

$O(f(n))$

$$f_1(n) = \sqrt{n} \rightarrow O(\sqrt{n})$$

$$f_2(n) = n^3 \rightarrow O(n^3)$$

$$f_3(n) = \binom{n}{4}$$

$$= \frac{n!}{4!(n-4)!}$$

$$= \frac{n(n-1)(n-2)(n-3)\cancel{(n-4)!}}{4!(n-4)!}$$

$$= \frac{(n^2 - n)(n-2)(n-3)}{24}$$

$$= \frac{\textcircled{n^4} - 6n^3 + 11n^2 - 6n}{24} \rightarrow O(n^4)$$

$$f_4(n) = \sum_{i=2}^n (i-1)$$

$$= 1 + 2 + 3 + 4 + 5 + 6 + 7 + \dots + n-1$$

$$= \frac{n(n-1)}{2}$$

$$= \frac{\textcircled{n^2} - n}{2} \rightarrow O(n^2)$$

$$f_3 > f_2 > f_4 > f_1$$

$$\binom{n}{4} > n^3 > \sum_{i=2}^n (i-1) > \sqrt{n}$$