

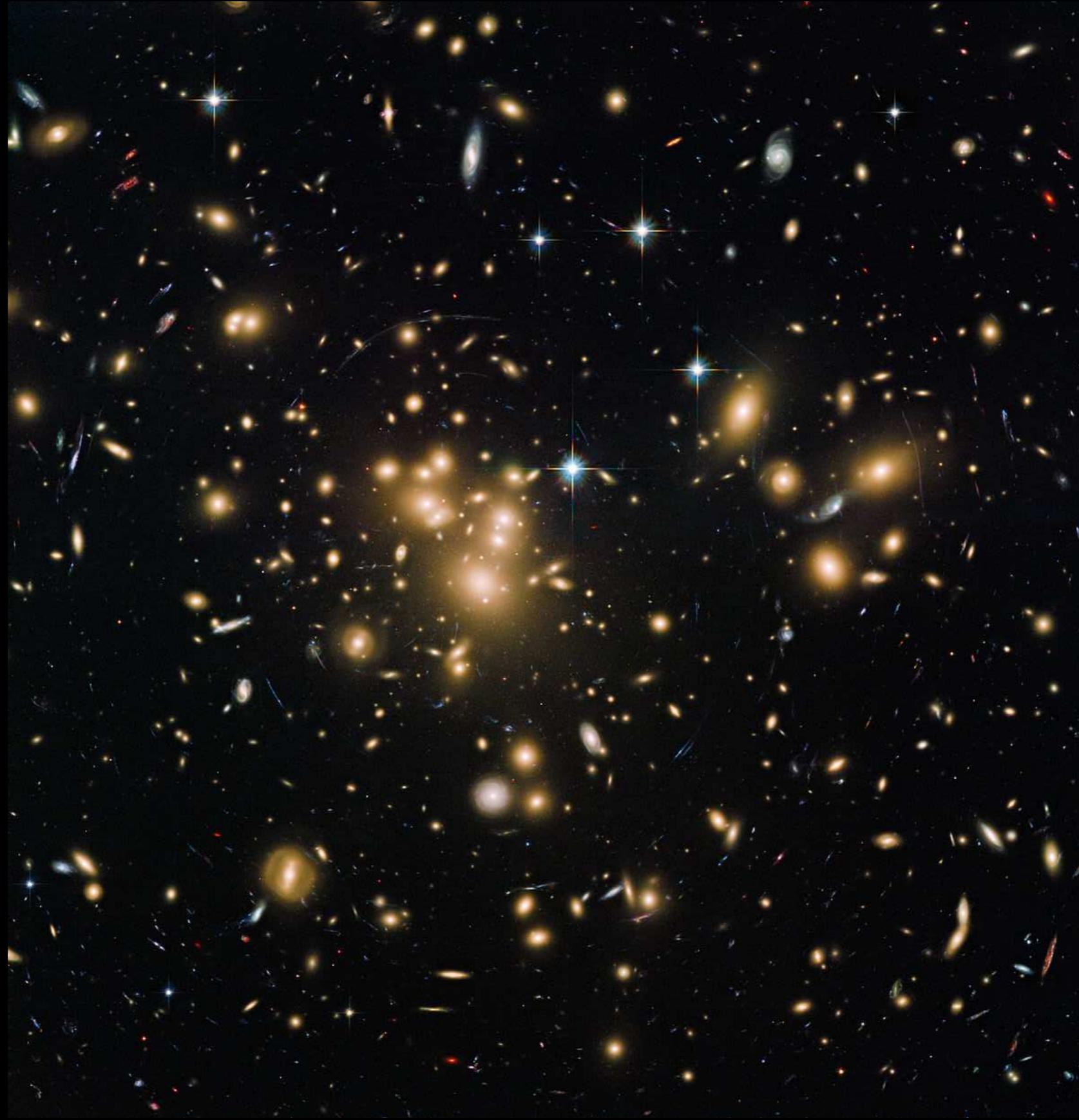
The Space of Collider Events

Jesse Thaler

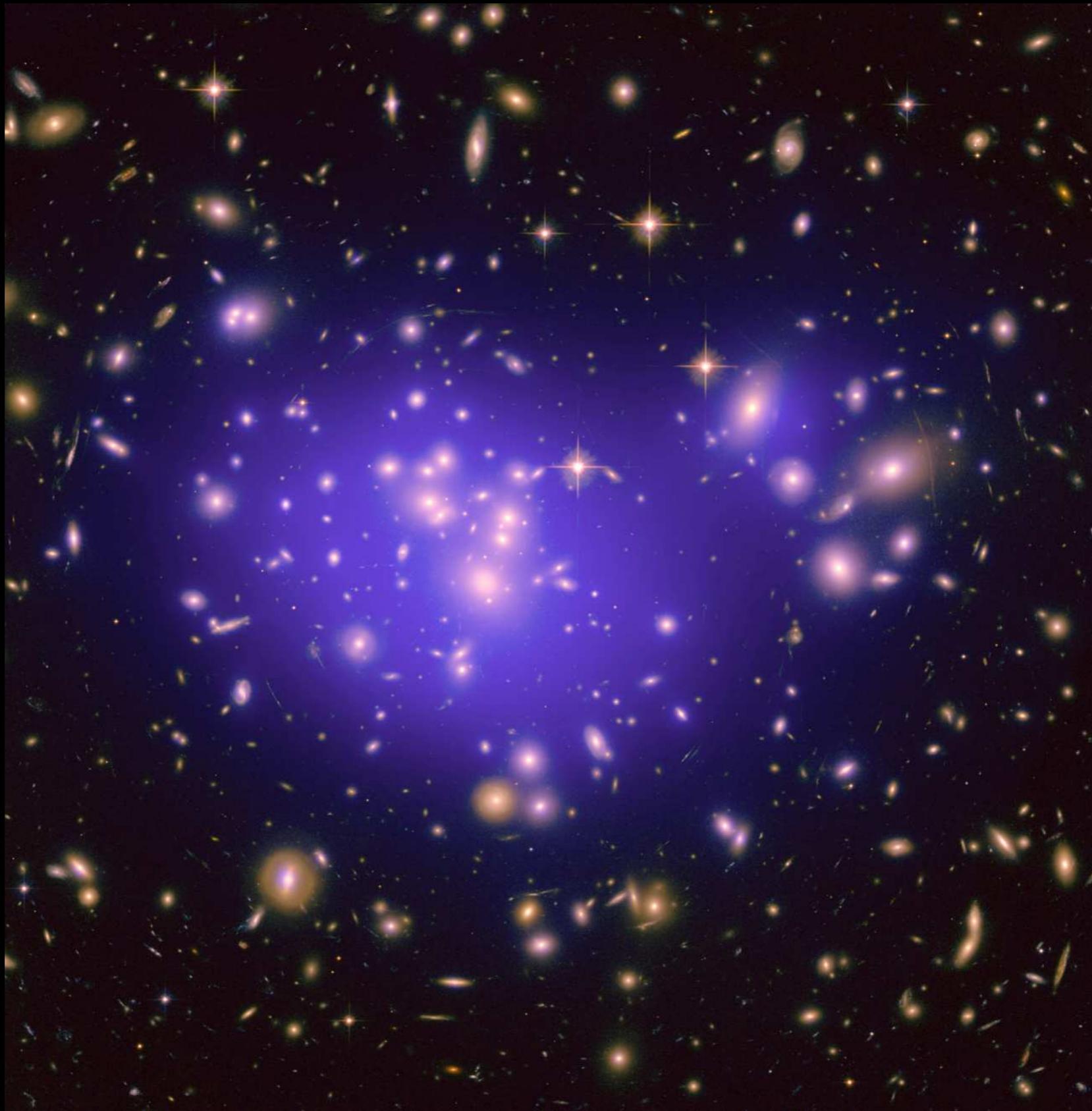


with Patrick Komiske & Eric Metodiev, [1902.02346](#)

EPP Theory Seminar, SLAC — April 24, 2019

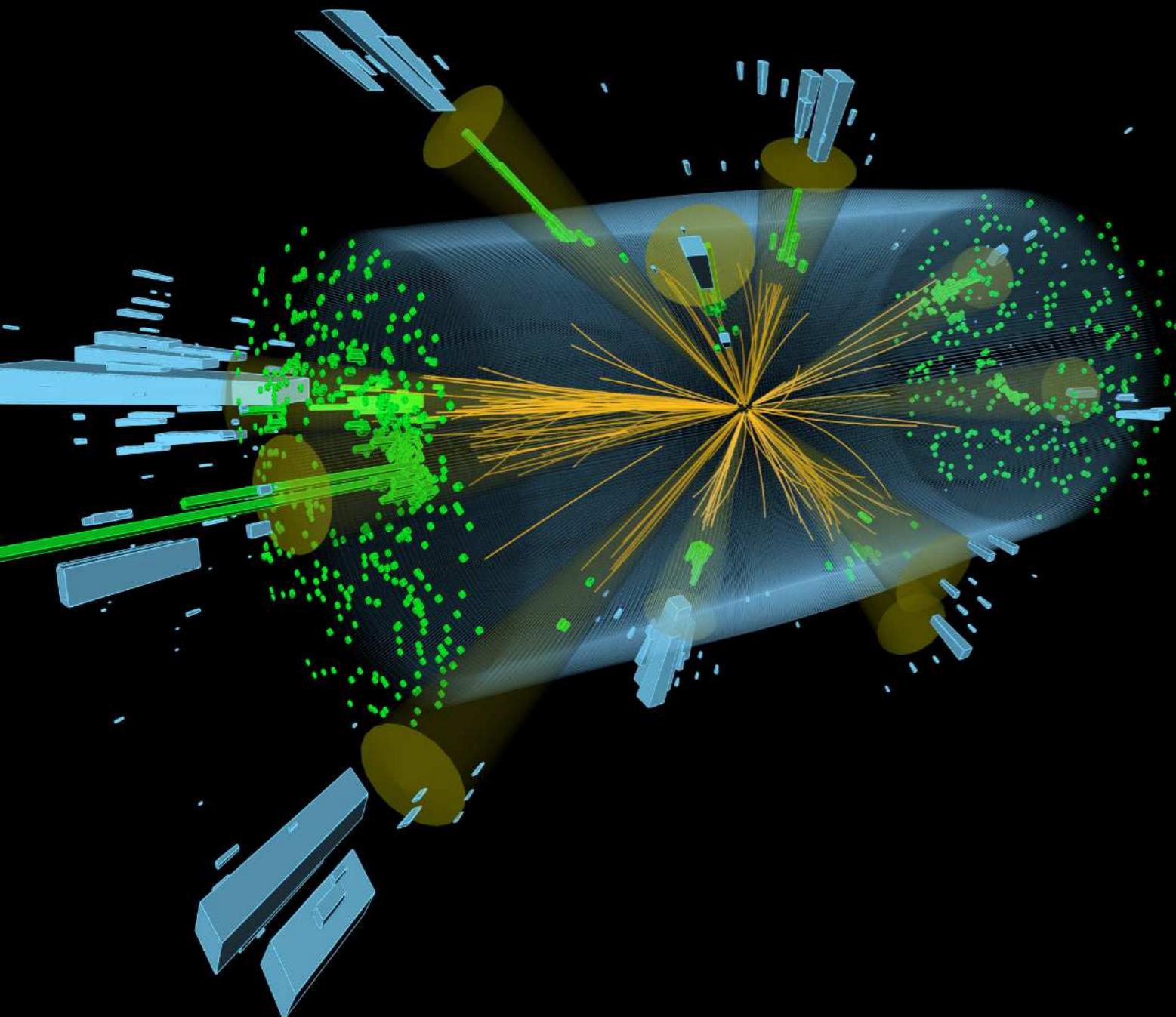


ESA/Hubble: Abell 1689



ESA/Hubble: Abell 1689

Event Displays ...



T E H M

 γ

photon

 e^+

electron

 μ^+

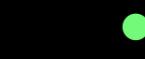
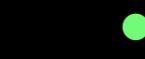
muon

 π^+

pion

 K^+

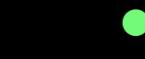
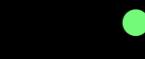
kaon

 K_L^0

K-long

 p/\bar{p}

proton

 n/\bar{n}

neutron

elementary

composite

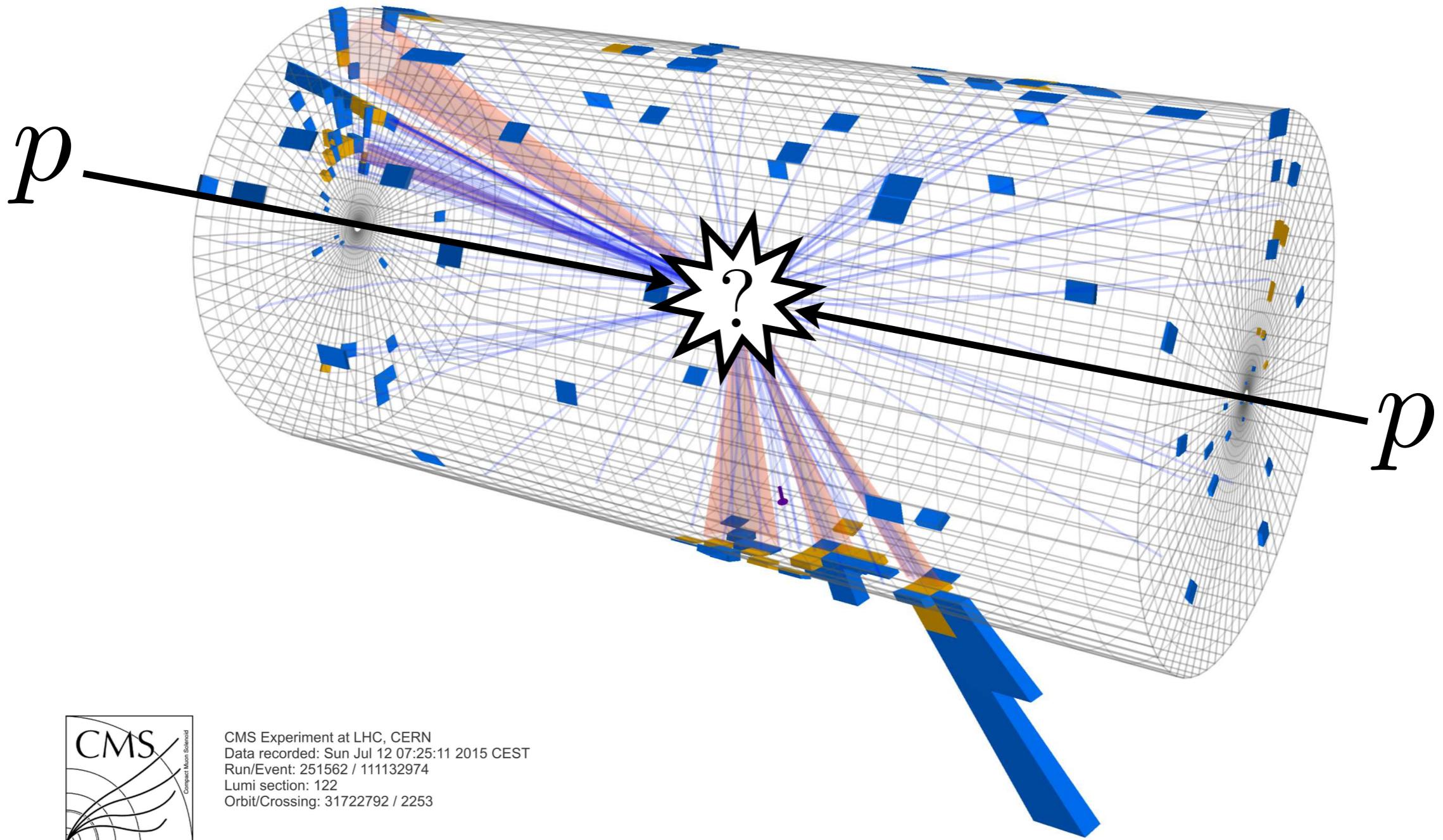
Event Displays (for an Event)



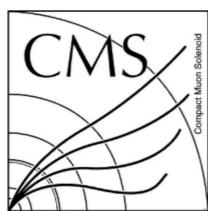
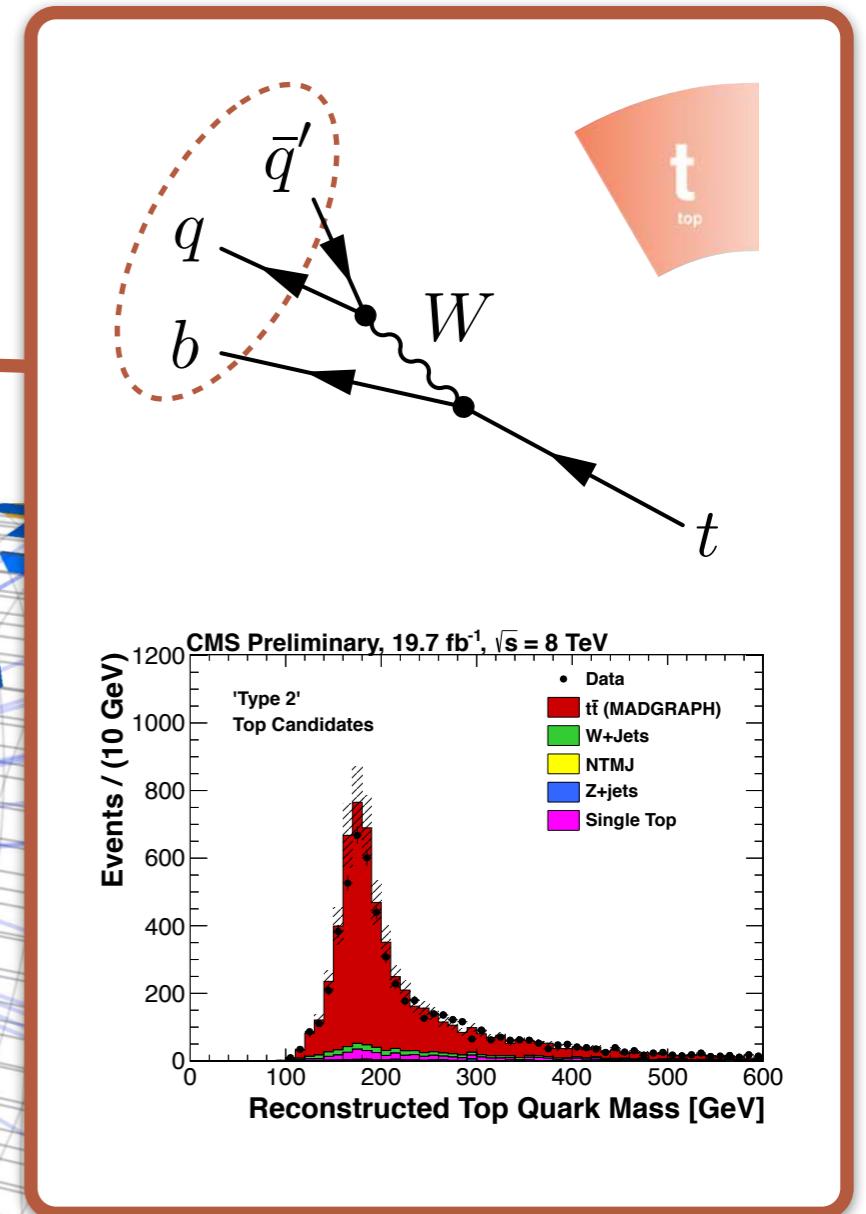
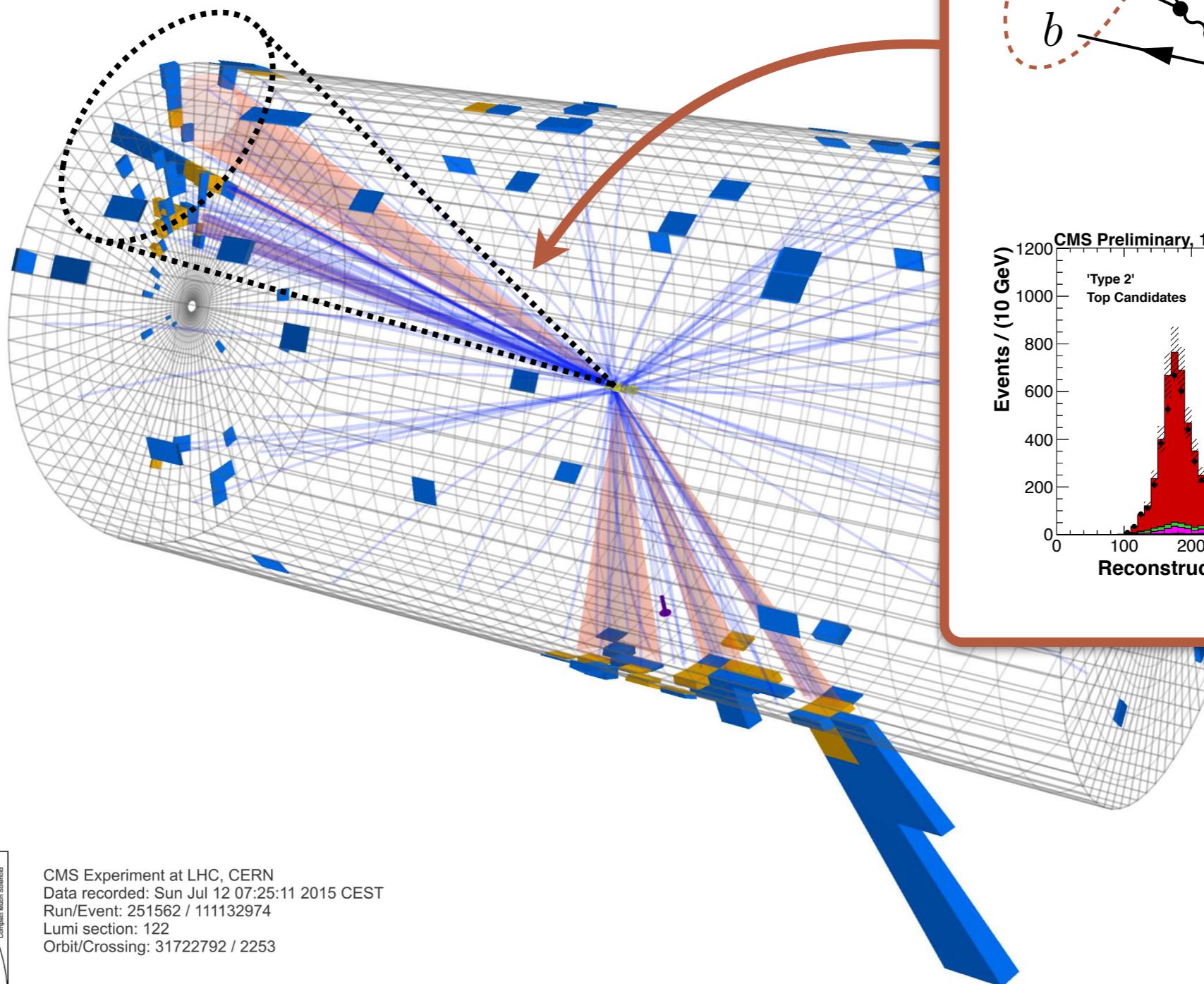
BOOST 2019

[[BOOST 2019](#): July 22-26, 2019, MIT]

Science in the Visualization?

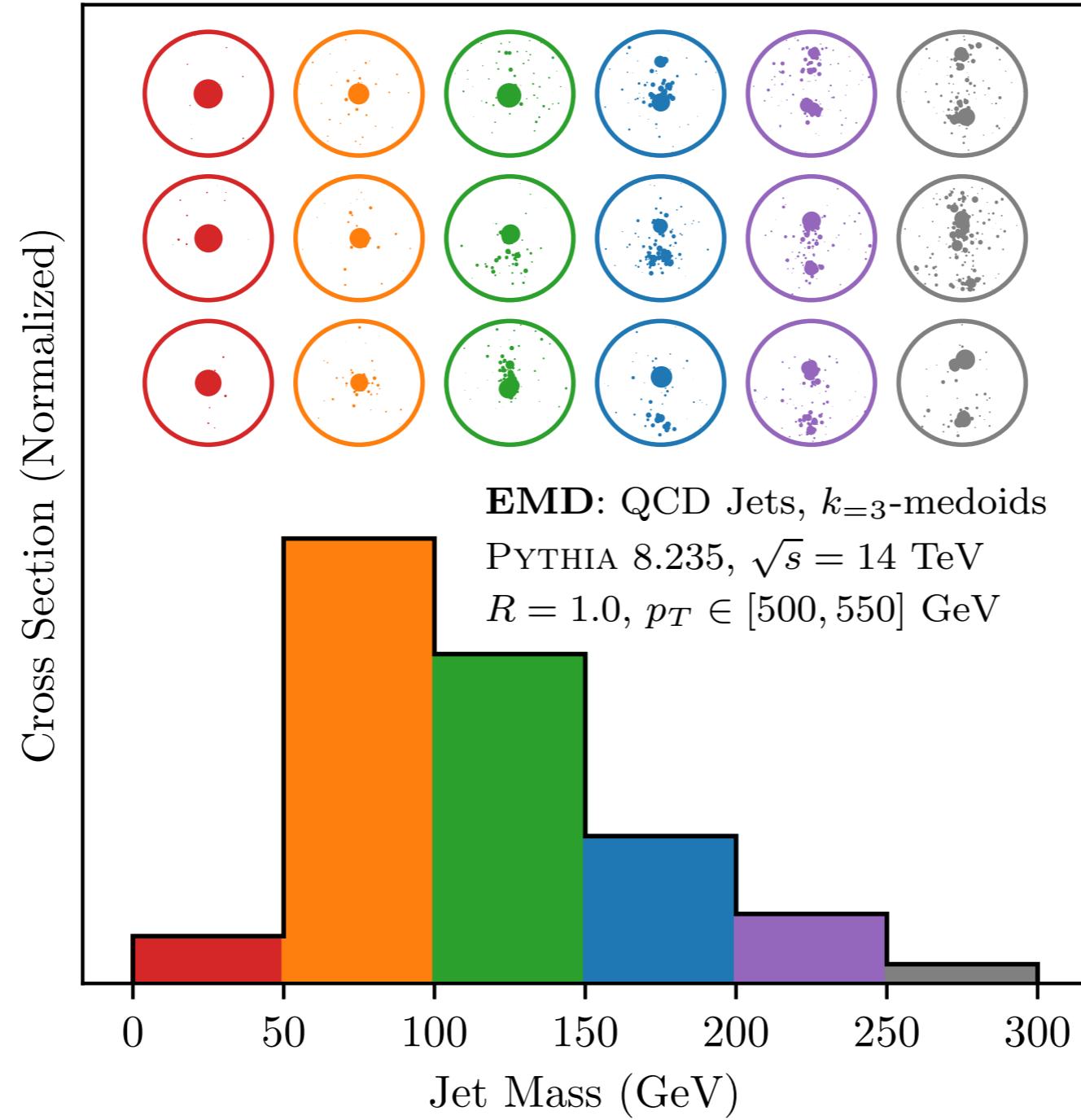
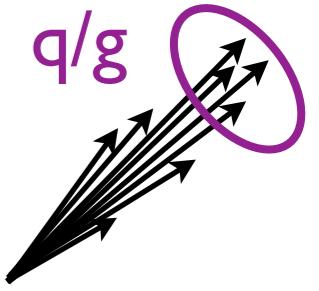


Science in the Visualization?



CMS Experiment at LHC, CERN
Data recorded: Sun Jul 12 07:25:11 2015 CEST
Run/Event: 251562 / 111132974
Lumi section: 122
Orbit/Crossing: 31722792 / 2253

My New Favorite Histogram

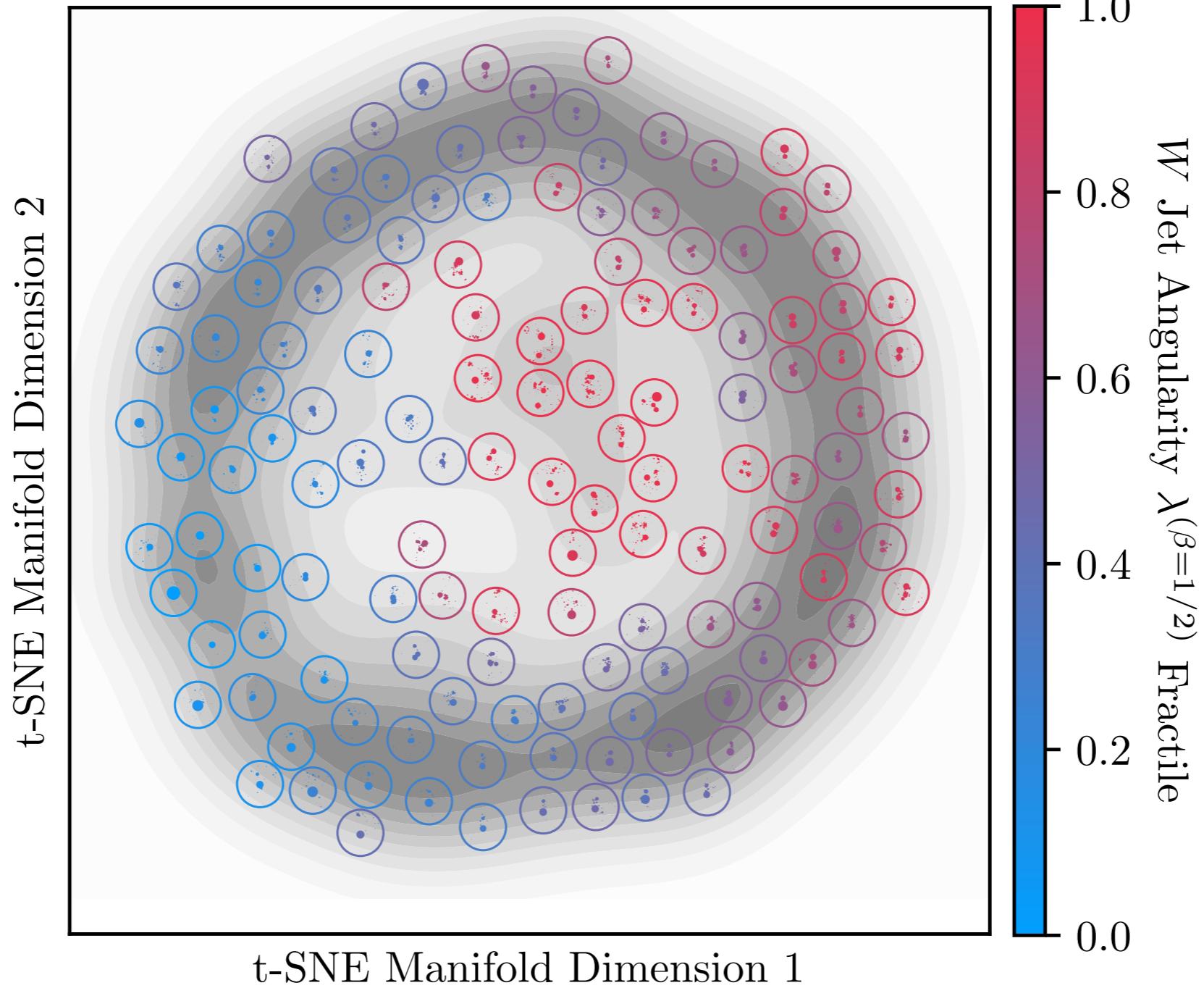
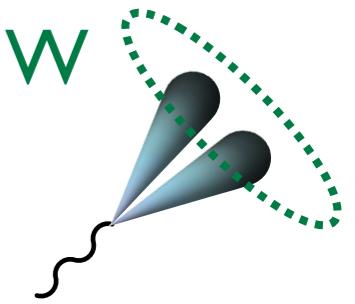


Three most
representative
jets in each bin



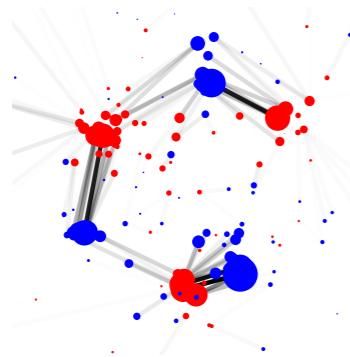
[Komiske, Metodiev, JDT, [1902.02346](#)]

The Space of Boosted W Bosons

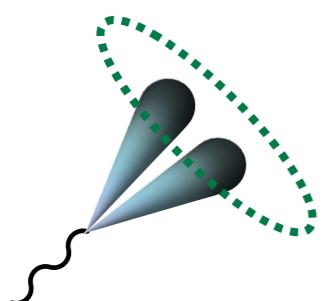


[Komiske, Metodiev, JDT, [1902.02346](#)]

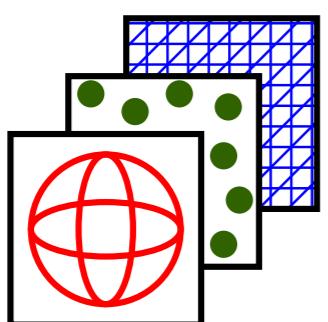
Outline



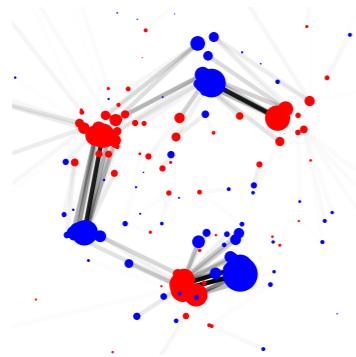
The Energy Mover's Distance



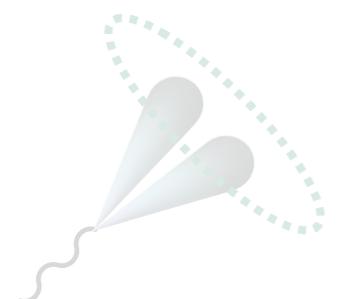
Initial Physics Studies



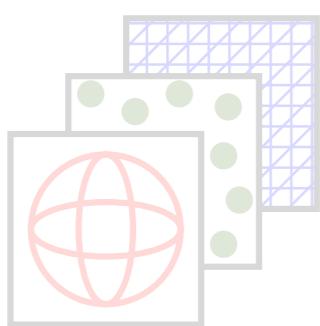
(Broader Comments)



The Energy Mover's Distance

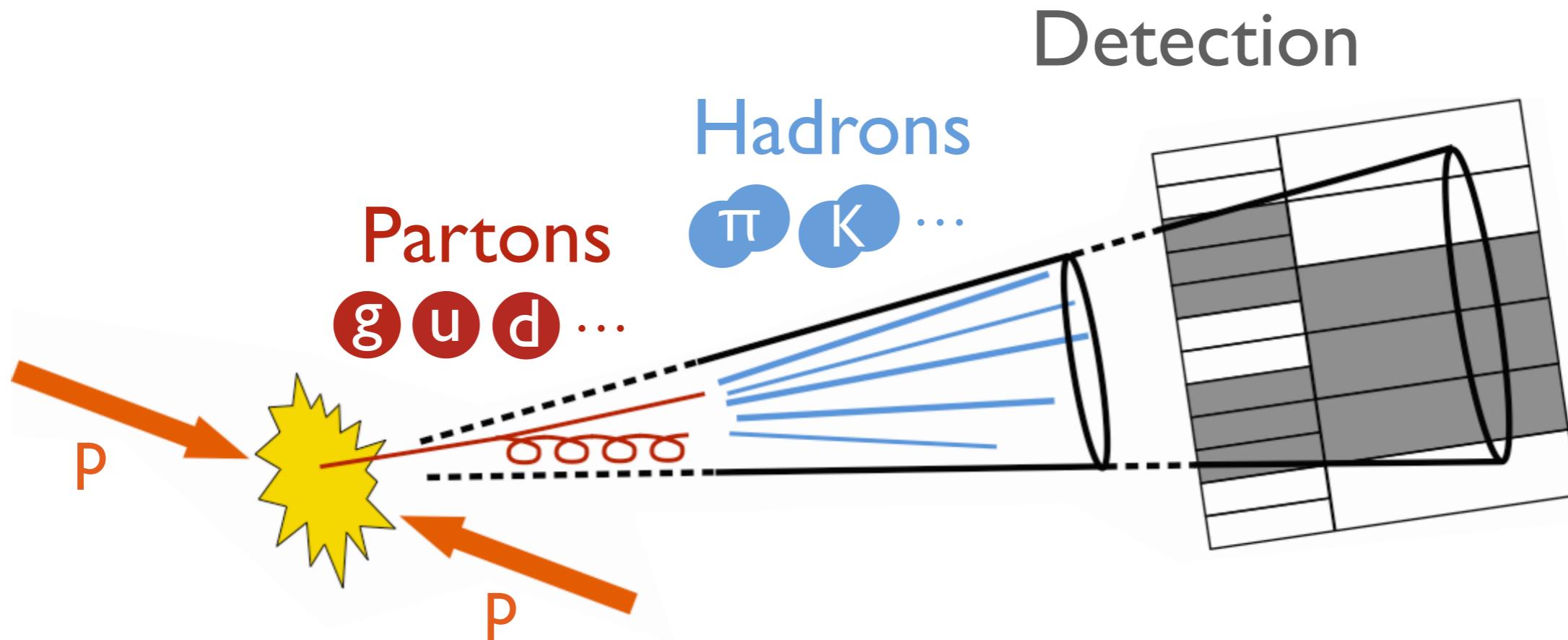


Initial Physics Studies



(Broader Comments)

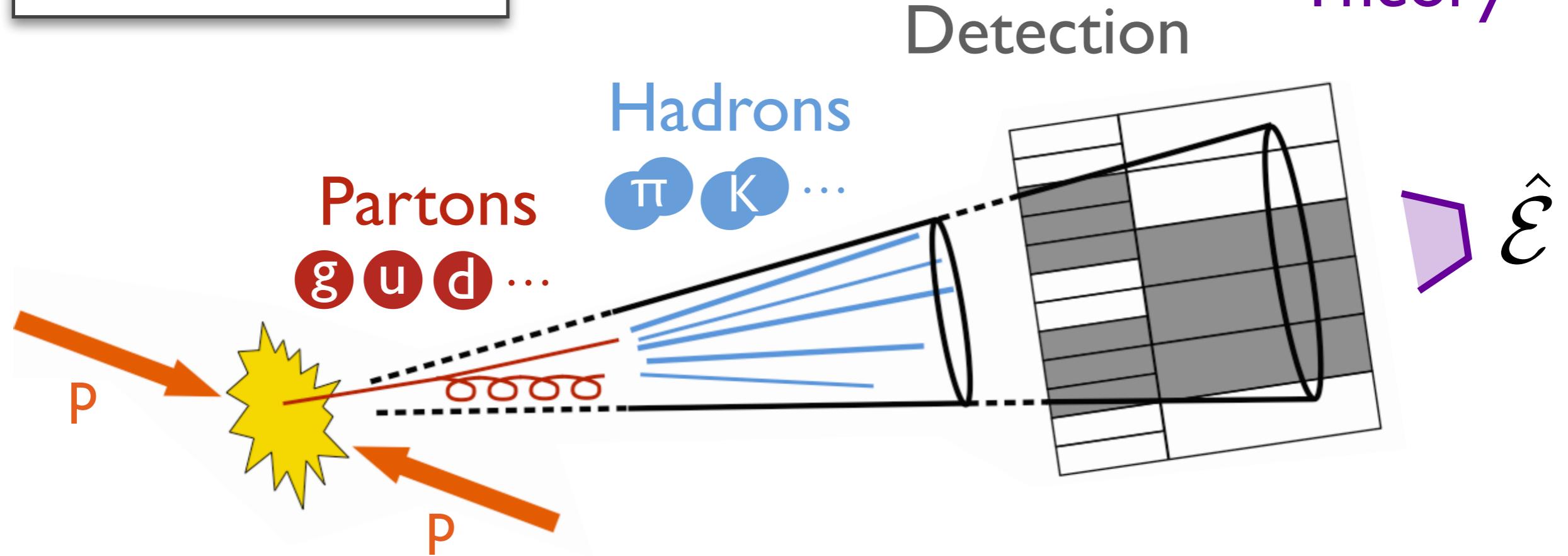
Focus on Energy Flow



[Sveshnikov, Tkachov, [hep-ph/9512370](#); Hofman, Maldacena, [0803.1467](#); Mateu, Stewart, JDT, [1209.3781](#); Komiske, Metodiev, JDT, [1712.07124](#), [1810.05165](#)]

Focus on Energy Flow

$$\hat{\mathcal{E}} \simeq \lim_{t \rightarrow \infty} \hat{n}_i T^{0i}(t, vt\hat{n})$$



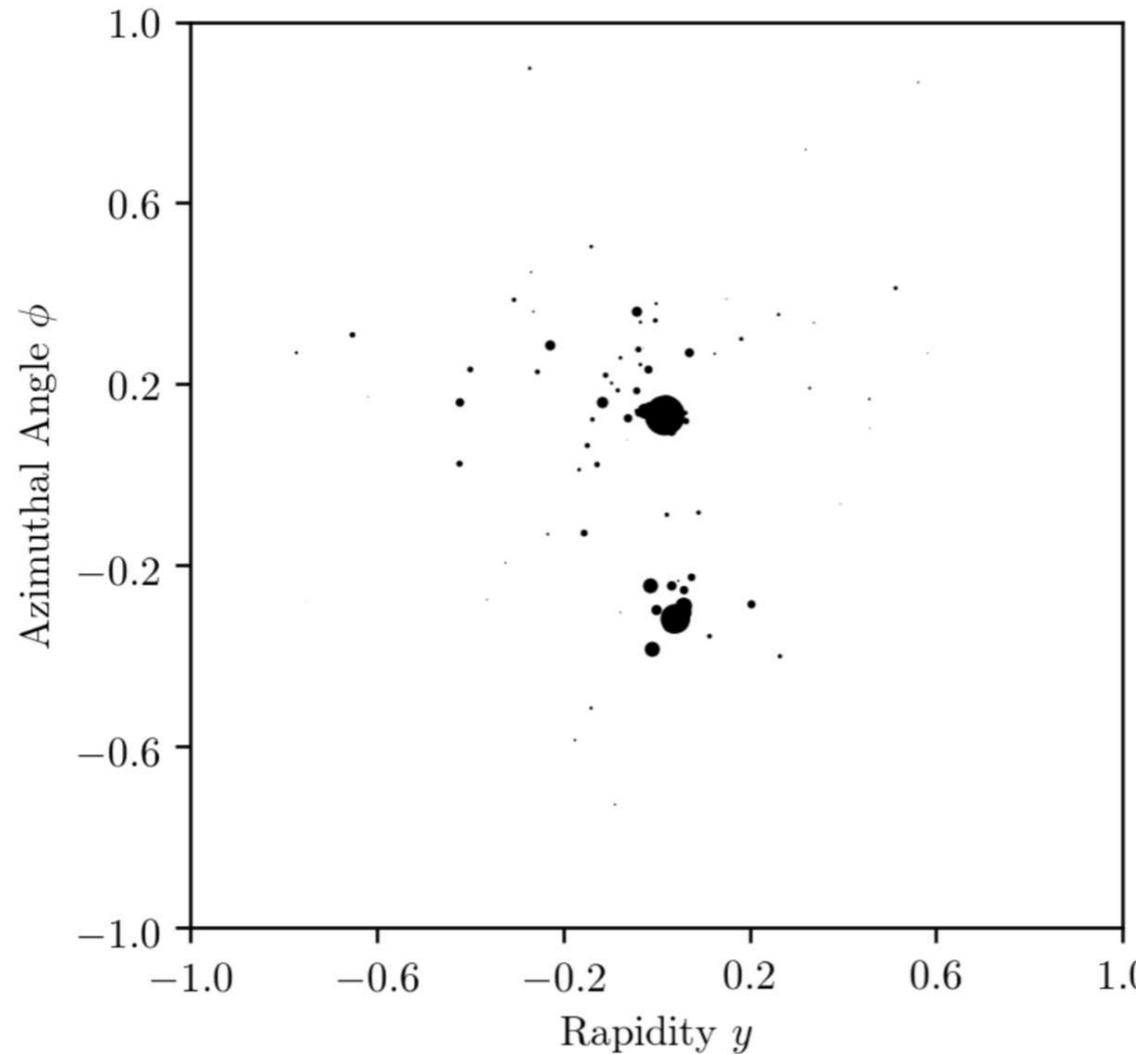
Detection

Theory

*Stress-energy flow: Measure of event/jet structure
robust to non-perturbative and detector effects (i.e. **IRC safe**)*

[Sveshnikov, Tkachov, [hep-ph/9512370](#); Hofman, Maldacena, [0803.1467](#); Mateu, Stewart, JDT, [I209.3781](#); Komiske, Metodiev, JDT, [I712.07124](#), [I810.05165](#)]

Focus on Energy Flow



Represent jet as:

$$\rho(\hat{p}) = \sum_{i \in \text{jet}} E_i \delta(\hat{p} - \hat{p}_i)$$

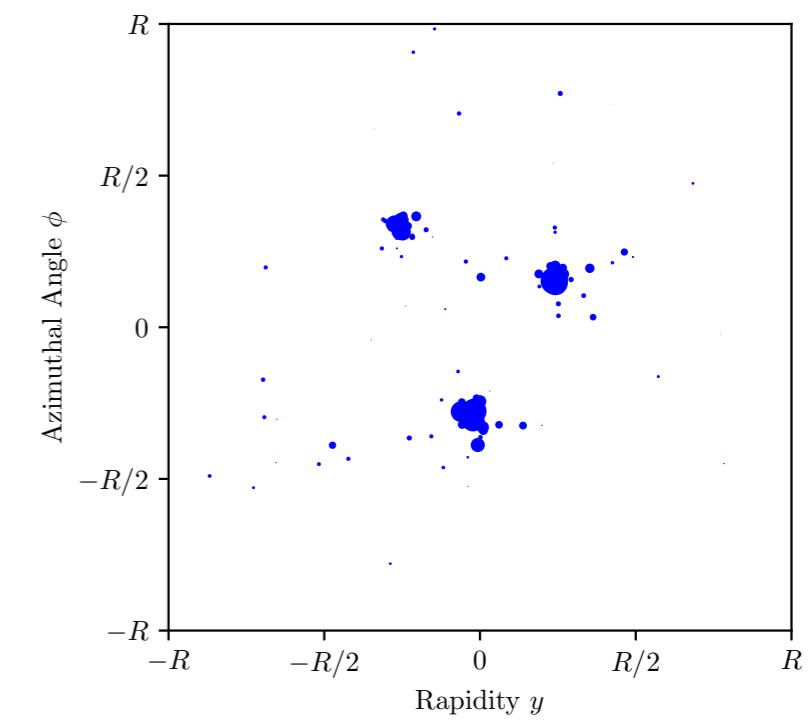
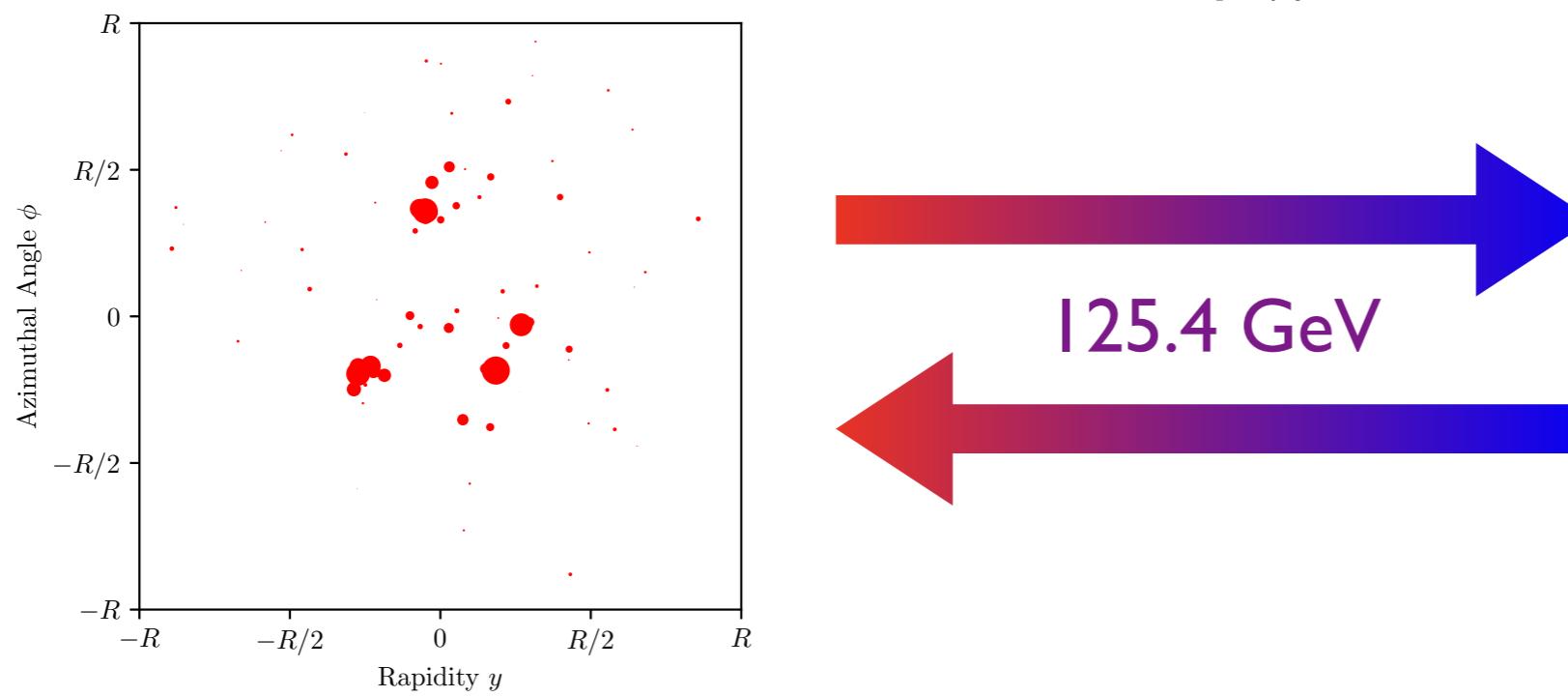
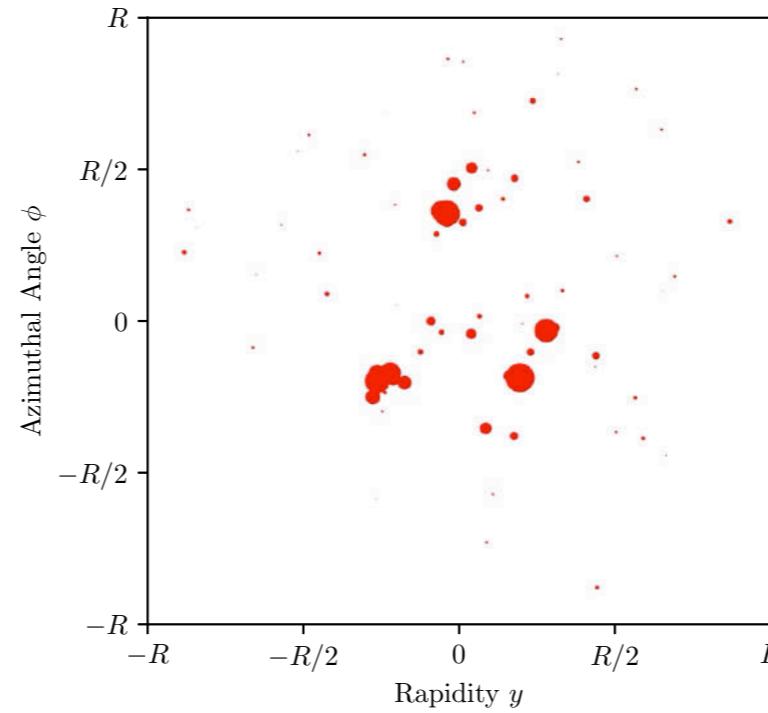
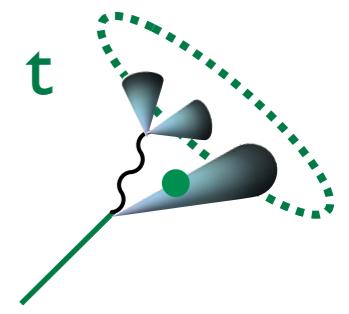
↑
Energy (p_T) ↑
Direction (y, ϕ)

Safe to infrared & collinear splittings
No flavor/charge information
No pixelation needed

*Stress-energy flow: Measure of event/jet structure
robust to non-perturbative and detector effects (i.e. **IRC safe**)*

[Sveshnikov, Tkachov, [hep-ph/9512370](#); Hofman, Maldacena, [0803.1467](#); Mateu, Stewart, JDT, [I209.3781](#); Komiske, Metodiev, JDT, [I712.07124](#), [I810.05165](#)]

Similarity of Two Energy Flows?



[h/t [@pkomiske](#) & [@EricMetodiev](#) for animations]

The Earth Mover's Distance

Optimal Transport:

[Peleg, Werman, Rom, [IEEE 1989](#);
Rubner, Tomasi, Guibas, [ICCV 1998](#), [ICJV 2000](#);
Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]

Minimum “work” (**stuff x distance**) to make
one distribution ...



The Earth Mover's Distance

Optimal Transport:

[Peleg, Werman, Rom, [IEEE 1989](#);
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Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]

Minimum “work” (**stuff** × **distance**) to make
one distribution look like **another distribution**



The Earth Mover's Distance

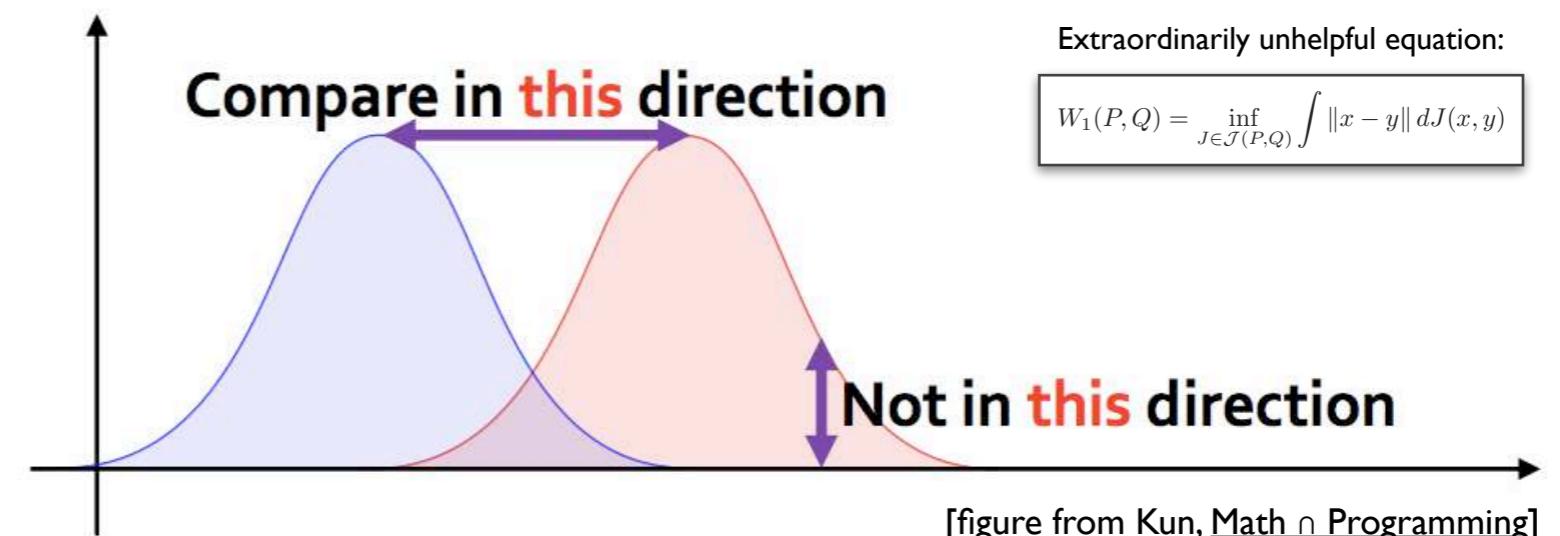
Optimal Transport:

[Peleg, Werman, Rom, [IEEE 1989](#); Rubner, Tomasi, Guibas, [ICCV 1998](#), [ICCV 2000](#); Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]

Minimum “work” (**stuff** × **distance**) to make one distribution look like another distribution

Equivalent to \mathbb{L} -Wasserstein:

Metric on normalized distributions
(symmetric, non-negative,
triangle inequality, zero iff equal)



Very popular in ML applications:

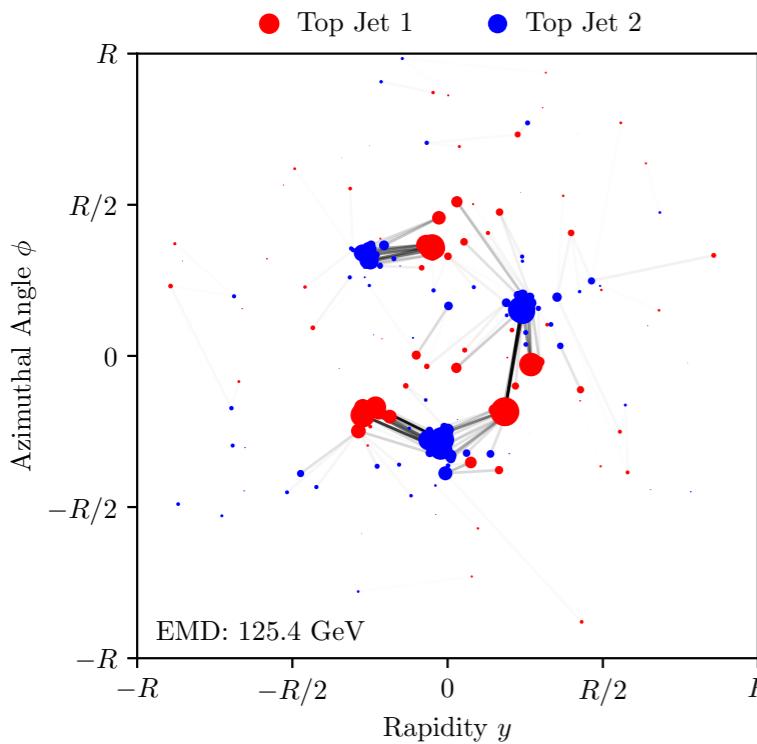
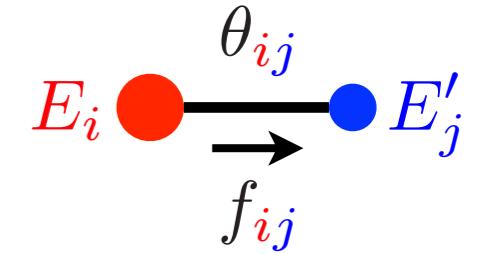
e.g. *Wasserstein Generative Adversarial Networks*

[Arjovsky, Chintala, Bottou, [1701.07875](#);
see also Erdmann, Geiger, Glombitza, Schmidt, [1802.03325](#); Erdmann, Glombitza, Quast, [1807.01954](#)]

e.g. *Wasserstein(-Wasserstein) Autoencoders*

[Tolstikhin, Bousquet, Gelly, Schoelkopf, [1711.01558](#); Zhang, Gao, Jiao, Liu, Wang, Yang, [1902.09323](#)]

The Energy Mover's Distance

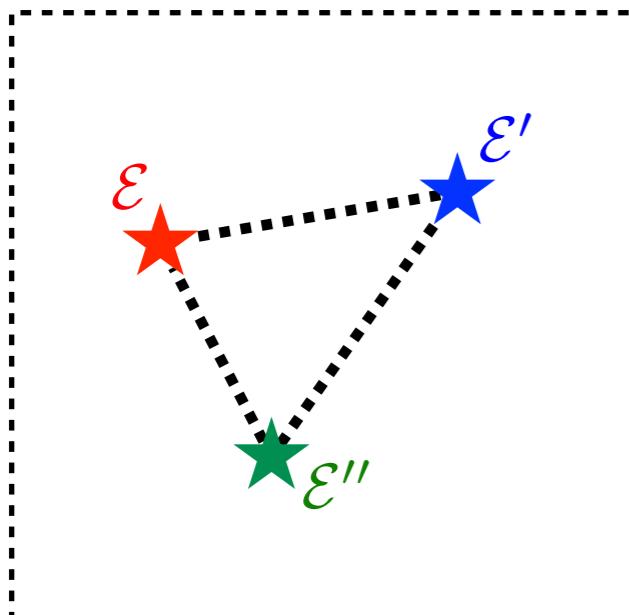


Optimal transport between energy flows...

$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_i \sum_j f_{ij} \frac{\theta_{ij}}{R} + \left| \sum_i E_i - \sum_j E'_j \right|$$

↑
in GeV

Cost to move energy **Cost to create energy**

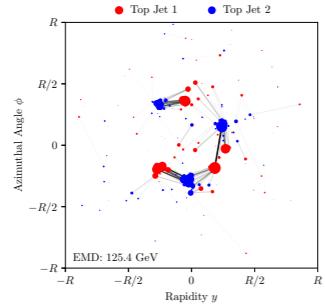


...defines a metric on the space of events

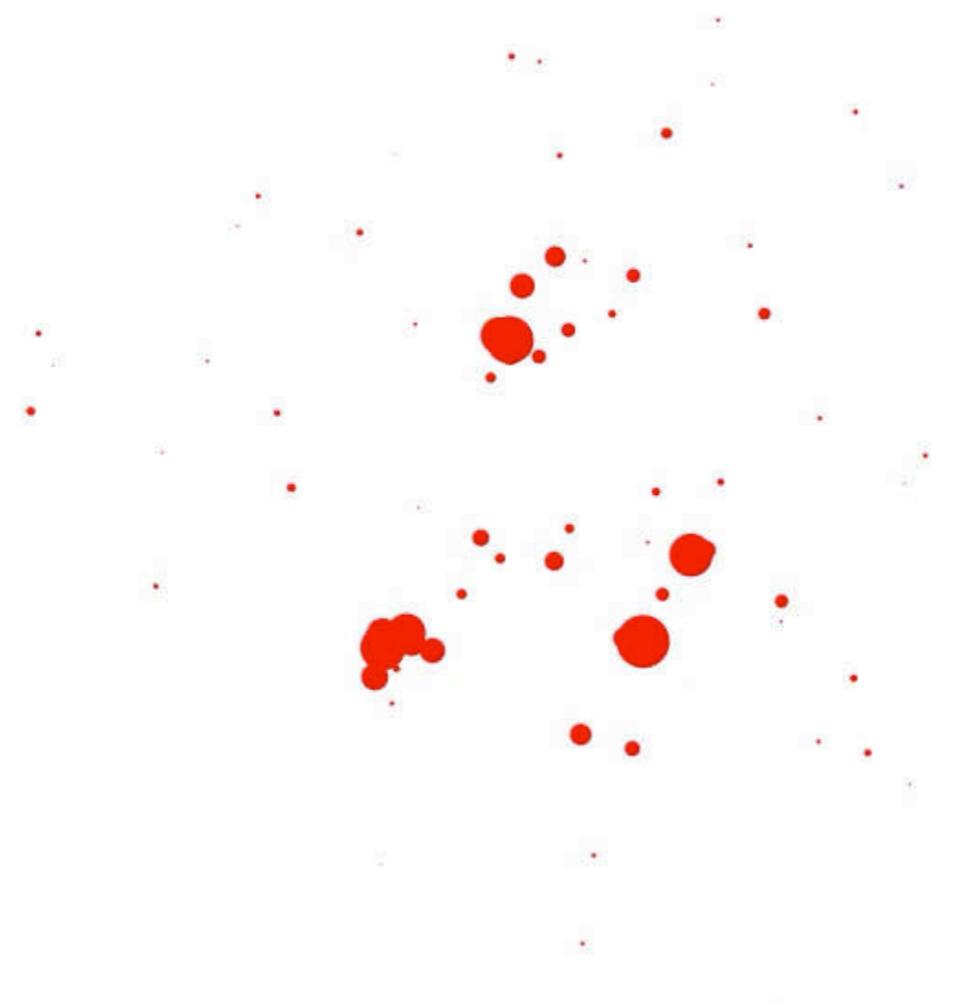
$$0 \leq \text{EMD}(\mathcal{E}, \mathcal{E}') \leq \text{EMD}(\mathcal{E}, \mathcal{E}'') + \text{EMD}(\mathcal{E}', \mathcal{E}'')$$

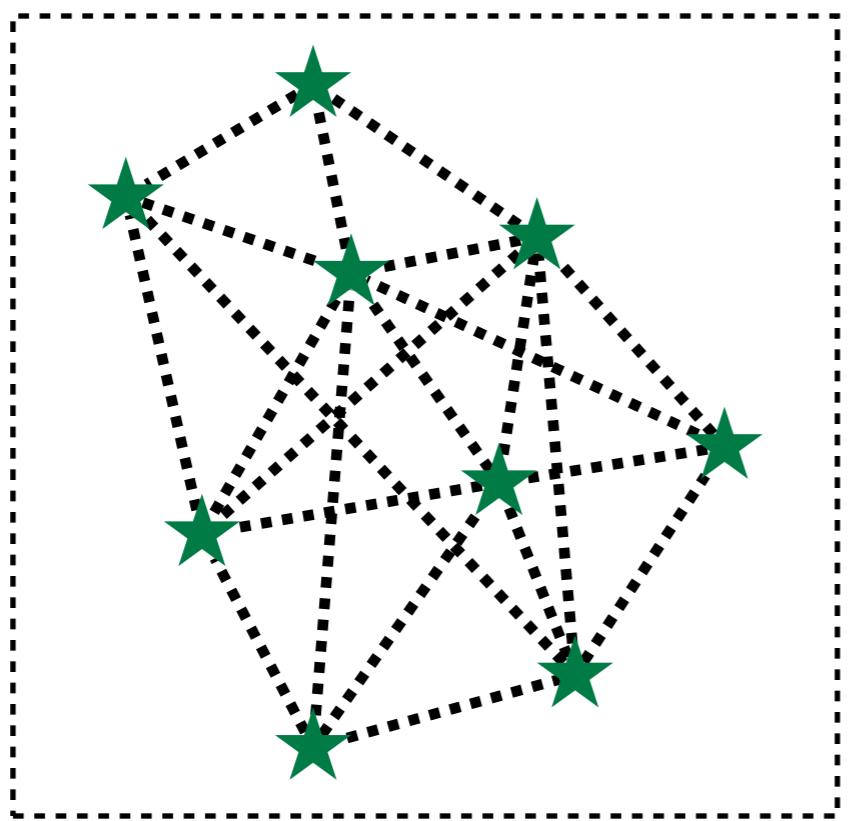
(assuming $R \geq \theta_{\max}/2$, i.e. $R \geq$ jet radius for conical jets)

[Komiske, Metodiev, JDT, [1902.02346](#);
see also Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]



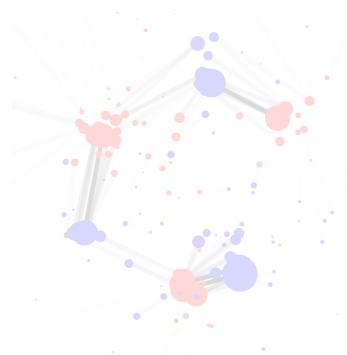
$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_i \sum_j f_{ij} \frac{\theta_{ij}}{R} + \left| \sum_i E_i - \sum_j E'_j \right|$$



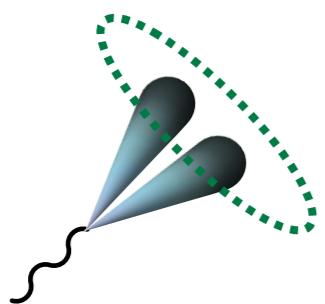


We defined a (metric)
space for collider events

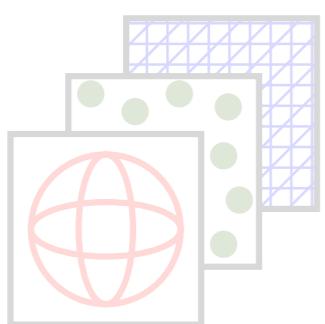
Now what?



The Energy Mover's Distance



Initial Physics Studies



(Broader Comments)

Visualizing Jet Evolution

500 GeV

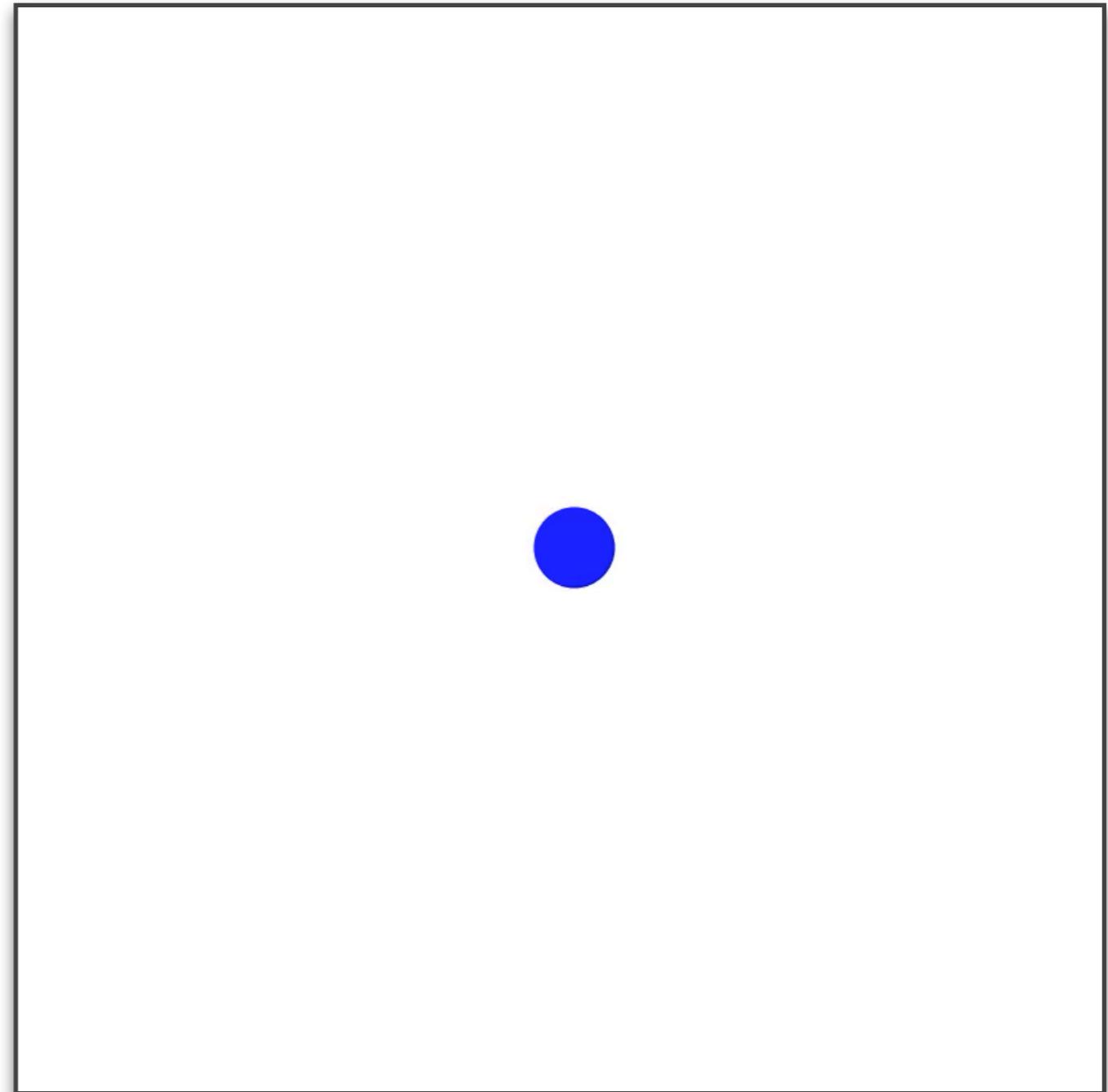
Hard Quark ●

Showering
EMD: 111.6 GeV

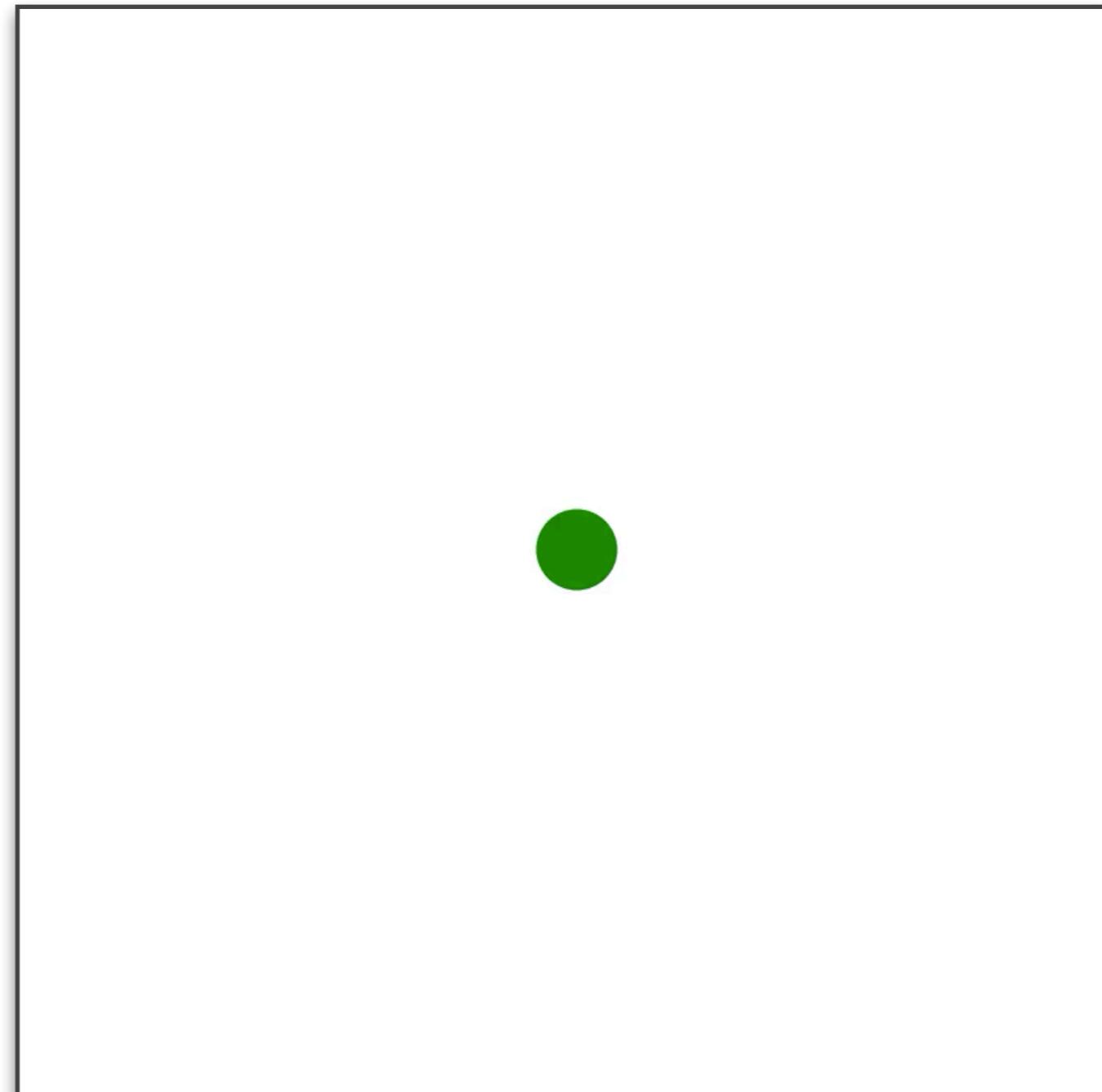
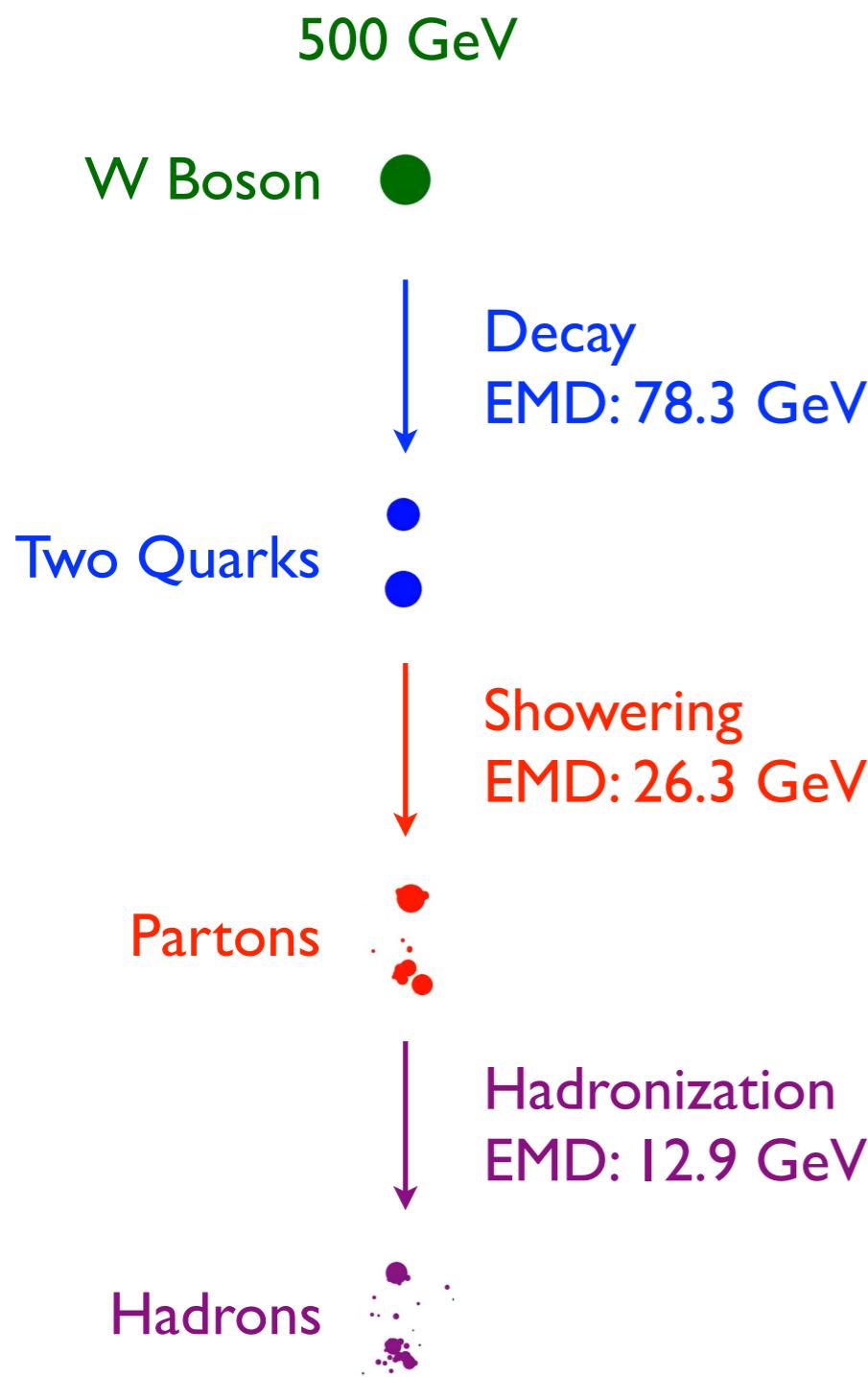
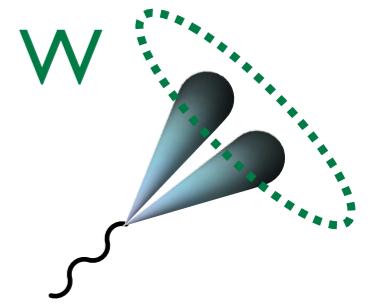
Partons

Hadronization
EMD: 18.1 GeV

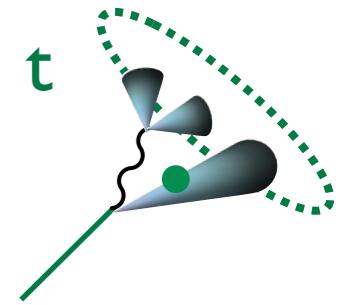
Hadrons



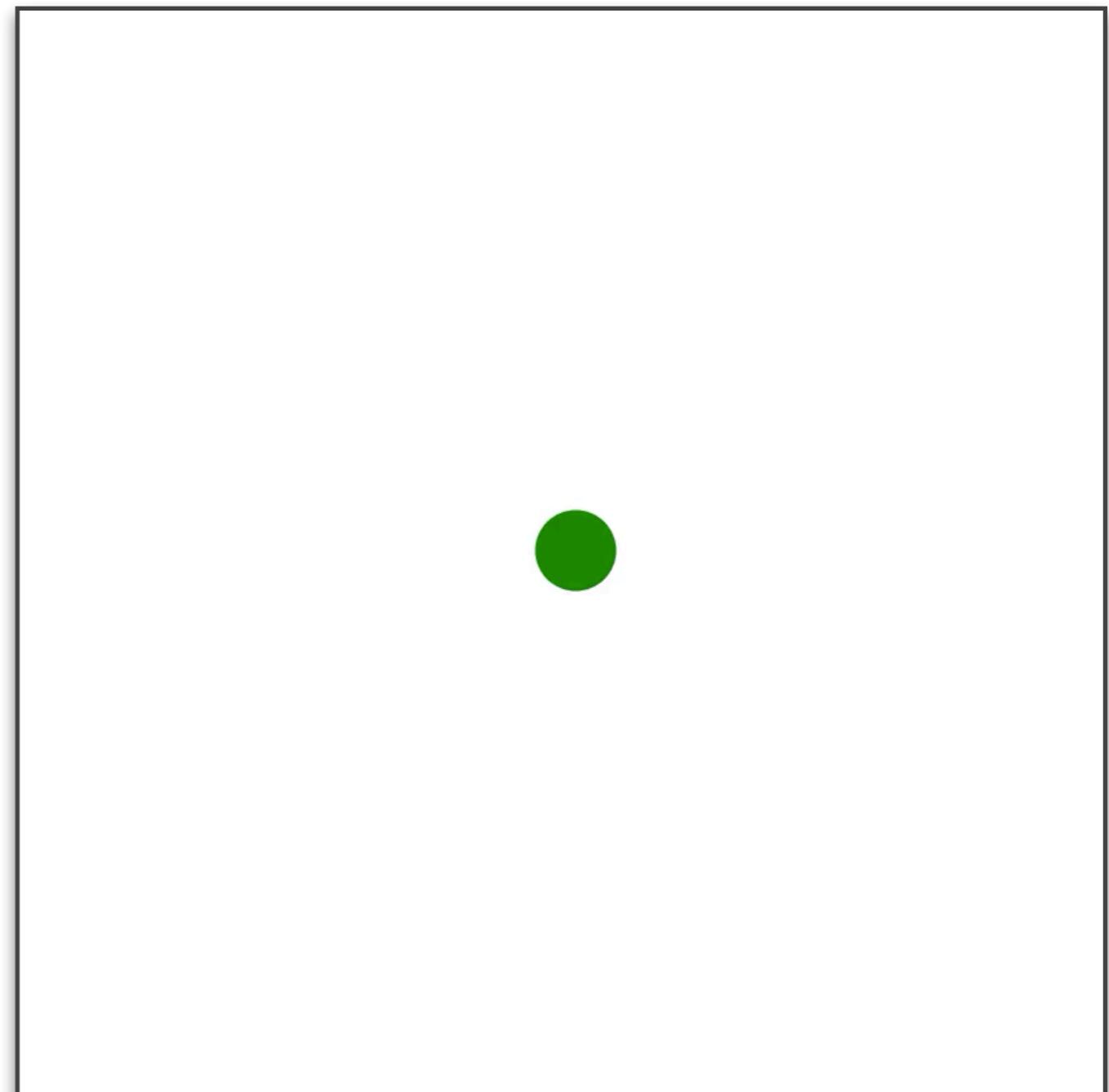
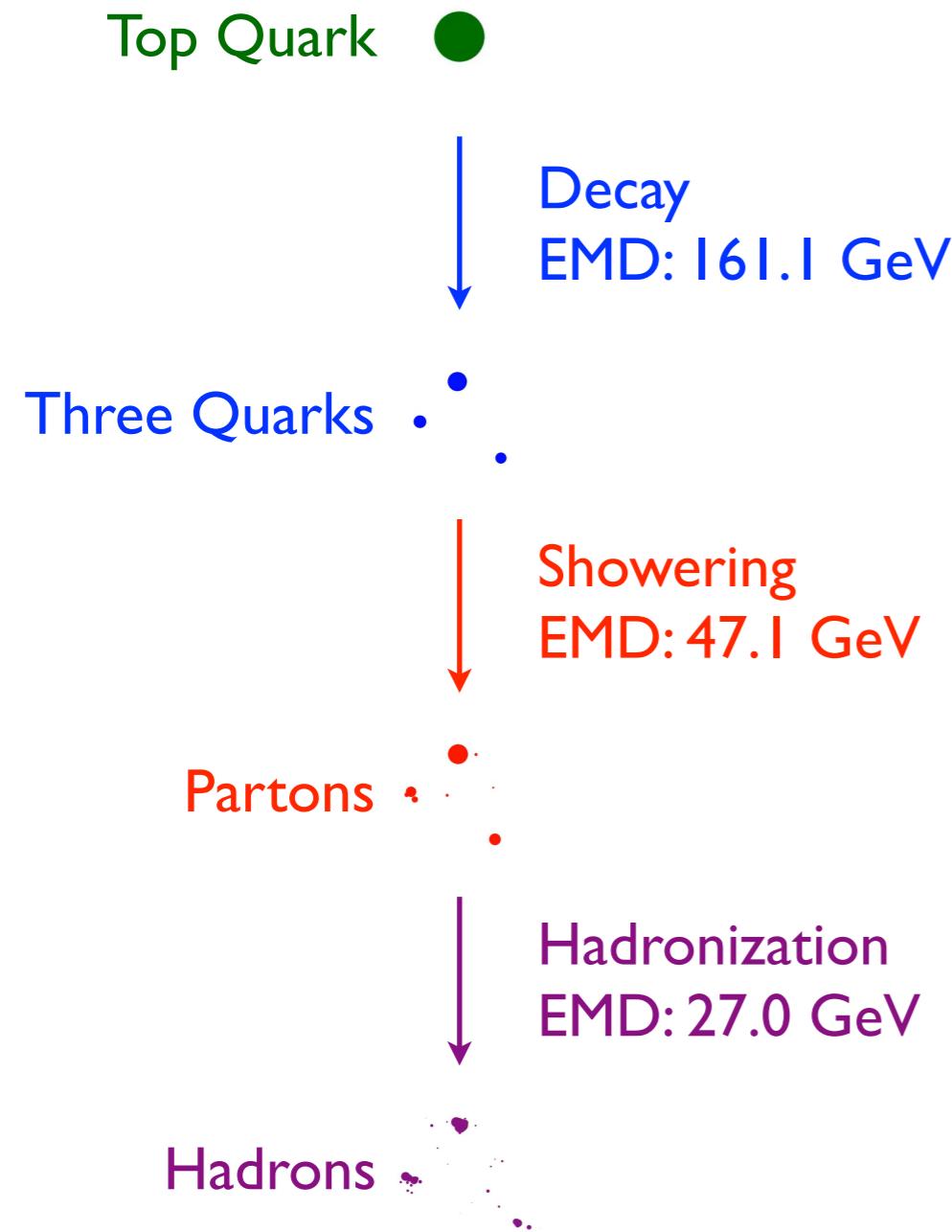
Visualizing W Boson Evolution



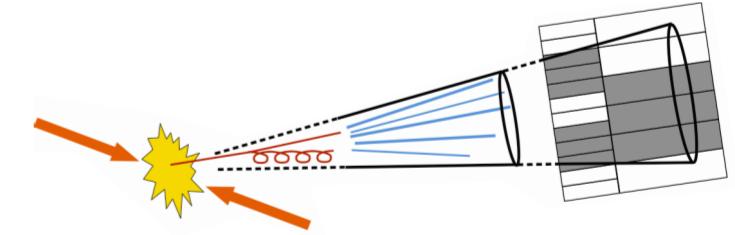
Visualizing Top Quark Evolution



500 GeV



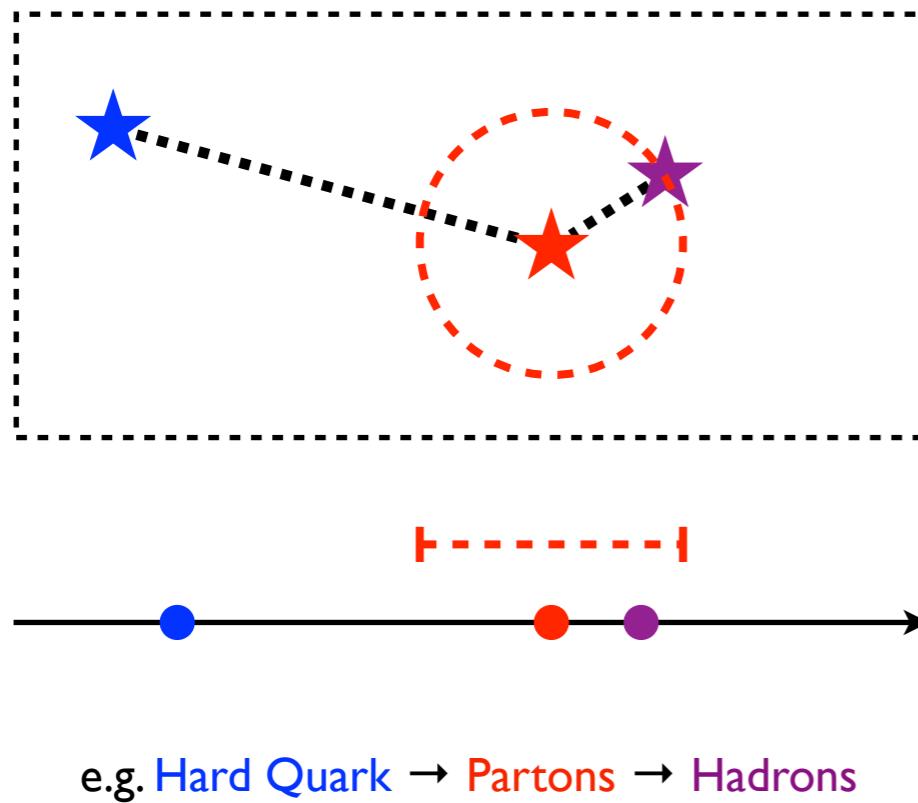
Quantifying Jet Evolution



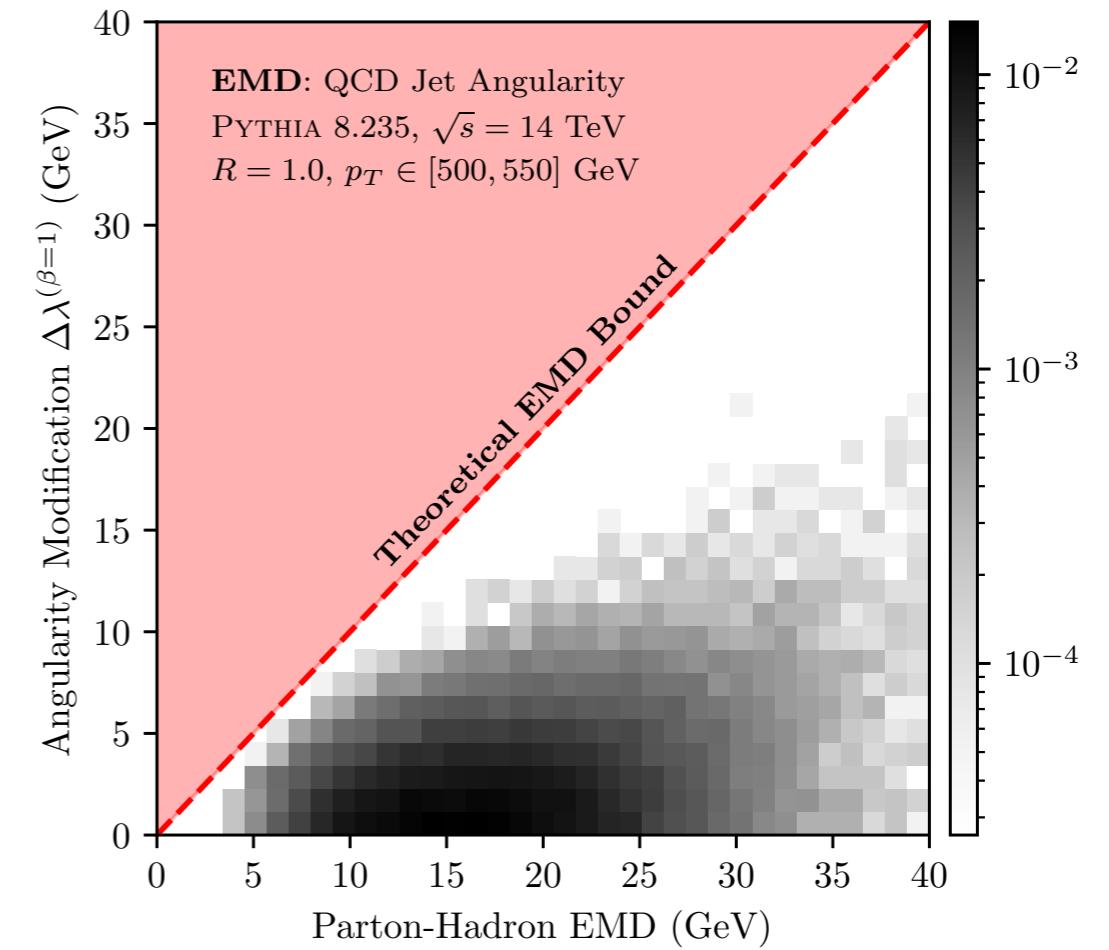
Events **close in EMD** are close in any* **IRC-safe** observable

Using Kantorovich-Rubinstein duality

$$|\lambda^{(\beta)}(\mathcal{E}) - \lambda^{(\beta)}(\mathcal{E}')| \leq \beta \text{EMD}(\mathcal{E}, \mathcal{E}')$$

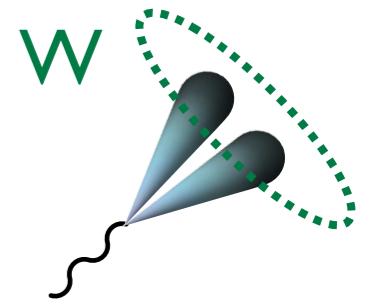


e.g. Angularities ($\beta \geq 1$) $\lambda^{(\beta)}(\mathcal{E}) = \sum_i E_i \theta_i^\beta$

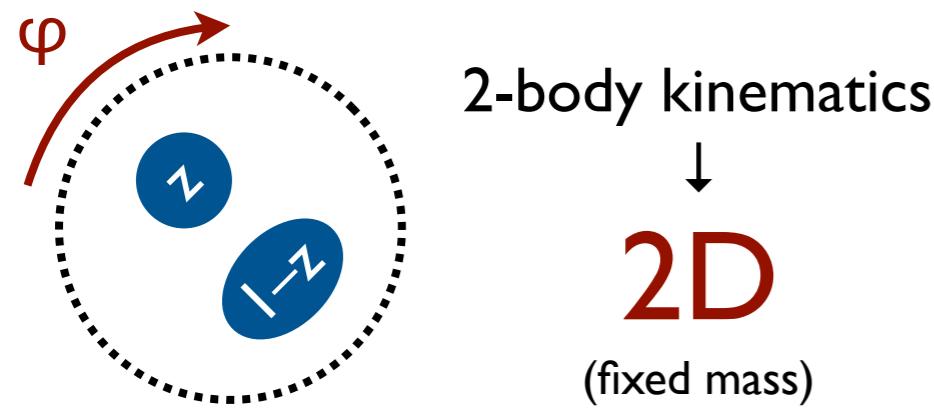


[Komiske, Metodiev, JDT, [1902.02346](#); using Berger, Kucs, Sterman, [hep-ph/0303051](#); Ellis, Vermilion, Walsh, Hornig, Lee, [1001.0014](#); Larkoski, JDT, Waalewijn, [1408.3122](#)]

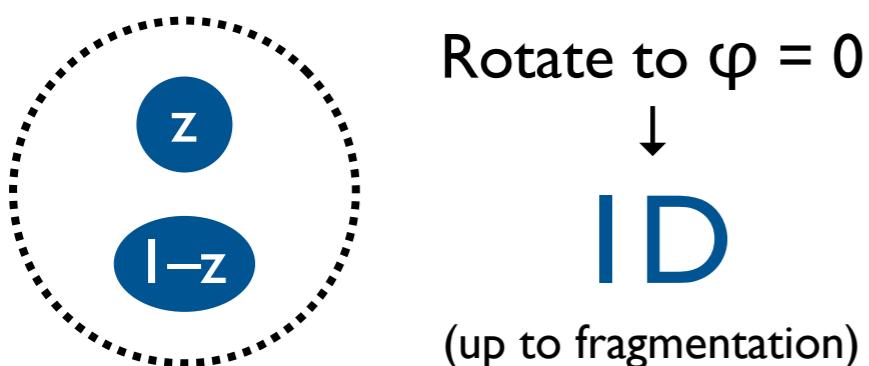
The Space of Boosted W Bosons



*Identify low-D manifold
in high-D space?*

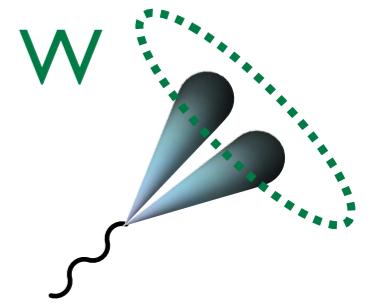


2-body kinematics
↓
2D
(fixed mass)



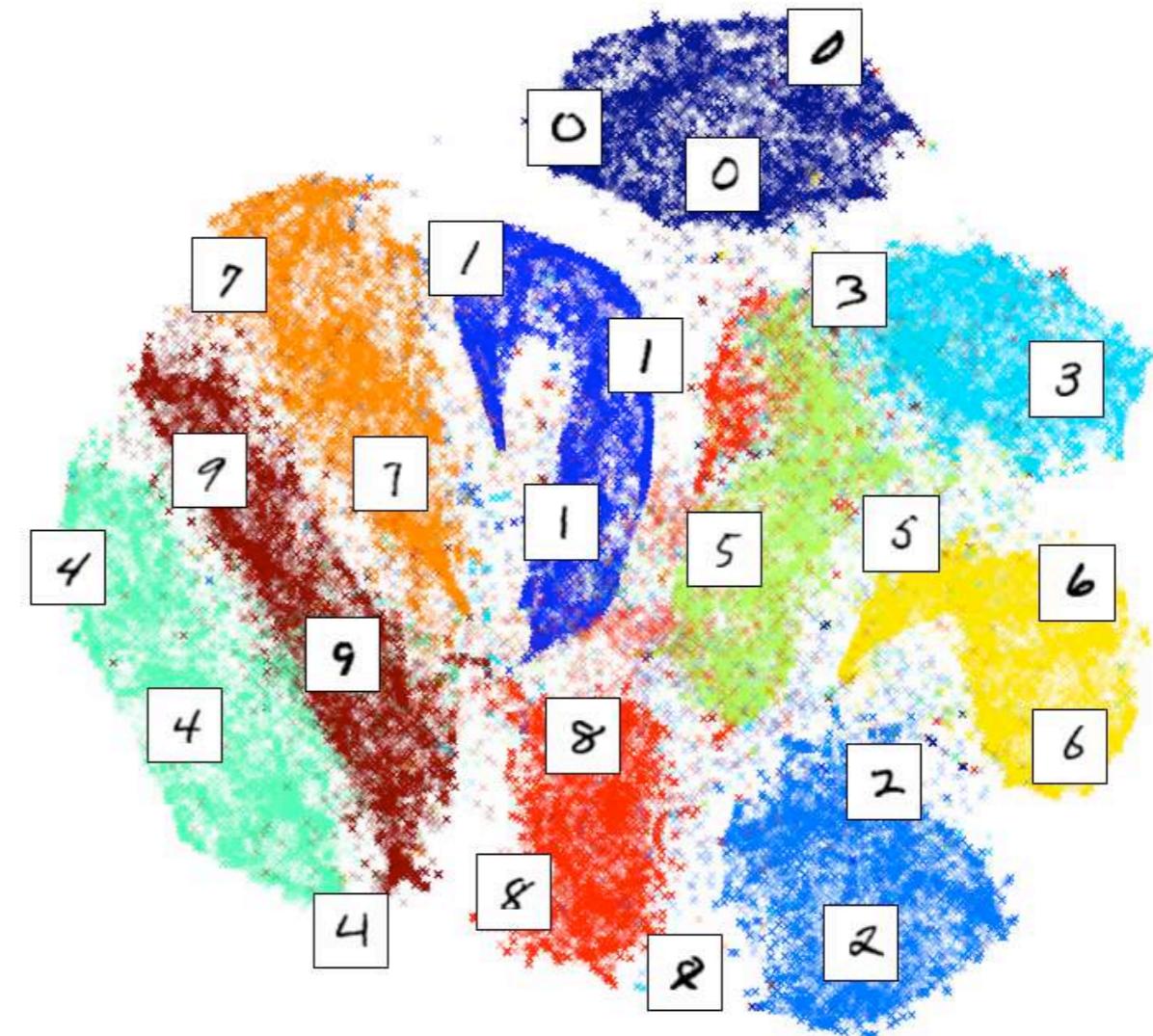
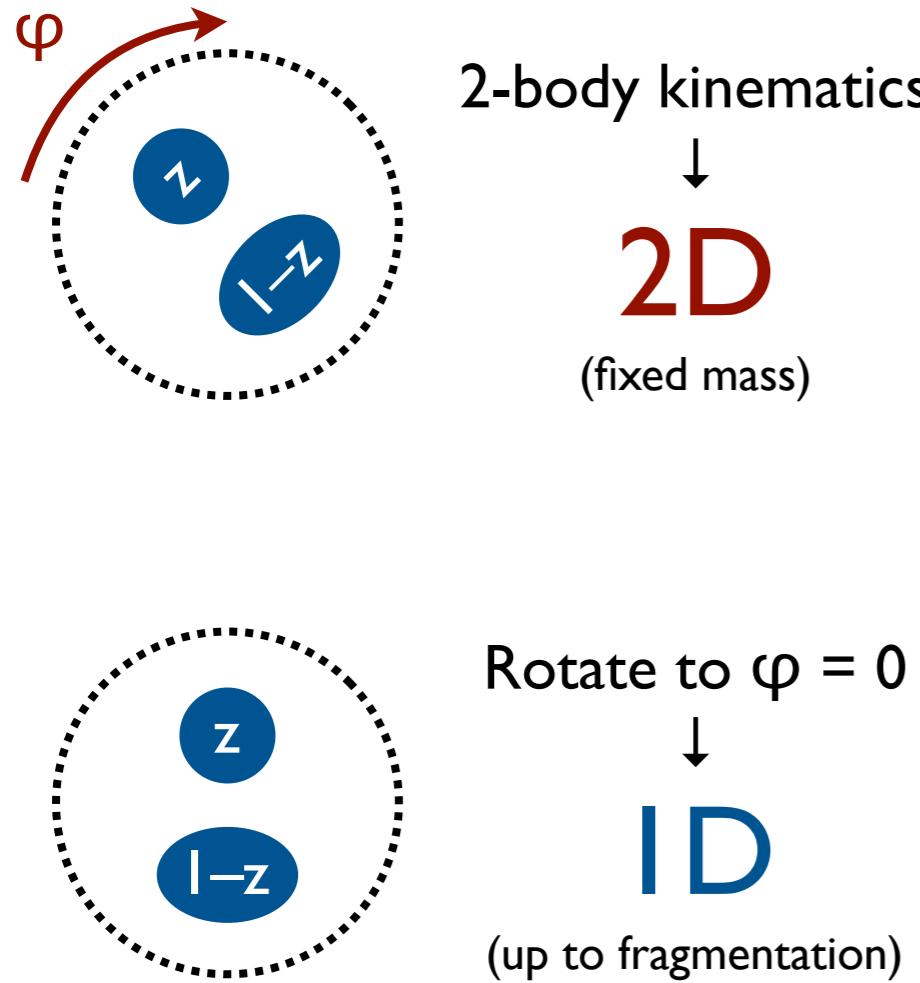
Rotate to $\varphi = 0$
↓
1D
(up to fragmentation)

The Space of Boosted W Bosons



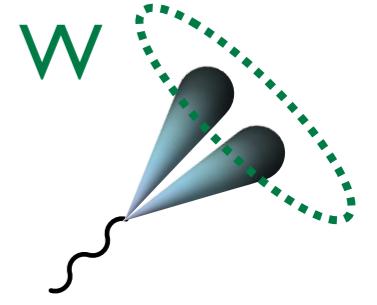
*Identify low-D manifold
in high-D space?*

e.g. t-SNE
(t-distributed Stochastic Neighbor Embedding)

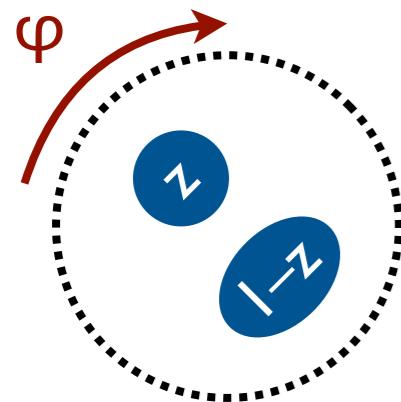


[van der Maaten, Hinton, *JMLR* 2008; figure from [BigSnarf](#)]

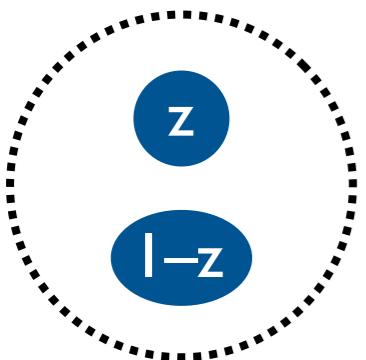
The Space of Boosted W Bosons



*Identify low-D manifold
in high-D space?*

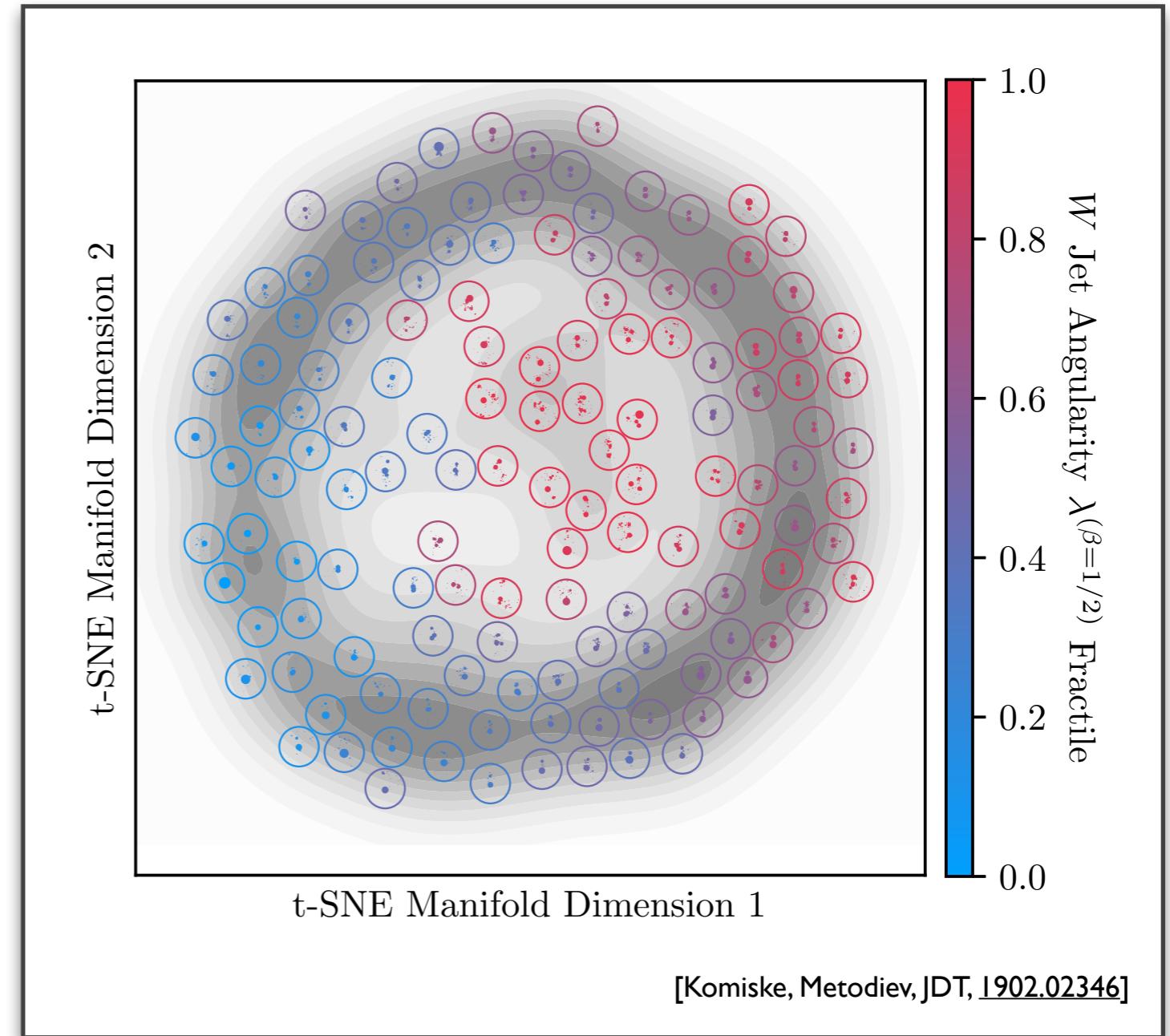


2-body kinematics
↓
2D
(fixed mass)



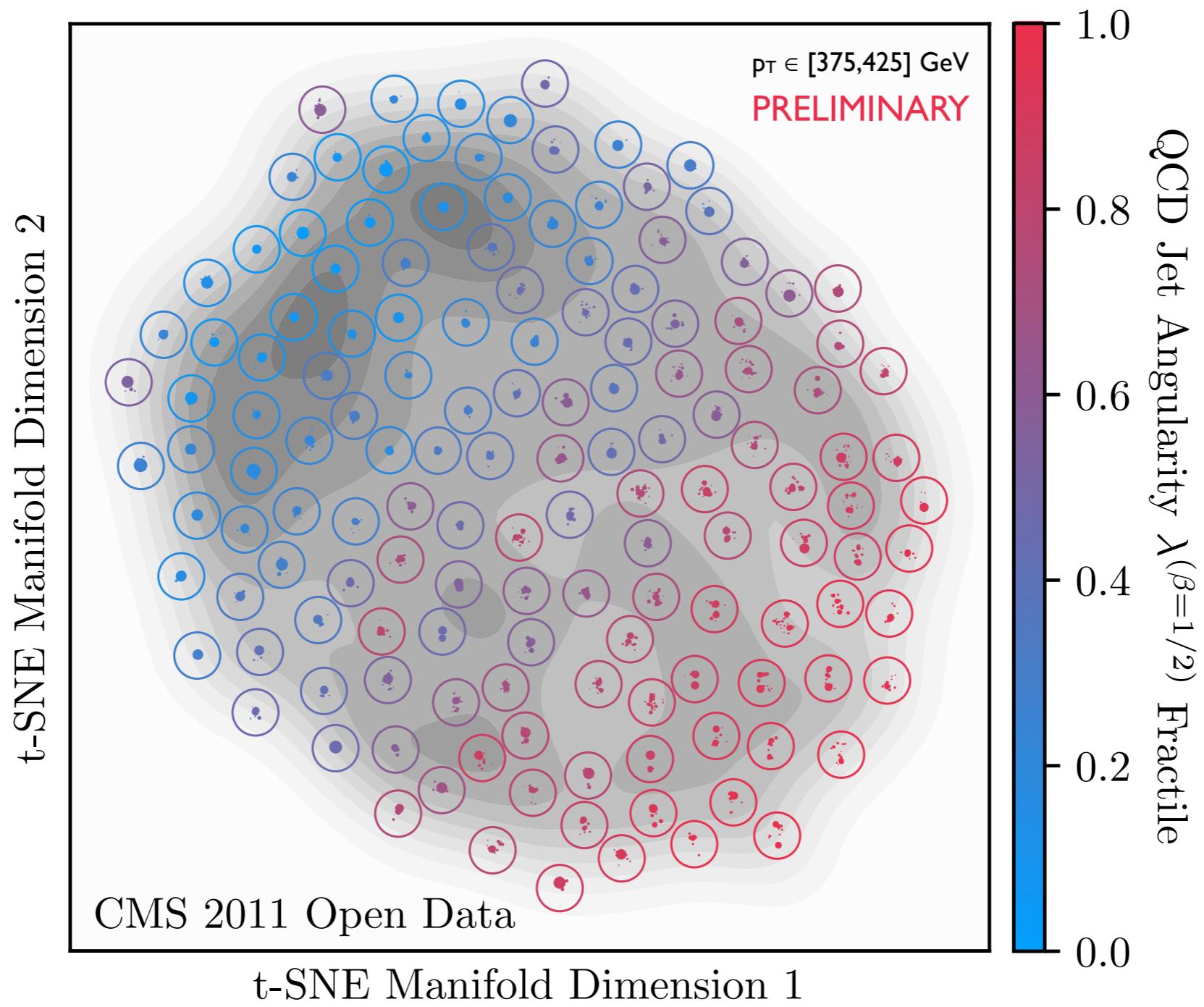
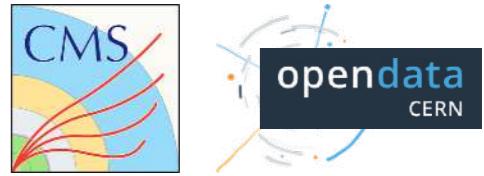
Rotate to $\varphi = 0$
↓
1D
(up to fragmentation)

e.g. t-SNE
(t-distributed Stochastic Neighbor Embedding)

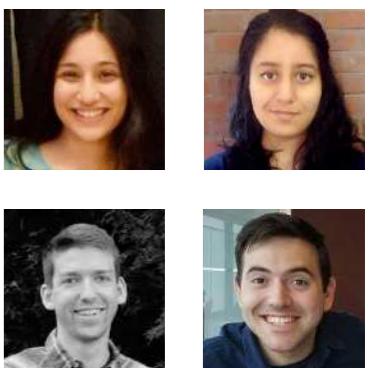


[van der Maaten, Hinton, [JMLR 2008](#); figure from [BigSnarf](#)]

Hot off the Press: The Space of Jets

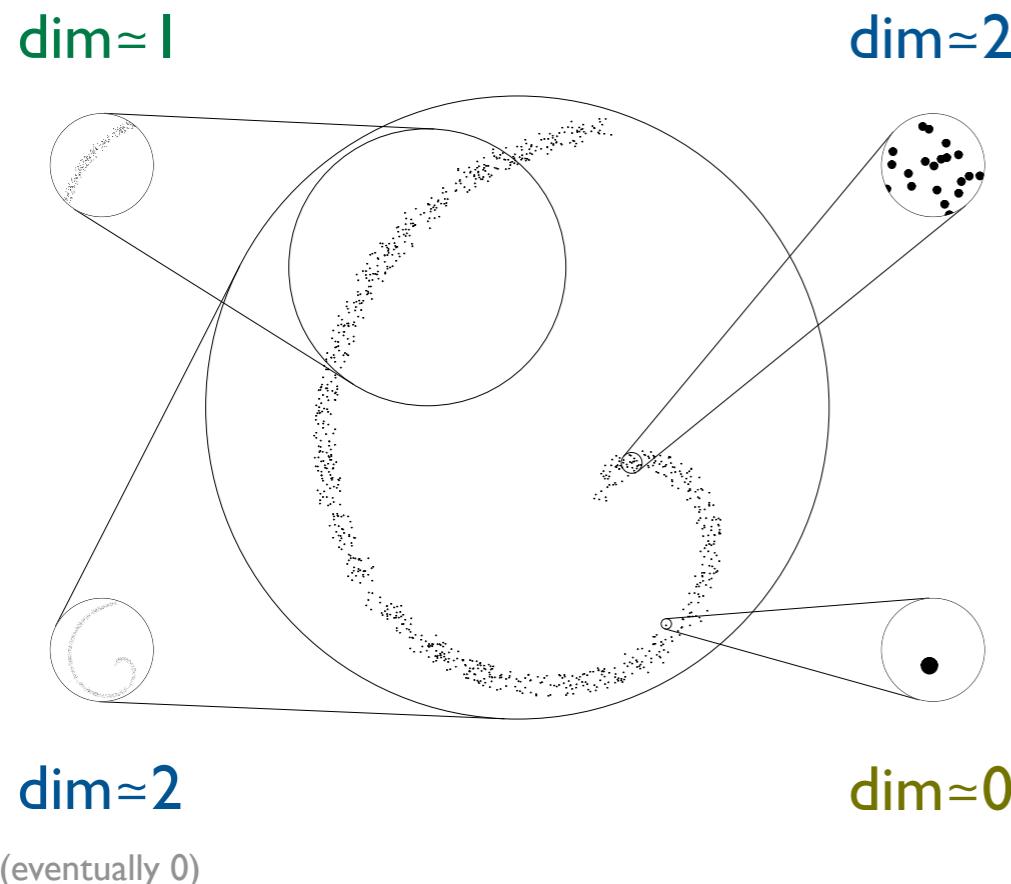


[Mastandrea, Naik, Komiske, Metodiev, JDT, in preparation]



Quantifying Dimensionality

Correlation Dimension: $\dim(Q) = Q \frac{\partial}{\partial Q} \ln \sum_i \sum_j \Theta(\text{EMD}(\mathcal{E}_i, \mathcal{E}_j) < Q)$



$$N_{\text{neighbors}}(r) \sim r^{\dim}$$



$$\dim(r) \sim r \frac{\partial}{\partial r} \ln N_{\text{neighbors}}(r)$$

[Grassberger, Procaccia, [PRL 1983](#); Kégl, [NIPS 2002](#)]

Decay-Level Dimension

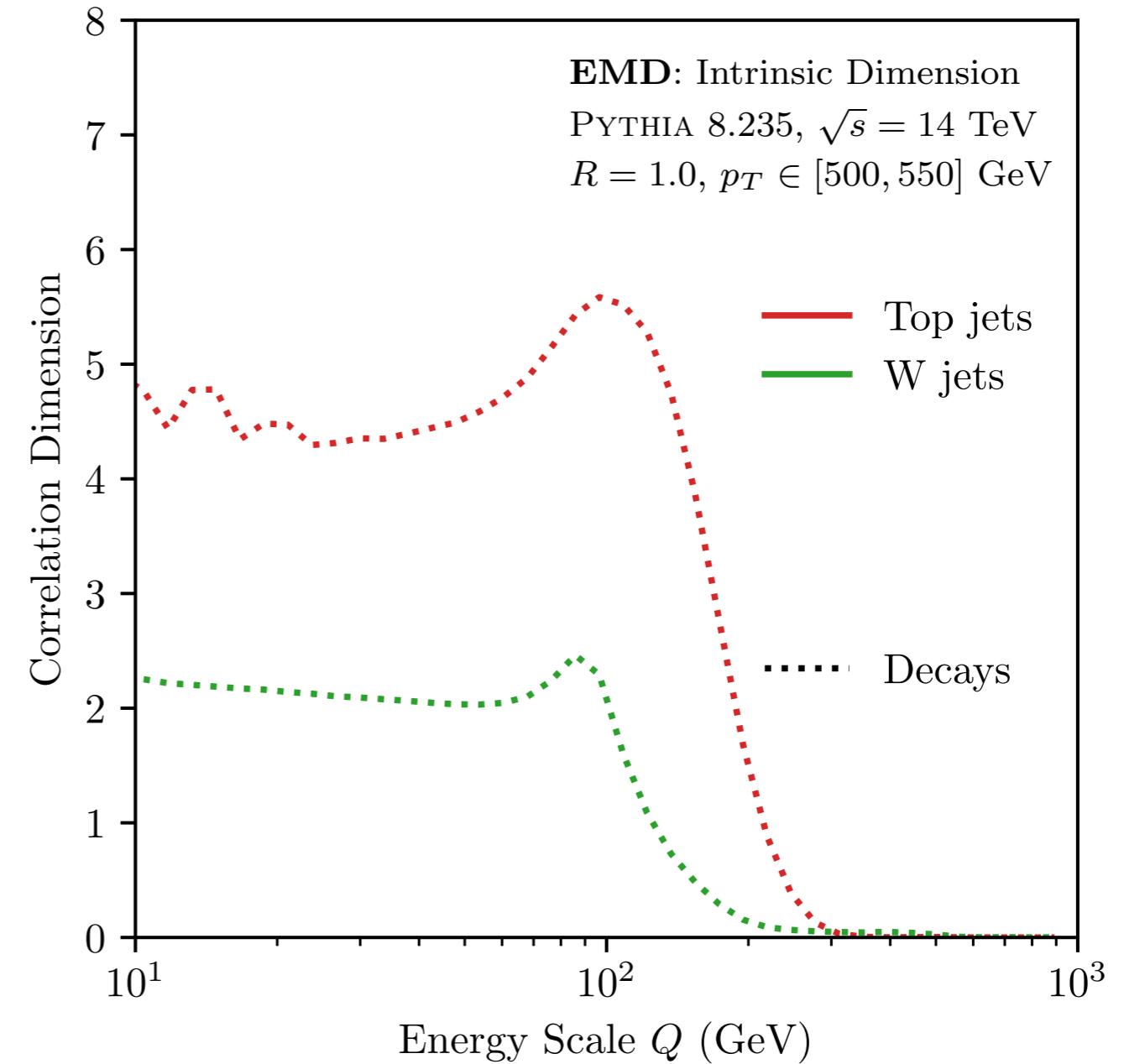
$$\dim(Q) = Q \frac{\partial}{\partial Q} \ln \sum_i \sum_j \Theta(\text{EMD}(\mathcal{E}_i, \mathcal{E}_j) < Q)$$

3-body phase space —

with W mass constraint

2-body phase space —

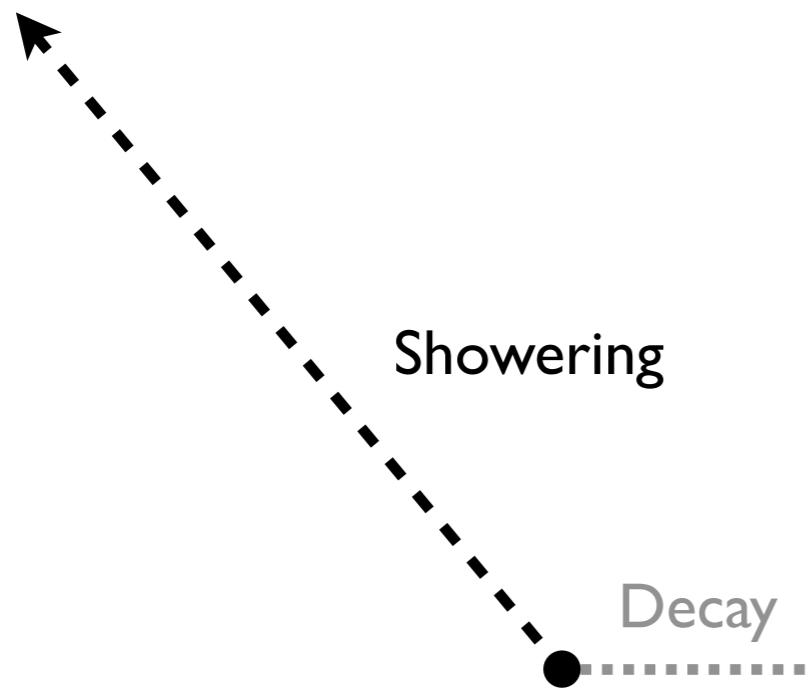
Increasing complexity: multi-body phase space



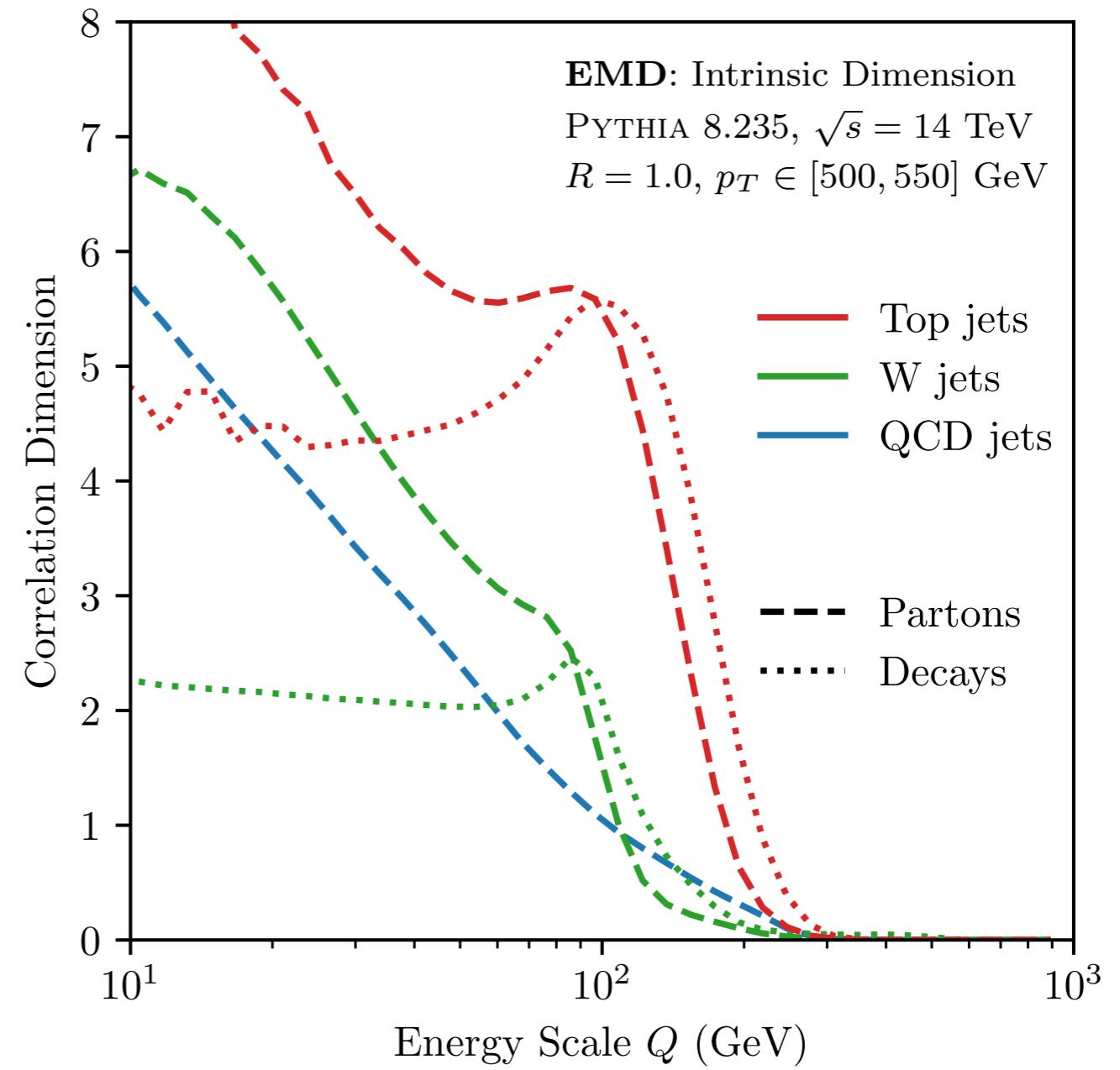
[Komiske, Metodiev, JDT, 1902.02346]

Parton-Level Dimension

$$\dim(Q) = Q \frac{\partial}{\partial Q} \ln \sum_i \sum_j \Theta(\text{EMD}(\mathcal{E}_i, \mathcal{E}_j) < Q)$$



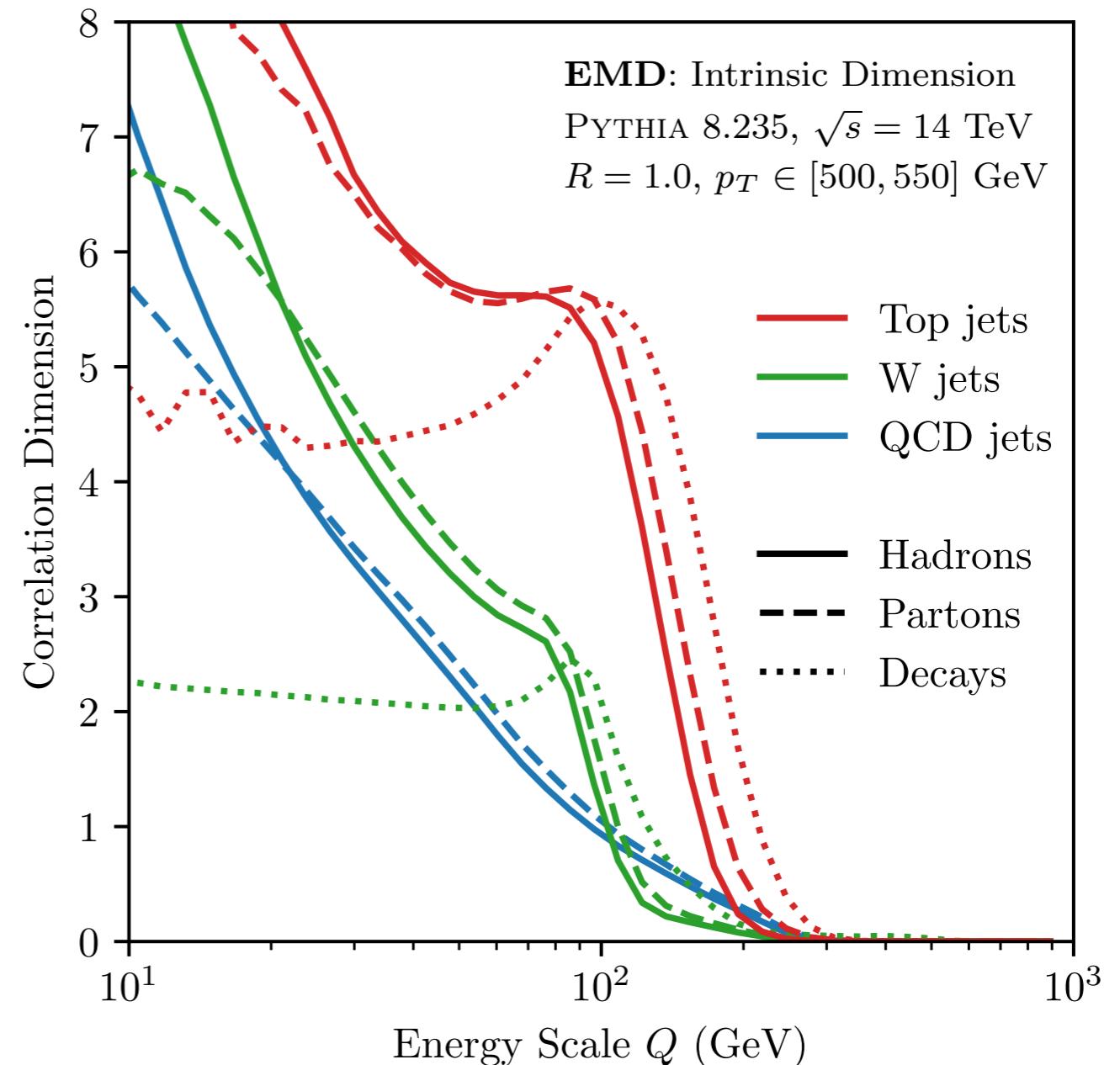
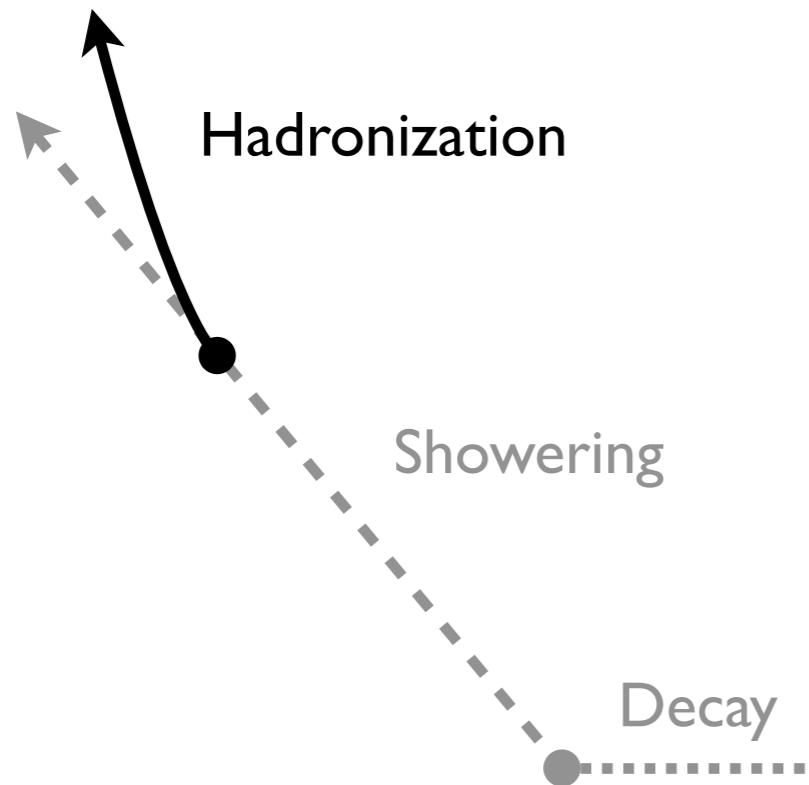
Increasing complexity: multi-body phase space
perturbative emissions



[Komiske, Metodiev, JDT, 1902.02346]

Hadron-Level Dimension

$$\text{dim}(Q) = Q \frac{\partial}{\partial Q} \ln \sum_i \sum_j \Theta(\text{EMD}(\mathcal{E}_i, \mathcal{E}_j) < Q)$$



Increasing complexity:

- multi-body phase space
- perturbative emissions
- non-perturbative dynamics

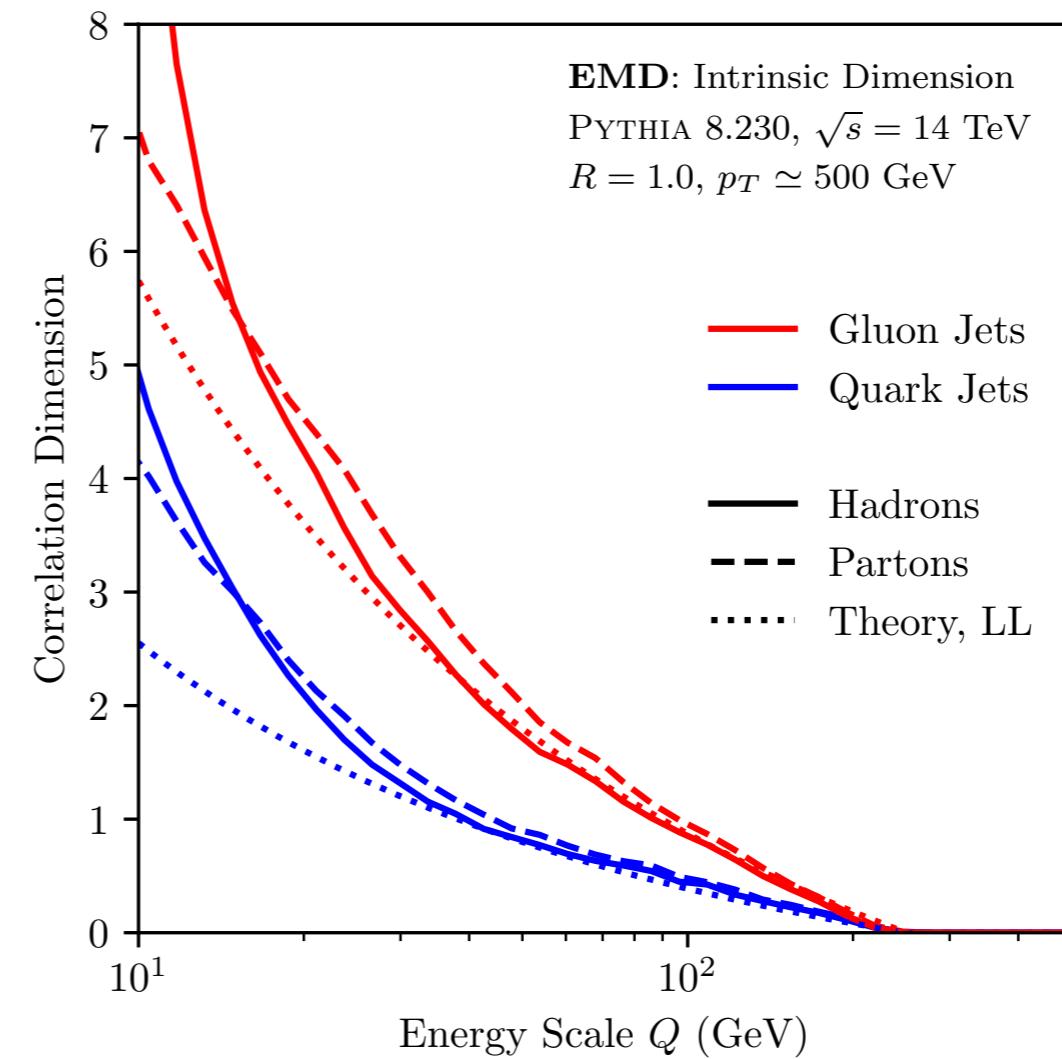
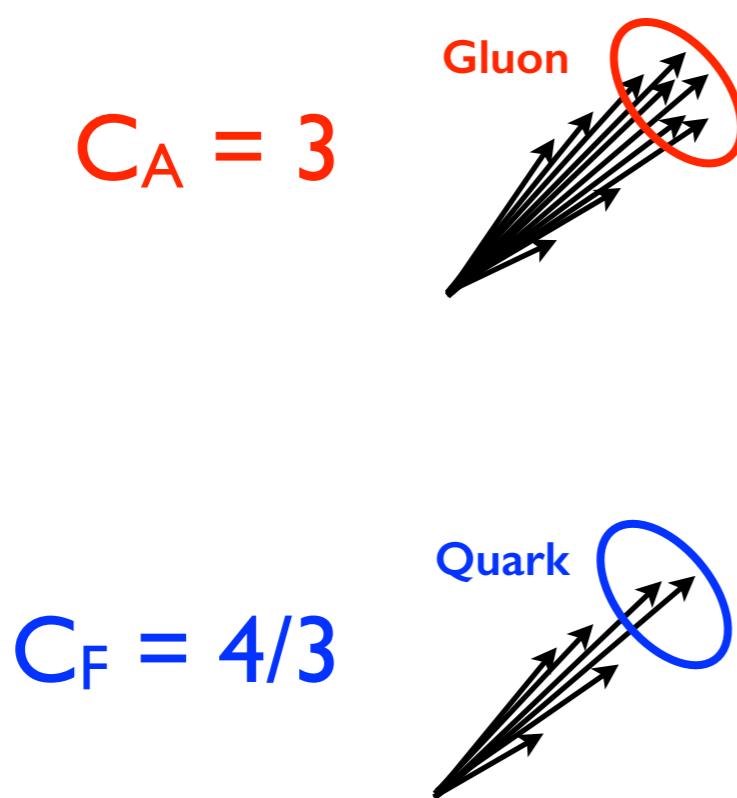
[Komiske, Metodiev, JDT, 1902.02346]

Preliminary Calculation

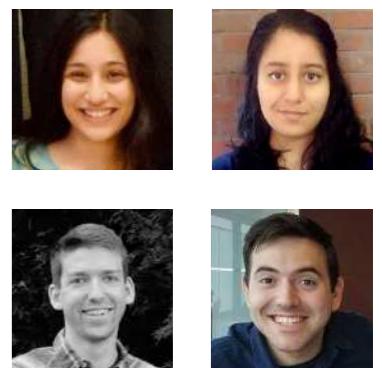
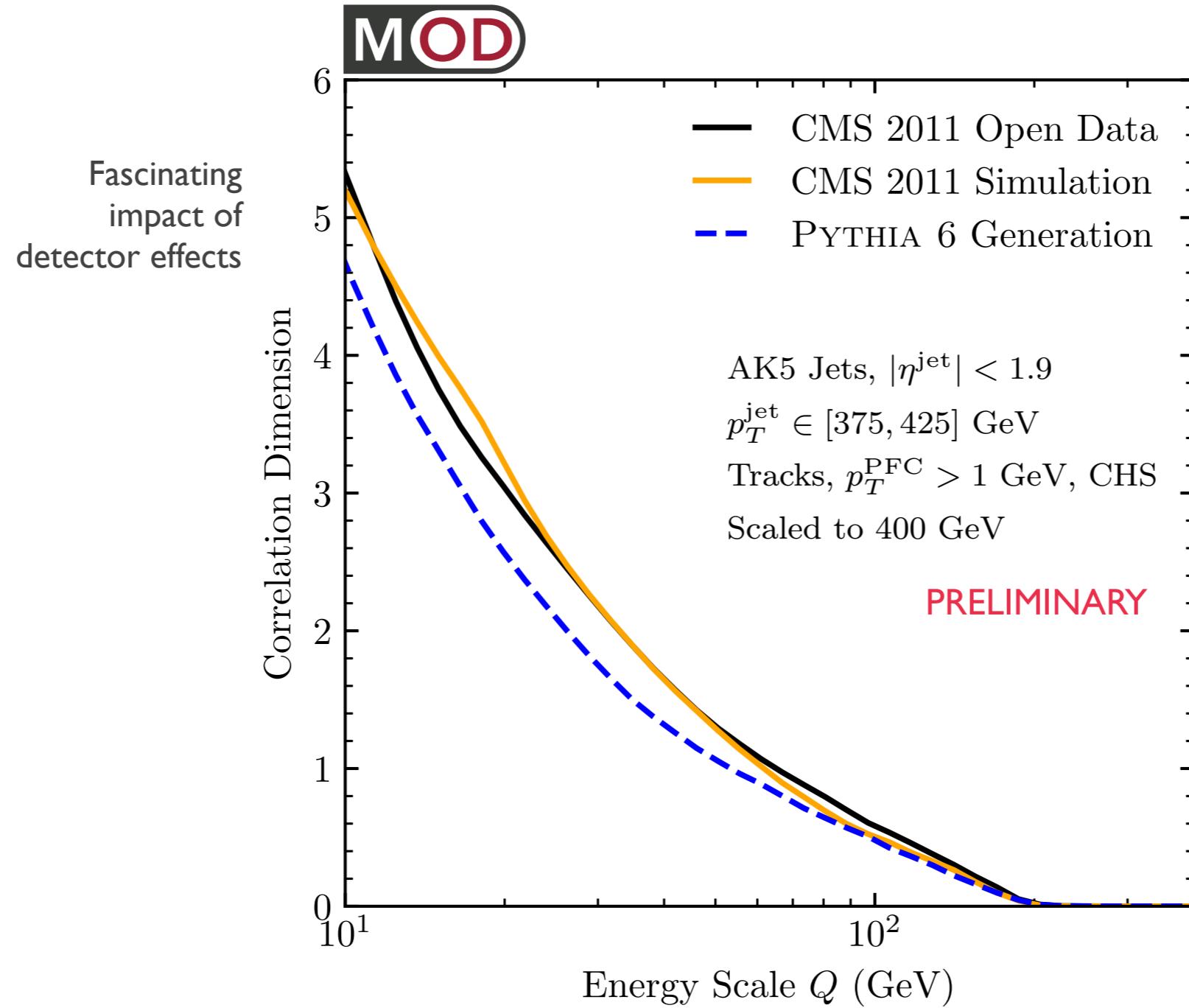
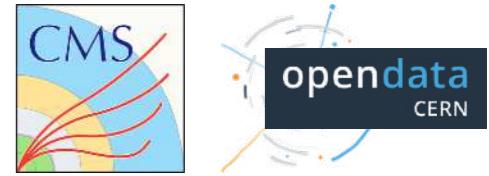
Leading Log:
(single log, since dim has derivative)

$$\dim_i(Q) \sim -\frac{8\alpha_s}{\pi} C_i \ln \frac{Q}{p_T}$$

↑
Color Factor

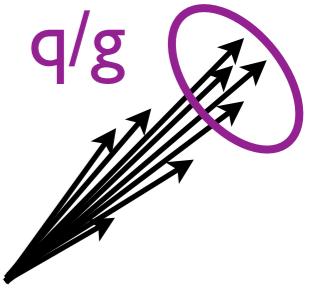


Hot off the Press: Dimension of Jets



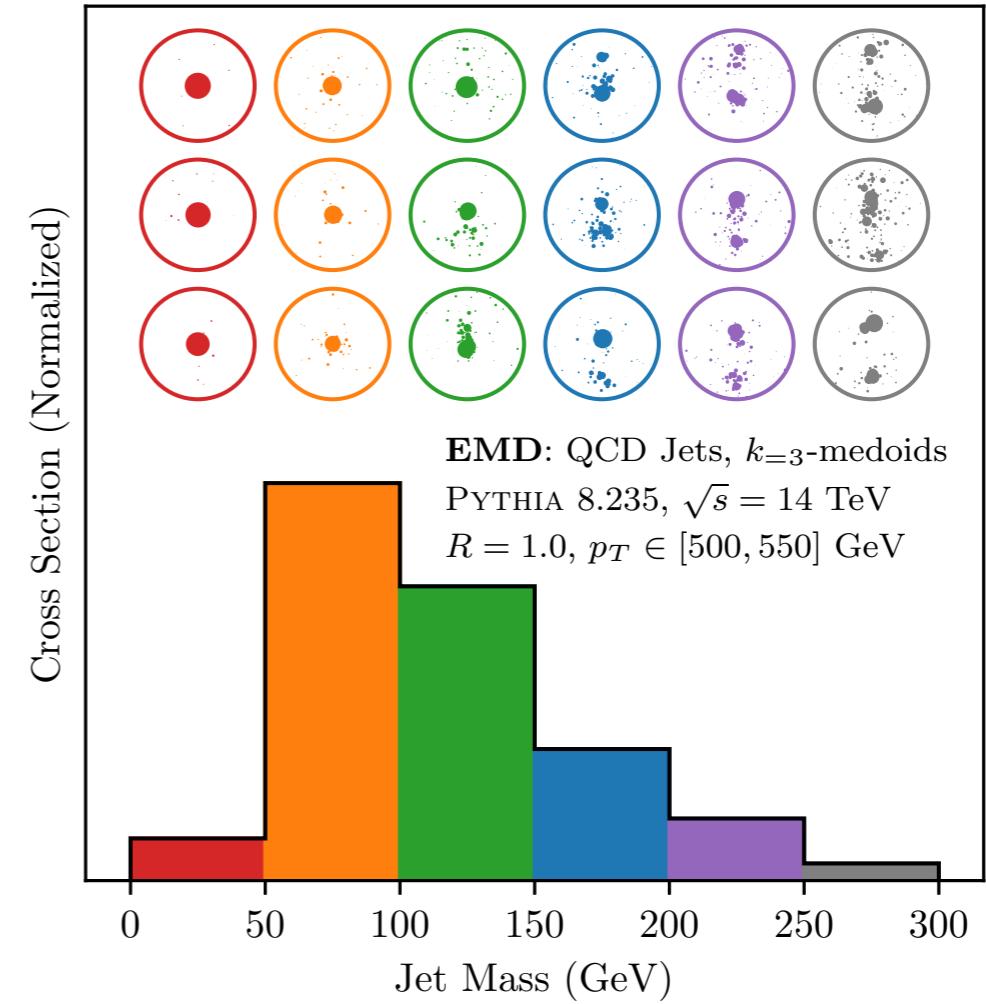
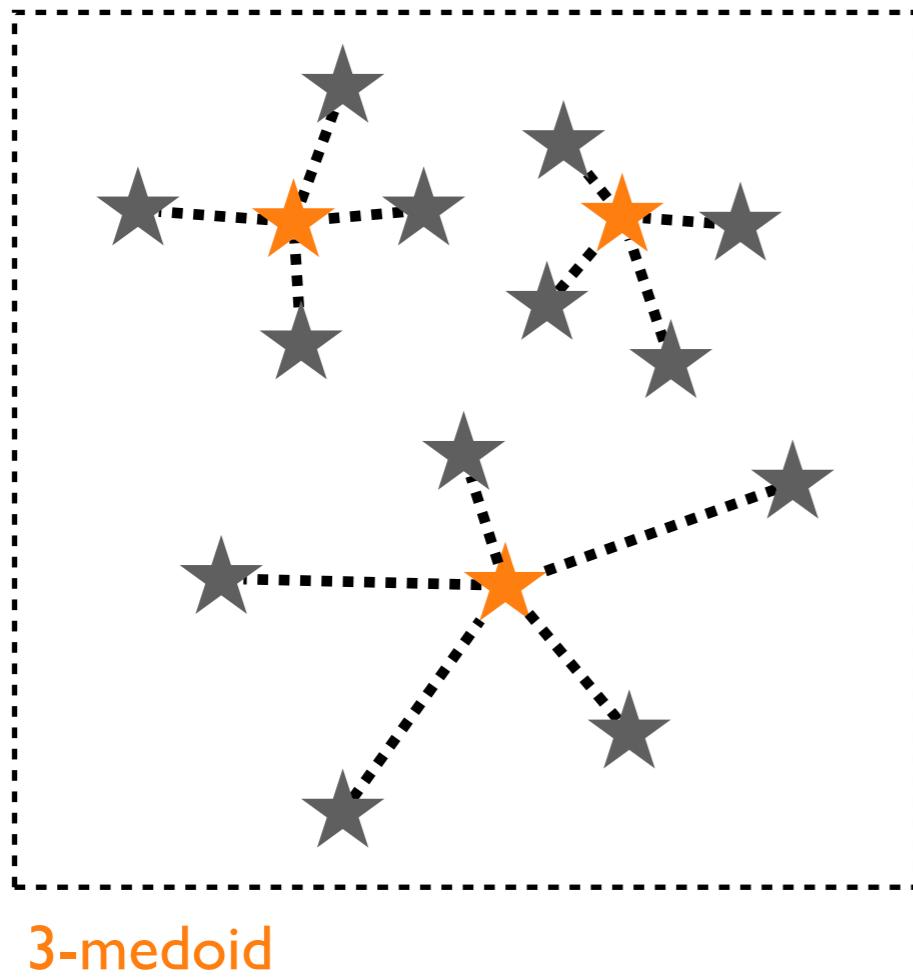
[Mastandrea, Naik, Komiske, Metodiev, JDT, in preparation]

Identifying Representative Jets



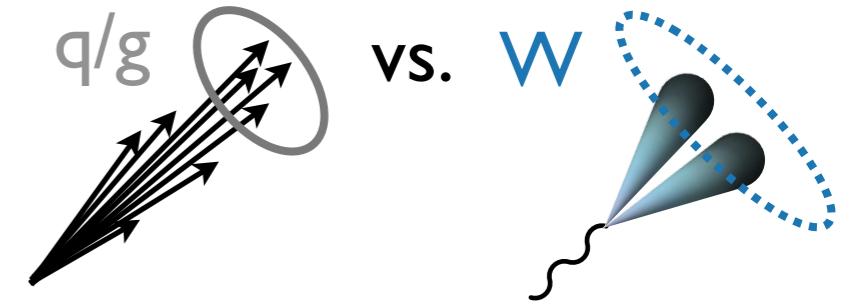
medoid: jet that minimizes total EMD to other jets

k-medoids: k clusters to minimize total medoid distance



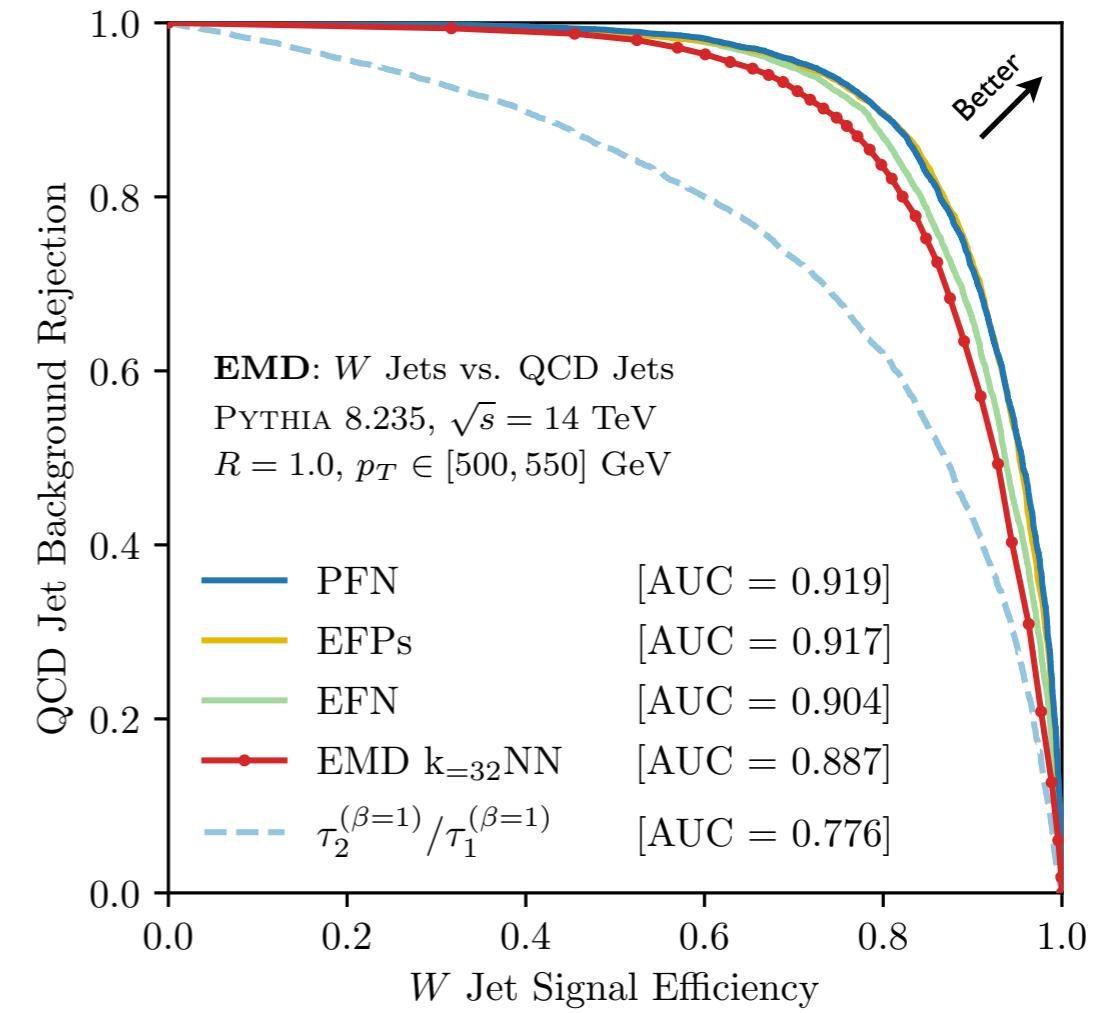
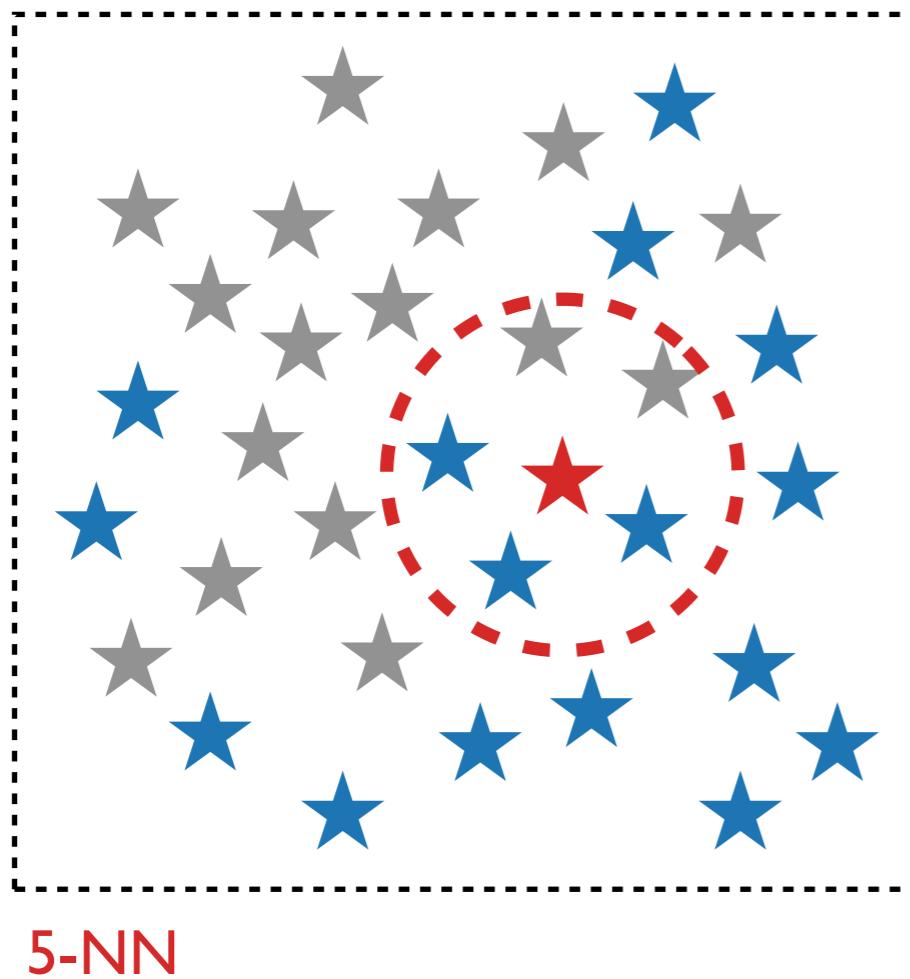
[Komiske, Metodiev, JDT, 1902.02346]

Jet Classification



Estimate jet label by **k nearest neighbors** in training data

Approaches performance of **modern machine learning**



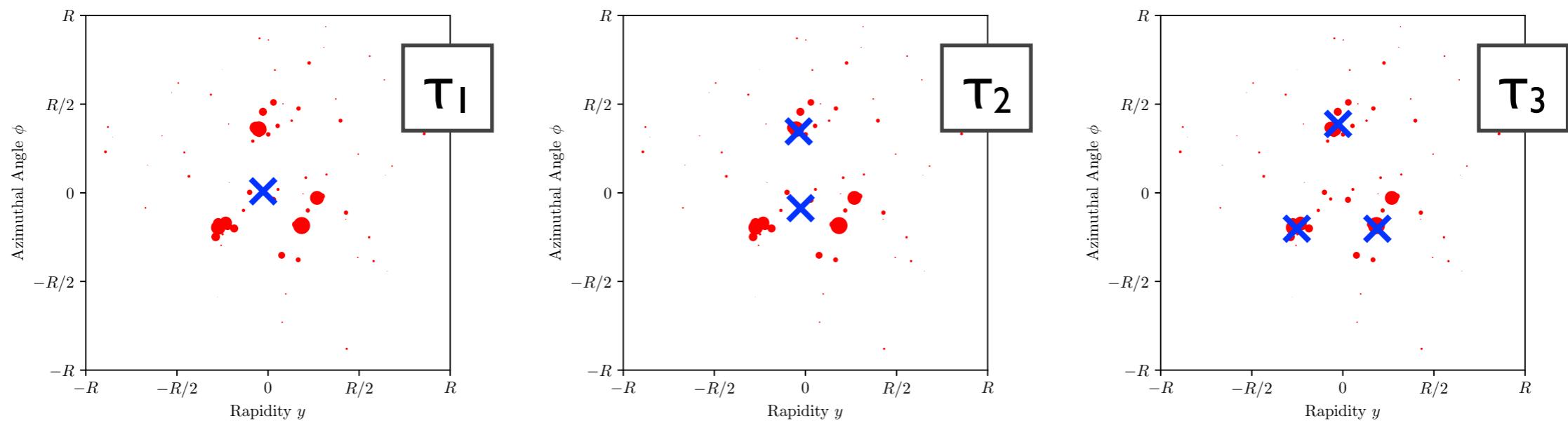
[Komiske, Metodiev, JDT, [1902.02346](#);
comparison to JDT, Van Tilburg, [1011.2268](#), [1108.2701](#); Komiske, Metodiev, JDT, [1712.07124](#), [1810.05165](#)]

Insight into N-subjettiness

$$\tau_N^{(\beta)}(\mathcal{E}) = \min_{N \text{ axes}} \sum_i E_i \min \left\{ \theta_{1,i}^\beta, \theta_{2,i}^\beta, \dots, \theta_{N,i}^\beta \right\}$$

↑ kind of arbitrary

↑ IRC safe



$$\tau_N(\mathcal{E}) = \min_{|\mathcal{E}'|=N} \text{EMD}(\mathcal{E}, \mathcal{E}') \quad \text{for } \beta = 1$$

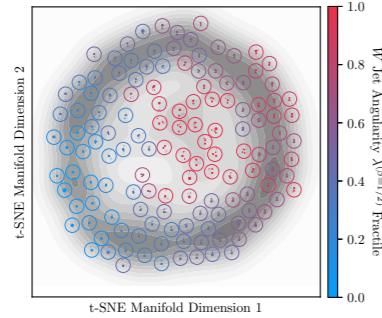
↑ very satisfying

Related to p-Wasserstein metric for $p = \beta > 1$

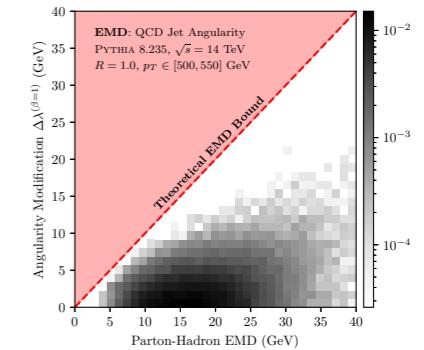
JDT, Van Tilburg, [1011.2268](#), [1108.2701](#);
based on Brandt, Dahmen, [ZPC 1979](#); Stewart, Tackmann, Waalewijn, [1004.2489](#)

Future Directions

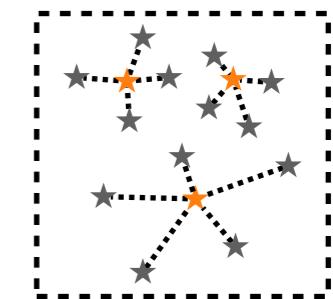
Quantify (and mitigate?) pileup/detector effects



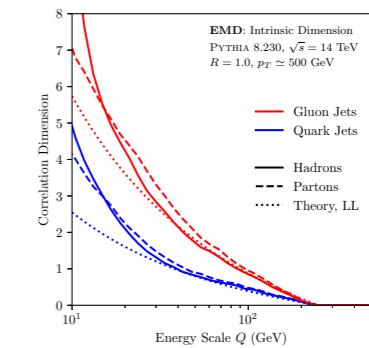
Non-parametric density estimates (& unfolding?)



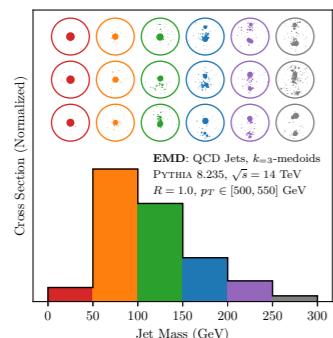
Automated data compression (& triggering?)



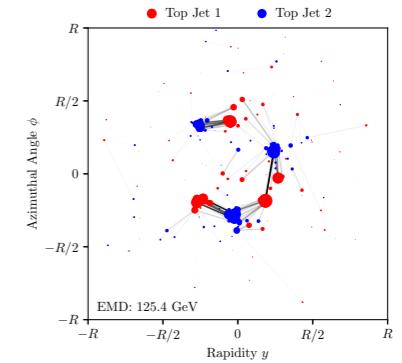
Define new observables through EMD geometry



Precision QCD calculations of pairwise metrics

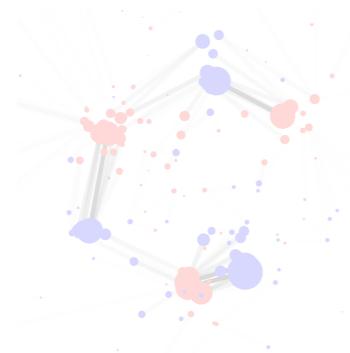


Novel analyses with and beyond histograms

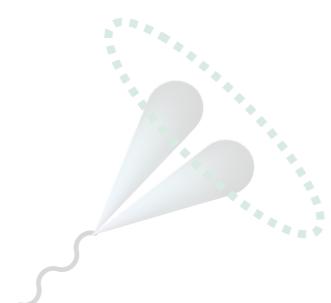


Event Mover's Distance between ensembles

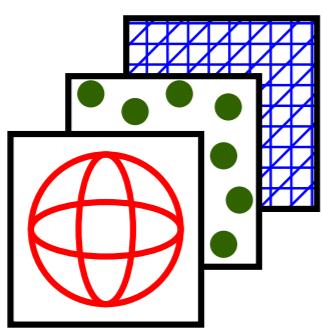
...



The Energy Mover's Distance



Initial Physics Studies



(Broader Comments)

High-Energy
Particle
Physics

Mathematics,
Statistics,
Computer Science



High-Energy Particle Physics



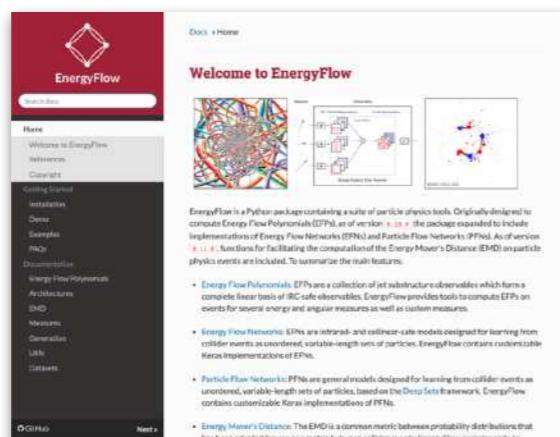
Patrick Komiske



Eric Metodiev



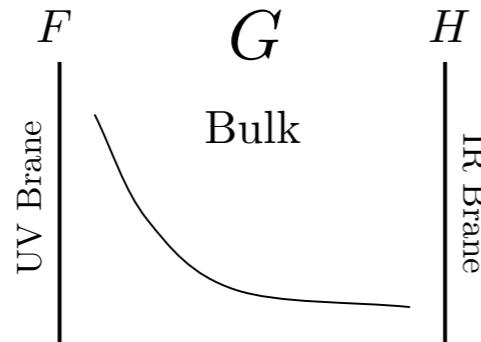
Mathematics,
Statistics,
Computer Science



Energy Flow Package

<https://energyflow.network/>

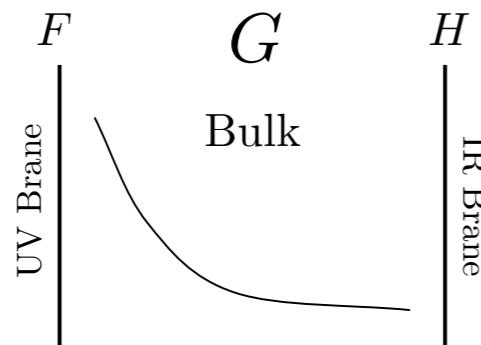
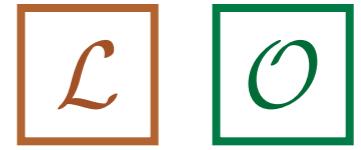
Evolution of a “Model Builder”



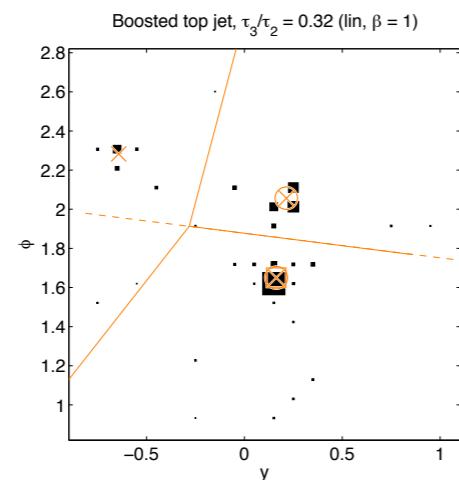
Build Lagrangians & Paradigms

[images from JDT, [hep-ph/0502175](#); JDT, Van Tilburg, [1108.2701](#); Komiske, Metodiev, JDT, [1810.05165](#)]

Evolution of a “Model Builder”



Build Lagrangians & Paradigms

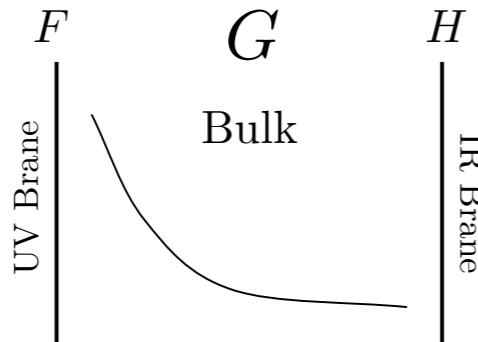


Build Observables & Algorithms

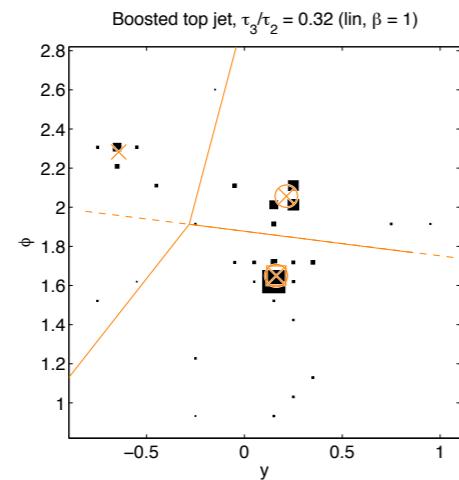
[images from JDT, [hep-ph/0502175](#); JDT, Van Tilburg, [1108.2701](#); Komiske, Metodiev, JDT, [1810.05165](#)]

Evolution of a “Model Builder”

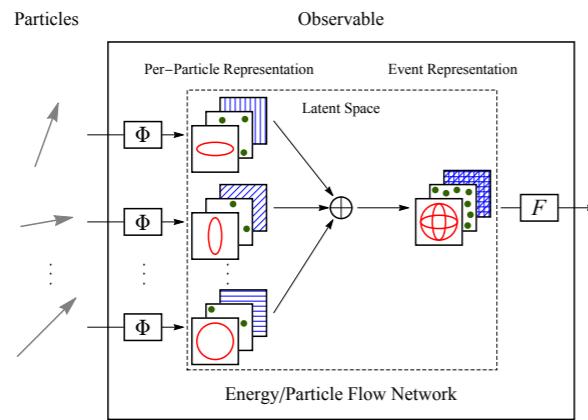
\mathcal{L} \mathcal{O} \mathcal{M}



Build Lagrangians & Paradigms



Build Observables & Algorithms



Build Models & Loss Functions

[images from JDT, [hep-ph/0502175](#); JDT, Van Tilburg, [1108.2701](#); Komiske, Metodiev, JDT, [1810.05165](#)]

Evolution of a “Model Builder”



Given current status of the LHC, which strategy:

*Makes maximal **verifiable** use of collider data?*

Can scale up to the challenges of HL-LHC?

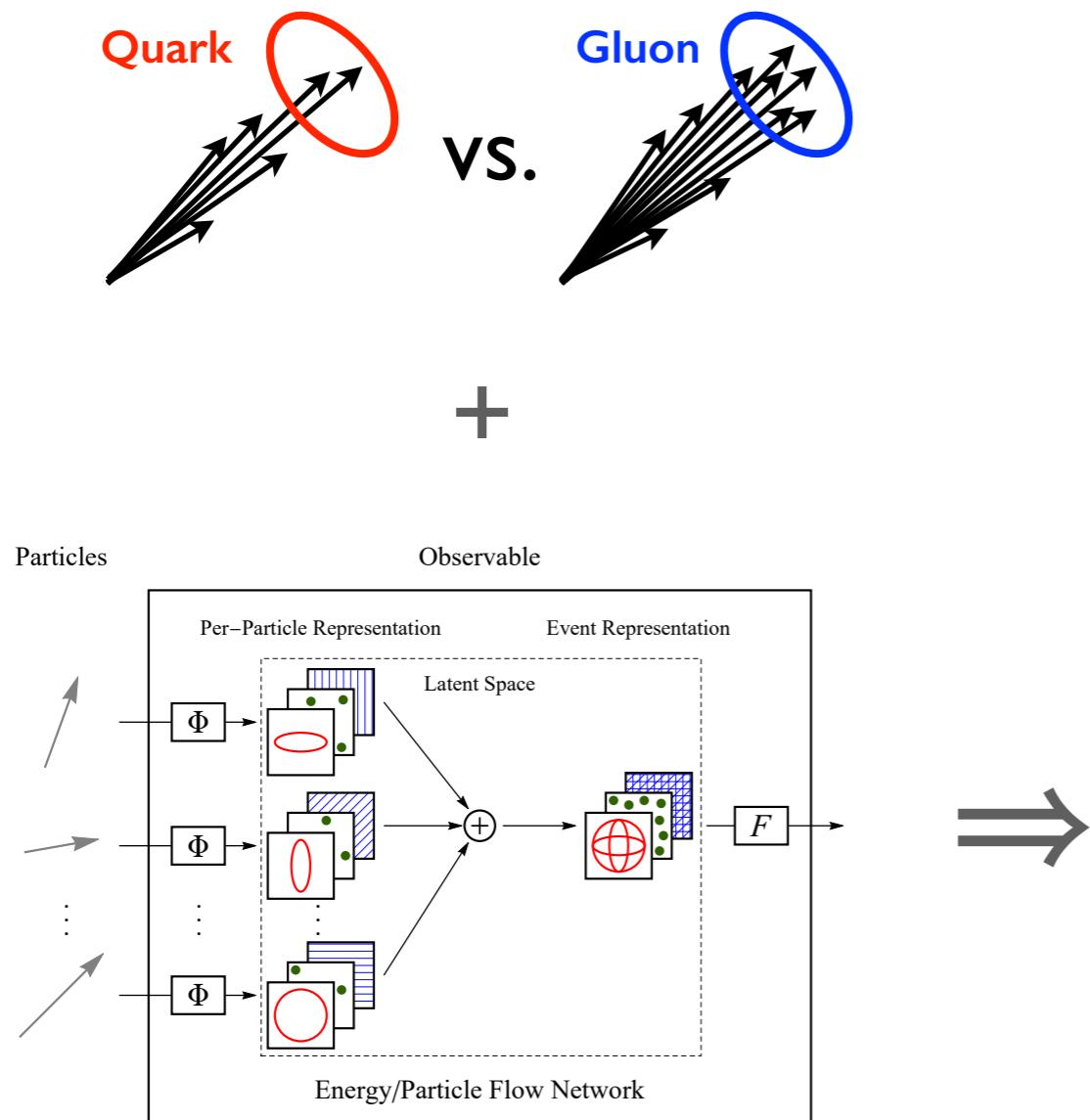
*Has the greatest **discovery potential**?*

*Offers new **insights** into fundamental physics?*

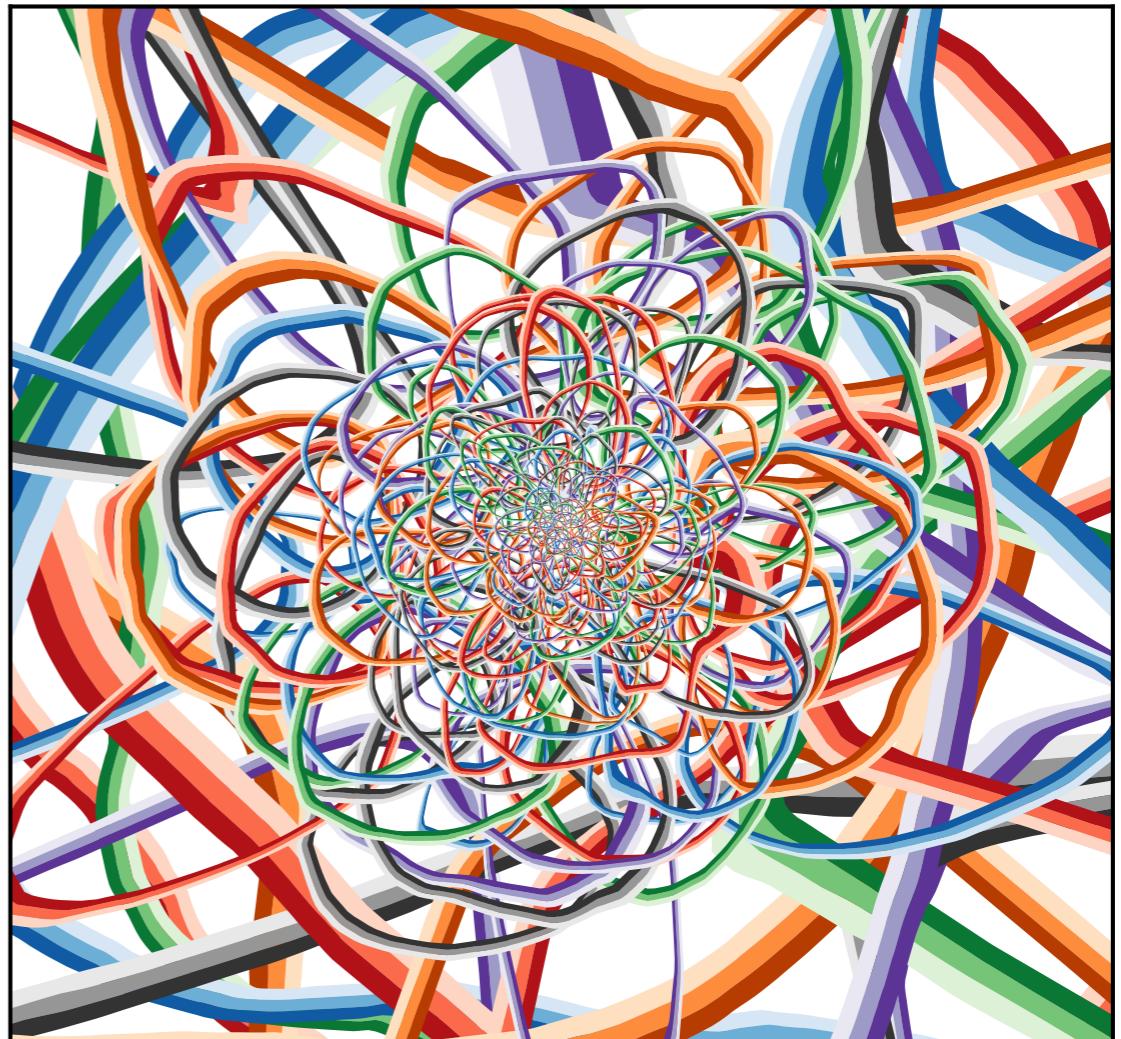
[images from JDT, [hep-ph/0502175](#); JDT, Van Tilburg, [1108.2701](#); Komiske, Metodiev, JDT, [1810.05165](#)]

Opportunities for Visualization

\mathcal{L} \mathcal{O} \mathcal{M}

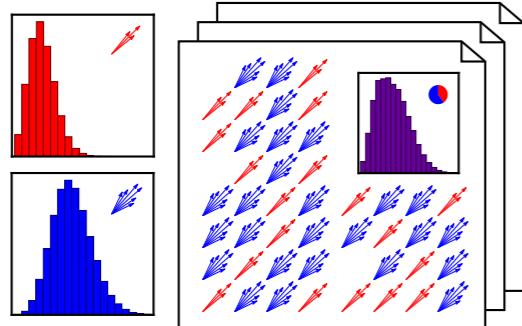


“Seeing” the collinear singularity of QCD



Augmenting our exceptional human/scientific ability to recognize patterns

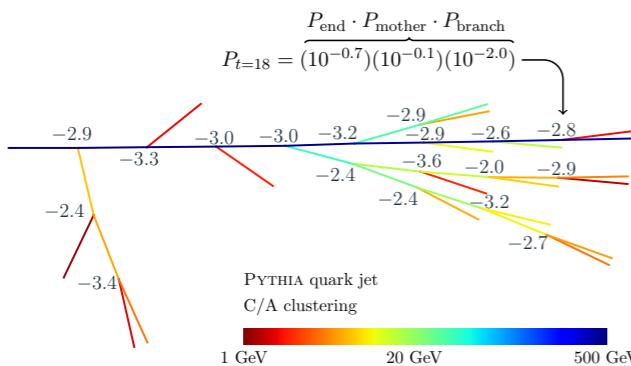
The Rise of Unsupervised Learning



Jet Topics

Blind Source Separation

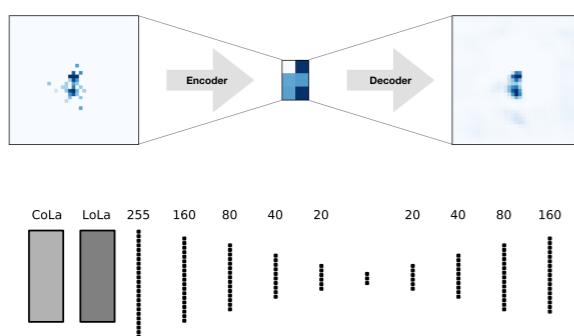
[Metodiev, JDT, [I802.00008](#); Komiske, Metodiev, JDT, [I809.01140](#); see also Metodiev, Nachman, JDT, [I708.02949](#)]



JUNIPR

Probability Modeling

[Andreassen, Feige, Frye, Schwartz, [I804.09720](#); see also Monk, [I807.03685](#)]



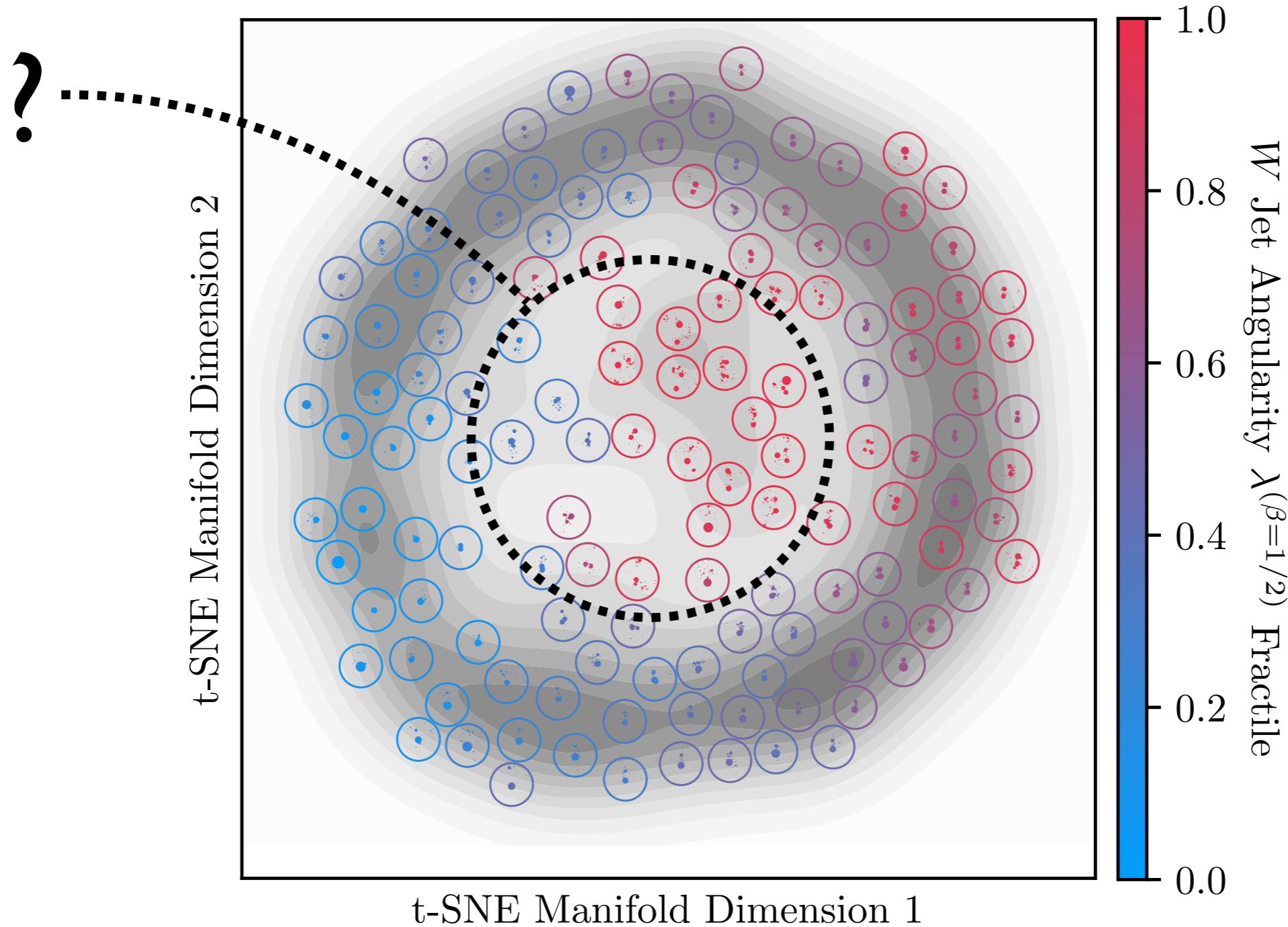
Autoencoders

Anomaly Detection

[Hajer, Li, Liu, Wang, [I807.10261](#); Heimel, Kasieczka, Plehn, Thompson, [I808.08979](#); Farina, Nakai, Shih, [I808.08992](#); Cerri, Nguyen, Pierini, Spiropulu, Vlimant, [I811.10276](#); see also Collins, Howe, Nachman, [I805.02664](#), [I902.02634](#); De Simone, Jacques, [I807.06038](#)]

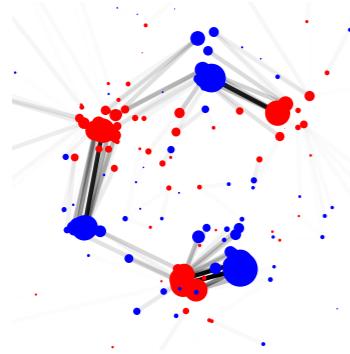
Common theme: Analyze *event ensembles*, not individual events

Visualization meets Anomaly Detection

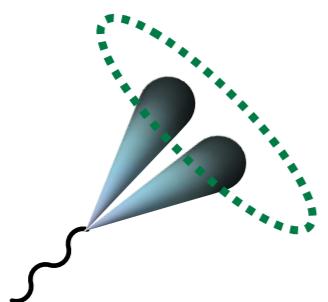


[Komiske, Metodiev, JDT, 1902.02346]

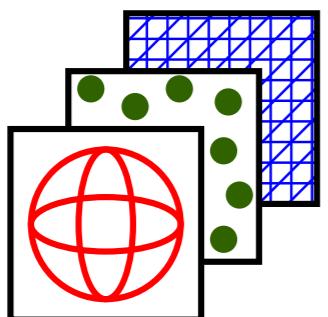
Summary



The Energy Mover's Distance
A metric on the space of IRC-safe energy flows



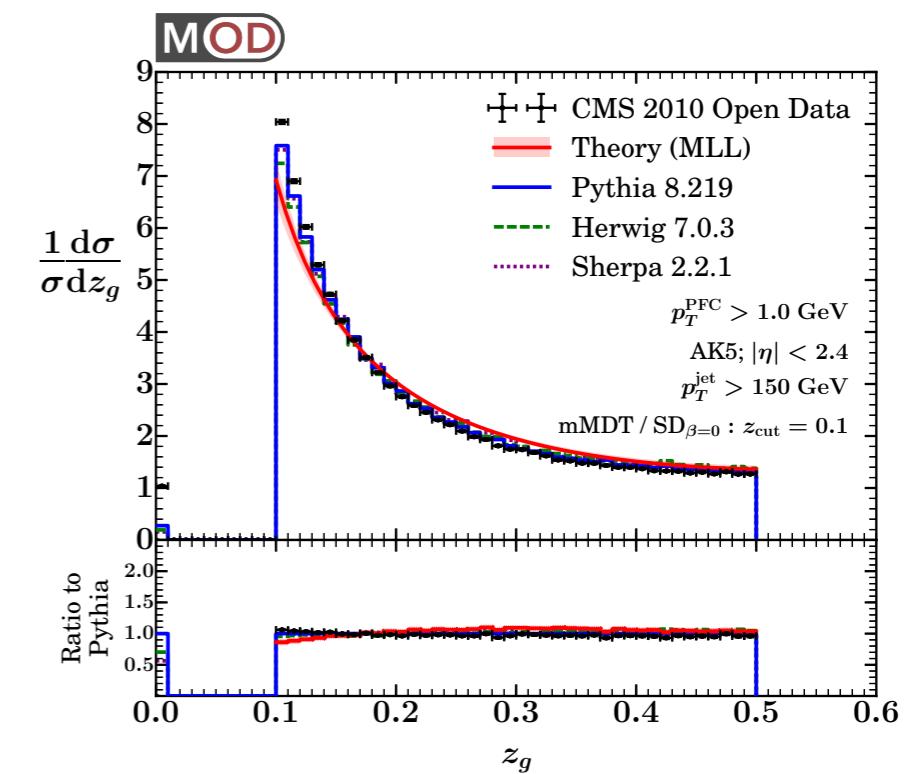
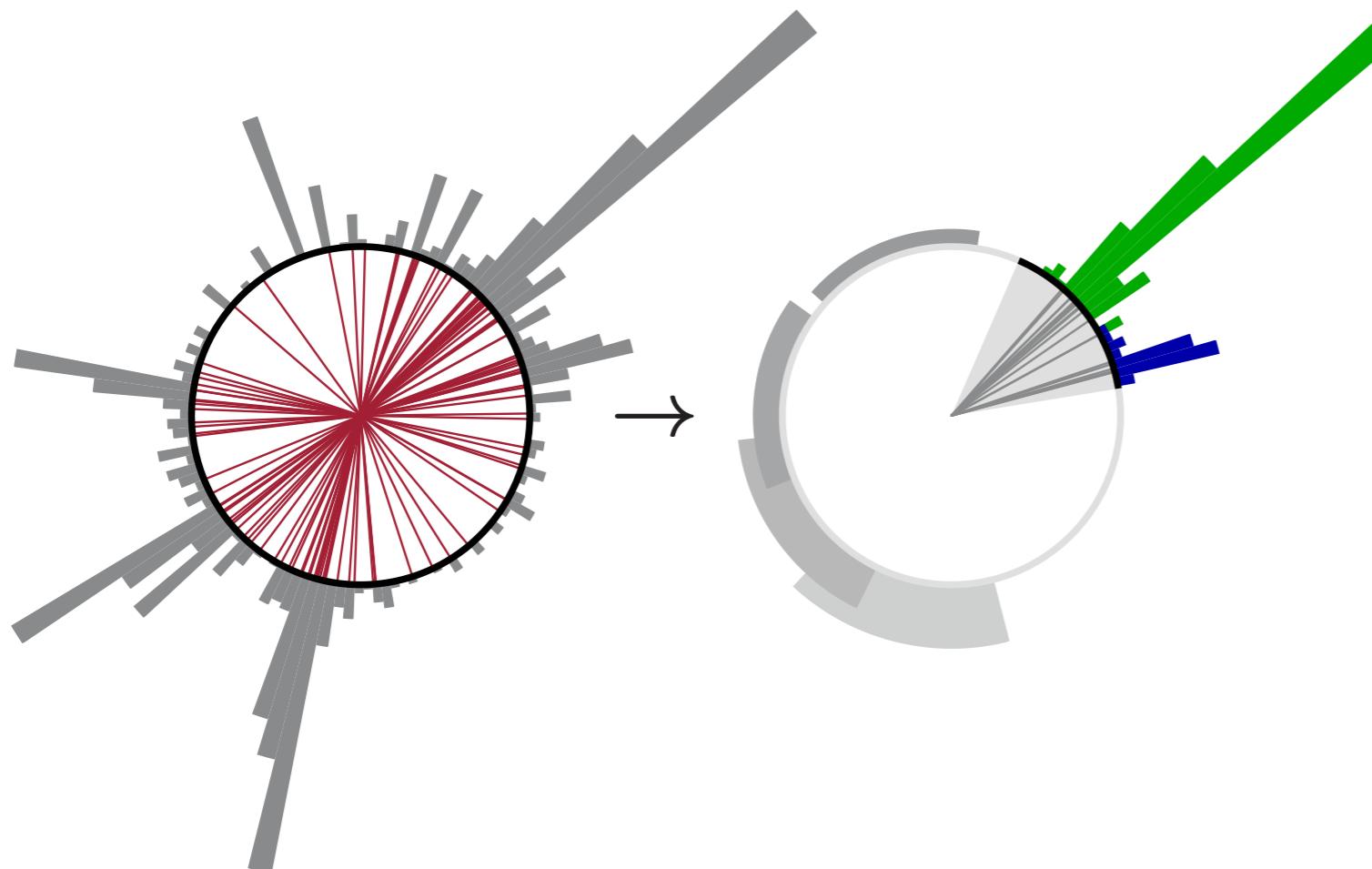
Initial Physics Studies
A geometric language for collider data exploration



(Broader Comments)
Machine learning as a pathway to LHC discoveries

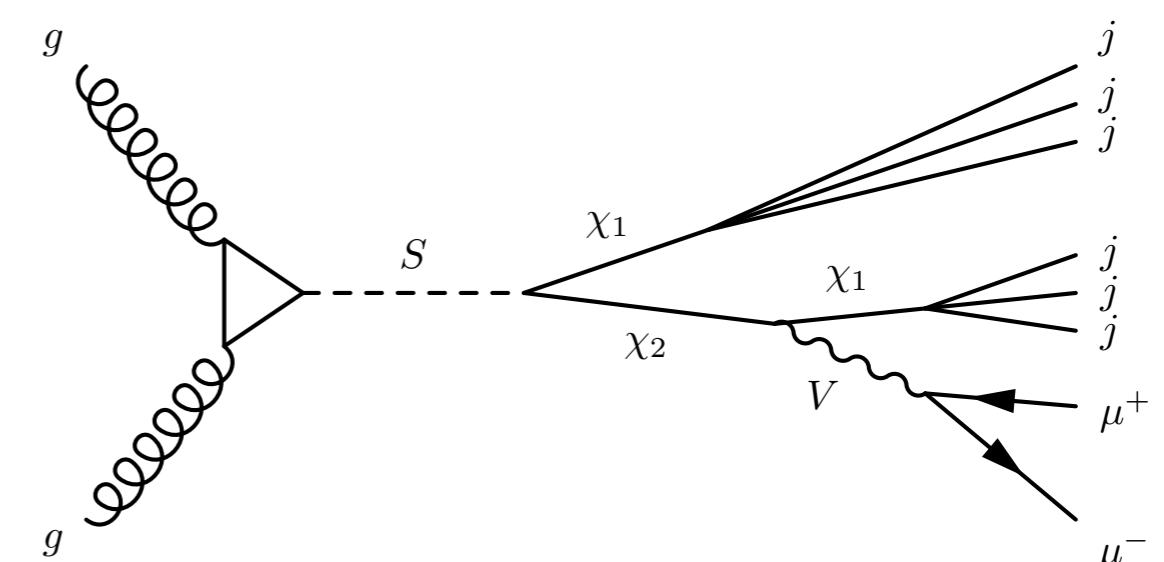
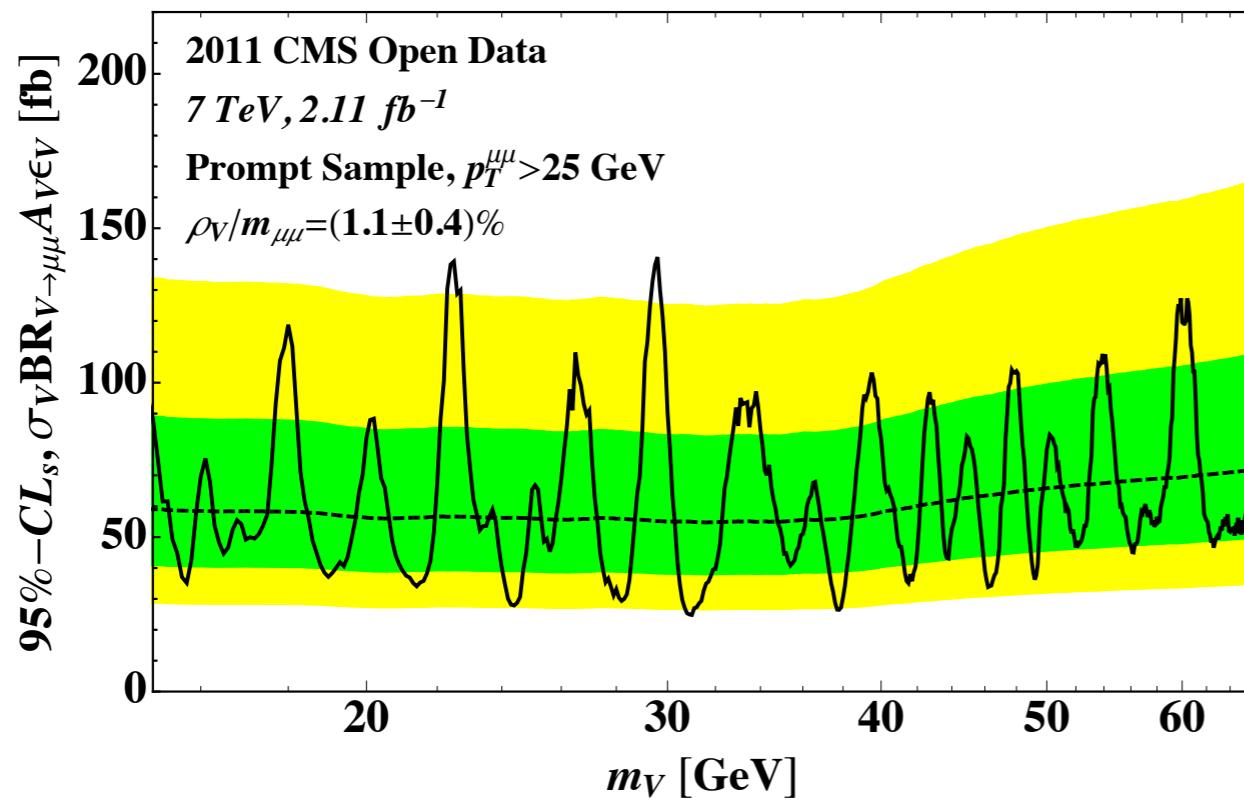
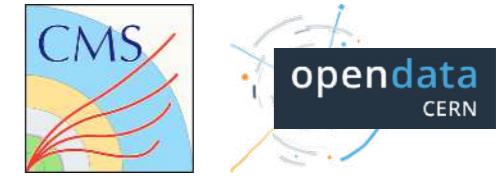
Backup Slides

Event Displays vs. Histograms ...



[Larkoski, Marzani, JDT, Tripathee, Xue, [I704.05066](#)]

... vs. Brazil Plots vs. Cartoons



[Cesarotti, Soreq, Strassler, JDT, Xue, [1902.04222](#)]