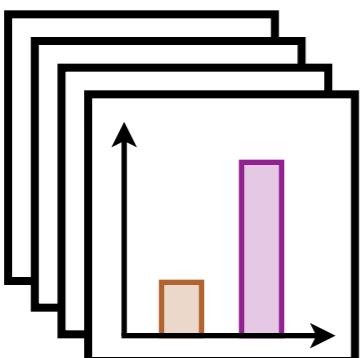
## A Basis for Jet Substructure

*“Solving” the problem of jet classification*



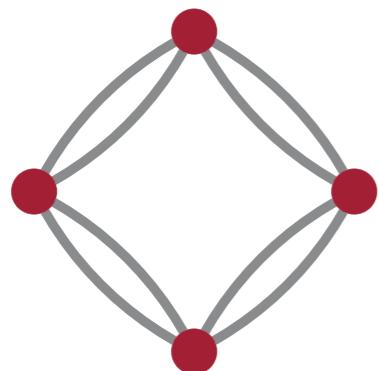
## Learning Without Labels

*Trustable training samples from data*

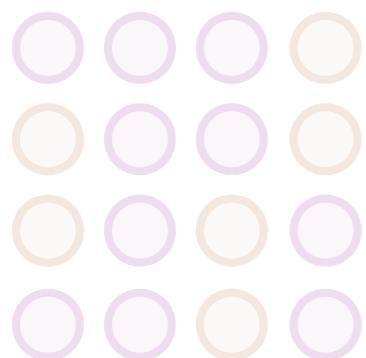


## Introducing Jet Topics

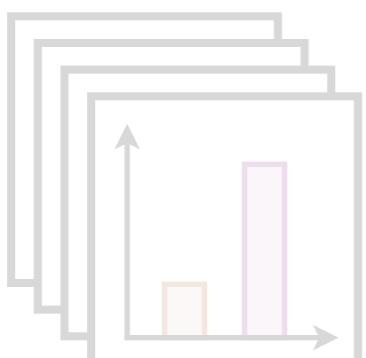
*Well-defined categories by construction*



## A Basis for Jet Substructure



Learning Without Labels

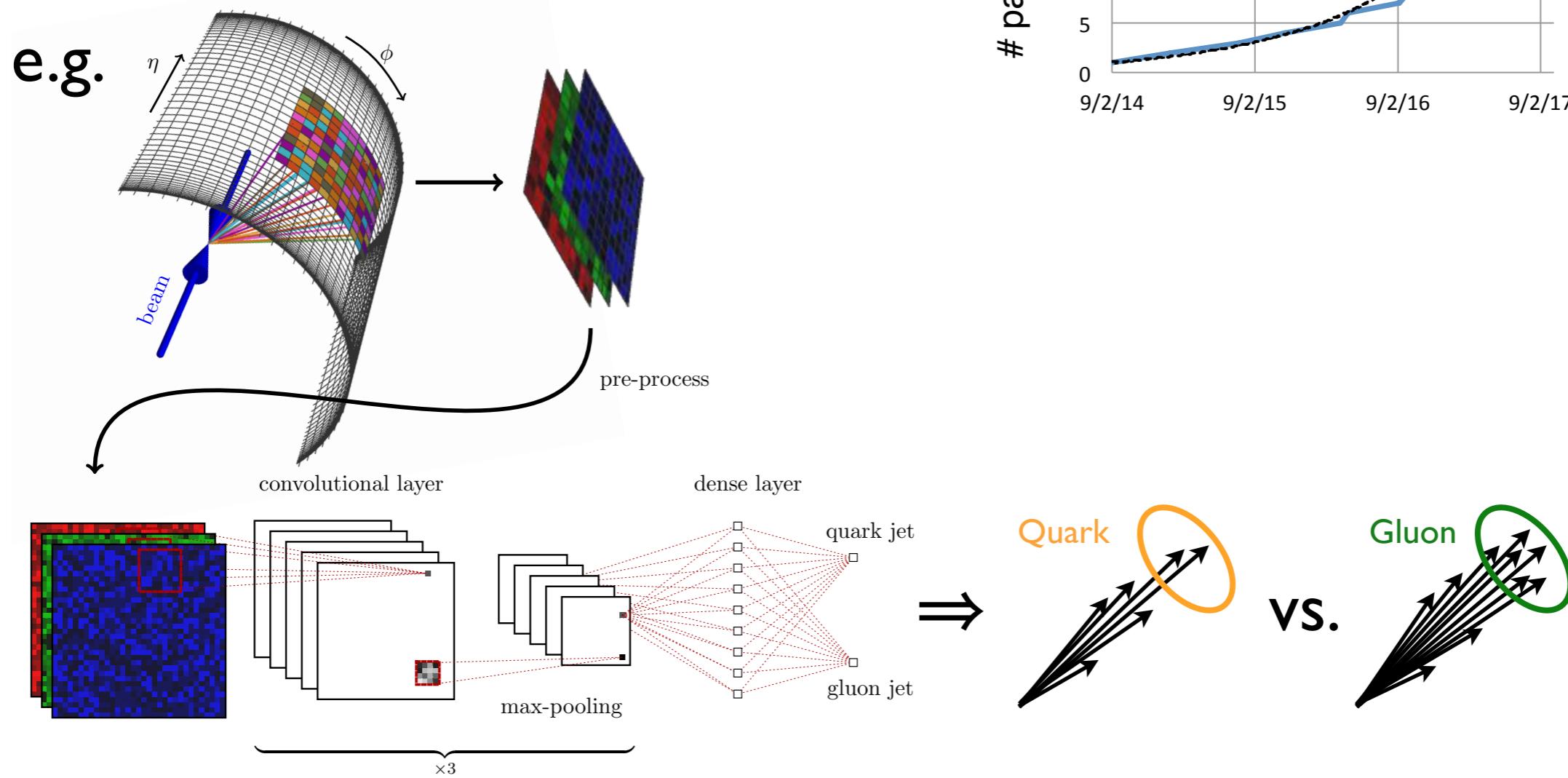


Introducing Jet Topics

# 10 Years of Jet Substructure!



# The Rise of Machine Learning for Jets



[e.g. Komiske, Metodiev, Schwartz, 2016; Nachman, Machine Learning for Jets Workshop, 2017]

“Deep Learning”

&

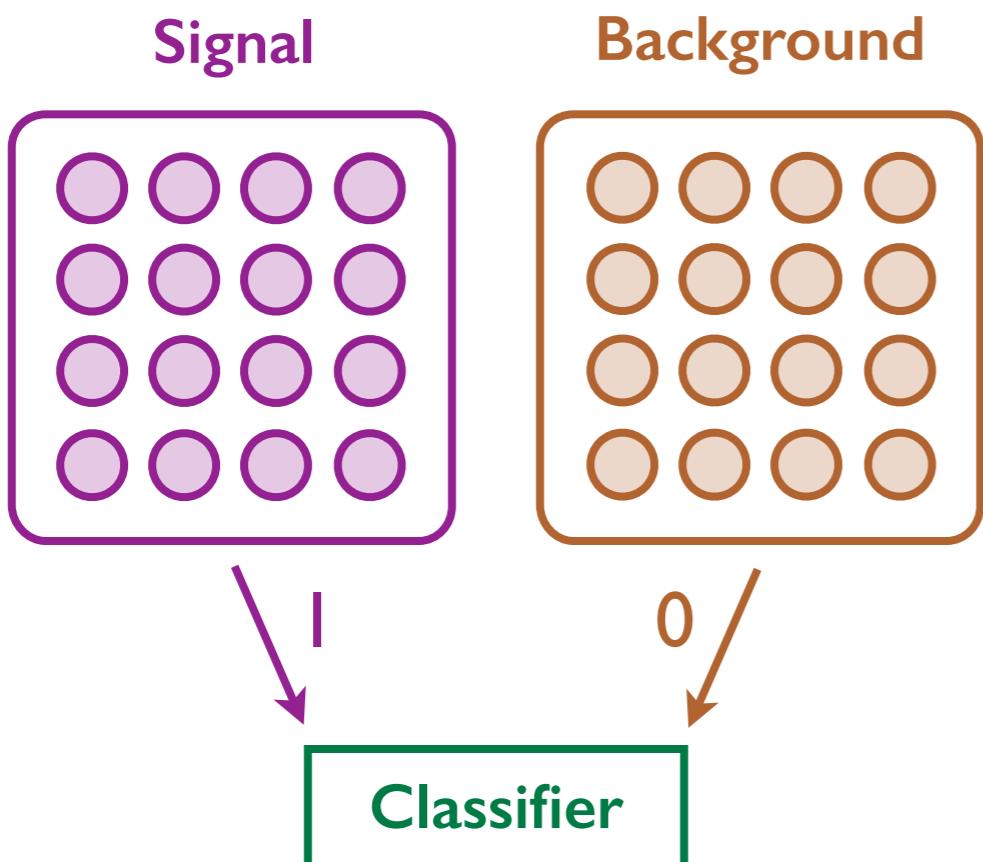
~~vs.~~

“Deep Thinking”

# A Cartoon of Machine Learning

$$\ell_{\text{MSE}} = \left\langle (\mathbf{h}(\vec{x}) - 1)^2 \right\rangle_{\text{signal}} + \left\langle (\mathbf{h}(\vec{x}) - 0)^2 \right\rangle_{\text{background}}$$

↑  
Set of observables



**Minimize Loss Function**

(assuming infinite training sets)

$$\mathbf{h}(\vec{x}) = \frac{p_{\text{sig}}(\vec{x})}{p_{\text{sig}}(\vec{x}) + p_{\text{bkgd}}(\vec{x})}$$

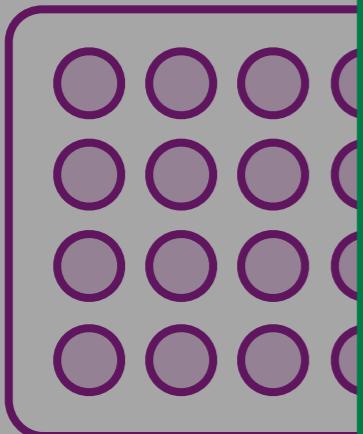
Optimal Classifier (Neyman–Pearson)

# A Cartoon of Machine Learning

$$\ell_{\text{MSE}} =$$

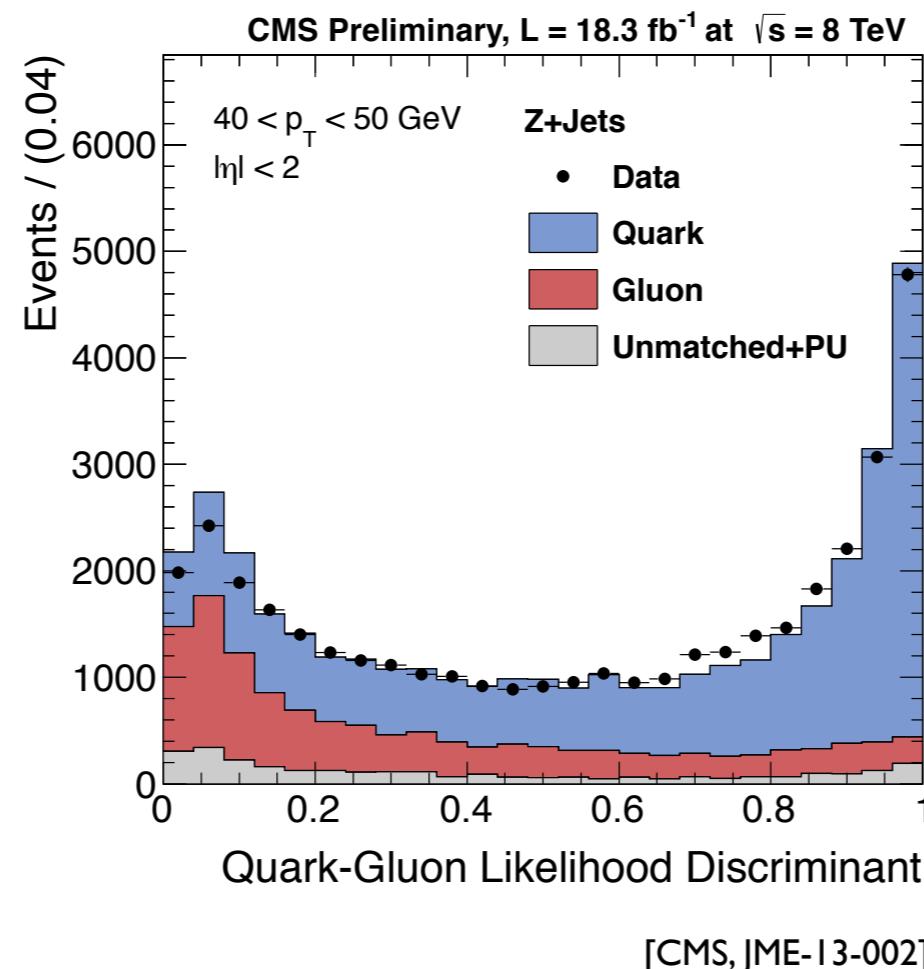
$$S =$$

Signal



## CMS Quark/Gluon Classifier

Three Observables ( $n_{\text{had}}$ ,  $p_T^D$ ,  $\sigma_2$ )



background

function

(training sets)

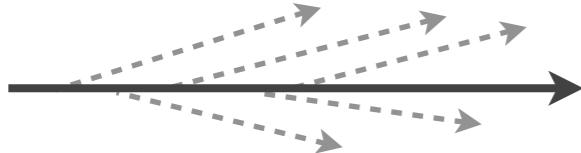
$$f(\vec{x})$$

$$p_{\text{bkgd}}(\vec{x})$$

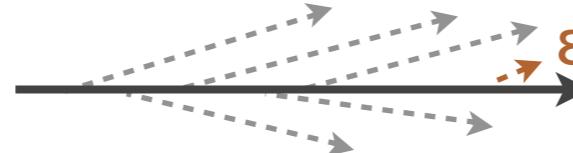
(chi-Pearson)

# A Cartoon of Infrared/Collinear Safety

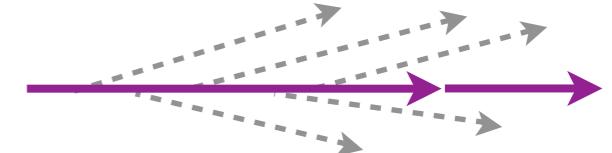
Original Jet



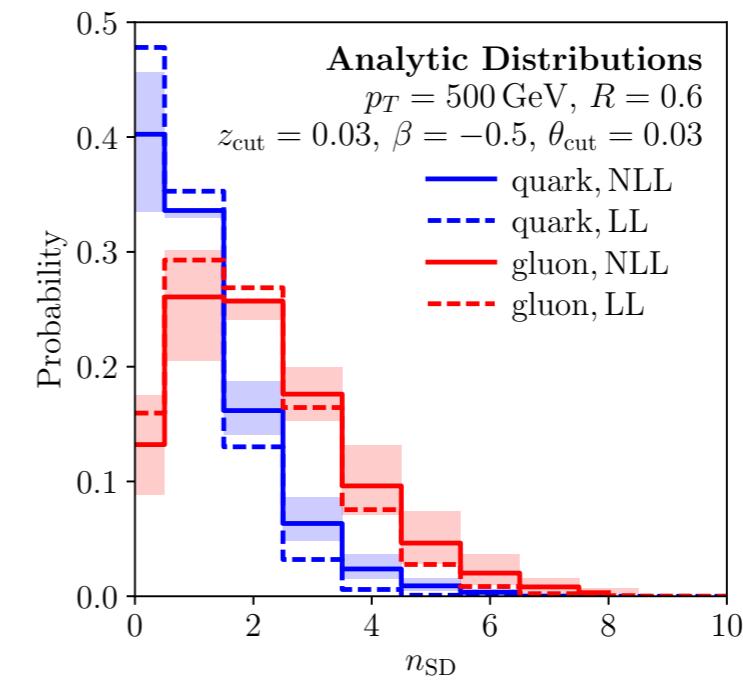
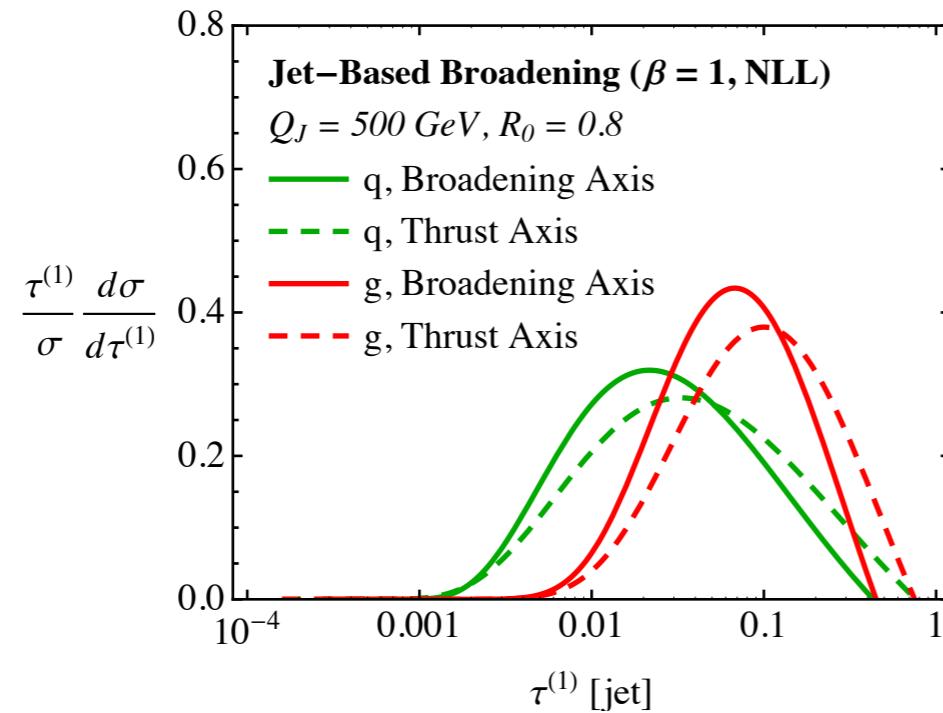
Infrared



Collinear



IRC Safe Observable: Insensitive to IR or C emissions



[e.g. Larkoski, Neill, JDT, 1401.2158; Frye, Larkoski, JDT, Zhou, 1704.06266]

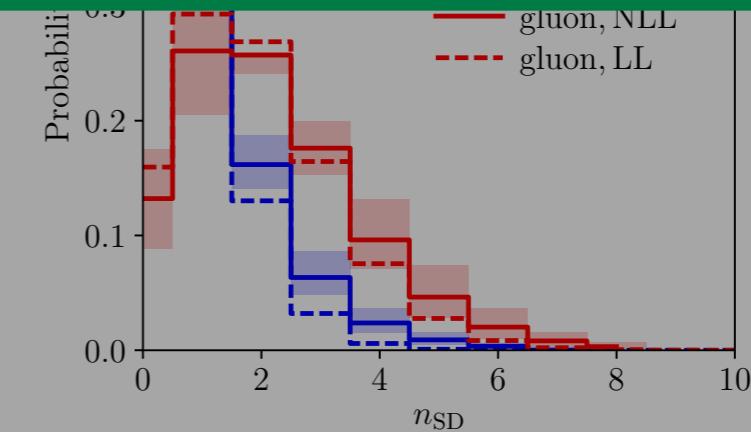
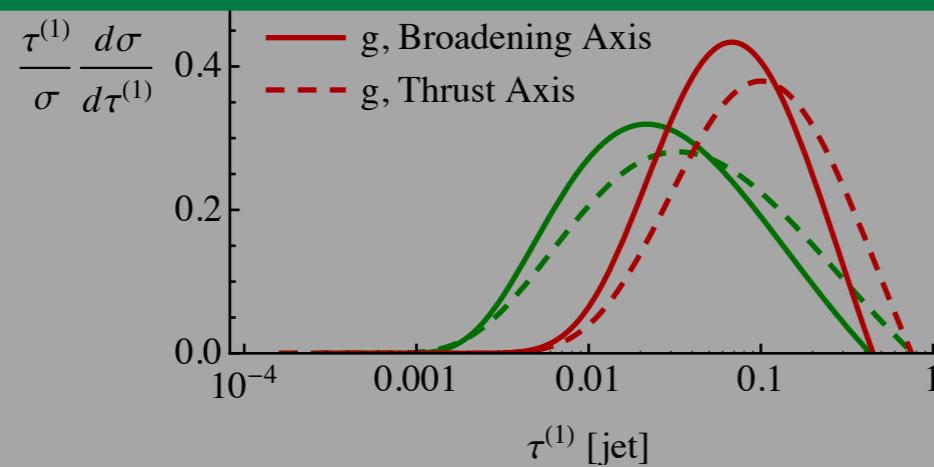
# A Cartoon of Infrared/Collinear Safety

Original Jet

Infrared

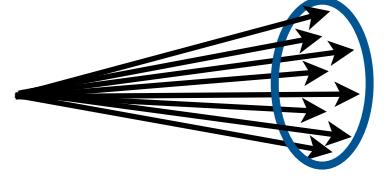
Collinear

What if *optimal* jet classifier  
is IRC safe observable?



[e.g. Larkoski, Neill, JDT, 1401.2158; Frye, Larkoski, JDT, Zhou, 1704.06266]

# A Systematic Expansion



Expand\* any IRC safe observable in small energy limit

$$\begin{aligned} \mathcal{S} = & \sum_i E_i f_1^{\mathcal{S}}(\hat{n}_i) + \sum_{ij} E_i E_j f_2^{\mathcal{S}}(\hat{n}_i, \hat{n}_j) \\ & + \sum_{ijk} E_i E_j E_k f_3^{\mathcal{S}}(\hat{n}_i, \hat{n}_j, \hat{n}_k) + \dots \end{aligned}$$

Form enforced by:	Particle Relabeling	Infrared Safety	Collinear Safety
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Further expand\* each angular function in pairwise angles

$$z_i = \frac{E_i}{E_{\text{jet}}} \quad \cos \theta_{ij} = \hat{n}_i \cdot \hat{n}_j$$

[Komiske, Metodiev, JDT, 1712.07124; see also Tkachov, hep-ph/9601308]

# Introducing the Energy Flow Polynomials

$$\text{EFP}_G = \sum_{i_1=1}^M \cdots \sum_{i_N=1}^M z_{i_1} \cdots z_{i_N} \prod_{(k,\ell) \in G} \theta_{i_k i_\ell}^\beta$$

*Multigraph*
*Angular Scaling*

All N-tuples
N Energy Fractions
Polynomial in Pairwise Angles

e.g.

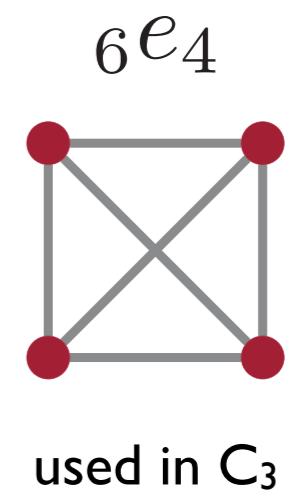
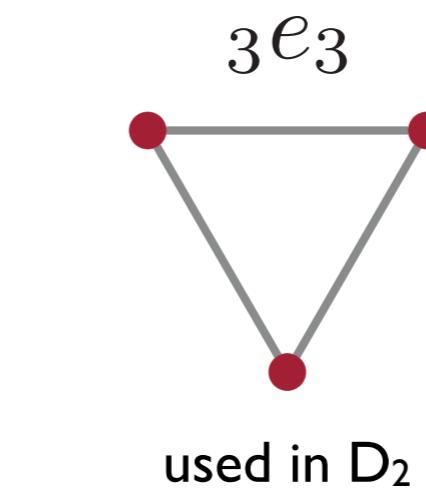
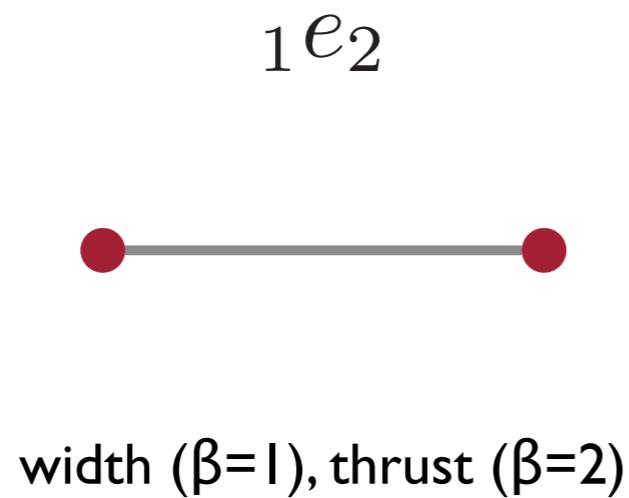
$$= \sum_{ijkl} z_i z_j z_k z_l \theta_{ij} \theta_{jk} \theta_{jl}^2 \theta_{kl}$$

*A Linear Basis for Jet Substructure (!)*

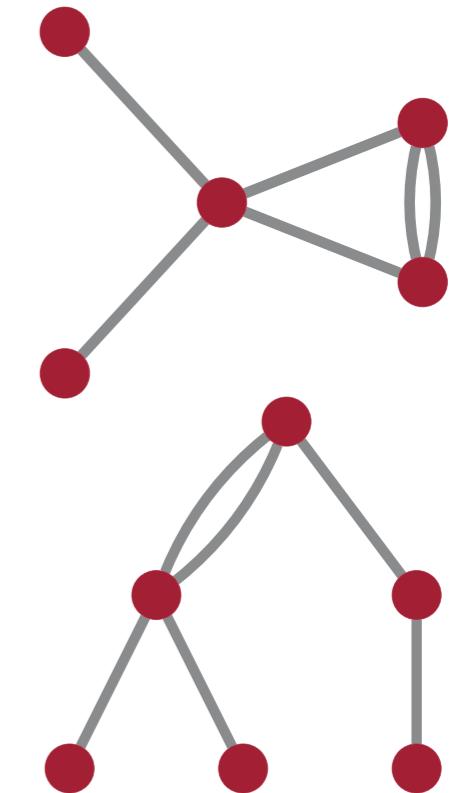
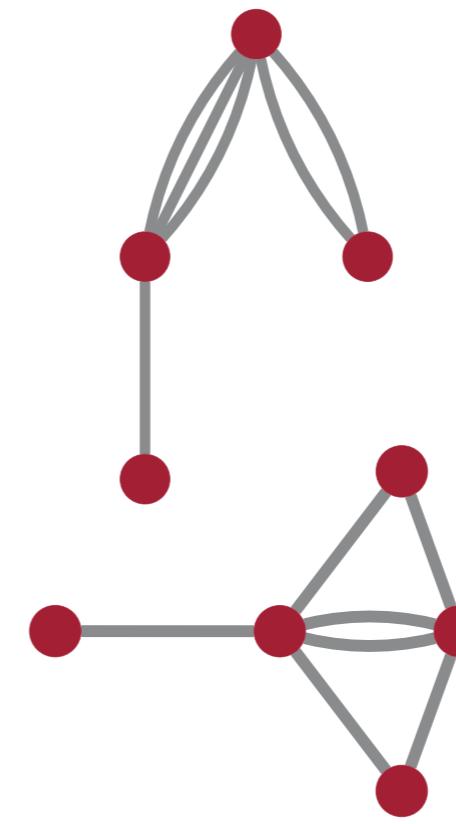
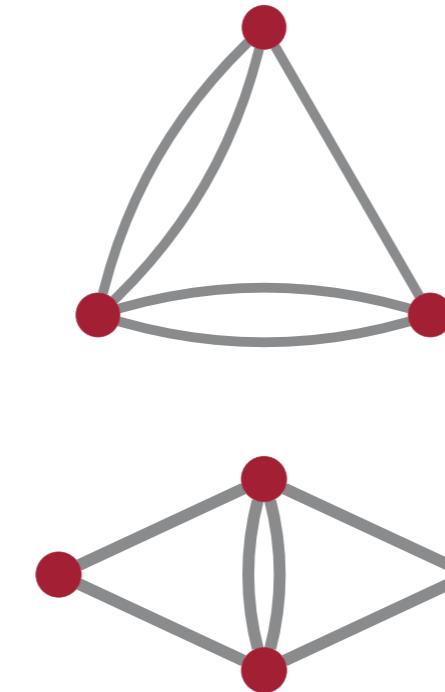
[Komiske, Metodiev, JDT, 1712.07124]

# Down the Rabbit Hole

Known  
Structures:

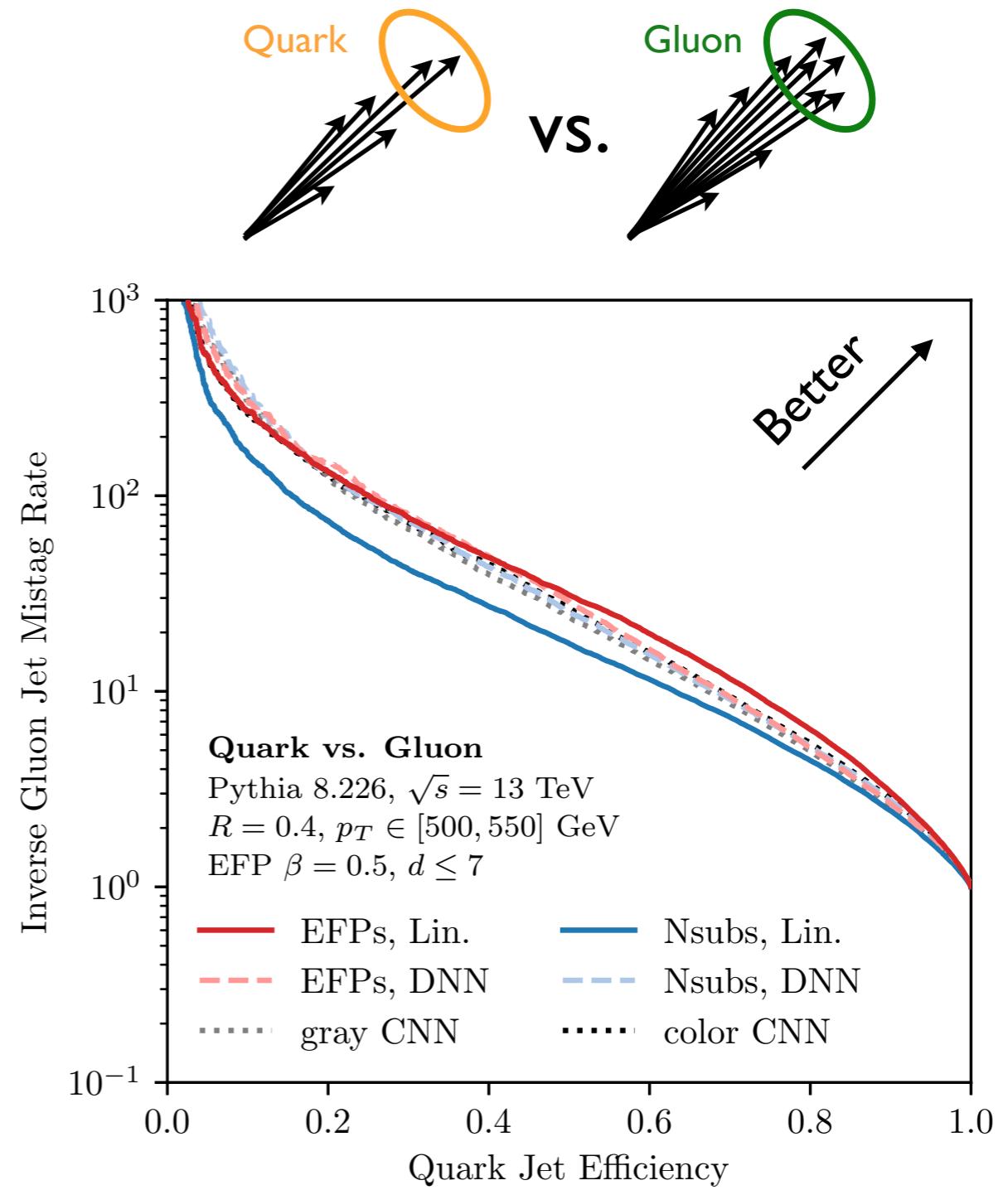
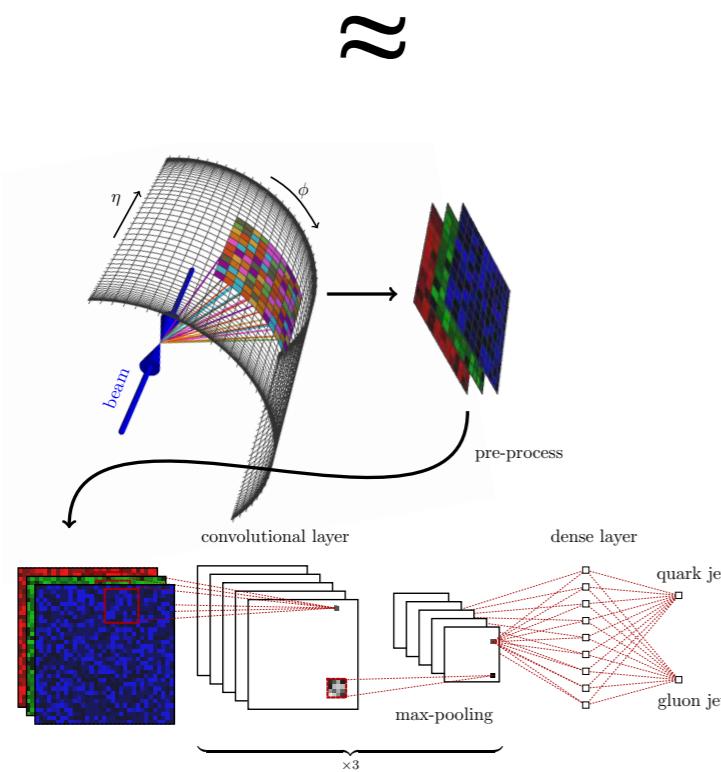


No Idea:



# Linear Regression or Neural Network?

$$\mathcal{S} = \sum_G s_G \text{EFP}_G$$



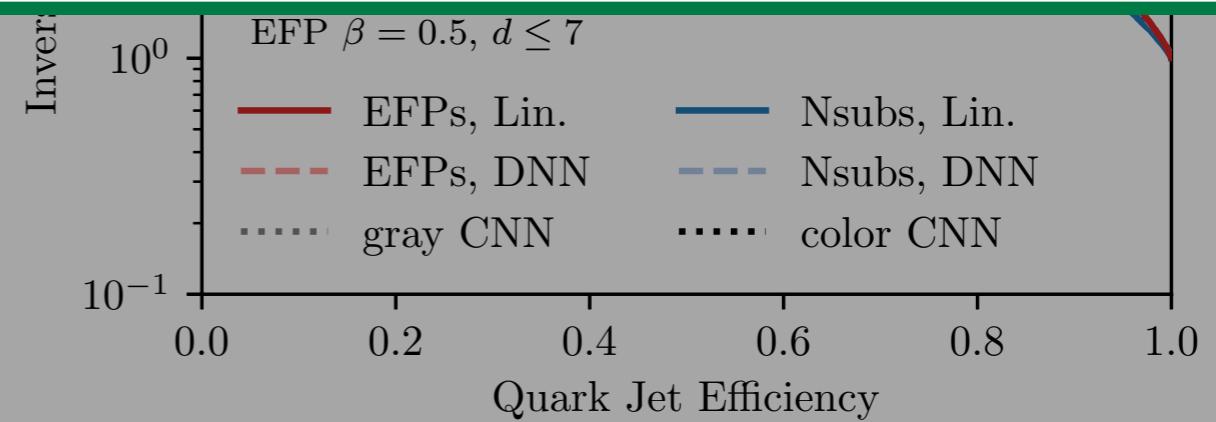
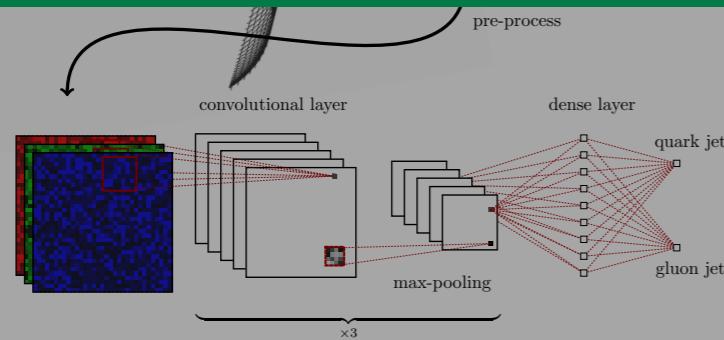
[Komiske, Metodiev, JDT, 1712.07124; Komiske, Metodiev, Schwartz, 1612.01551]

# Linear Regression or Neural Network?

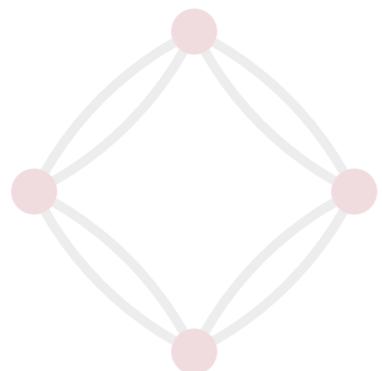


**Bottom Line:**  
**Jet Classification is “Solved”**

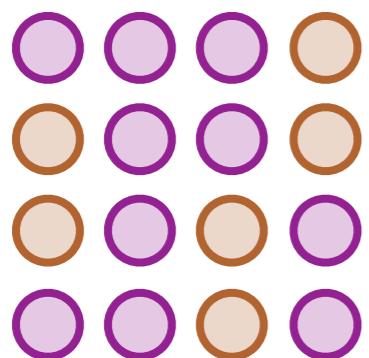
*Assuming trustable training samples, well-defined categories, etc.*



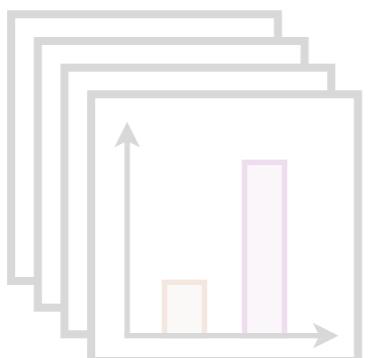
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A Basis for Jet Substructure



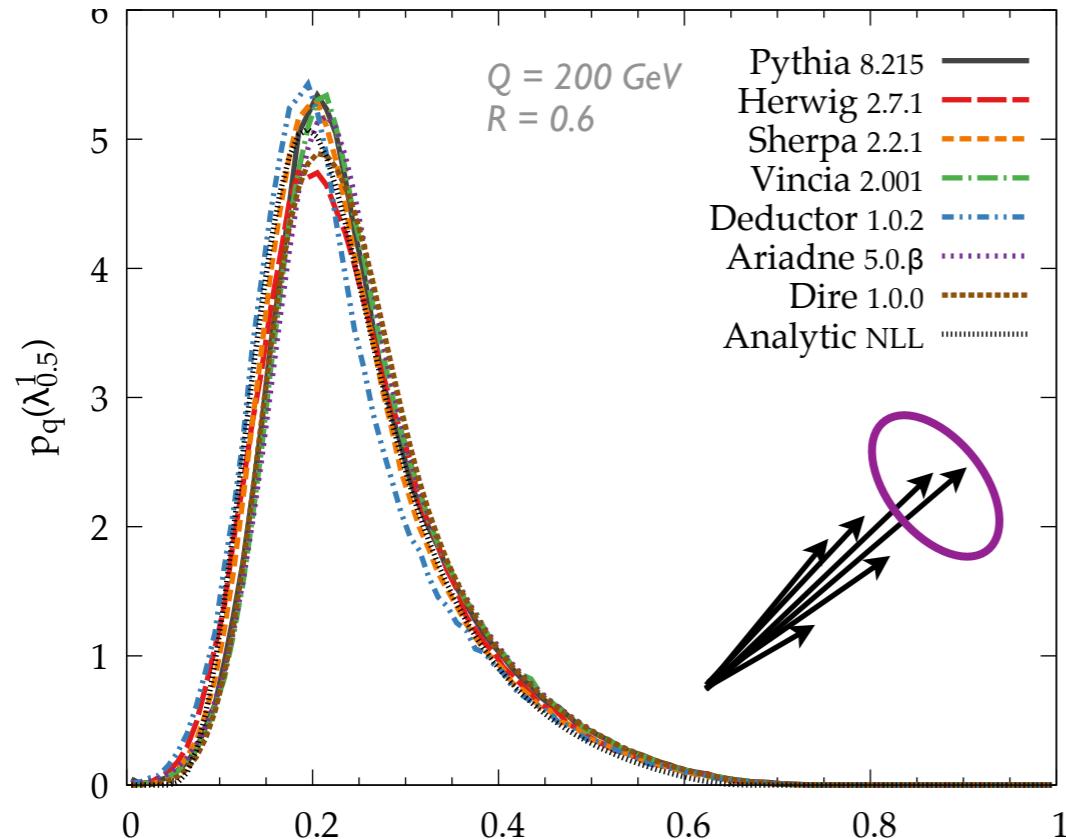
Learning Without Labels



Introducing Jet Topics

# Trustable Training Samples?

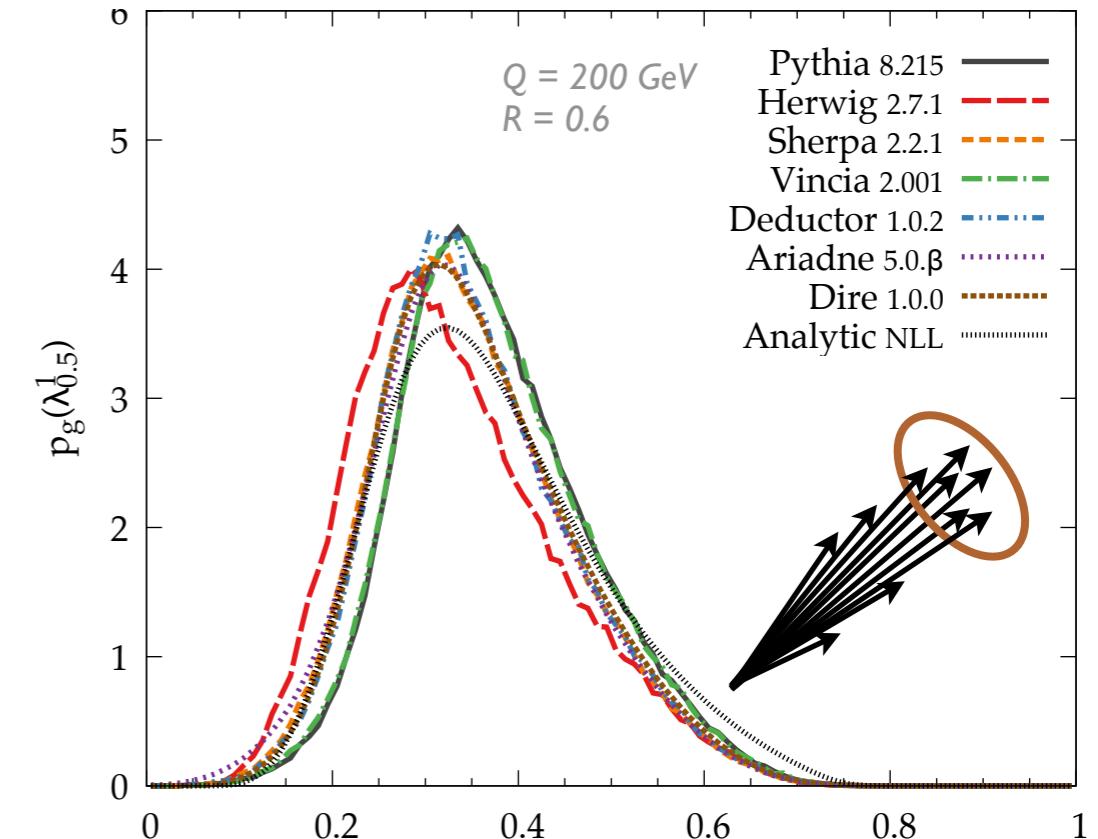
$e^+e^- \rightarrow \text{quarks } (C_F = 4/3)$



$$\text{LHA} = \sum_i z_i \sqrt{\theta_i}$$

VS.

$e^+e^- \rightarrow \text{gluons } (C_A = 3)$

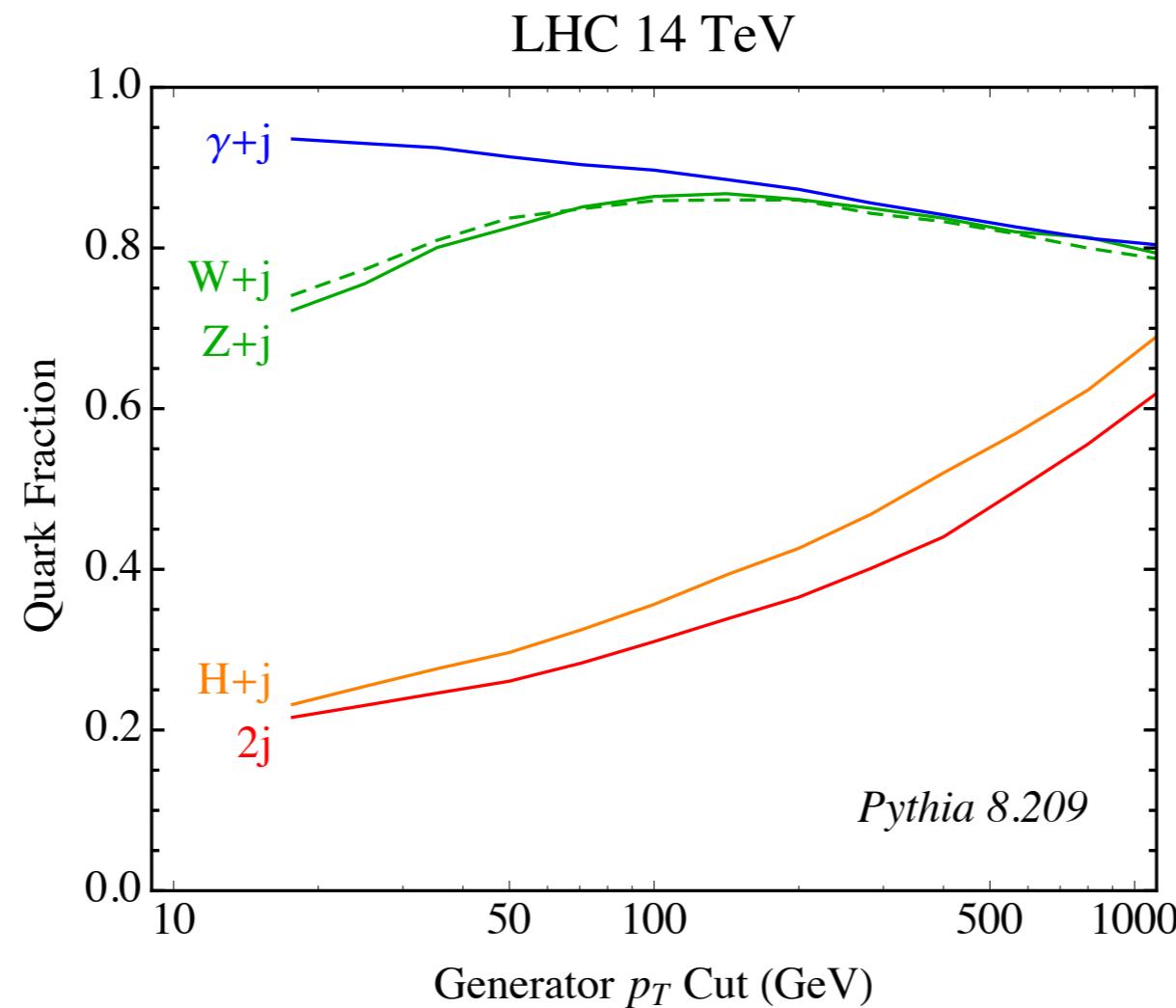


$$\text{LHA} = \sum_i z_i \sqrt{\theta_i}$$

*Large variations (esp. gluon jets, hard to tune from LEP)*

[Gras, Hoeche, Kar, Larkoski, Lönnblad, Plätzer, Siódlok, Skands, Soyez, JDT, 1704.03878;  
based on Soyez, JDT, Freytsis, Gras, Kar, Lönnblad, Plätzer, Siódlok, Skands, Soper, 1605.04692]

# Quark vs. Gluon from Data?



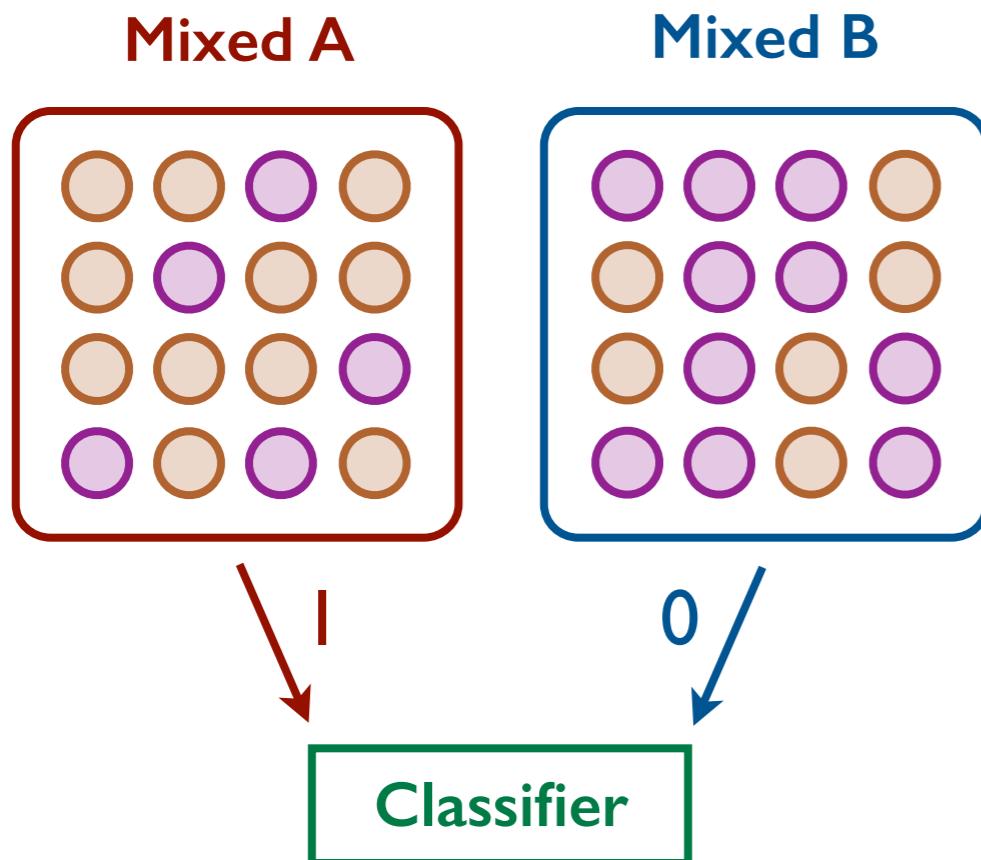
Plenty of (mixed) jets to study!

(Though plenty of uncertainties on quark/gluon fractions...)

[Gras, Hoeche, Kar, Larkoski, Lönnblad, Plätzer, Siódmok, Skands, Soyez, JDT, 1704.03878;  
see also Gallicchio, Schwartz, 1104.1175]

# Key Challenge: Mixed Samples are Mixtures

$$p_{\text{mixed}}(\vec{x}) = f_q \, p_{\text{quark}}(\vec{x}) + (1 - f_q) \, p_{\text{gluon}}(\vec{x})$$



**Mixed Classifier?**

$$h_{\text{mixed}}(\vec{x}) = \frac{p_A(\vec{x})}{p_A(\vec{x}) + p_B(\vec{x})}$$

$\neq$

$$h_{\text{pure}}(\vec{x}) = \frac{p_q(\vec{x})}{p_q(\vec{x}) + p_g(\vec{x})}$$

**but...**

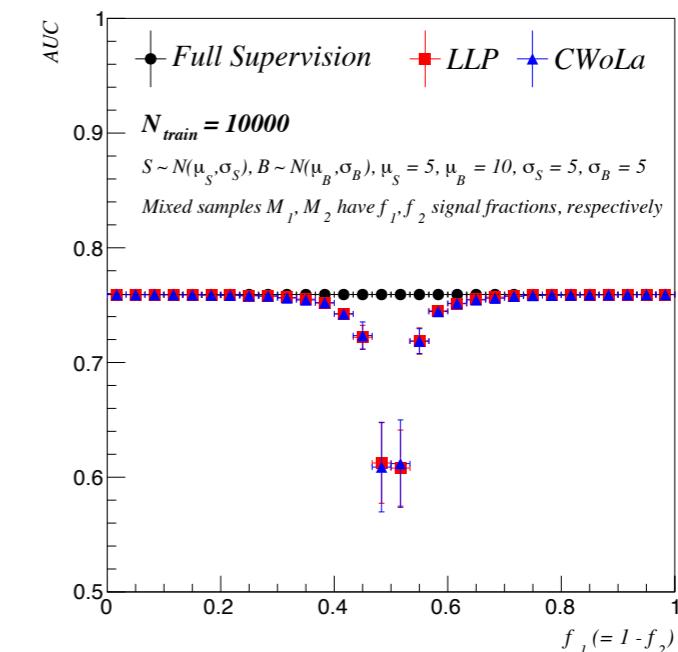
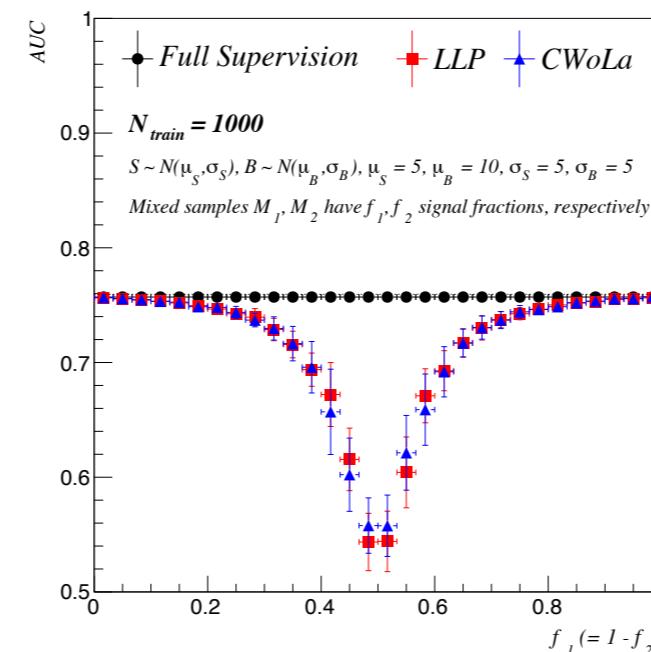
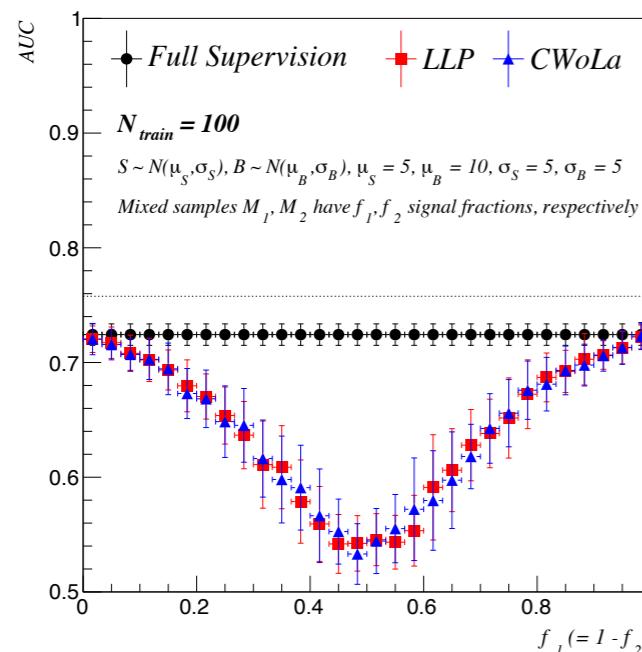
$$\frac{\partial h_{\text{mixed}}(\vec{x})}{\partial h_{\text{pure}}(\vec{x})} > 0$$

[Metodiev, Nachman, JDT, 1708.02949; see also Cranmer, Pavez, Louppe, 1506.02169;  
Blanchard, Flaska, Handy, Pozzi, Scott, 2016; Dery, Nachman, Rubbo, Schwartzman, 1702.00414; Cohen, Freytsis, Ostdiek, 1706.09451]

# Key Challenge: Mixed Samples are Mixtures

## Classification Without Labels

Slower training, but same ultimate performance



(Subtlety: Some fraction information needed to calibrate classifier)

[Metodiev, Nachman, JDT, 1708.02949; see also Cranmer, Pavez, Louppe, 1506.02169;

Blanchard, Flaska, Handy, Pozzi, Scott, 2016; Dery, Nachman, Rubbo, Schwartzman, 1702.00414; Cohen, Freytsis, Ostdiek, 1706.09451]

# Key Assumption: Mixed Samples are Mixtures

$$p_{\text{mixed}}(\vec{x}) = f_q \, p_{\text{quark}}(\vec{x}) + (1 - f_q) \, p_{\text{gluon}}(\vec{x})$$

Sensible?

No!

Well, ok...

## Sample Dependence

“Quark jet” in dijets vs. Z+jets are different  
because of color correlations with rest of event

## Approximate Sample Independence

Differences are power suppressed with small radius jets

Differences can be mitigated using jet grooming

[see Banfi, Dasgupta, Khelifa-Kerfa, Marzani, 1004.3483; Frye, Larkoski, Schwartz, Yan, 1603.06375, 1603.09338]

# Key Assumption: Mixed Samples are Mixtures

$$p_{\text{mixed}}(\vec{x}) = f_q \, p_{\text{quark}}(\vec{x}) + (1 - f_q) \, p_{\text{gluon}}(\vec{x})$$

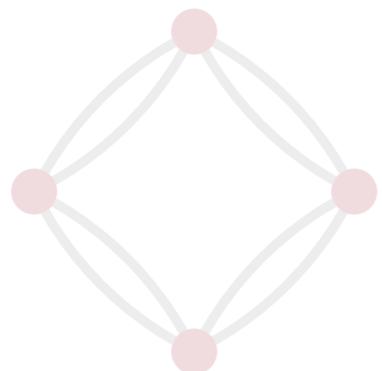
**Bottom Line:**  
**Jet Classification is “Solved”**  
with trustable mixed training samples from data

Assuming *sample independence*, well-defined categories, etc.

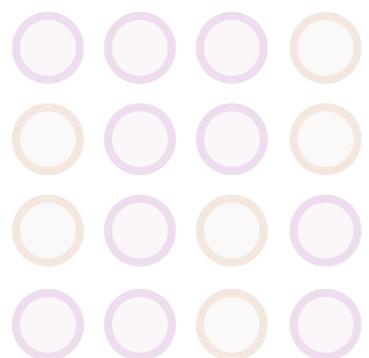
## Approximate Sample Independence

Differences are power suppressed with small radius jets  
Differences can be mitigated using jet grooming

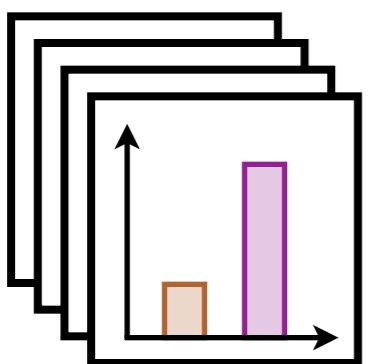
[see Banfi, Dasgupta, Khelifa-Kerfa, Marzani, 1004.3483; Frye, Larkoski, Schwartz, Yan, 1603.06375, 1603.09338]



A Basis for Jet Substructure



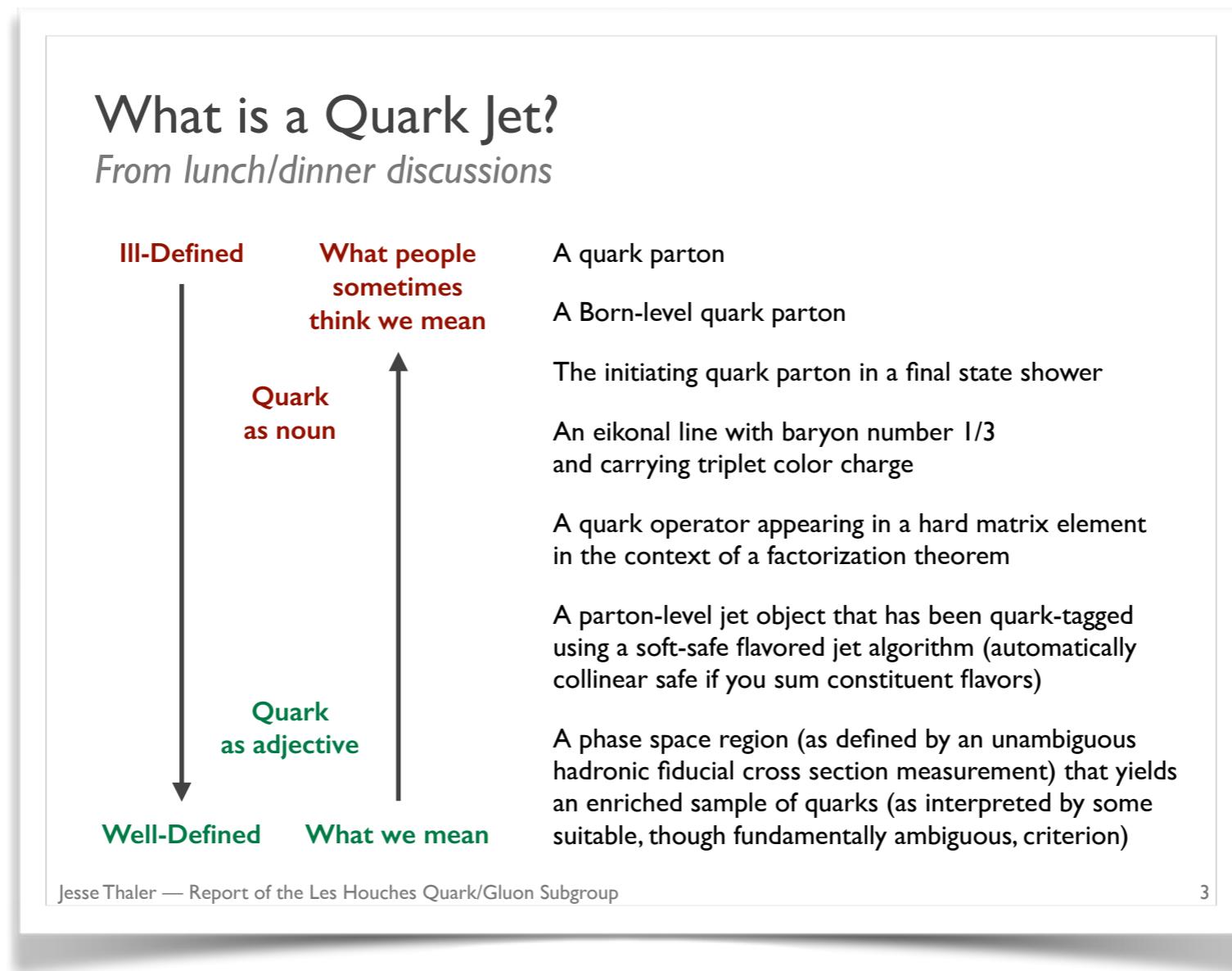
Learning Without Labels



Introducing Jet Topics

# Well-Defined Categories?

Quark (color triplet) vs. Gluon (color octet)?  
But jet constituents are color-singlet hadrons!



[Gras, Hoeche, Kar, Larkoski, Lönnblad, Plätzer, Siódtek, Skands, Soyez, JDT, 1704.03878;  
based on Soyez, JDT, Freytsis, Gras, Kar, Lönnblad, Plätzer, Siódtek, Skands, Soper, 1605.04692]

# Assume “Quark” and “Gluon” Exist

i.e. *Sample Independence*

$$p_{\text{mixed A}}(\vec{x}) = f_q^A p_{\text{quark}}(\vec{x}) + (1 - f_q^A) p_{\text{gluon}}(\vec{x})$$

$$p_{\text{mixed B}}(\vec{x}) = f_q^B p_{\text{quark}}(\vec{x}) + (1 - f_q^B) p_{\text{gluon}}(\vec{x})$$

If you can extract these...

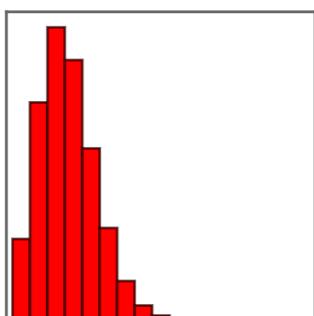
$$f_q^A \quad f_q^B \quad p_{\text{quark}}(\vec{x}) \quad p_{\text{gluon}}(\vec{x})$$

...then you have effectively defined “quark/gluon”

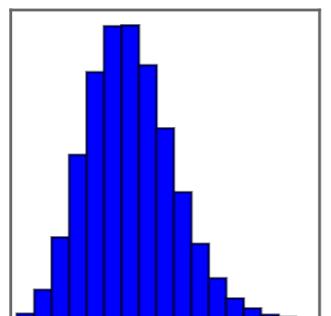
Too good to be true? Or already solved?

# Generation (Easy)

Jet Topics



Quark Jet

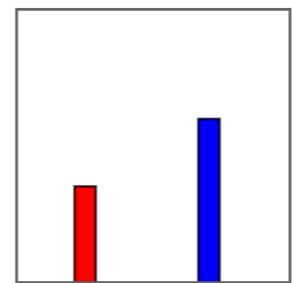


Gluon Jet

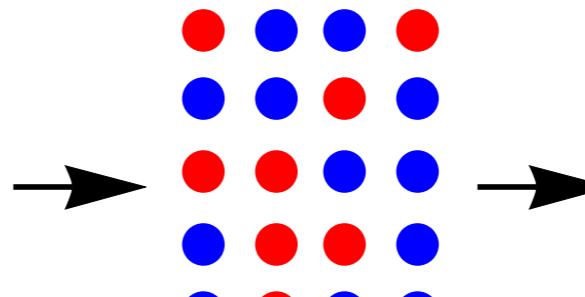
Mixed Jet Sample N

...

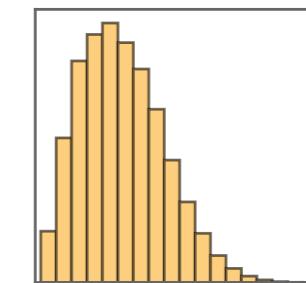
Mixed Jet Sample I



Jet Fractions



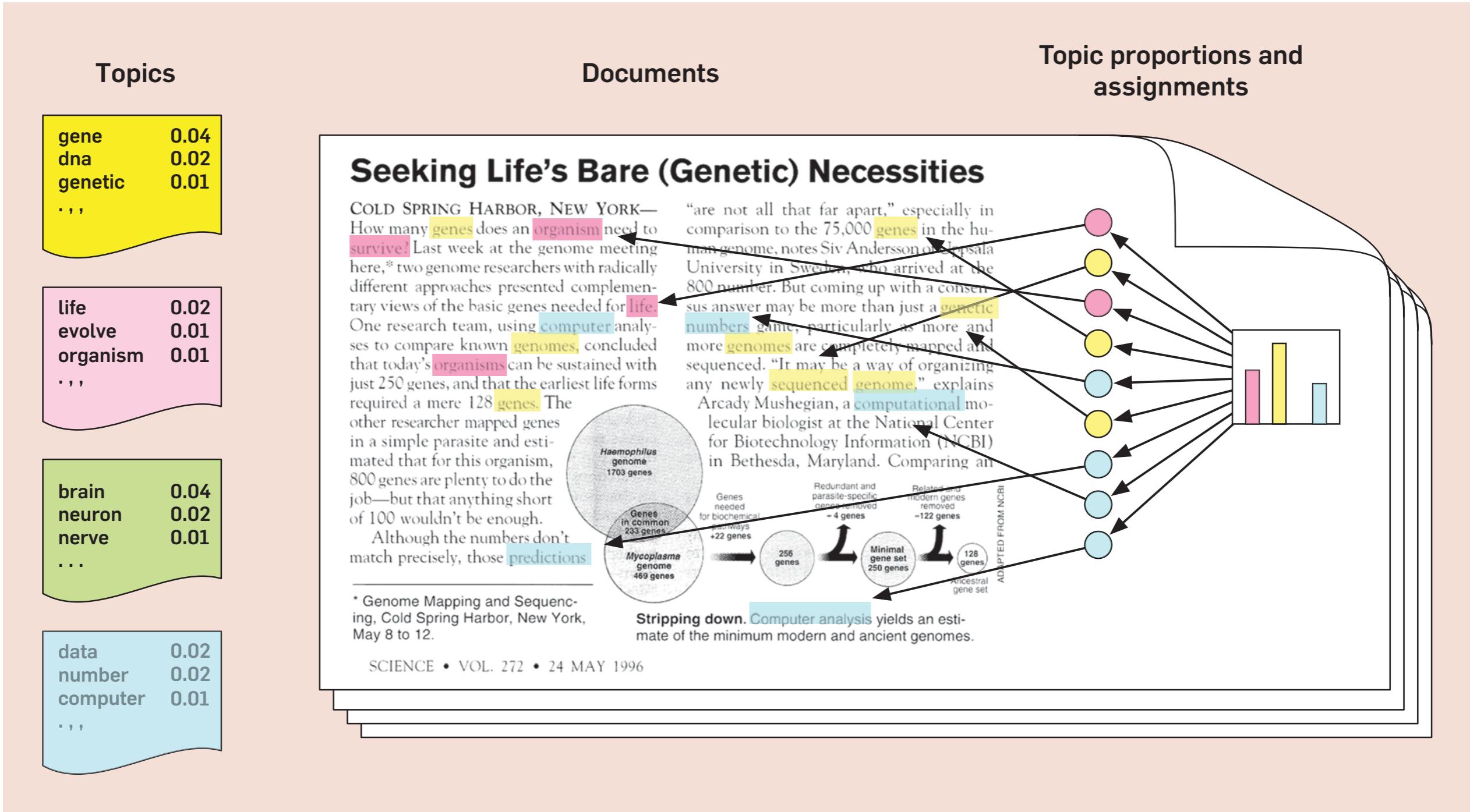
Mixed Data



Histogram

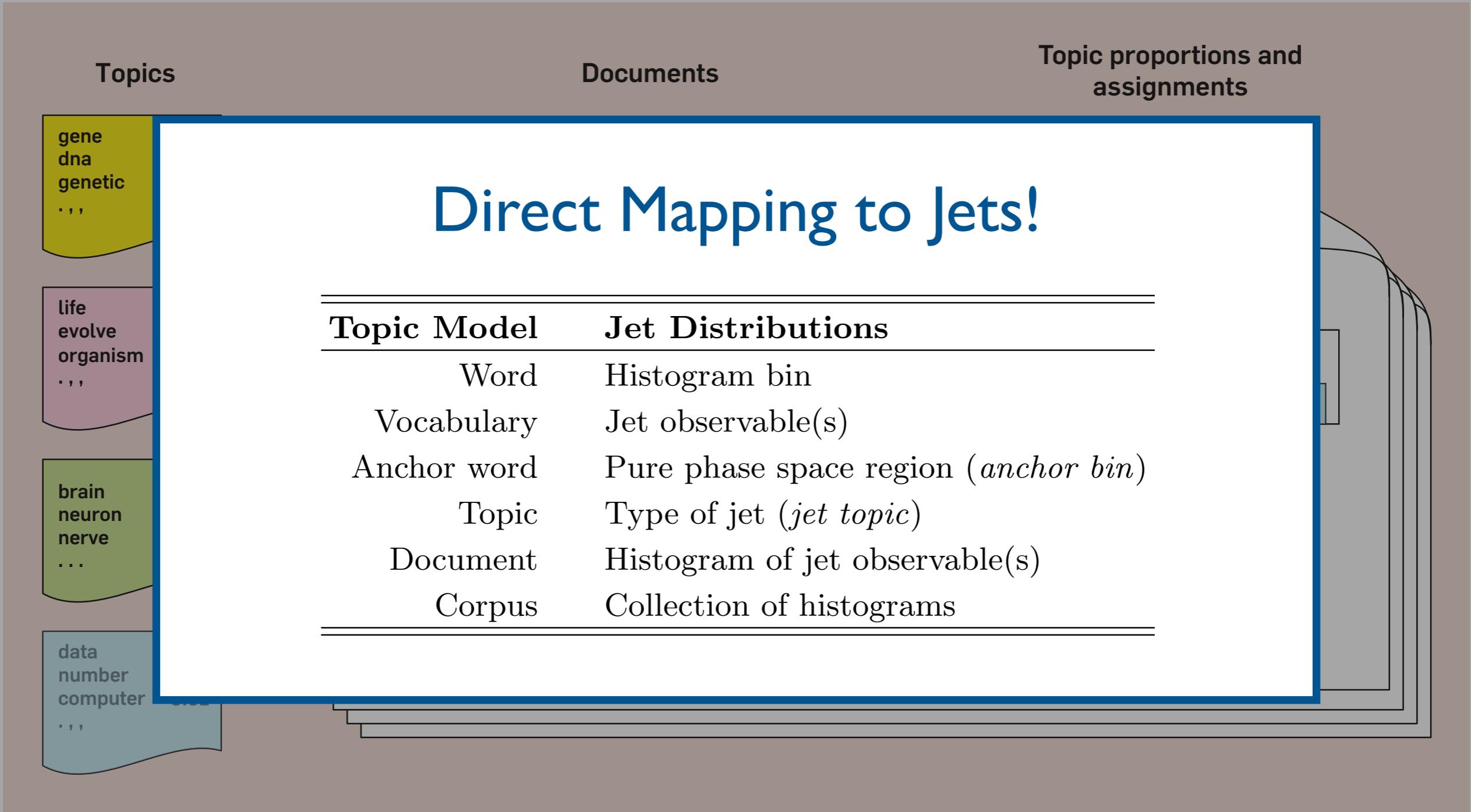
← Demixing (Impossible?)

# Topic Modeling



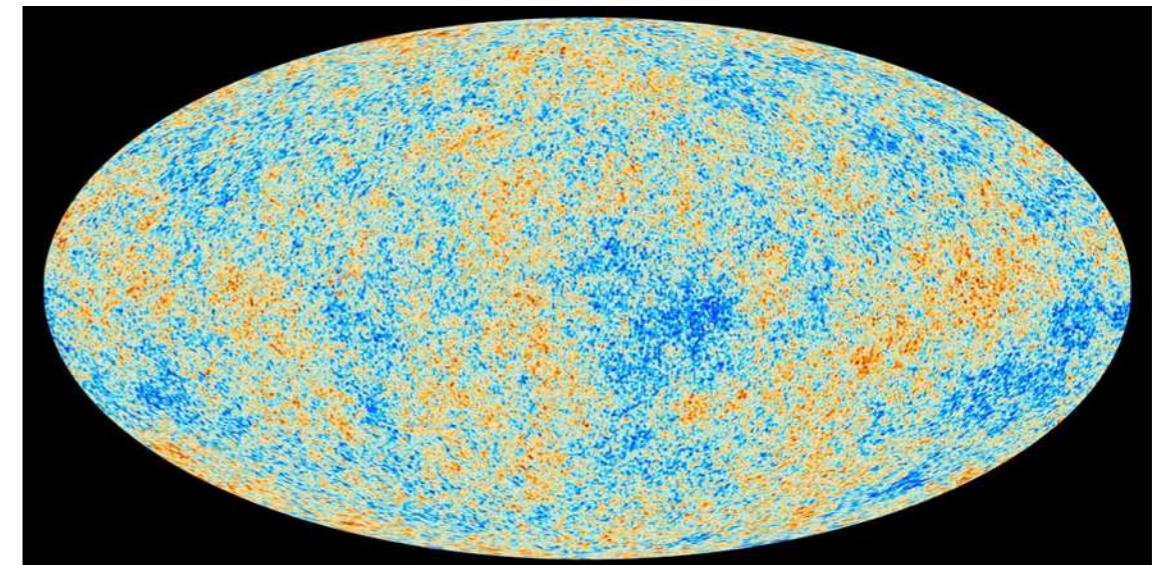
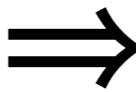
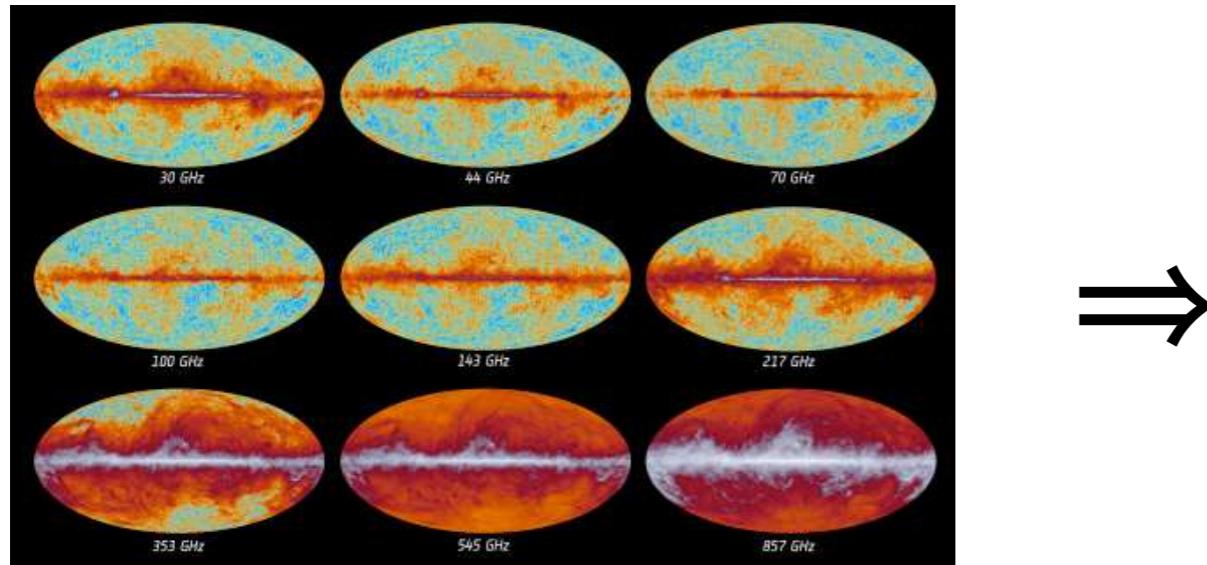
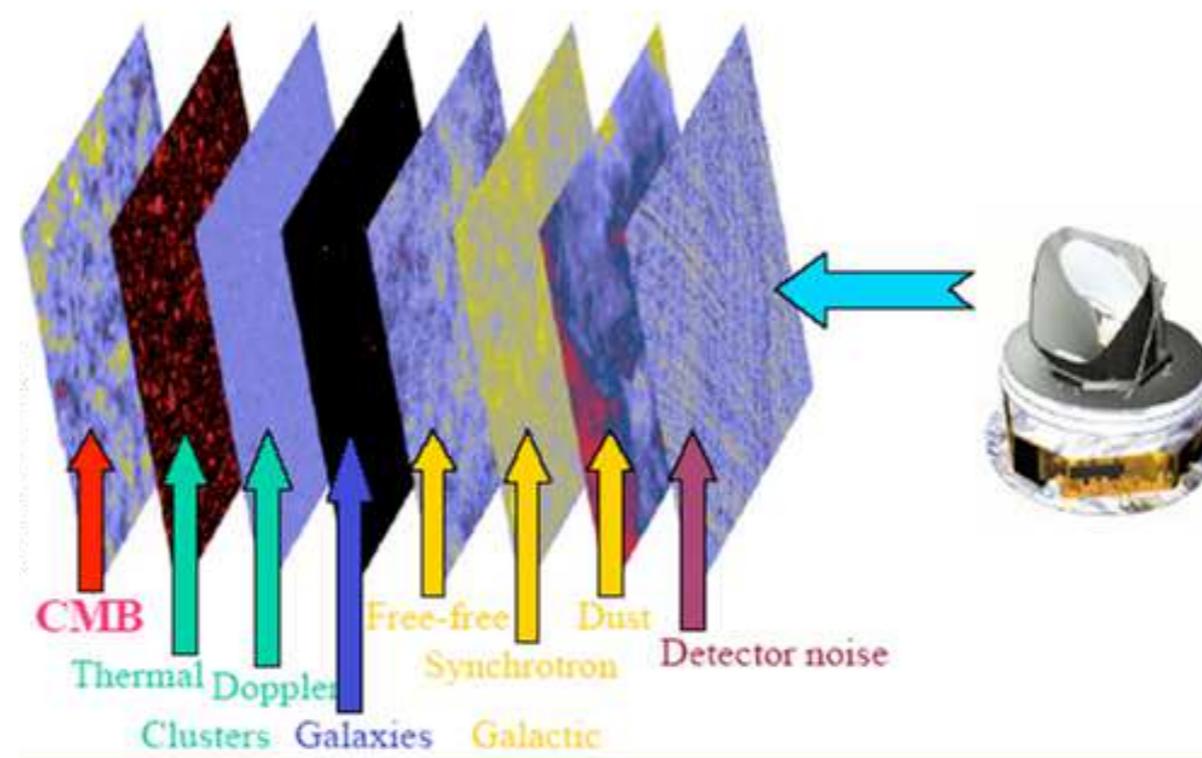
[Blei, 2012]

# Topic Modeling



[Blei, 2012]

# Related to CMB Foreground Separation



[Planck Outreach]

# The Demix Algorithm

*Simplifying to two mixtures of two topics*

Just subtract the mixed distributions!

$$p_{T1}(\vec{x}) = \frac{p_A(\vec{x}) - p_B(\vec{x}) \kappa_{A|B}}{1 - \kappa_{A|B}}$$
$$p_{T2}(\vec{x}) = \frac{p_B(\vec{x}) - p_A(\vec{x}) \kappa_{B|A}}{1 - \kappa_{B|A}}$$

Reducibility Factors

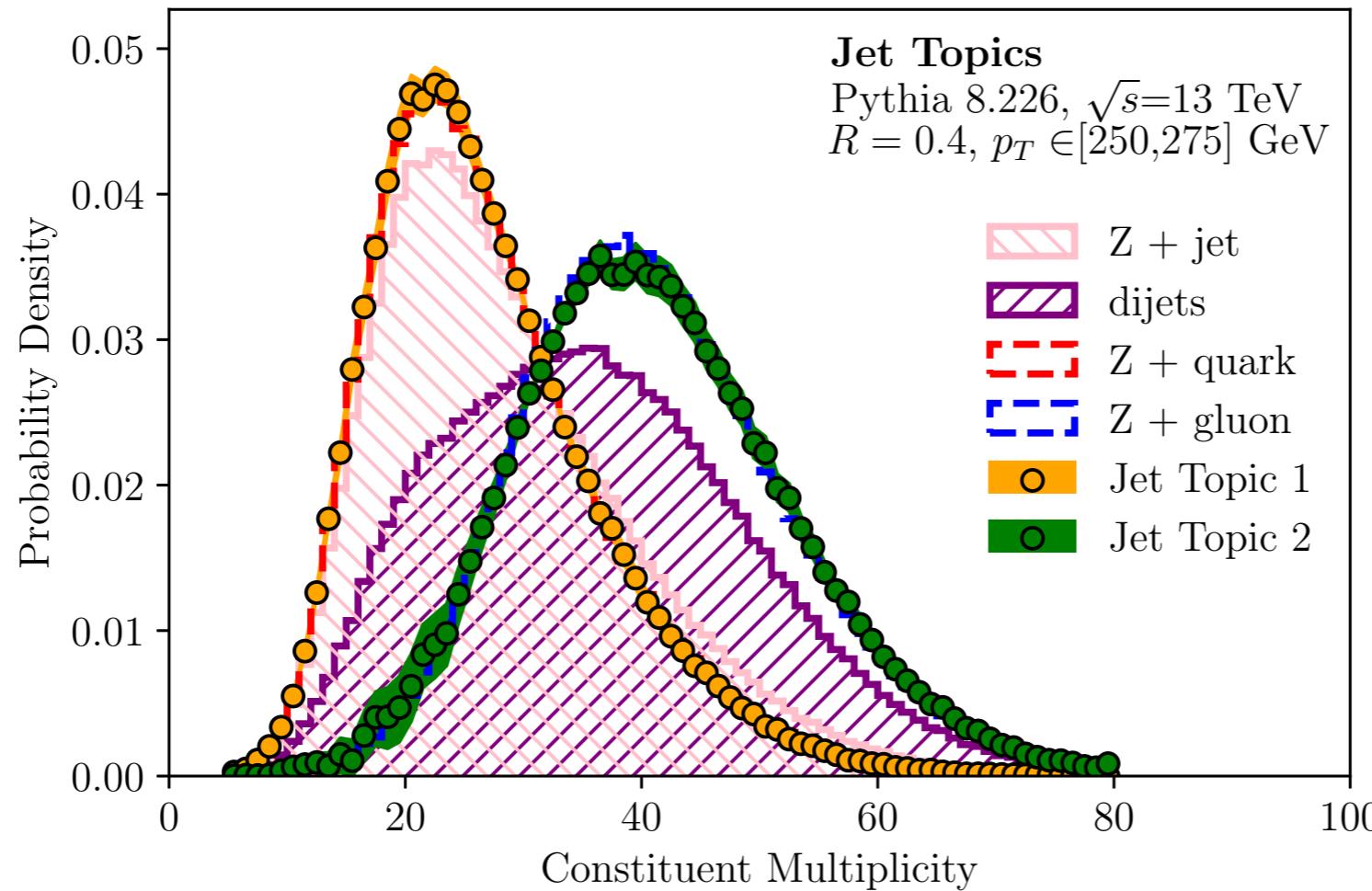
Requires Anchor Bins / “Mutual Irreducibility”

Region of 100% purity for each topic (even if tiny efficiency)  
Probabilities are positive, so make  $\kappa$  as large as possible

[Katz-Samuels, Blanchard, Scott, 1710.01167]

# Jet Topics

Extract jet categories from data...



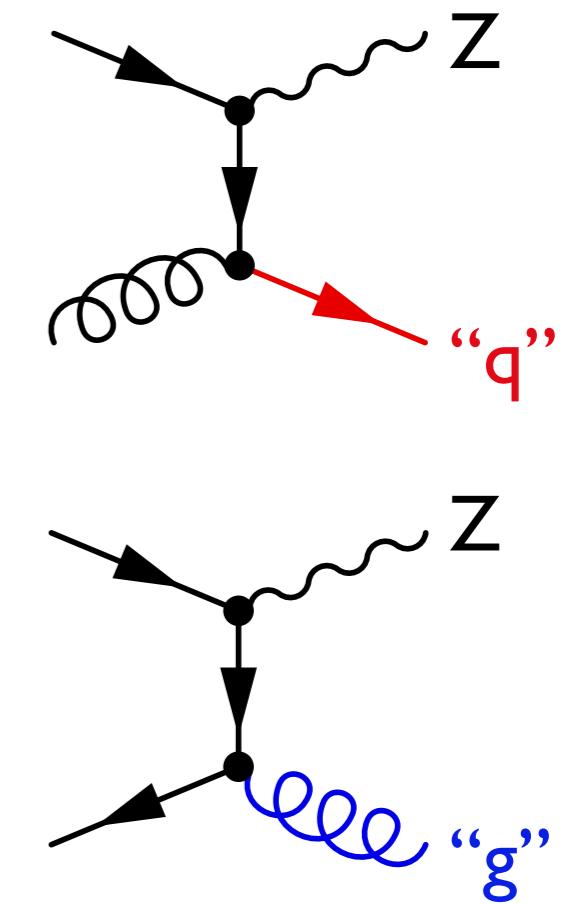
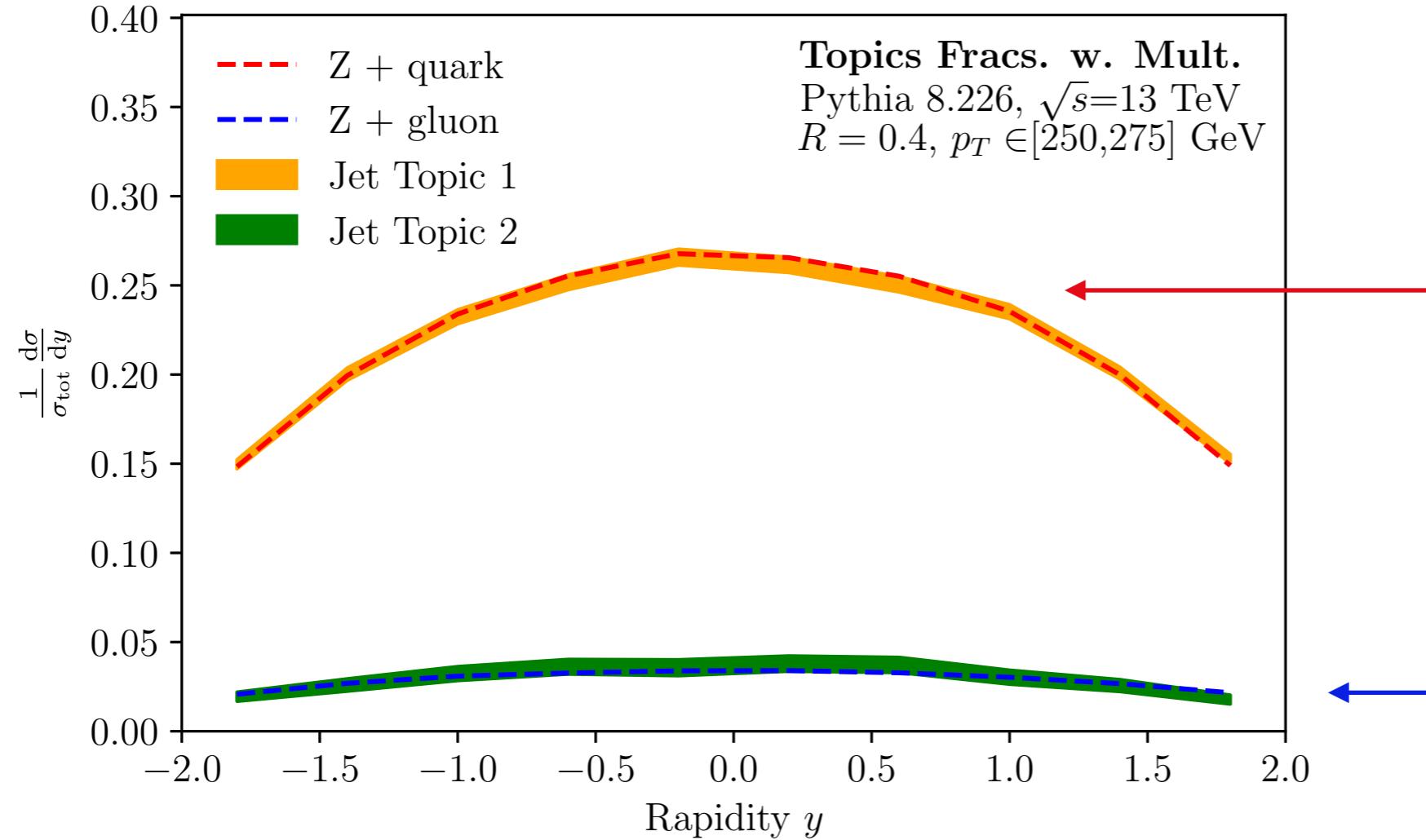
...solely\* from the assumption they exist



Sample Independence, Different Fractions, Mutual Irreducibility

[Metodiev, JDT, 1802.00008]

# “Parton”-Labeled Cross Sections?

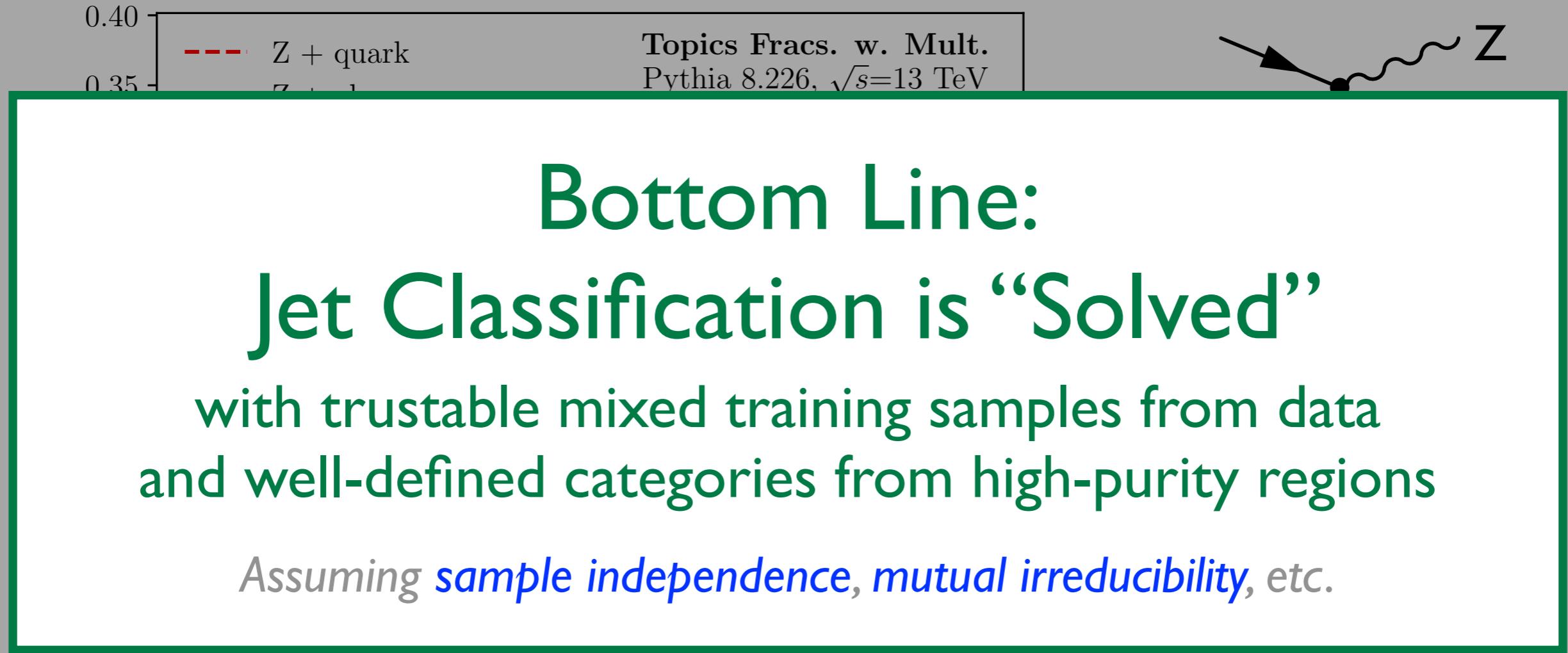


Implications for PDF extraction?

Key challenge: Defining jet topics at fixed order

[Metodiev, JDT, 1802.00008]

# “Parton”-Labeled Cross Sections?

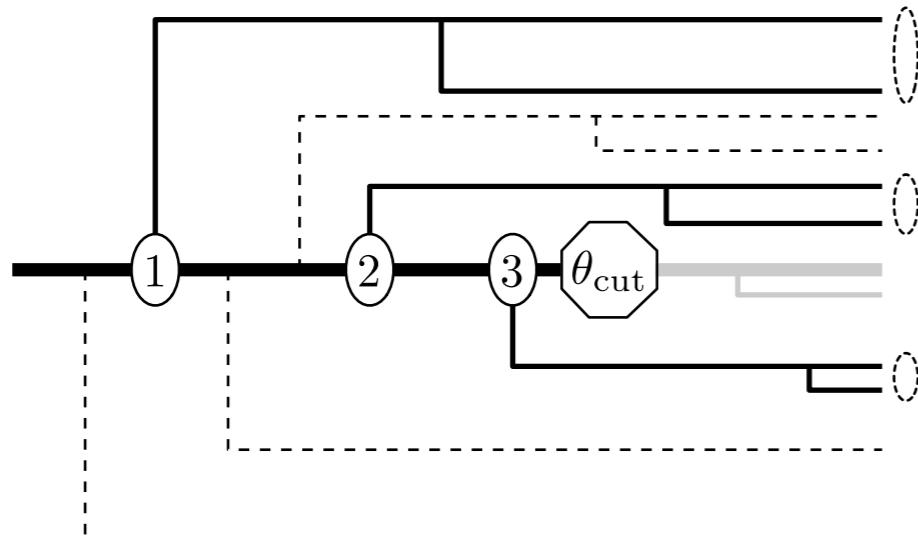


Implications for PDF extraction?  
Key challenge: Defining jet topics at fixed order

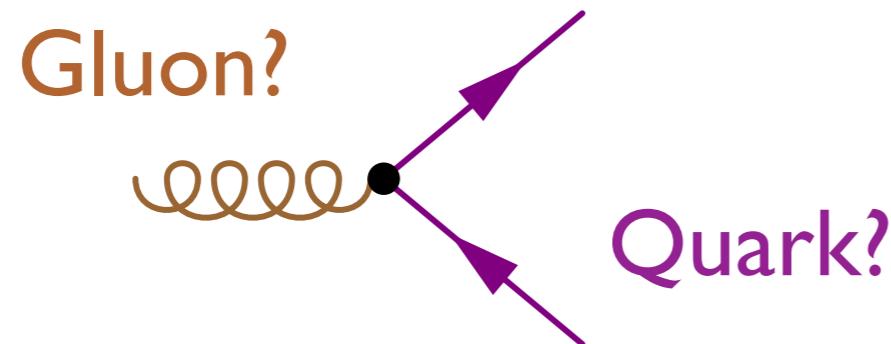
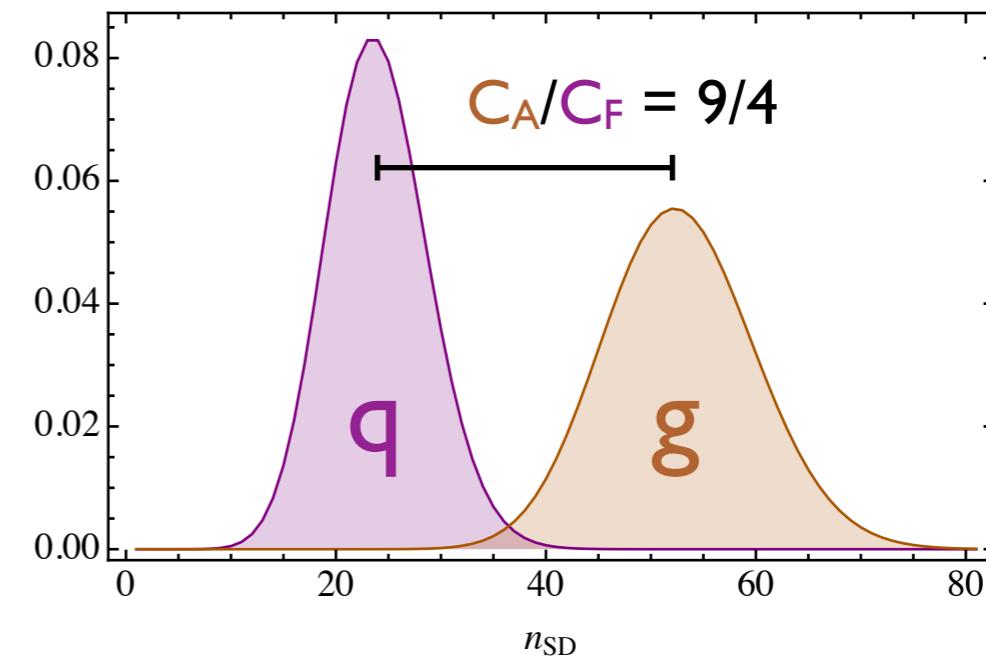
[Metodiev, JDT, 1802.00008]

# Mutual Irreducibility from QCD?

Count emissions using  
“soft drop multiplicity” (IRC safe)



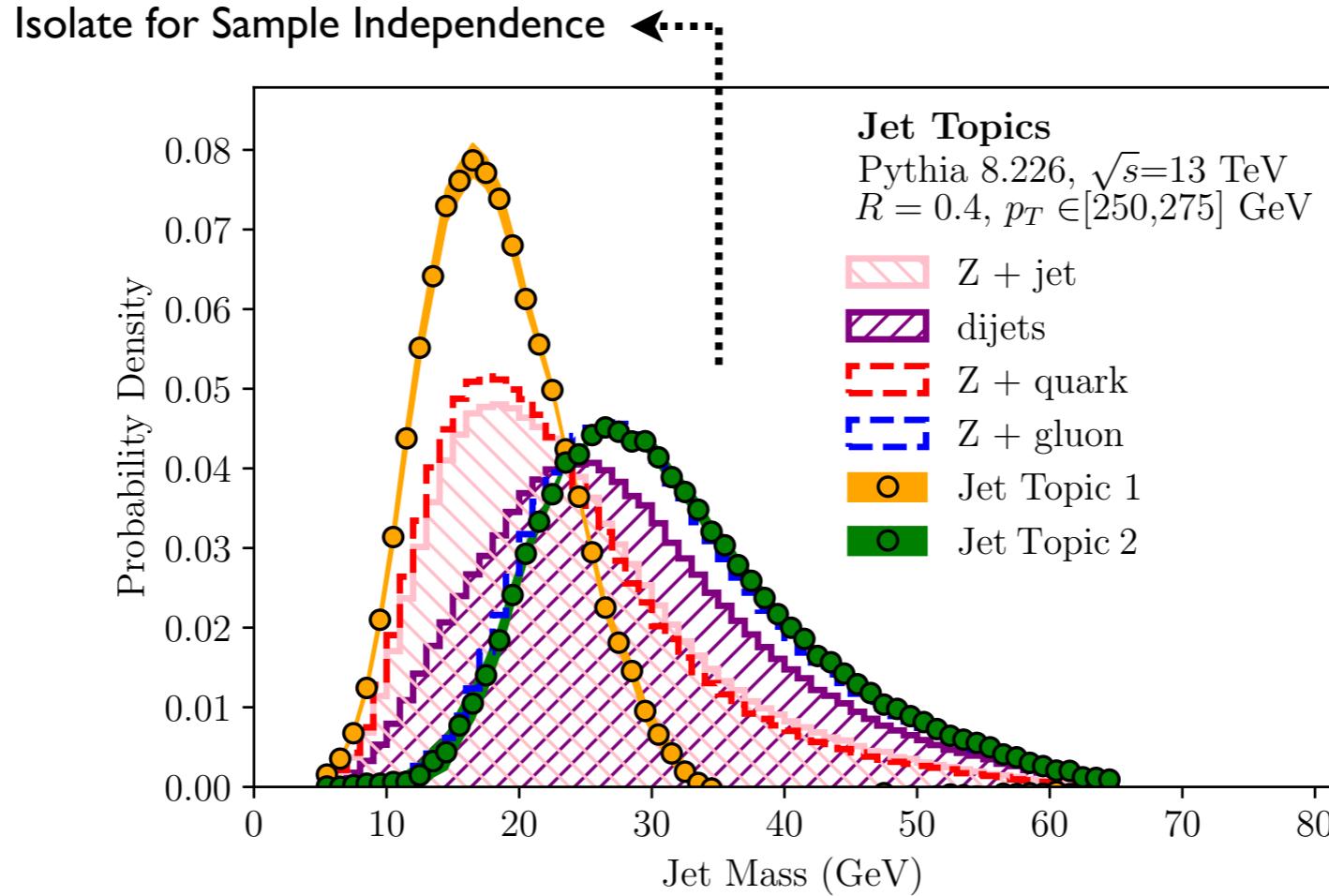
Asymptotes to Poissonians  
in high energy limit



One solution:  
Define “quark”/“gluon”  
by mutual irreducibility

[Frye, Larkoski, Thaler, Zhou, 1704.06266]

# Jet Mass is not Mutually Irreducible



Casimir  
Scaling  
at LL

$$\kappa(g|q) = \frac{C_A}{C_F} \min \Sigma_q^{\frac{C_A}{C_F}-1} = 0$$

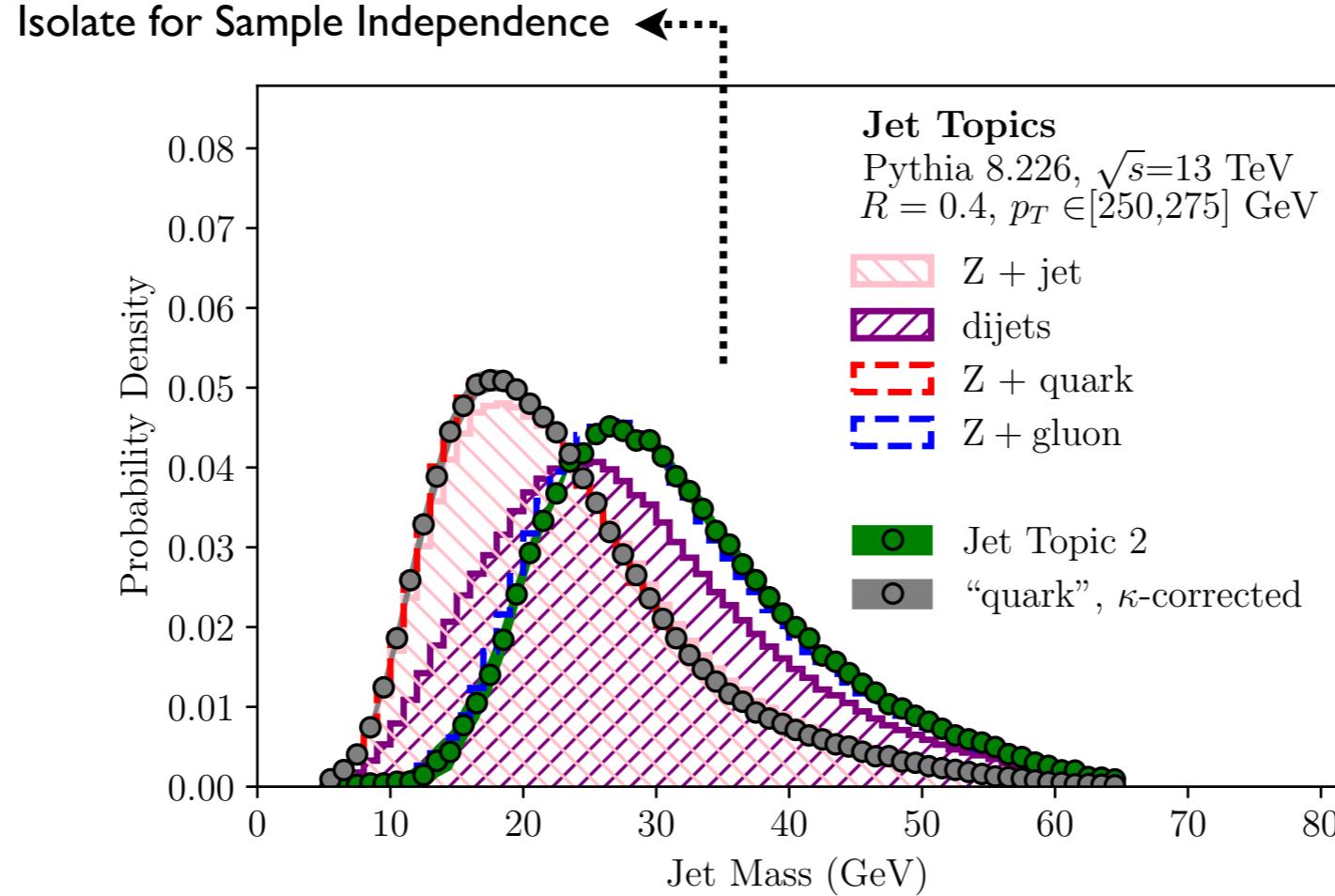
“Gluon” Topic is Pure

$$\kappa(q|g) = \frac{C_F}{C_A} \min \Sigma_q^{1-\frac{C_A}{C_F}} = \frac{C_F}{C_A}$$

“Quark” Topic is Distorted

[Metodiev, JDT, 1802.00008]

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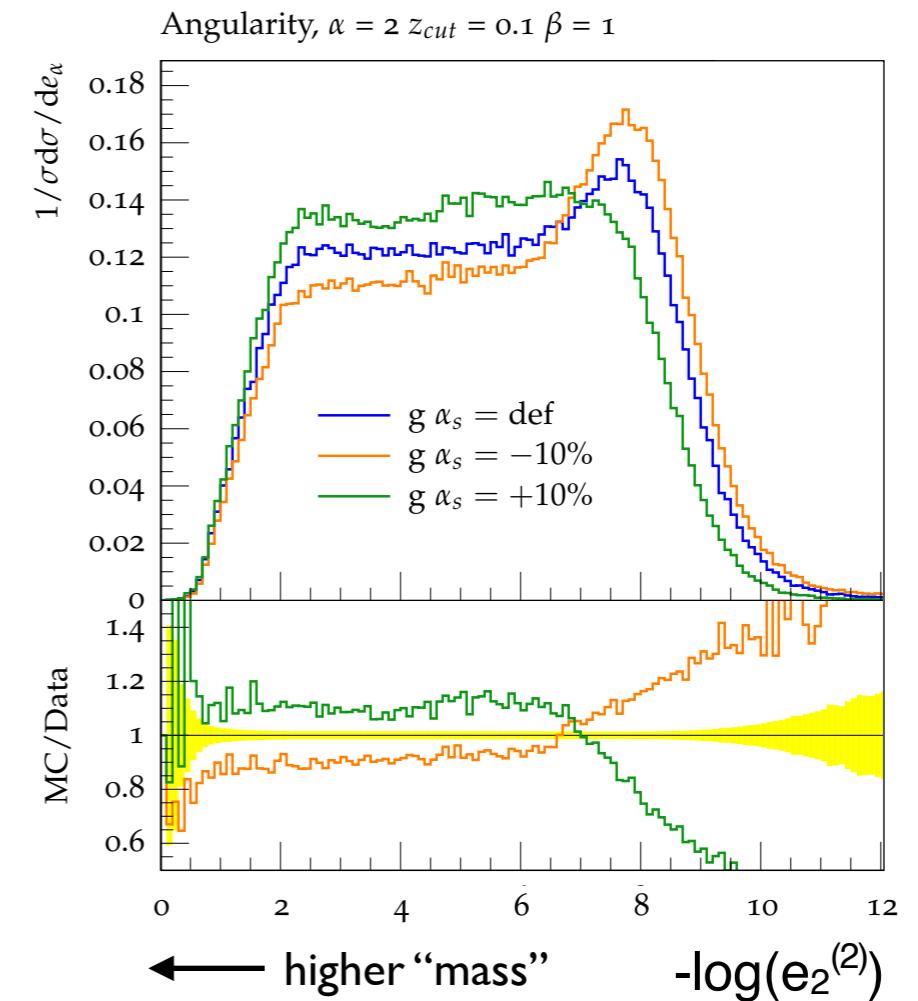
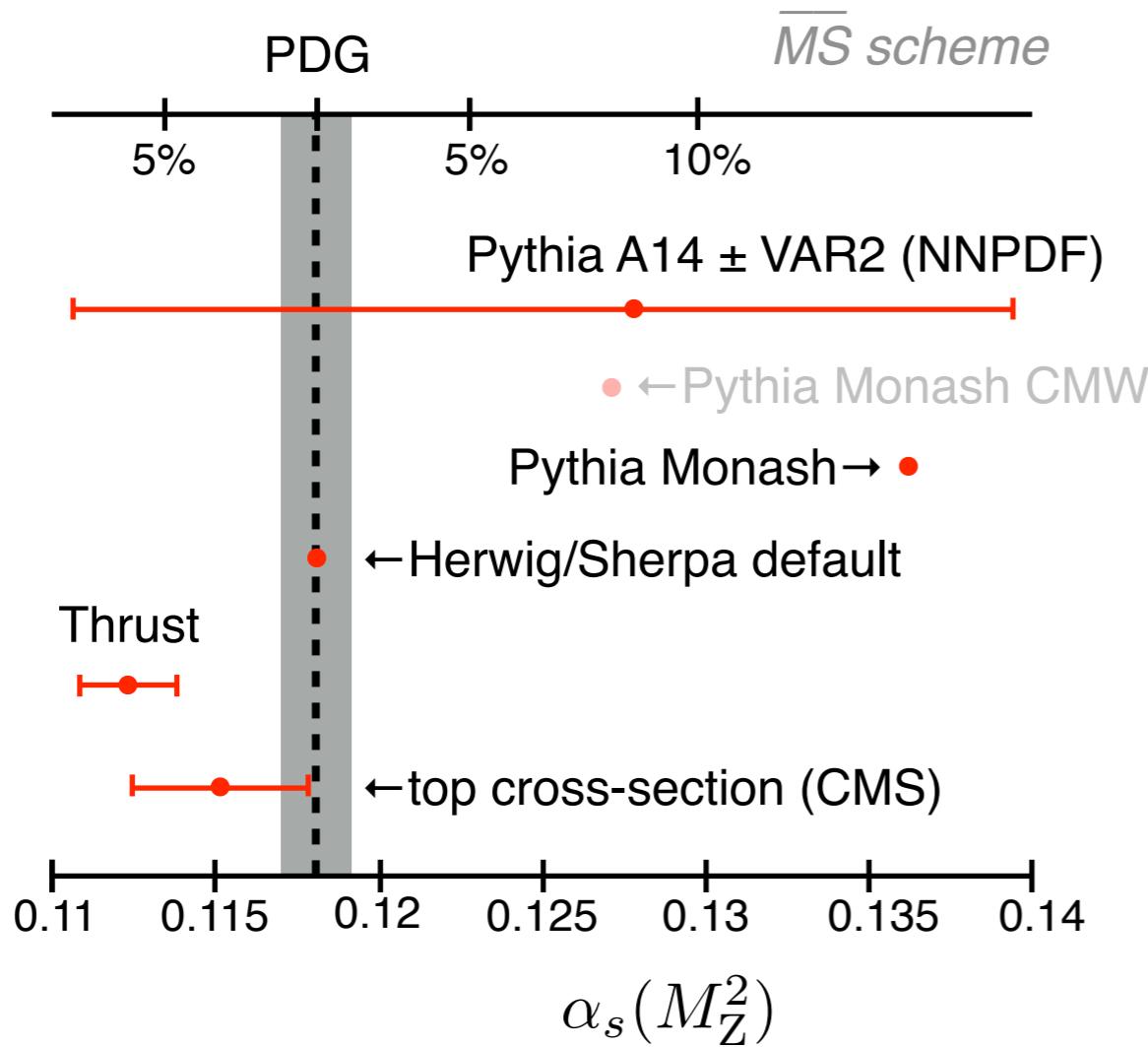
If you know K...

“Quark” Topic can be Corrected

[Metodiev, JDT, 1802.00008]

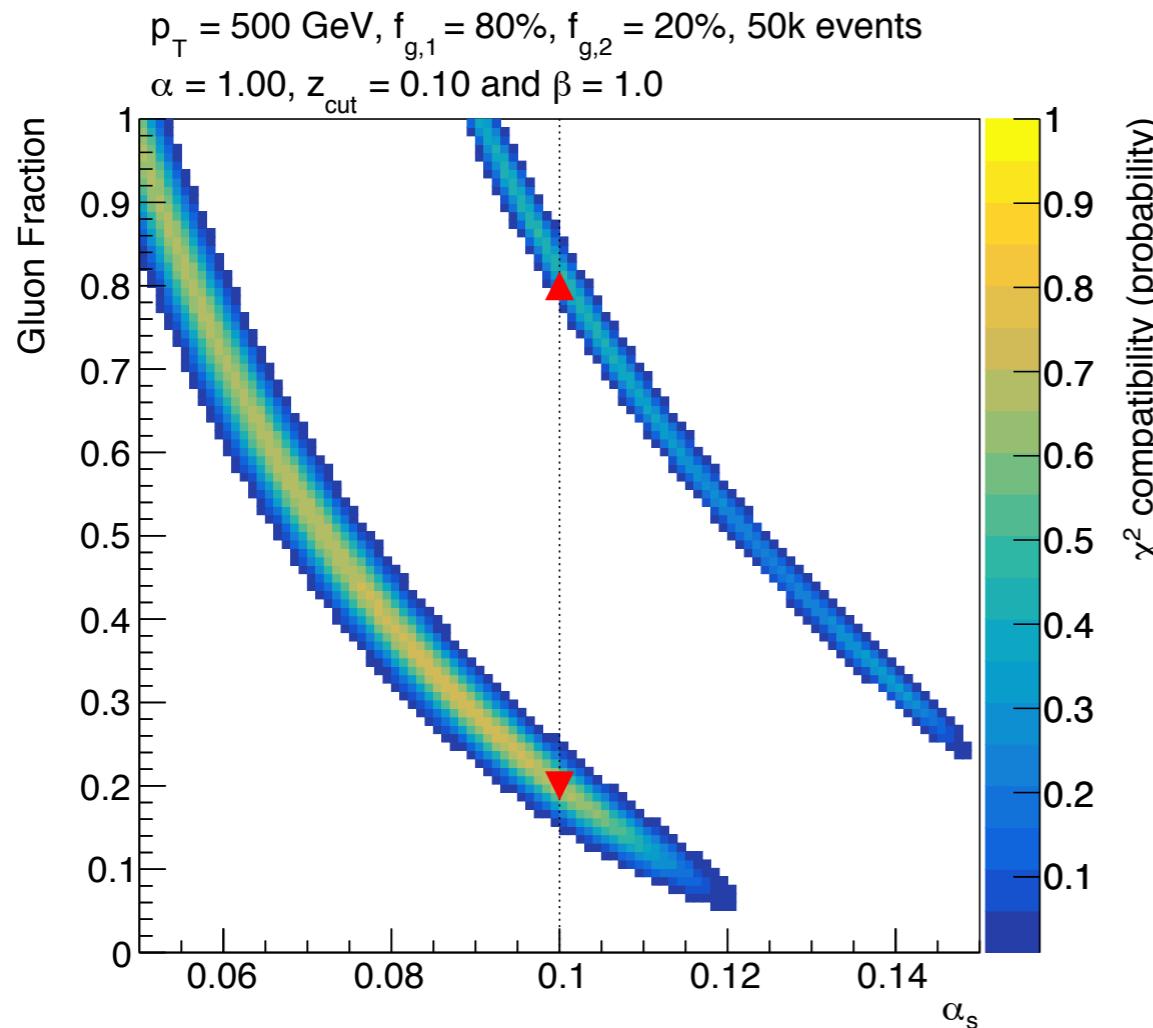
# The Next Precision Frontier

## Extract Strong Coupling Constant from Jet Substructure



[see Moult, Nachman, Soyez, JDT, Chatterjee, Dreyer, Vittoria Garzelli, Gras, Larkoski, Marzani, Siódmok, Papaefstathiou, Richardson, Samui, in 1803.07977]

# Key Issue for Precision Extraction



Correlation between  
quark/gluon fraction and  $\alpha_s$

$$\Sigma(\lambda) \simeq \exp \left[ -\frac{\alpha_s C_i}{\pi} \log^2(\lambda) \right]$$

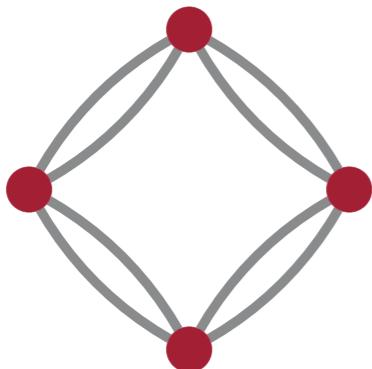
Introduces residual dependence on PDFs

By construction, jet topics  
are fraction independent

With or without mutual irreducibility

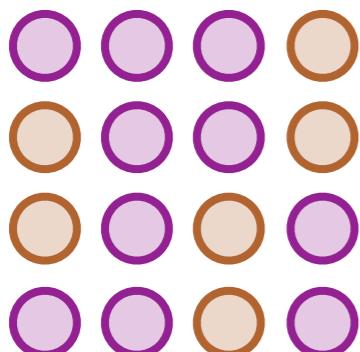
[see Moult, Nachman, Soyez, JDT, Chatterjee, Dreyer, Vittoria Garzelli, Gras, Larkoski, Marzani, Siódmok, Papaefstathiou, Richardson, Samui, in 1803.07977]

# Summary



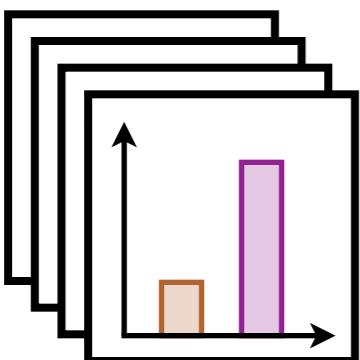
## A Basis for Jet Substructure

*Energy flow polynomials for linear classification*



## Learning Without Labels

*Data-driven classifiers from mixed samples*



## Introducing Jet Topics

*Defining jet categories by mutual irreducibility*

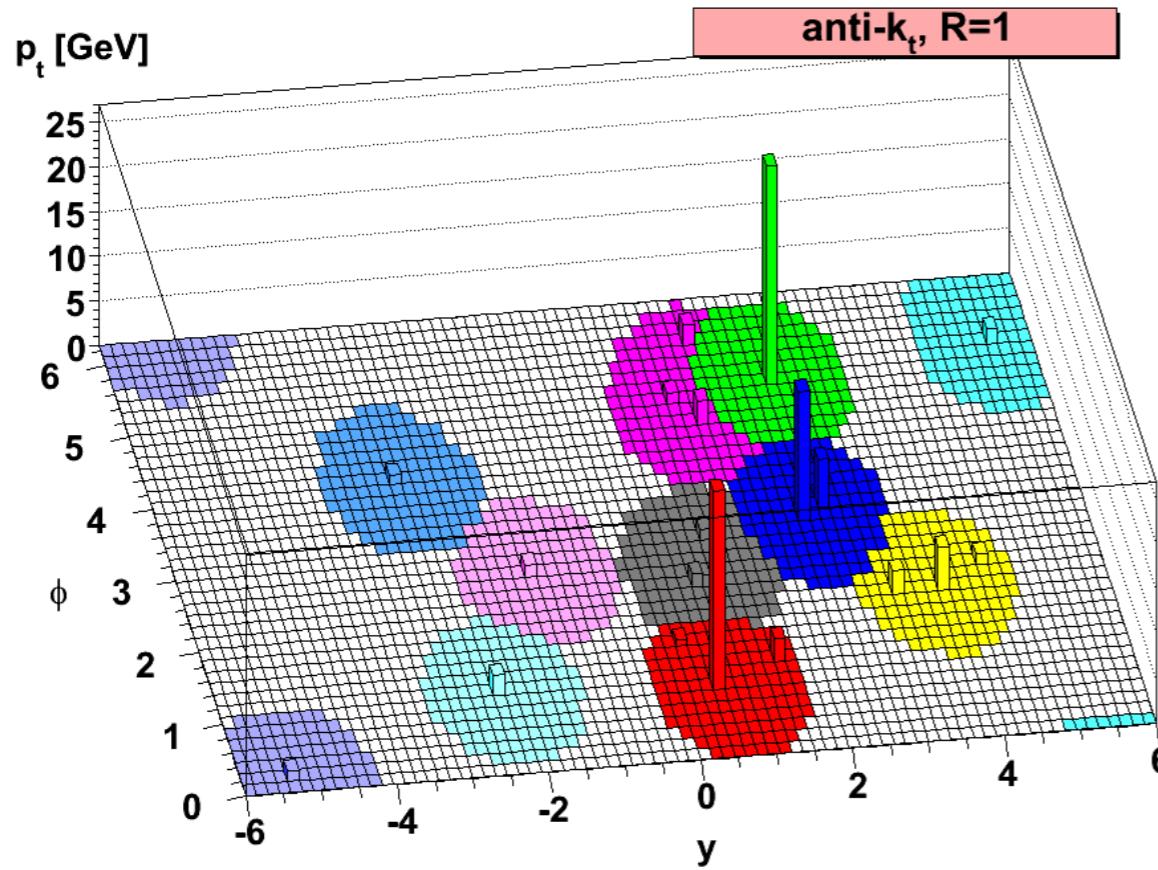
“Deep Learning” & “Deep Thinking”  
~~vs.~~

New first-principles studies of QCD  
facilitated by advances in  
statistics, mathematics, and computer science

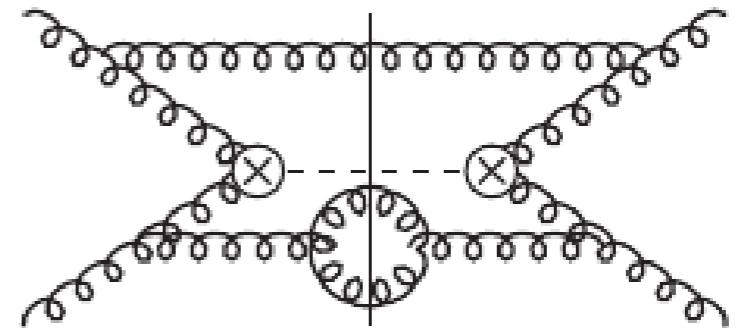
# *Backup Slides*

# A QCD Renaissance

Theory c. 2008–present



New Jet Algorithms



Loop/Leg/Log Explosion

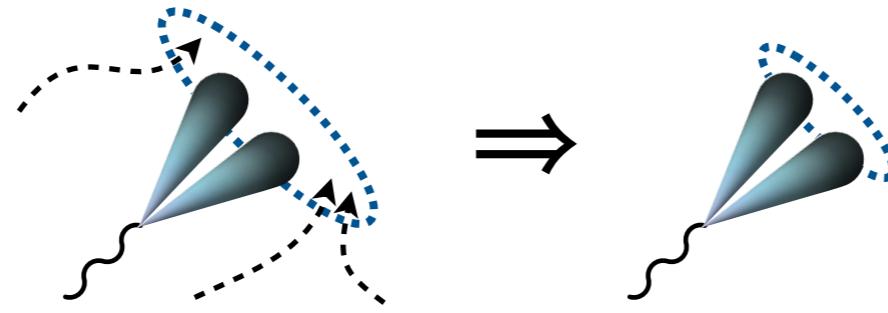


Jet Substructure

[Anti- $k_t$ : Cacciari, Salam, Soyez, 2008; see also Delsart, 2006] [N<sup>3</sup>LO: Anastasiou, Duhr, Dulat, Herzog, Mistlberger, 2015]  
[BDRS: Butterworth, Davison, Rubin, Salam, 2008; see also Seymour, 1991, 1994]

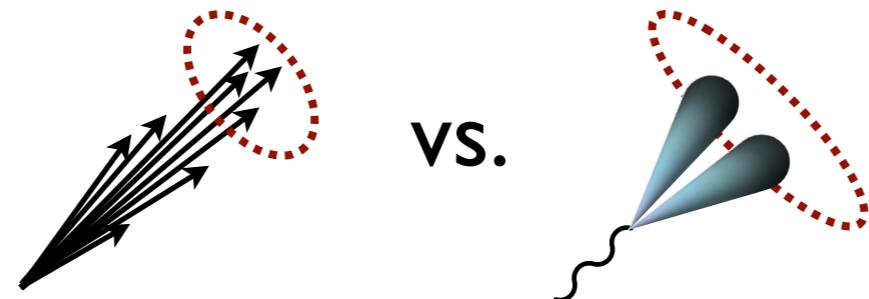
# The Substructure Toolbox

## Grooming: e.g. ISR/UE/pileup



[Mass Drop/Filtering, Trimming, Pruning, Soft Drop, Jet Reclustering...;  
for pileup: Area Subtraction, Jet Cleansing, SoftKiller, PUPPI,  
Constituent Subtraction, PUMML...]

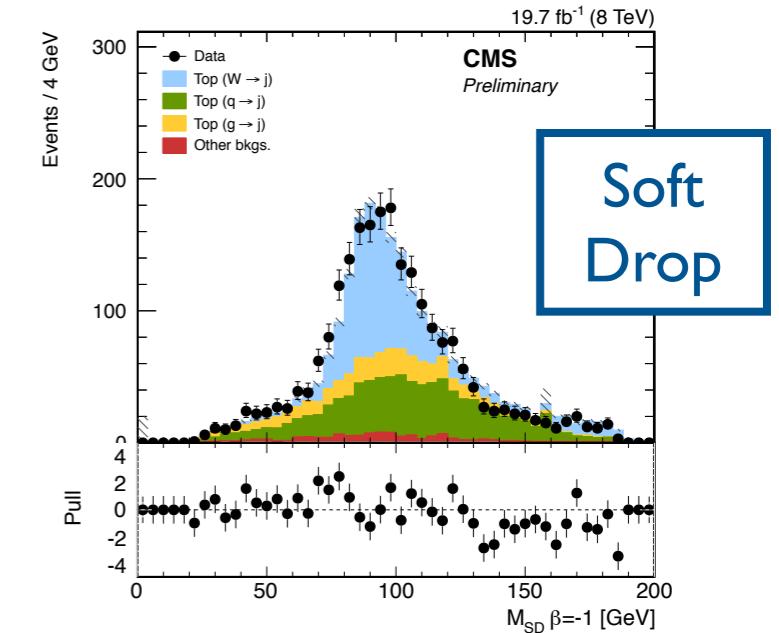
## Discrimination: e.g. 1-prong vs. N-prong



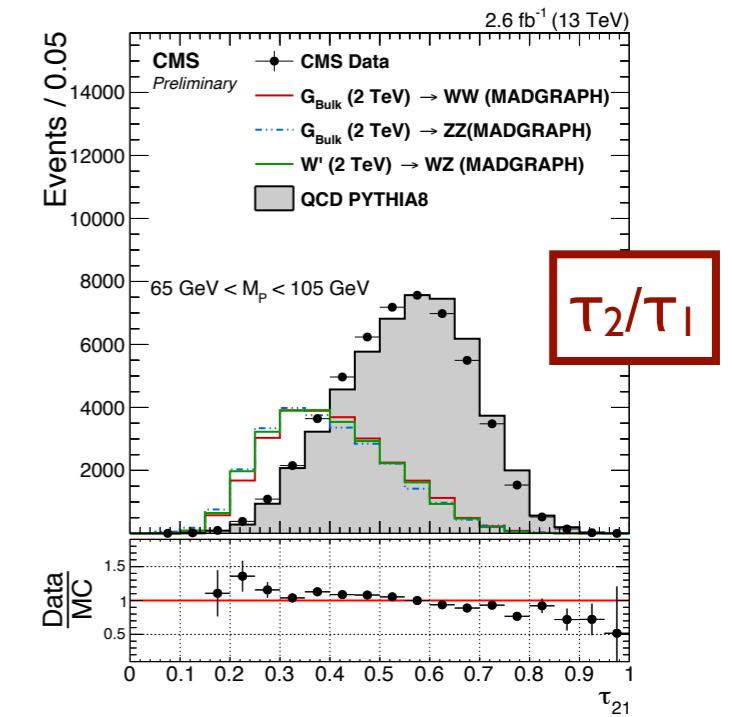
[ $p_T$  Balance, Y-splitter, Angularities, Planar Flow, N-subjettiness, Angular Structure Functions, Jet Charge, Jet Pull, Energy Correlation Functions, Dipolarity,  $p_T^D$ , Zernike Coefficients, LHA, Fox-Wolfram Moments, JHU/CMS Top Tagger, HEPTopTagger, Template Method, Shower Deconstruction, Subjet Counting, Wavelets, Q-Jets, Telescoping Jets, Deep Learning...]

## W/Z-Tagging @ CMS

[JME-14-002, CMS-PAS-EXO-15-002]



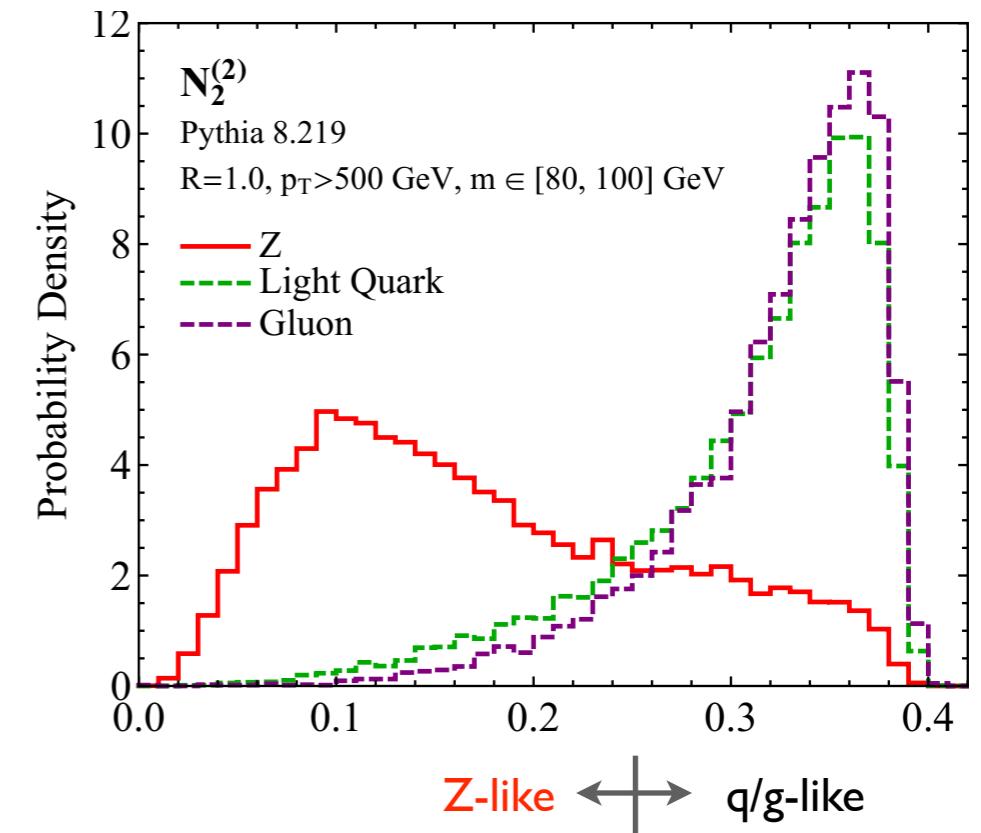
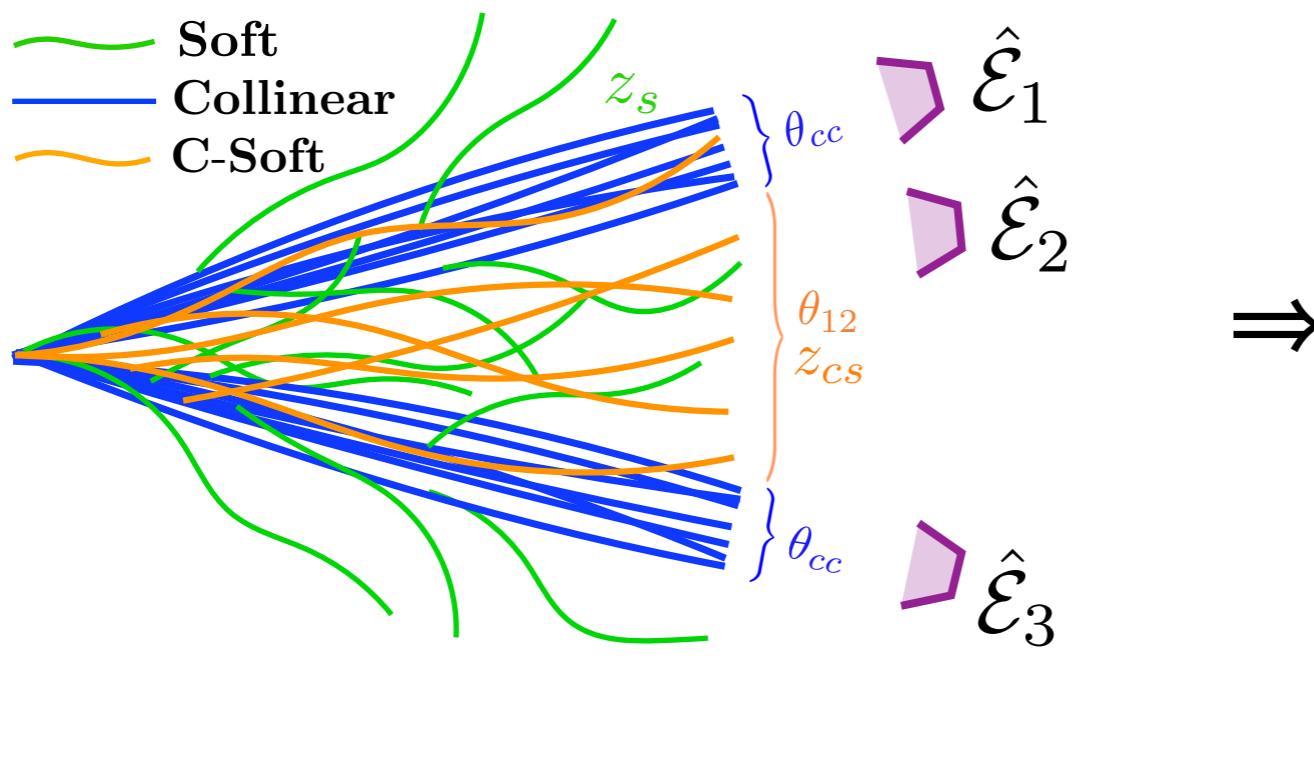
[using Larkoski, Marzani, Soyez, JDT, 1402.2657]



[using JDT, Van Tilburg, 1011.2268, 1108.2701]

# 2-prong Discrimination with Energy Correlators

$$N_2 = \frac{\sum_{i < j < k} p_{Ti} p_{Tj} p_{Tk} \min \left\{ (R_{ij} R_{jk})^2, (R_{jk} R_{ki})^2, (R_{ki} R_{ij})^2 \right\}}{\left( \sum_{i < j} p_{Ti} p_{Tj} R_{ij}^2 \right)^2 / \sum_i p_{Ti}}$$



[Moult, Necib, JDT, 1609.07483; based on Larkoski, Salam, JDT, 1305.0007]

# Frequency of Symbols on the arXiv



# arXiv 2.0: Determine categories just from documents? (Without training from hep-ph, hep-ex, etc.)

[Wolfram Summer School, 2017]