

# Deep Learning for Collider Physics Simulation

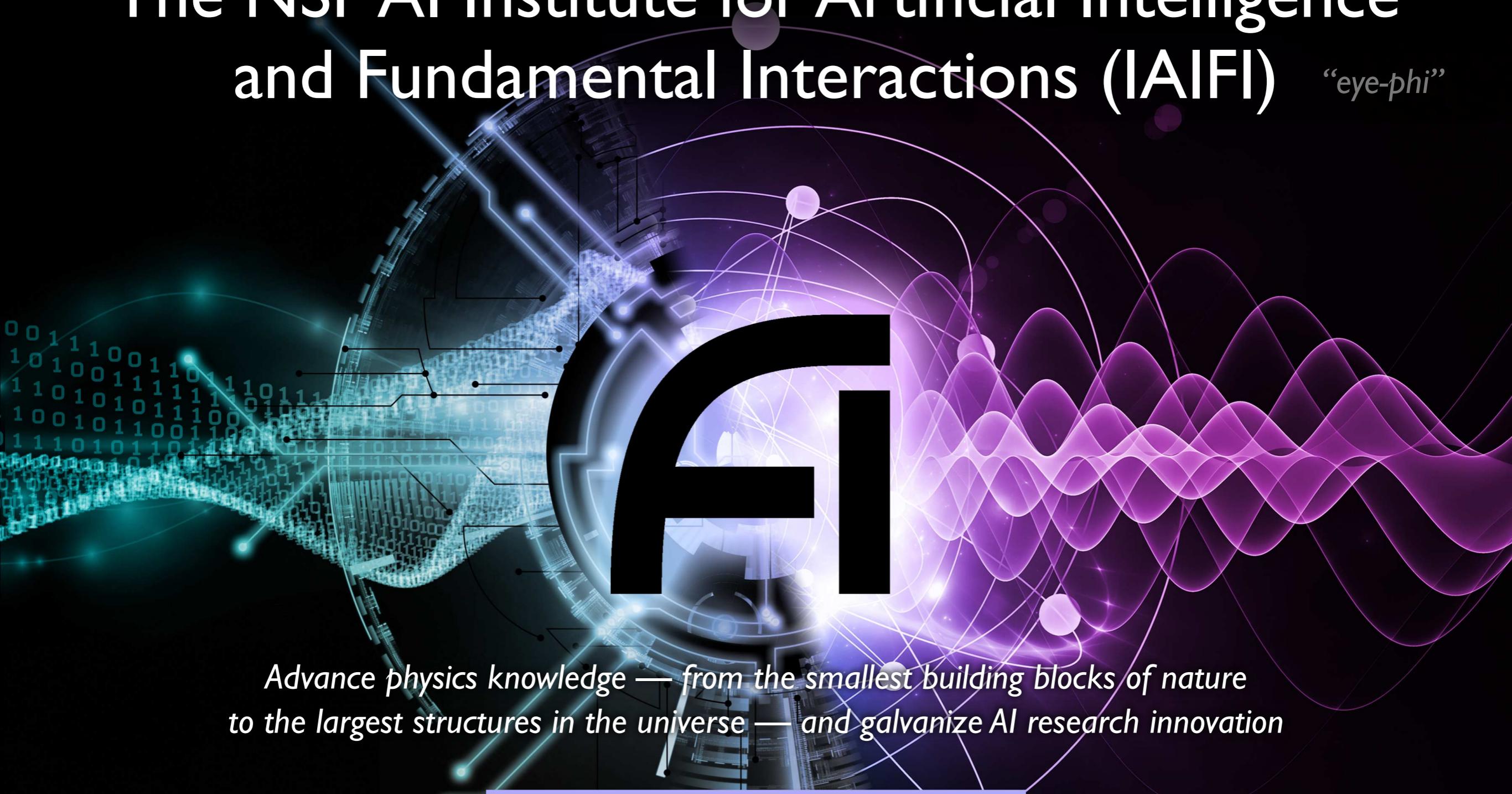
Jesse Thaler



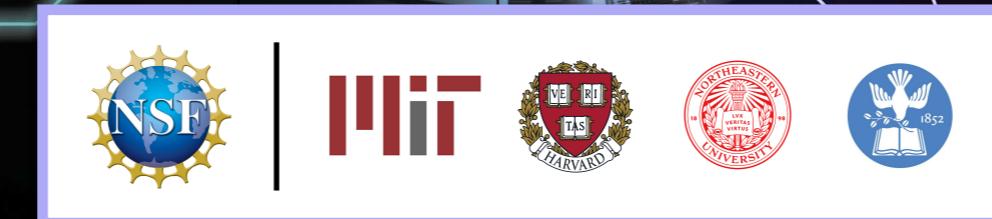
Deep Learning for Simulation, ICLR 2021 Workshop — May 7, 2021

# The NSF AI Institute for Artificial Intelligence and Fundamental Interactions (IAIFI)

“eye-phi”



*Advance physics knowledge — from the smallest building blocks of nature  
to the largest structures in the universe — and galvanize AI research innovation*



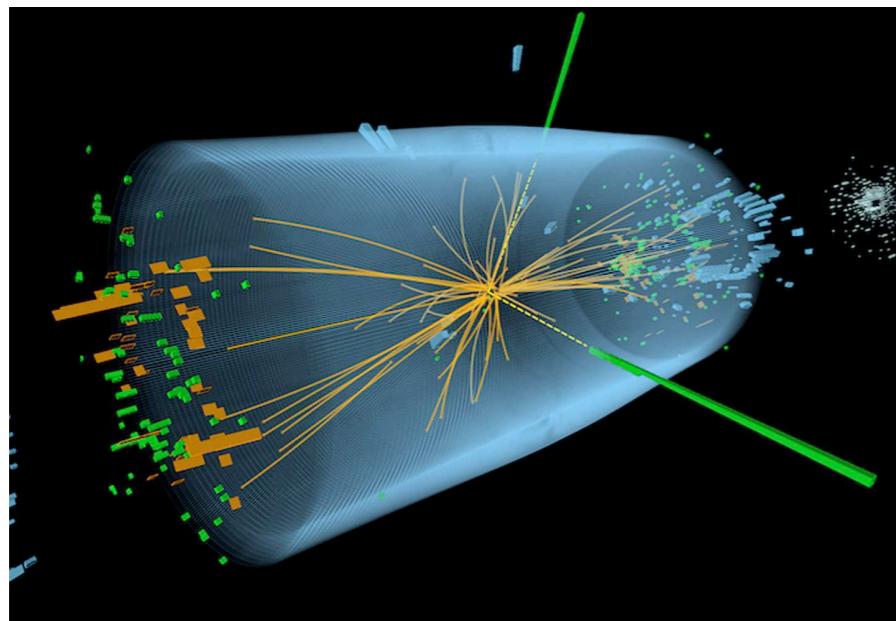
[<http://iaifi.org>, MIT News Announcement]

# Simulation in Collider Physics?

*SimDL: “We define simulation as the process of **iteratively generating output** of the next time step using the **output** of the previous time step as **input** **starting from an initial condition.**”*

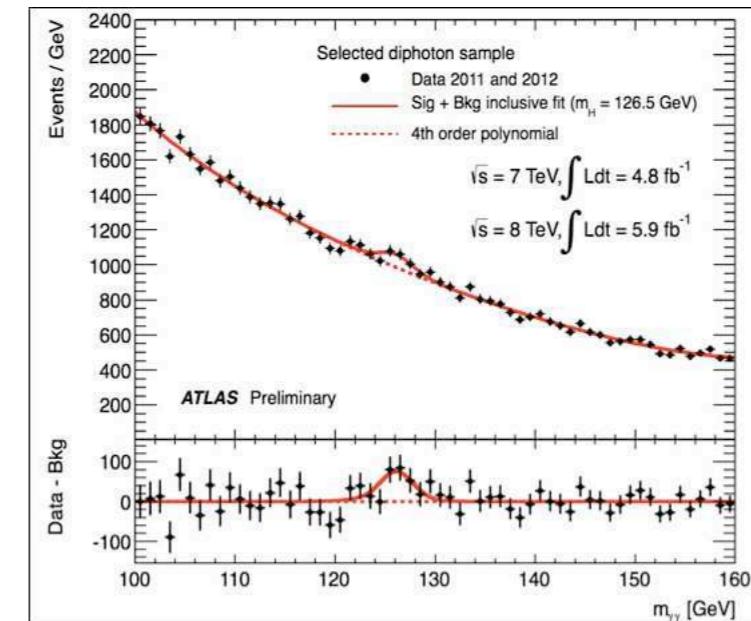
Does collider physics fit into this paradigm?

Yes, for simulating  
one collision event



(not my area of expertise)

No, when considering an  
ensemble of collisions

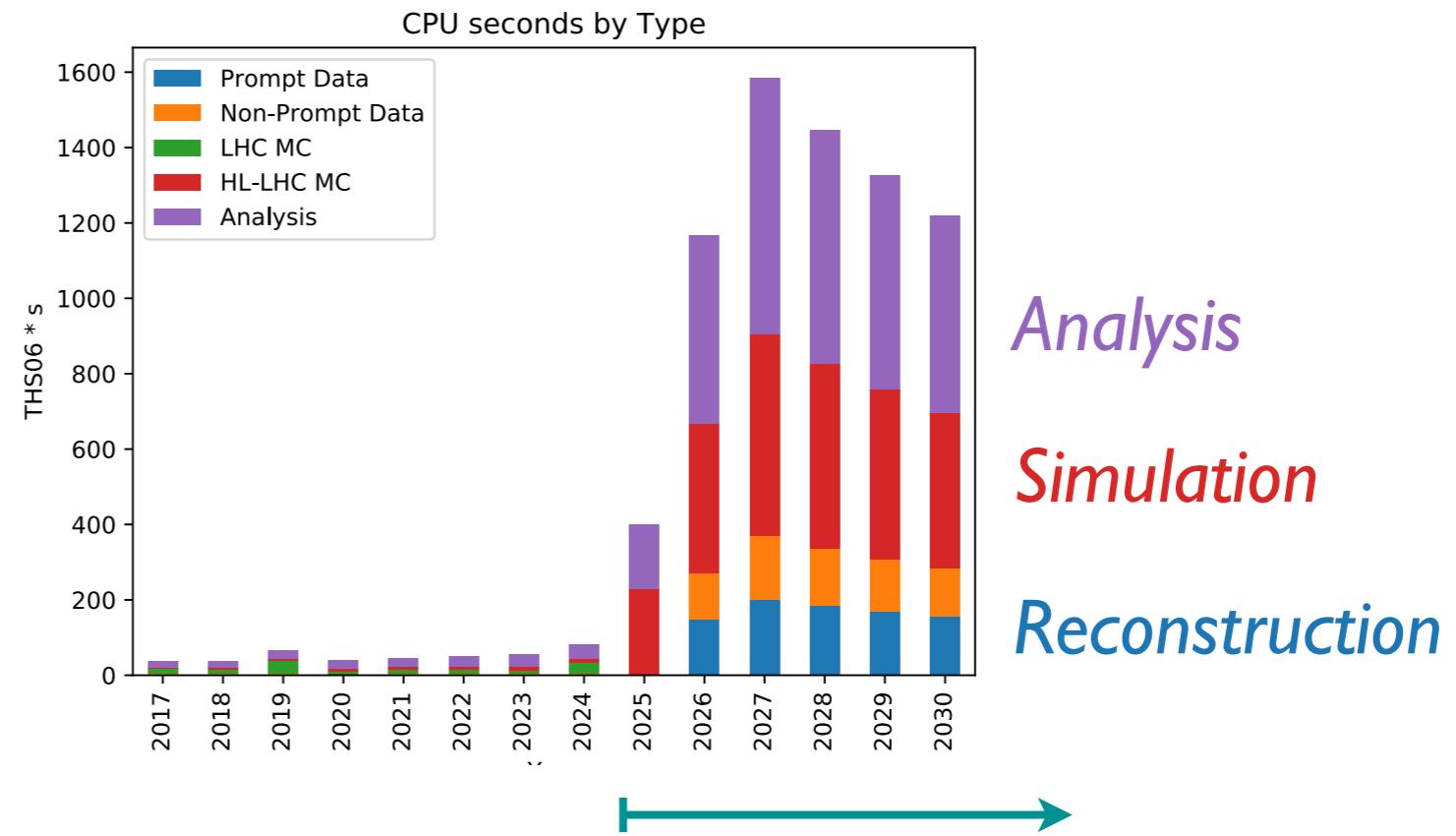
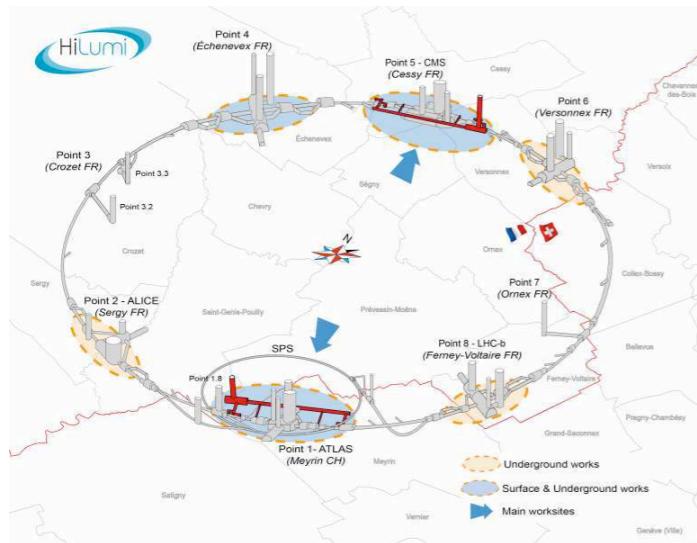


(key focus of my machine learning research)

# Challenges for Simulating One Collision

(again & again & again  
& again & again & ...)

## Ballooning Computational Cost for the High Luminosity Large Hadron Collider



Plus: Few intermediate checkpoints, heterogeneous software tools, inefficient computational workflows, supporting career development...

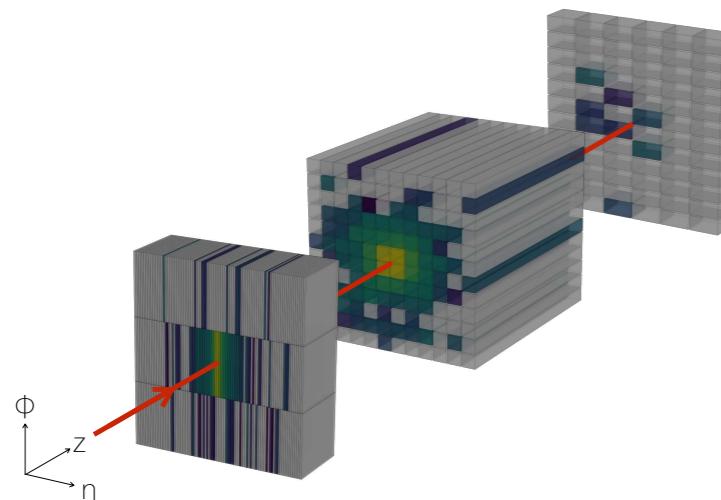
[HEP Software Foundation, [CSBS 2019](#), HSF Physics Event Generator Working Group, [arXiv 2020](#)]

# Challenges for Simulating One Collision

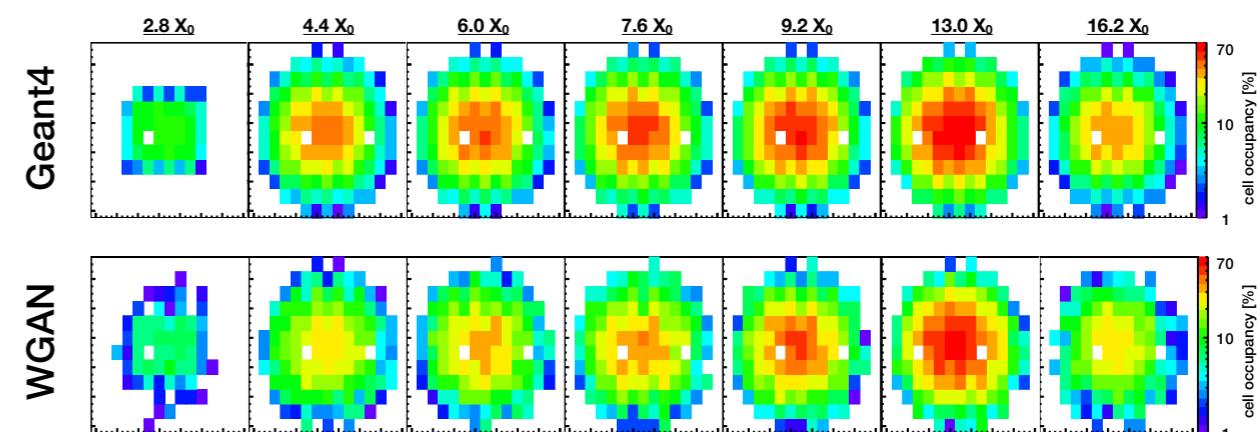
(again & again & again  
& again & again & ...)

*For Another Talk: Accelerating Simulation with Deep Learning*

e.g. Electromagnetic Calorimetry with Adversarial Networks



[Paganini, de Oliveira, Nachman, [PRD 2018](#)]



[Erdmann, Glombitza, Quast, [CSBS 2019](#)]

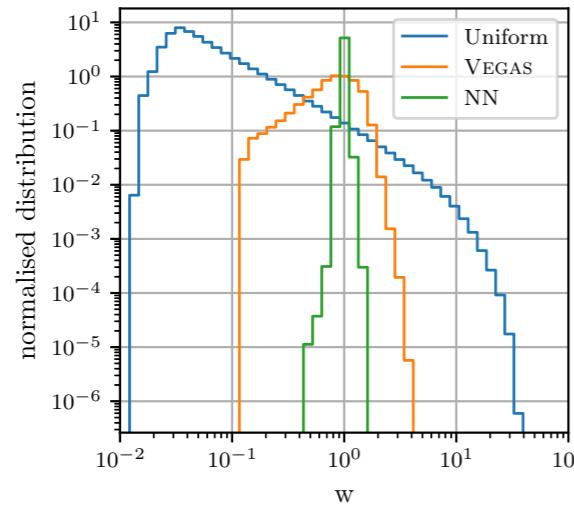
[for complete bibliography, see [HEP-ML Living Review](#)]

Plus: Few intermediate checkpoints, heterogeneous software tools,  
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[HEP Software Foundation, [CSBS 2019](#), HSF Physics Event Generator Working Group, [arXiv 2020](#)]

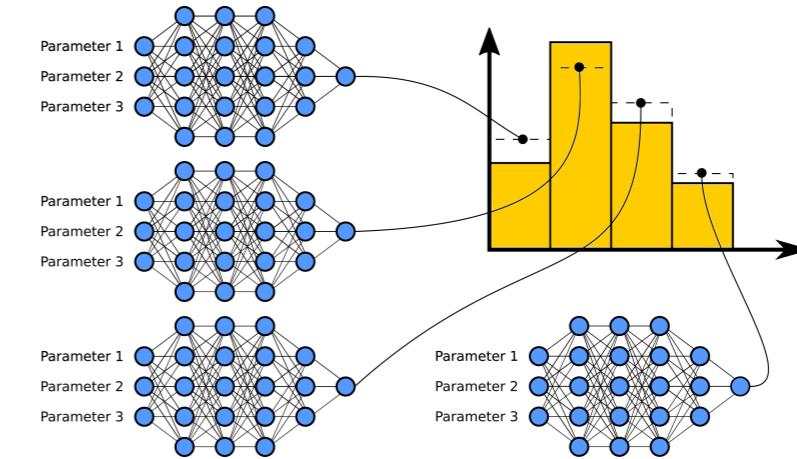
# Challenges for Simulating Collision Ensembles

## Phase Space Sampling



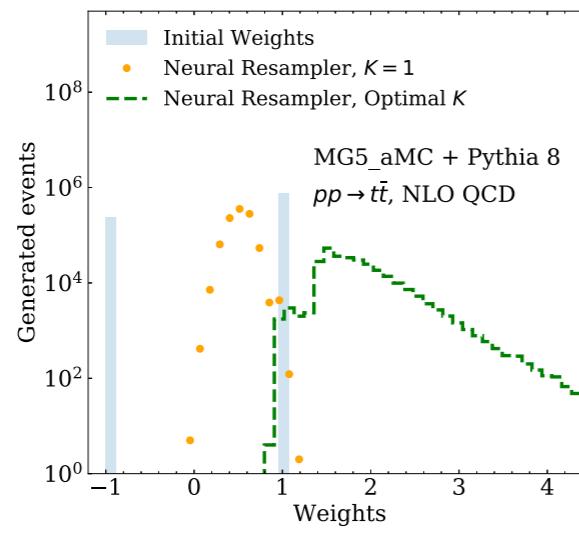
[Bothmann, Janßen, Knobbe, Schmale, Schumann, [SciPost 2020](#)]

## Parameter Tuning



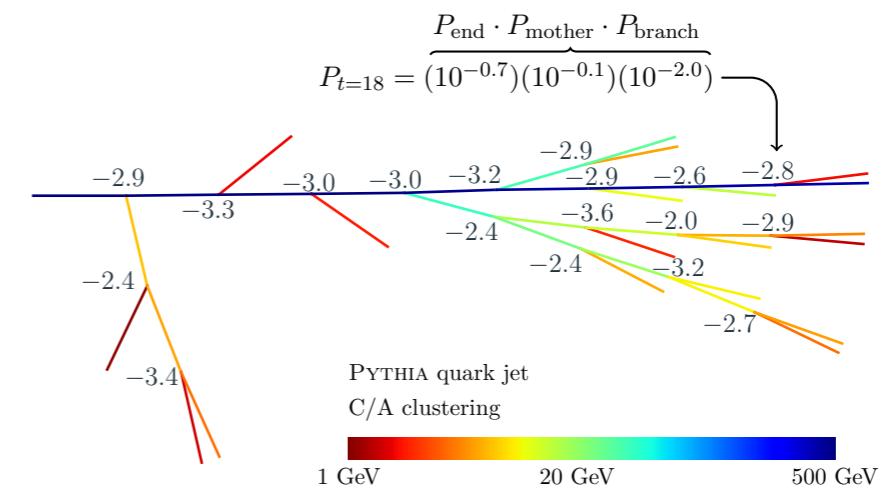
[Lazzarin, Alioli, Carrazza, [CPC 2021](#)]

## Negative Weights



[Nachman, JDT, [PRD 2020](#)]

## Interpretability



[Andreassen, Feige, Frye, Schwartz, [EPJC 2019](#)]

[for complete bibliography, see [HEP-ML Living Review](#)]

# Challenges for Simulating Collision Ensembles

*Key take away from this talk:*

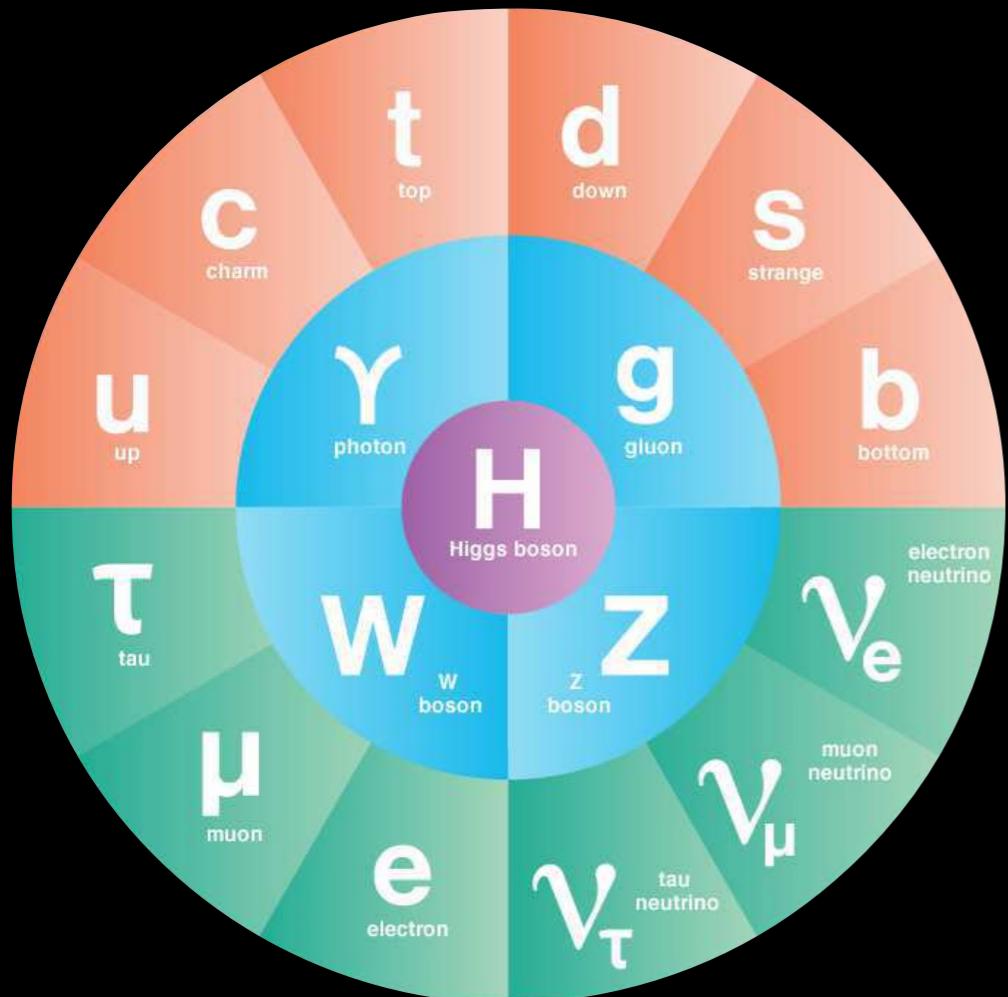
Collider physics deals with large sets of  
**independent and identically distributed data**

Here, **simulation tasks** (generative modeling)  
often map to **classification tasks** (inference)

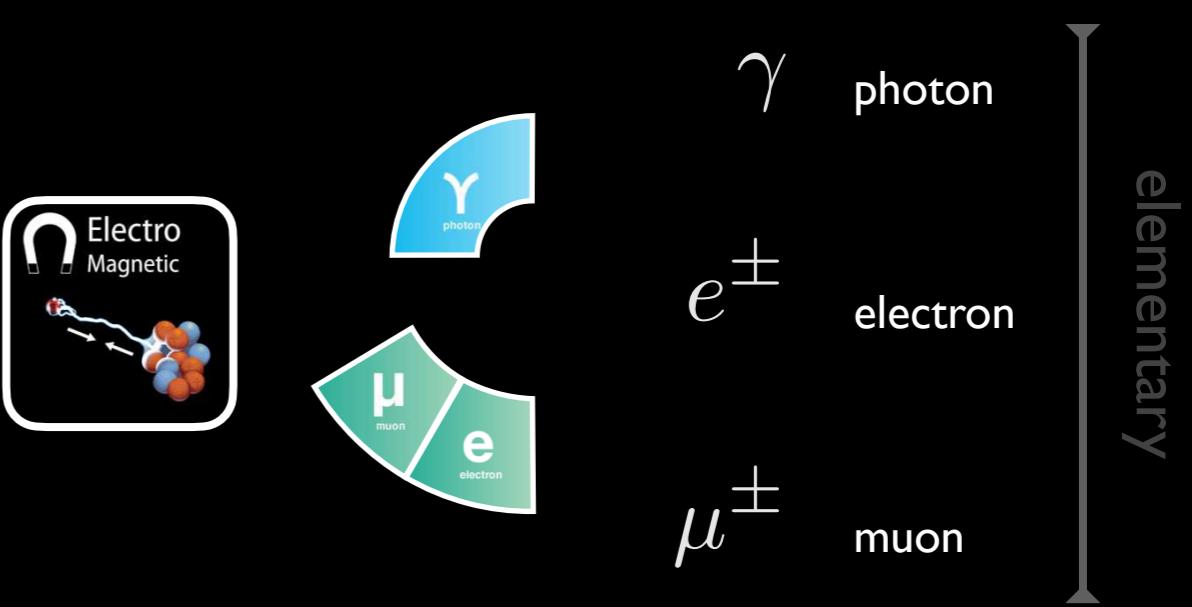
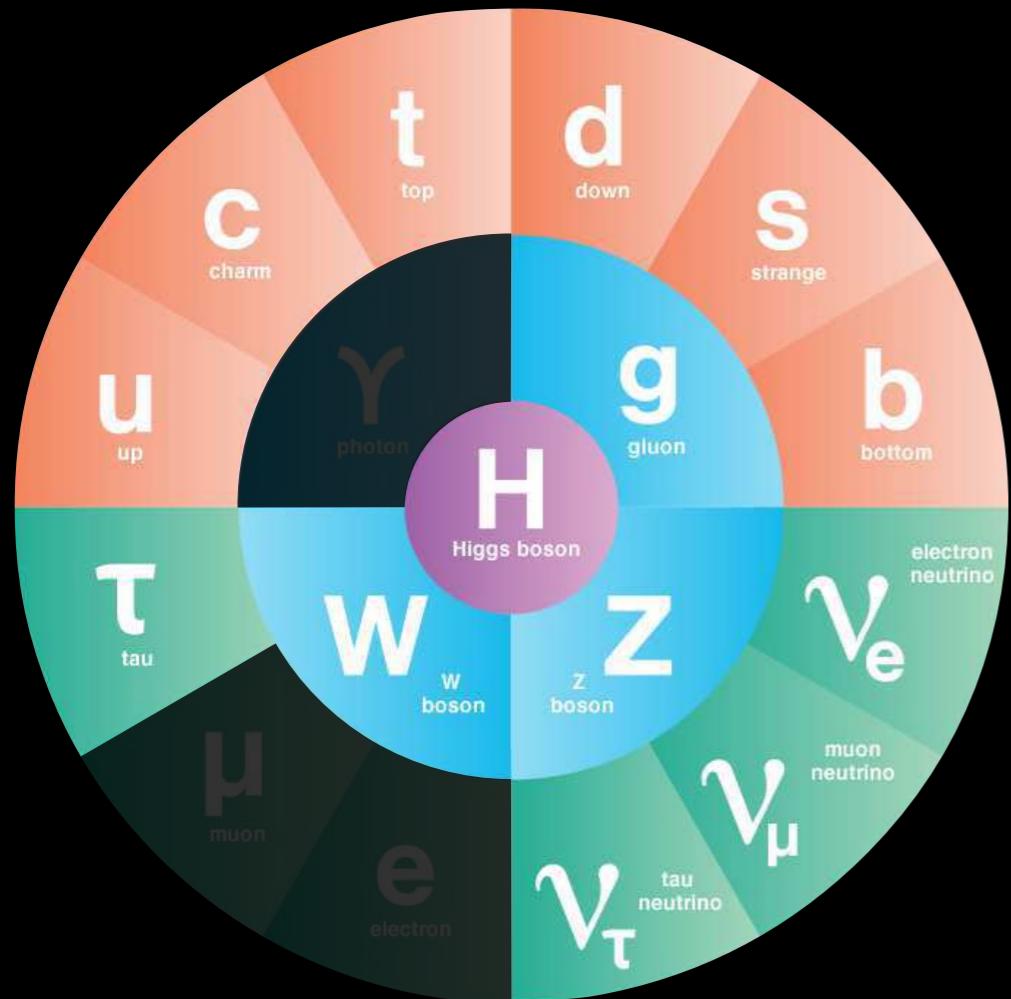
*Deep learning excels at classification*

[for complete bibliography, see [HEP-ML Living Review](#)]

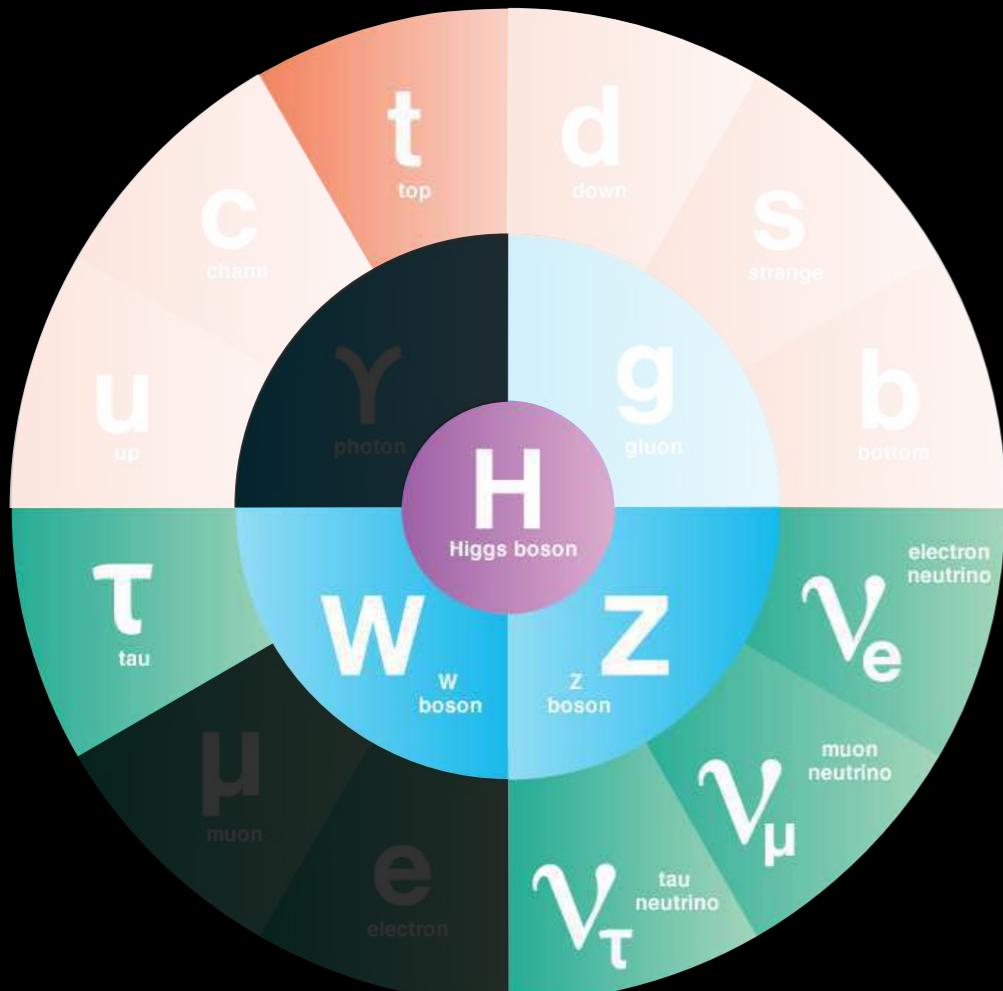
# Particle Physics 101



# Particle Physics 101

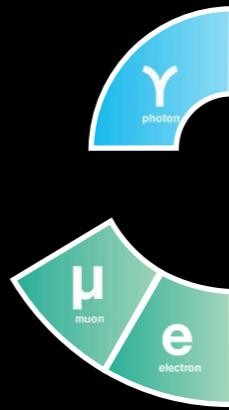
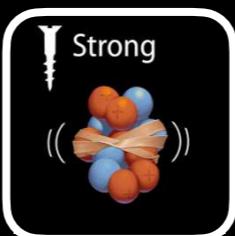


# Particle Physics 101



*QCD Confinement*

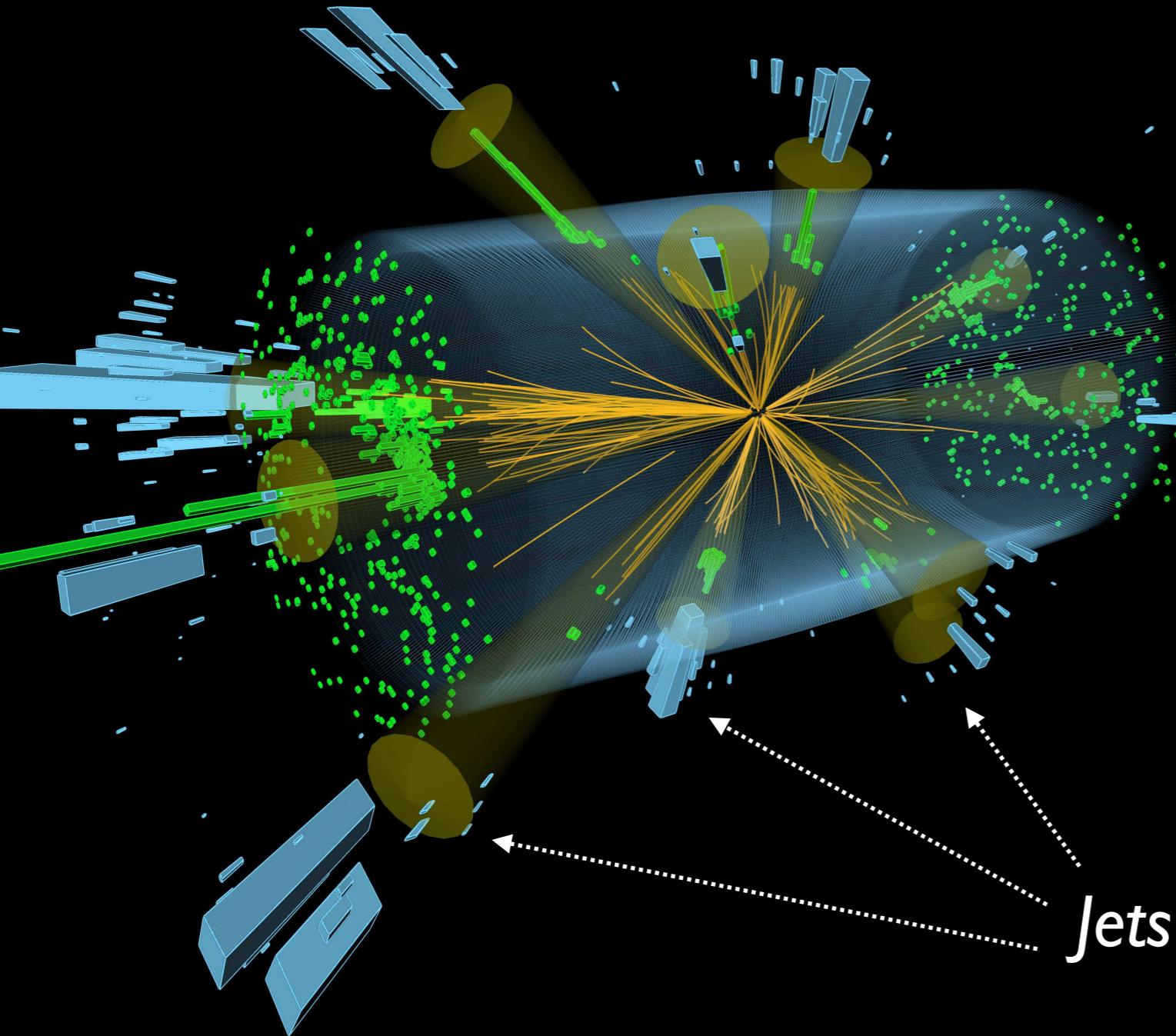
Quarks  
&  
Gluons



$\gamma$	photon	elementary
$e^+$	electron	
$\mu^+$	muon	composite
$\pi^+$	pion	
$K^+$	kaon	composite
$K_L^0$	K-long	
$p/\bar{p}$	proton	composite
$n/\bar{n}$	neutron	

# Collider Event

Every 25 nanoseconds at the LHC



T E H M



$\gamma$

photon



$e^+$

electron



$\mu^+$

muon



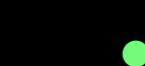
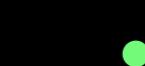
$\pi^+$

pion



$K^+$

kaon



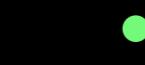
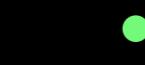
$K_L^0$

K-long



$p/\bar{p}$

proton



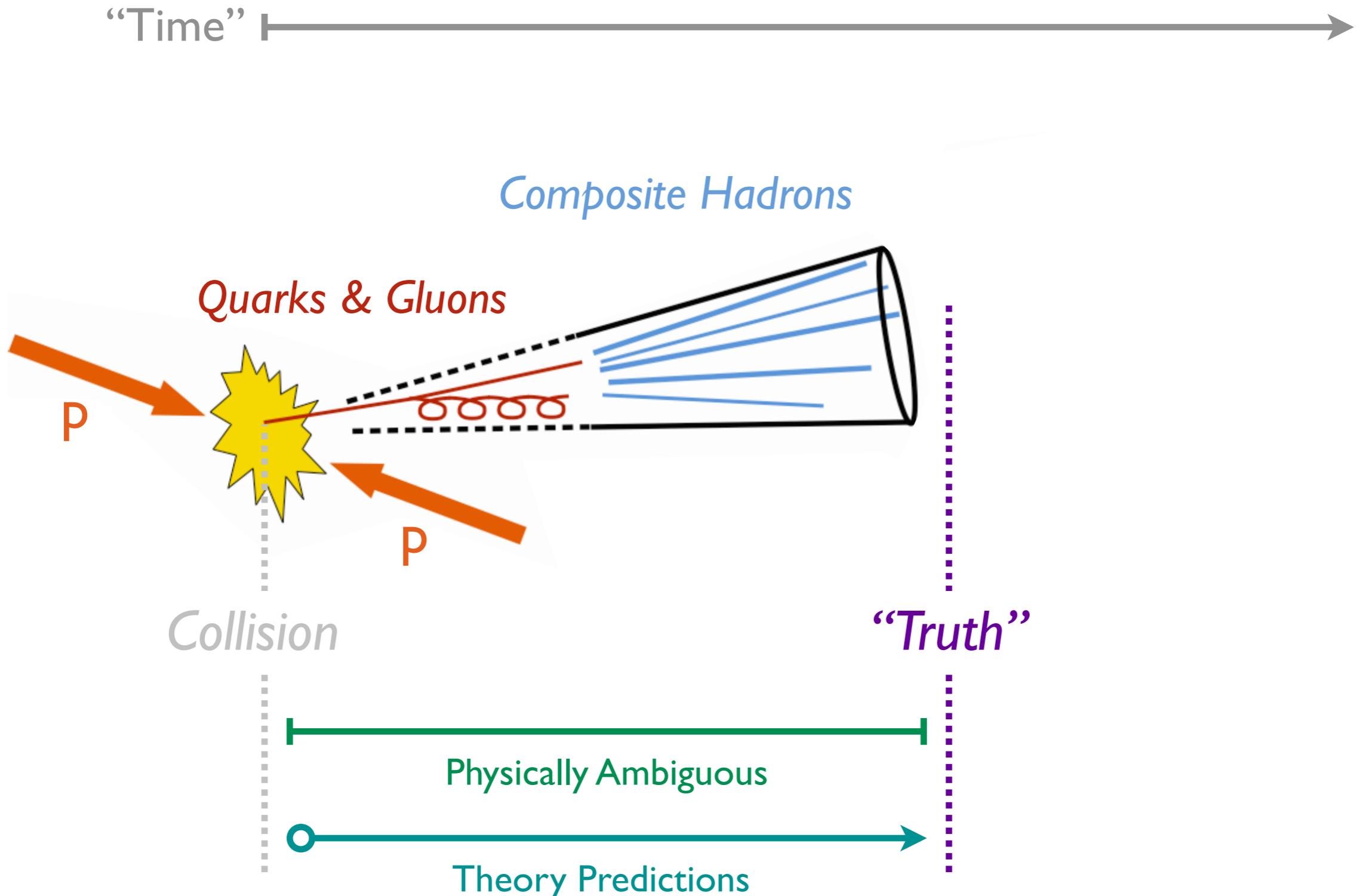
$n/\bar{n}$

neutron

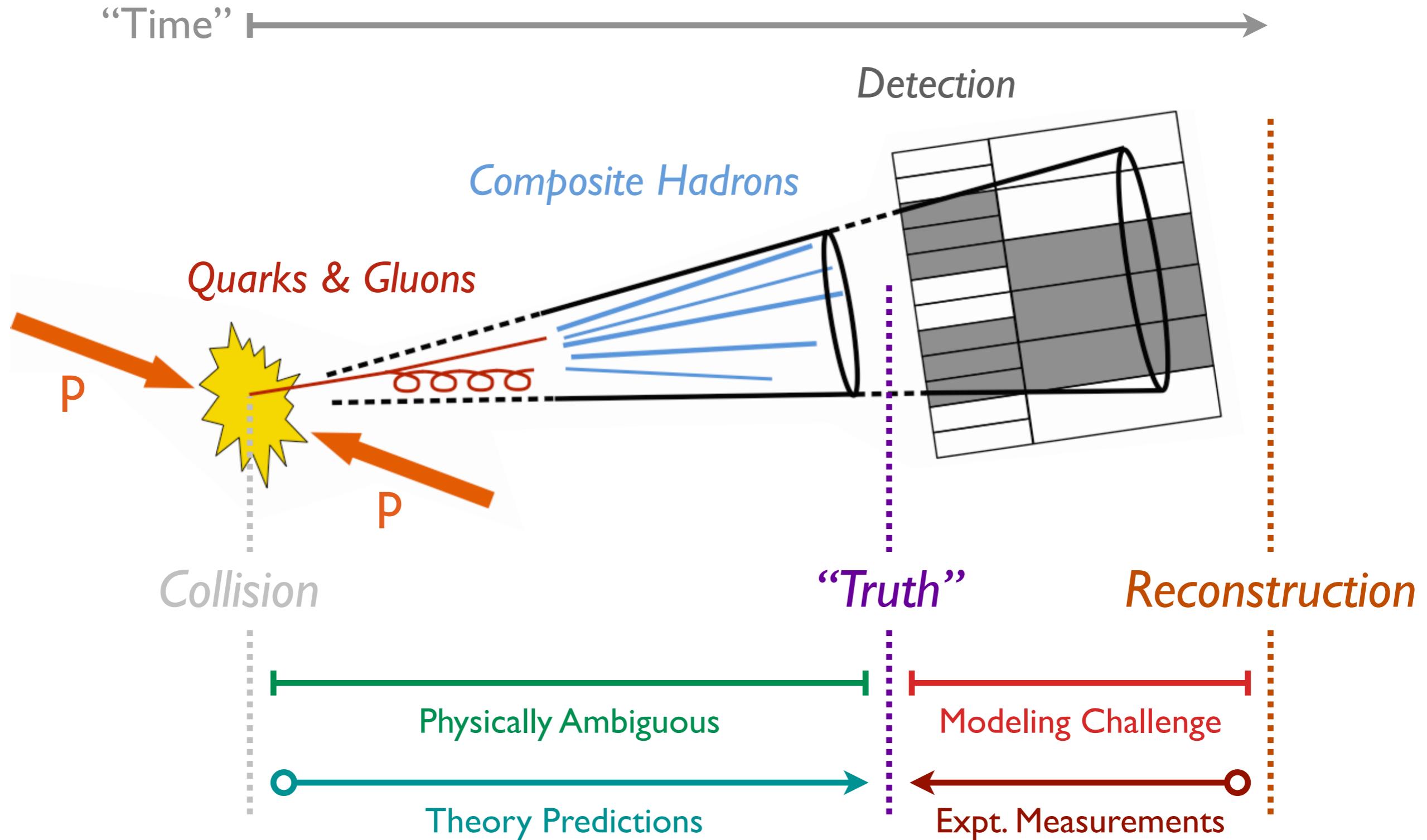
elementary

composite

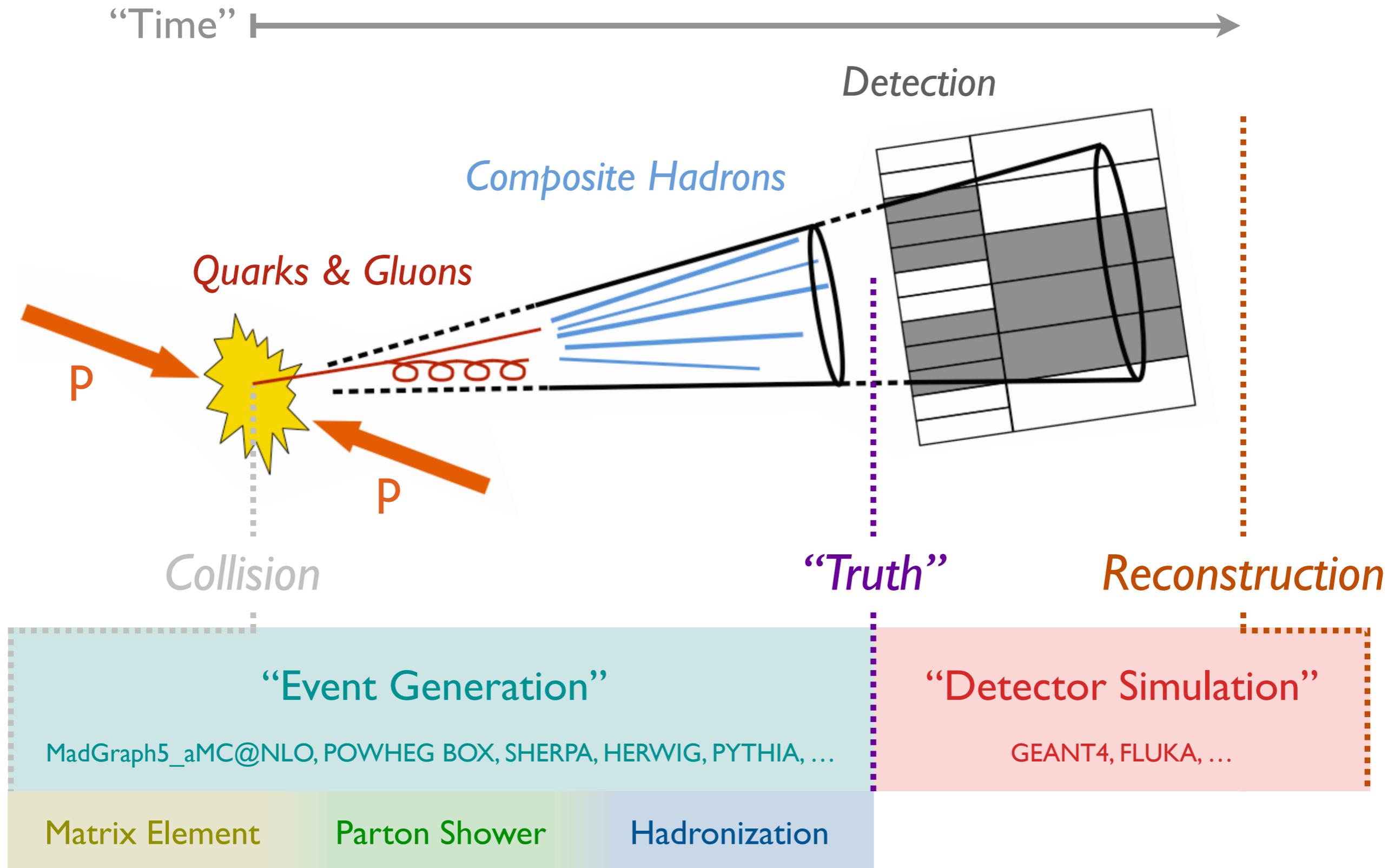
# Simulating LHC Collisions



# Simulating LHC Collisions



# Simulating LHC Collisions



# Simulating LHC Collisions

Key: *Collider data is i.i.d. to excellent approximation*

Independent  
& Identical:

$$p(\{x_1, x_2, \dots, x_N\}) = \prod_{i=1}^N p(x_i)$$

Simulation =  
“Generation” +  
“Simulation”:

$$\int dt \underbrace{p_{\text{Gen}}(t)}_{\text{———}} \underbrace{p_{\text{Sim}}(\mathbf{r}|t)}_{\text{———}} = p(\mathbf{r})$$

Collision

“Truth”

Reconstruction

“Event Generation”

“Detector Simulation”

MadGraph5\_aMC@NLO, POWHEG BOX, SHERPA, HERWIG, PYTHIA, ...

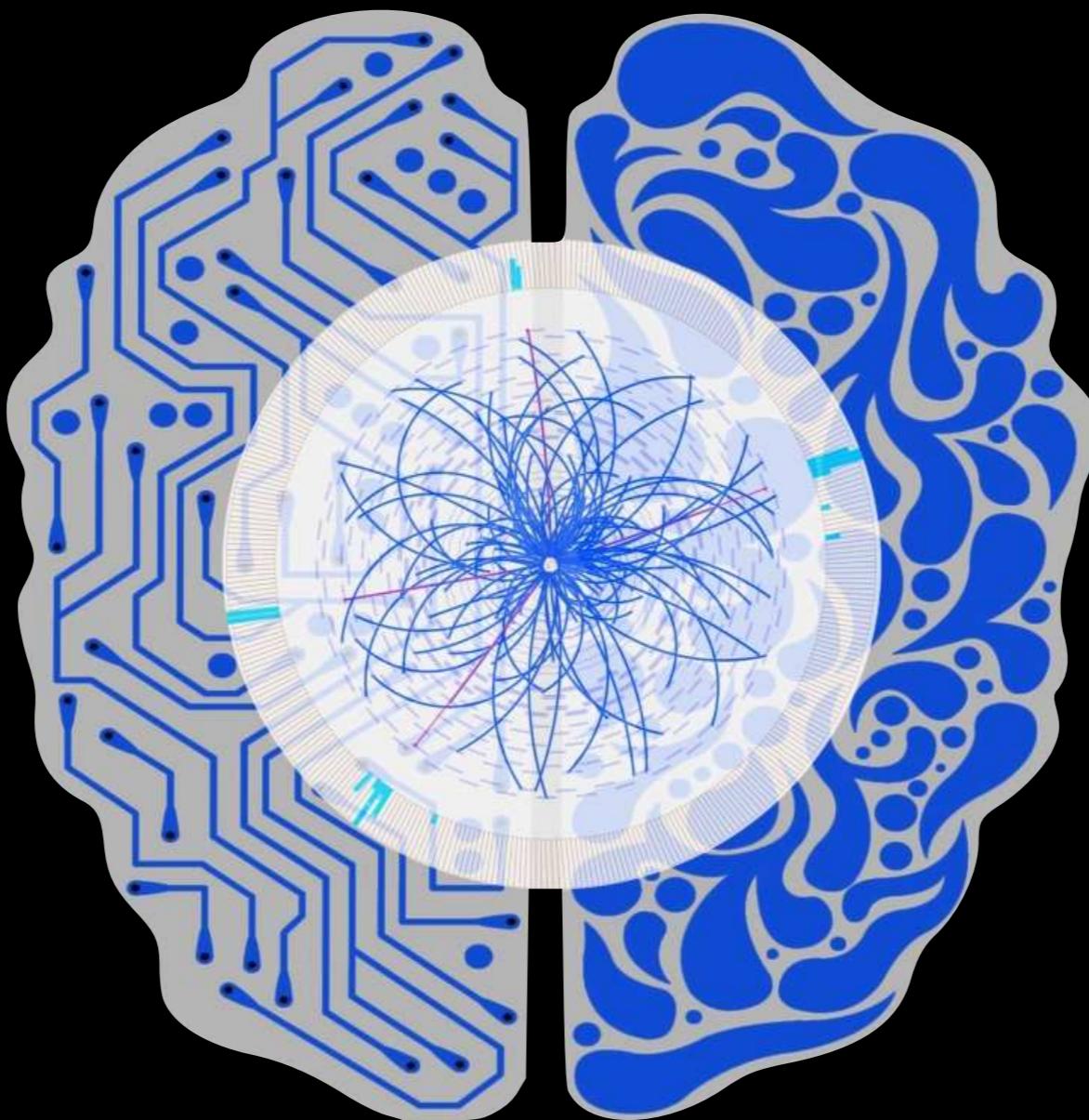
GEANT4, FLUKA, ...

Matrix Element

Parton Shower

Hadronization

# Deep Learning for Inference



*When can simulation be cast as classification?*

# Likelihood Ratio Trick

Many collider physics problems  
can be expressed in this form!

Key example of *simulation-based inference*

Goal: Estimate  $p(x)$  /  $q(x)$

Training Data: Finite samples  $P$  and  $Q$

Learnable Function:  $f(x)$  parametrized by, e.g., neural networks

Loss Function(al):  $L = -\langle \log f(x) \rangle_P + \langle f(x) - 1 \rangle_Q$

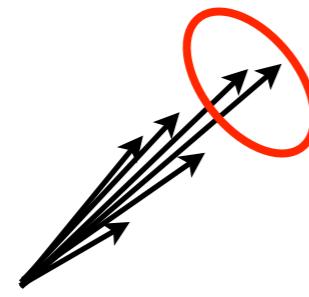
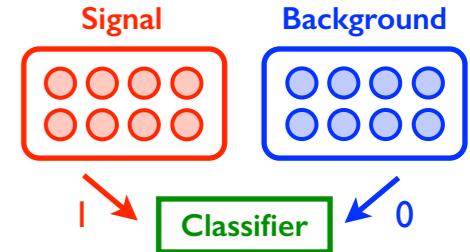
Asymptotically:  $\arg \min L = \frac{p(x)}{q(x)}$  *Likelihood ratio*

$-\min_{f(x)} L = \int dx p(x) \log \frac{p(x)}{q(x)}$  *Kullback–Leibler divergence*

[see e.g. D’Agnolo, Wulzer, [PRD 2019](#); simulation-based inference in Cranmer, Brehmer, Louppe, [PNAS 2020](#); relation to f-divergences in Nguyen, Wainwright, Jordan, [AoS 2009](#); Nachman, JDT, [arXiv 2021](#)]

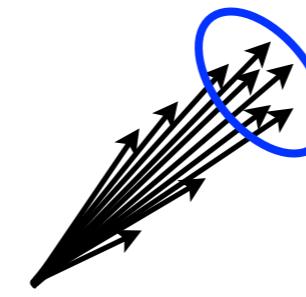
# Quark/Gluon Classification

“Hello, World!” of Jet Physics



Quark  
 $C_q = 4/3$

vs.



Gluon  
 $C_g = 3 = 9/3$

Find  $h\left(\begin{array}{c} \nearrow \\ \nearrow \\ \nearrow \\ \nearrow \\ \nearrow \end{array}\right)$

such that

$$h(\text{Quark}) = 1$$

$$h(\text{Gluon}) = 0$$

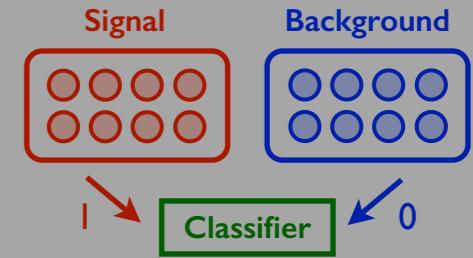
Best you can do: 
$$h(\mathcal{J}) = \left( 1 + \frac{p(\mathcal{J}|G)}{p(\mathcal{J}|Q)} \right)^{-1}$$
  
(Neyman-Pearson lemma)

*Likelihood ratio yields optimal binary classifier (and vice versa)*

[see e.g. Gras, Höche, Kar, Larkoski, Lönnblad, Plätzer, Siódmok, Skands, Soyez, JDT, [JHEP 2017](#); Komiske, Metodiev, Schwartz, [JHEP 2017](#); Komiske, Metodiev, JDT, [JHEP 2018](#)]

# Quark/Gluon Classification

“Hello, World!” of Jet Physics



*This is all well and good,  
but what does **binary classification**  
have to do with **simulation**?*

*Likelihood ratio yields optimal **binary classifier** (and vice versa)*

[see e.g. Gras, Höche, Kar, Larkoski, Lönnblad, Plätzer, Siódmok, Skands, Soyez, JDT, [JHEP 2017](#); Komiske, Metodiev, Schwartz, [JHEP 2017](#); Komiske, Metodiev, JDT, [JHEP 2018](#)]

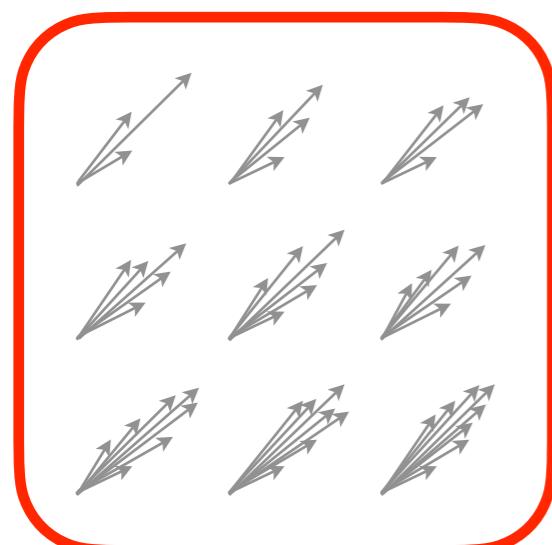
# From Tautology to Essential Tool

Remember that *collider data is i.i.d.*

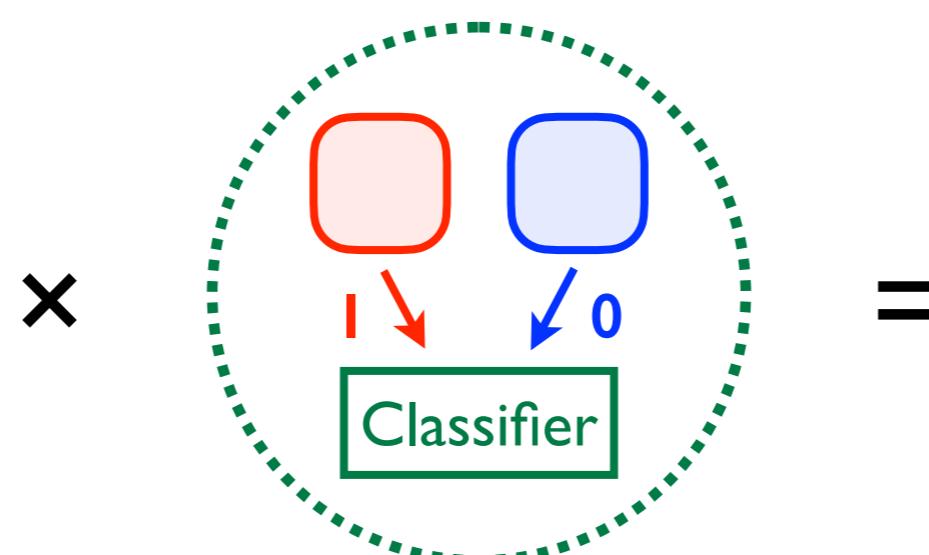
[see i.i.d. discussion in  
Nachman, JDT, arXiv 2021]

$$q(x) \times \frac{p(x)}{q(x)} = p(x)$$

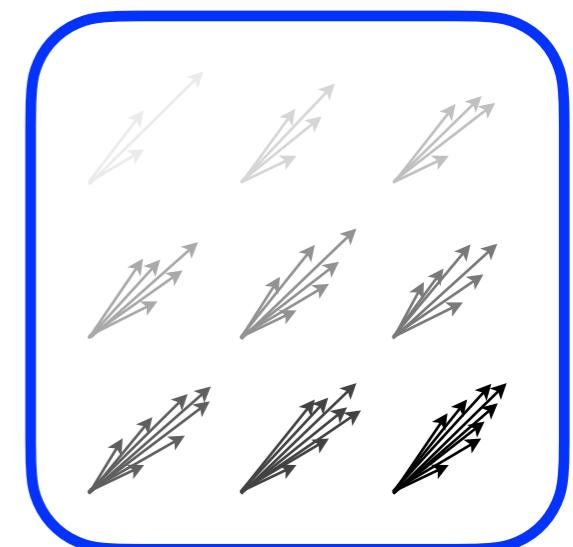
Generate samples  
according to Q



Weight each sample by  
likelihood ratio



Obtain weighted samples  
distributed according to P



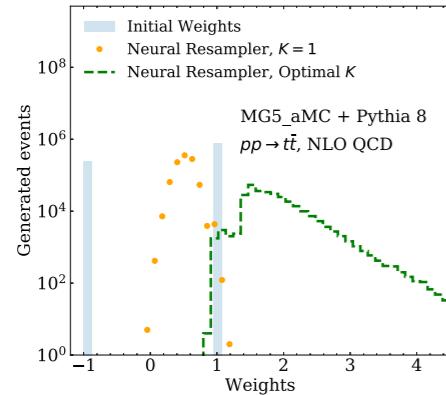
With large enough data samples,  
*binary classification* yield *weighted simulation tool*

# From Curmudgeon to Evangelist



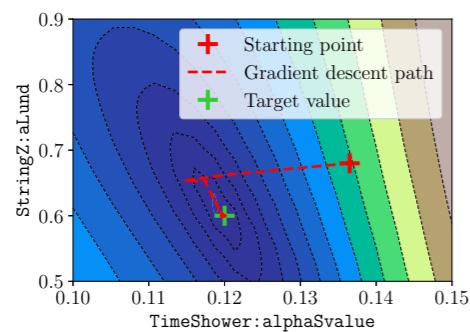
*What simulation problems can be solved with deep learning?*

# Three Collider Simulation Examples



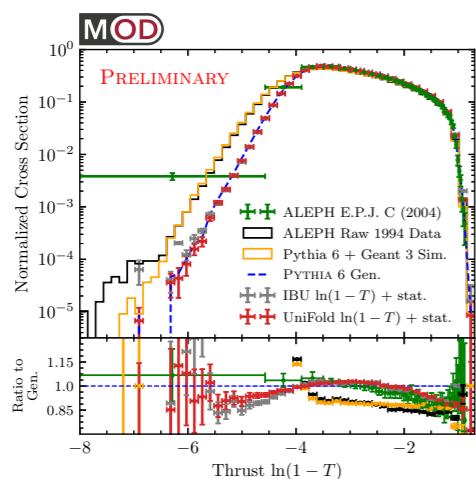
## Removing Negative Weights

Leverages deep learning as *function learning*



## Interpolating Simulation Parameters

Leverages *robust generalizability*



## Deconvolving Detector Effects

Leverages ability to handle *high-dimensional inputs*

# The Challenge of Negative Weights



*How do you interpolate between different calculational schemes?*

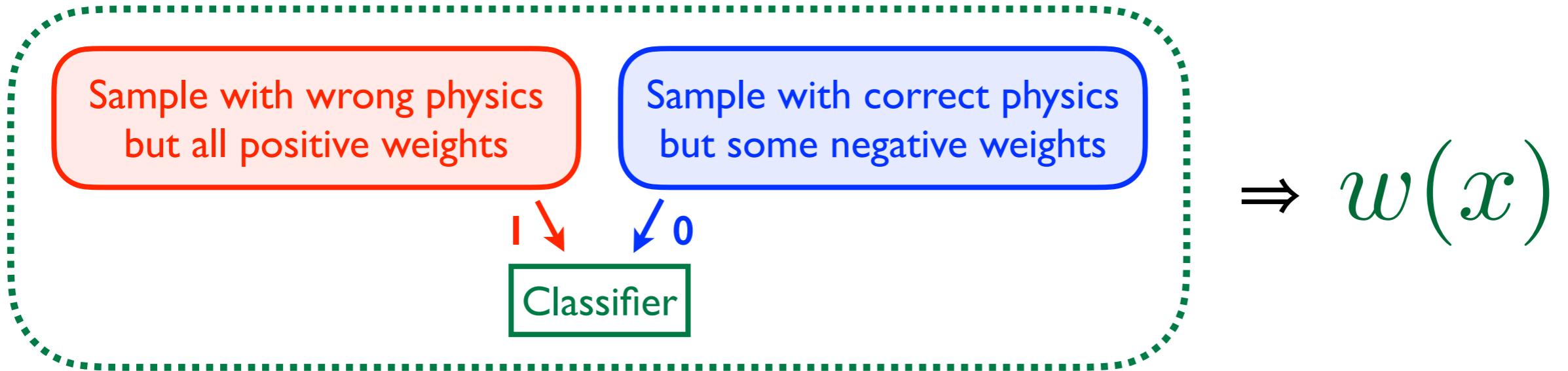
$$p_{\text{improved}}(x) = p_{\text{baseline}}(x) + p_{\text{correction}}(x)$$

↑                      ↑                      ↑  
Positive              Positive by           Could be positive  
(if physics is correct) construction      or negative!

*Often need negative weight events to describe correct physics,  
leading to downstream computational inefficiencies*

[see discussion in Andersen, Gütschow, Maier, Prestel, [EPJC 2020](#)]

# Neural Resampling



**Plain reweighting** yields all positive weights with correct asymptotic probability density

$$p_{\text{wrong}}(x) \times w(x) = p_{\text{correct}}(x)$$

**Improved resampling** through auxiliary neural network yields correct statistical uncertainties

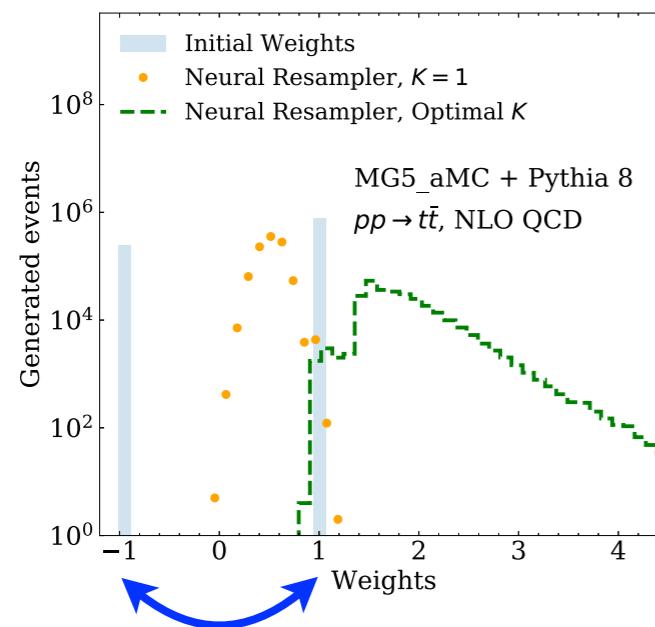
$$\left(\frac{\delta p}{p}\right)^2 = \frac{\langle w^2 \rangle}{\langle w \rangle^2}$$

[Nachman, JDT, PRD 2020]

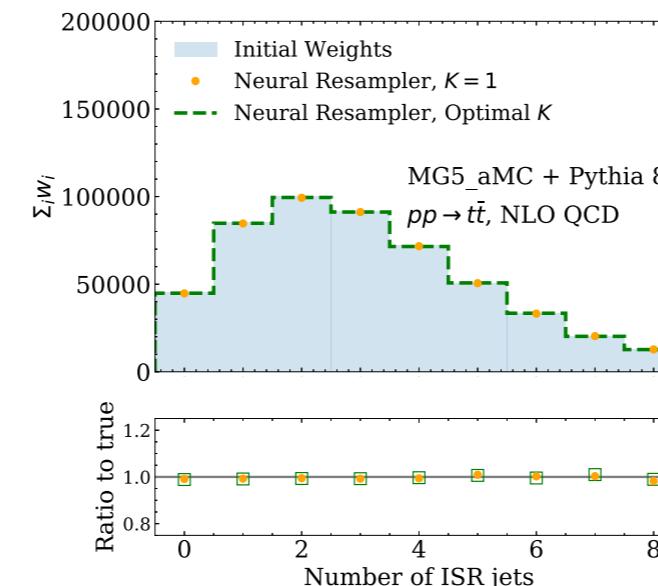
# Neural Resampling

## *Case Study in Jet Physics at Large Hadron Collider*

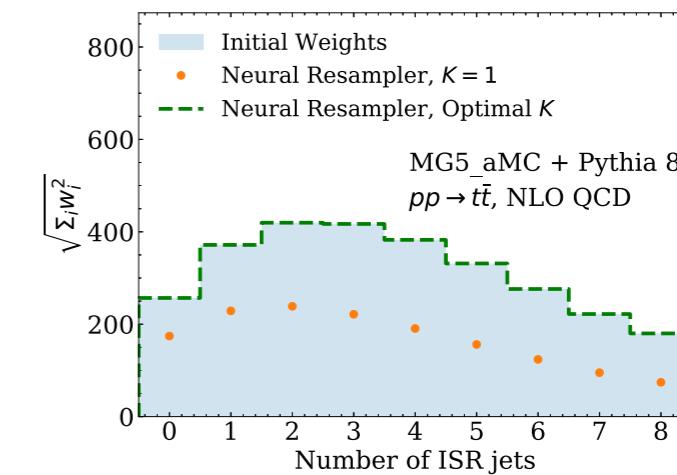
Original sample: large weight cancellations



Reweighting recovers desired distribution



Resampling recovers desired uncertainties



Improved resampling through auxiliary neural network yields correct statistical uncertainties

$$\left( \frac{\delta p}{p} \right)^2 = \frac{\langle w^2 \rangle}{\langle w \rangle^2}$$

[Nachman, JDT, PRD 2020]

# The Challenge of Monte Carlo Tuning



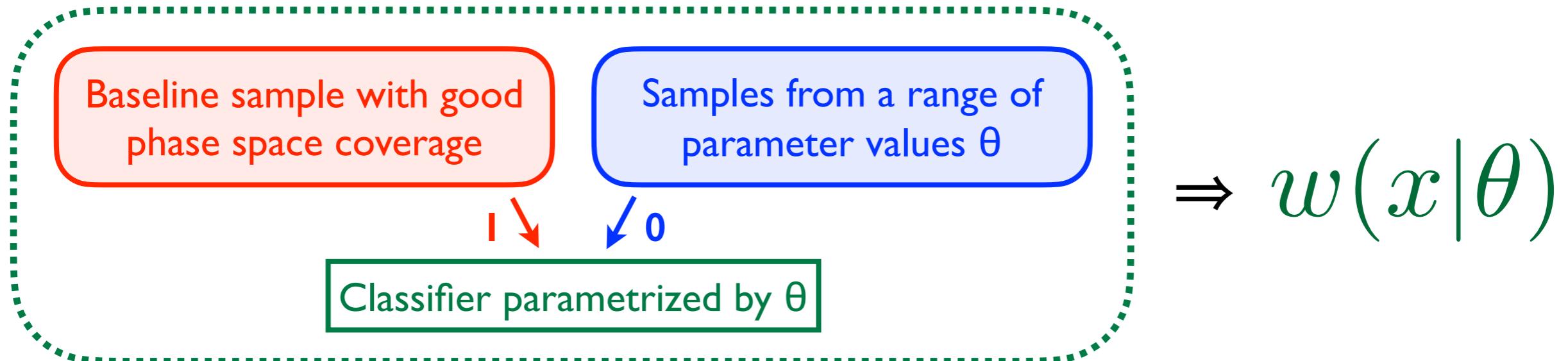
*How do you account for modeling parameters that cannot be predicted from first principles?*

$$\arg \min_{\theta} \text{Dist} \left[ p_{\text{simulation}}(x|\theta) \parallel p_{\text{validation data}}(x) \right]$$

$\uparrow$   
O(10-100) parameter to optimize over

*Daunting computational challenge to simulate all variants*

# Parametrized Classification for Simulation



With good generalizability,  
parametrized classification  
can interpolate parameters

$$p_{\text{baseline}}(x) \times w(x|\theta) = p_{\text{correct}}(x|\theta)$$

Or you can directly perform  
maximum likelihood analysis  
for parameter tuning

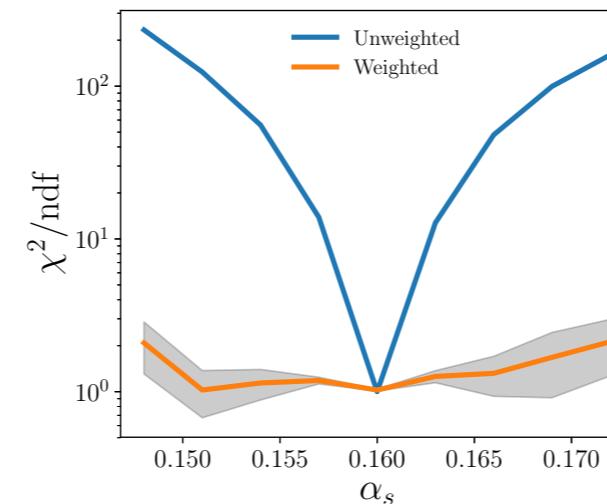
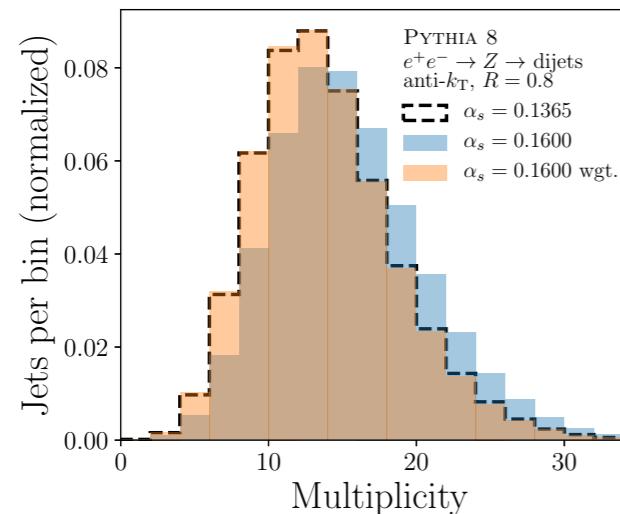
$$w(x|\theta) = \frac{p(x|\theta)}{p(x|\theta_0)}$$

[Cranmer, Pavez, Louppe, [arXiv 2015](#); Baldi, Cranmer, Faucett, Sadowski, Whiteson, [EPJC 2016](#)]

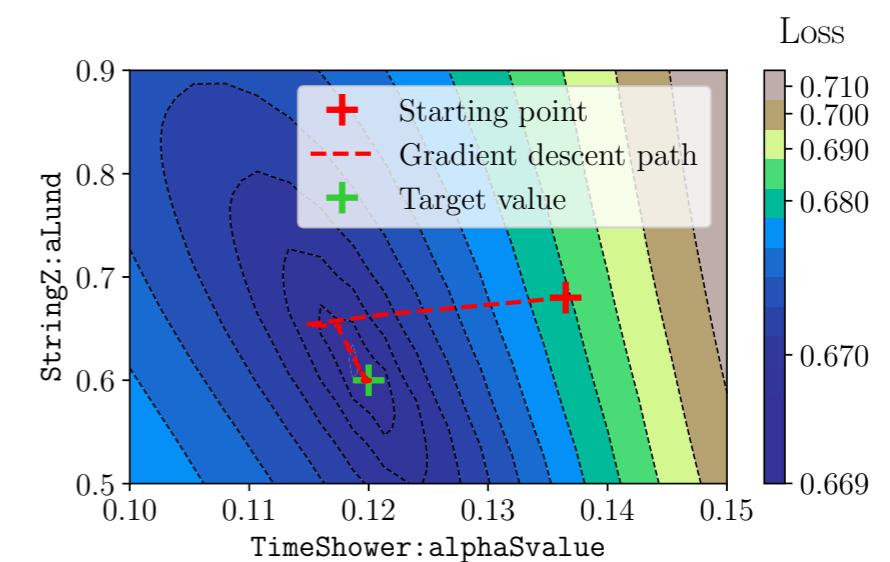
# Parametrized Classification for Simulation

## *Case Study in Tuning Monte Carlo Event Generators*

Reweighted simulation exhibits excellent fidelity with relatively low computational cost



Multidimensional maximum likelihood tuning



[Andreassen, Nachman, [PRD 2020](#)]

Or you can directly perform maximum likelihood analysis for parameter tuning

$$w(x|\theta) = \frac{p(x|\theta)}{p(x|\theta_0)}$$

[Cranmer, Pavez, Louppe, [arXiv 2015](#); Baldi, Cranmer, Fauchet, Sadowski, Whiteson, [EPJC 2016](#)]

# The Challenge of Unfolding

$$\int dt p_{\text{Gen}}(\textcolor{violet}{t}) p_{\text{Sim}}(\textcolor{brown}{r}|\textcolor{violet}{t}) = p(\textcolor{brown}{r})$$

“Truth”

Reconstruction

“Detector Simulation”

GEANT4, FLUKA, ...

*Detector effects must be deconvolved to compare theoretical calculations to experimental measurements*

Iterative reweighting is a known solution to this problem for binned histogram data in low dimensions

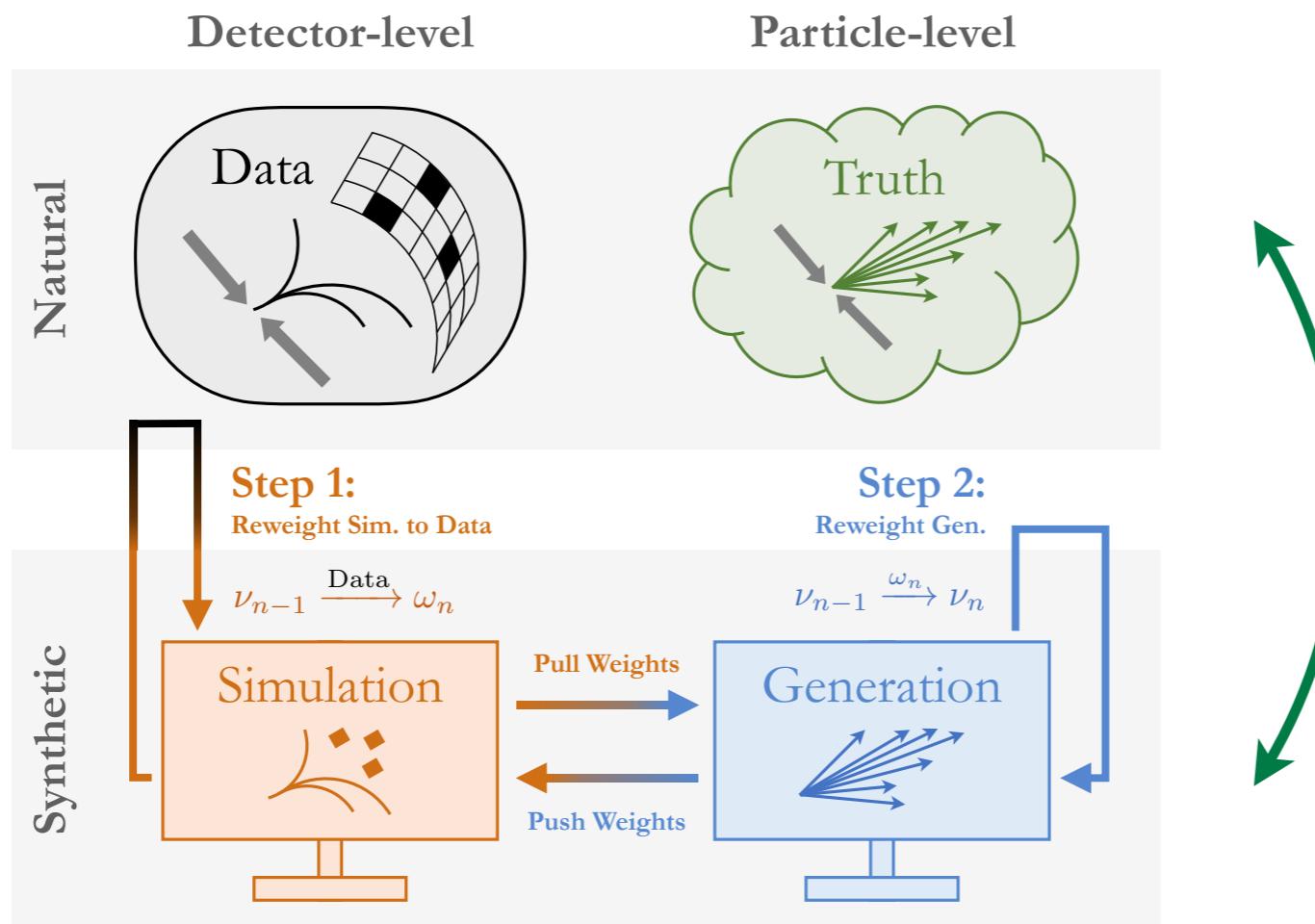
Deep learning can lift these methods to act on unbinned data in high-dimensional phase space

[Richardson-Lucy deconvolution: Richardson, [JOSA 1972](#); Lucy, [AJ 1974](#)] [Iterative Bayesian Unfolding: D'Agostini, [NIM 1995](#)  
[asymptotic equivalence to maximum likelihood reconstruction in Shepp, Vardi, [IEEE 1982](#)]

# Deconvolution with OmniFold



*Multi-dimensional unbinned detector corrections  
via iterated application of likelihood ratio trick*

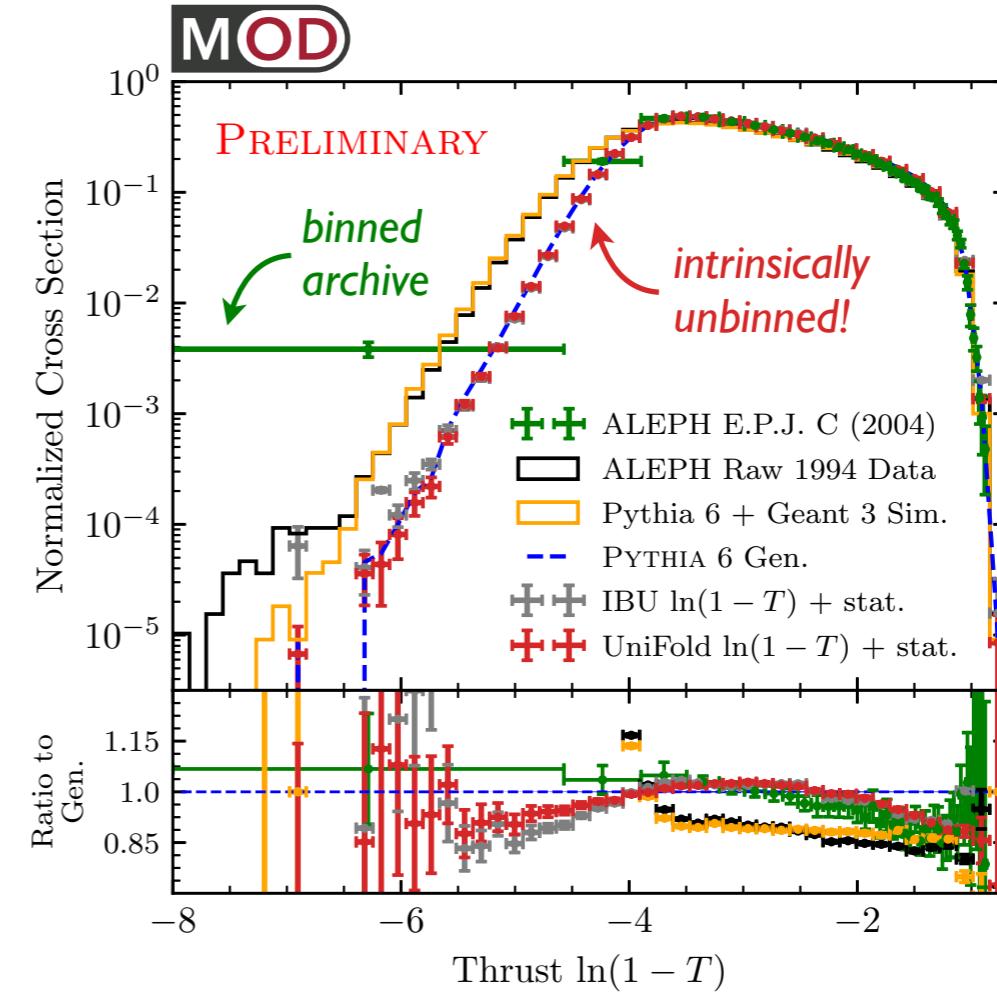
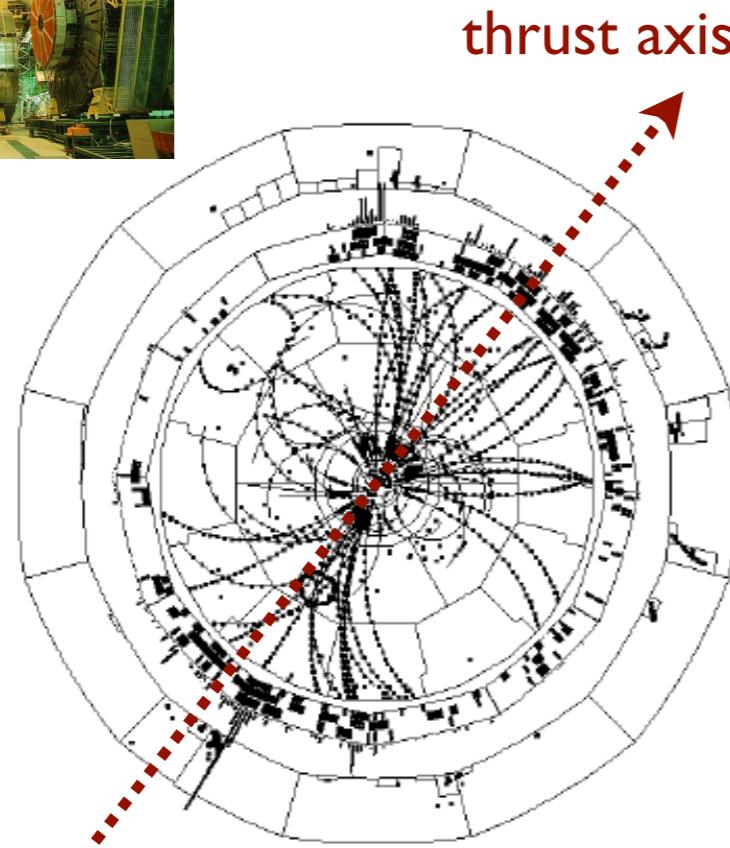


[Andreassen, Komiske, Metodiev, Nachman, JDT, [PRL 2020](#)]  
[see complimentary approach in Bellagente, et al., [SciPost 2020](#)]



# Deconvolution with OmniFold

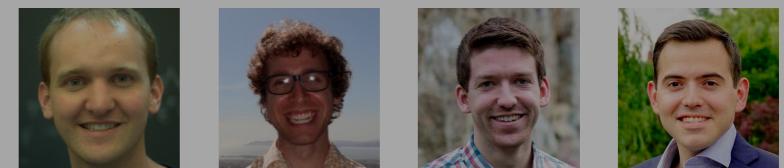
## Back to the Future with ALEPH Archival Data



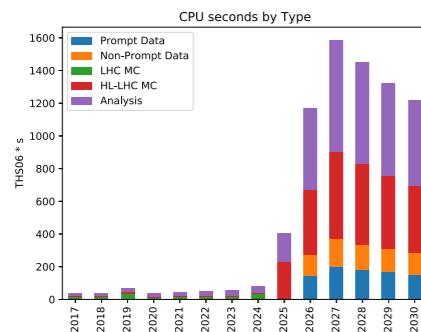
[talk by Badea, [ICHEP 2020](#); cf. ALEPH, [EPJC 2004](#)]  
[see also Badea, Baty, Chang, Innocenti, Maggi, McGinn, Peters, Sheng, JDT, Lee, [PRL 2019](#)]



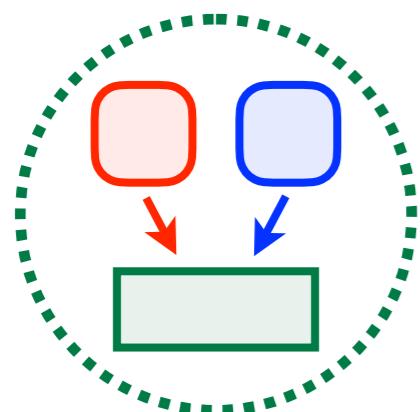
[Andreassen, Komiske, Metodiev, Nachman, JDT, [PRL 2020](#)]  
[see complimentary approach in Bellagente, et al., [SciPost 2020](#)]



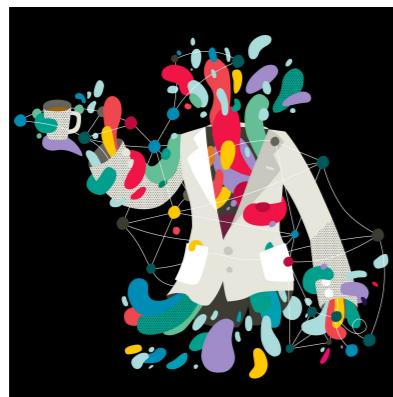
# Deep Learning for Collider Physics Simulation



For another talk: Computational cost of HL-LHC have inspired new ideas for **accelerating simulation**



With large sets of **i.i.d. data**, you can perform **weighted simulation via binary classification**



**Deep learning** can augment “**deep thinking**” and address key simulation challenges in collider physics