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Aligned Pair Exclusion

From sudokuwiki.com, the puzzle solver's site

2		
	3	6
5		7

This is an interesting strategy, known by the short-hand as APE, since it overlaps with [Y-Wings](#) and [XYZ-Wings](#) but uses very different logic. APE logic will solve an XY-Wing (3 bi-values) and an XYZ-Wing (bi-value \leftrightarrow tri-value \leftrightarrow bi-value).

There are two types of APE - the normal APE and Extended APE.

Aligned Pair Exclusion - Type 1

The [Aligned Pair Exclusion](#) can be succinctly stated: Any two cells aligned on a row or column within the same box CANNOT duplicate the contents of any two-candidate cell they both see.

The [Y-Wing strategy](#) has some diagrams (see Figure 2) to show how cells can see other cells along the row, column or box and how they intersect or overlap. In Figure 1 [X](#) and [Y](#) are two cells and the yellow shading shows the common cells they can both 'see'.

Lets consider all the possible pairs of numbers in [X](#) and [Y](#).

These are:

- 3 and 2 (in X and Y)
- 3 and 5
- 5 and 2
- 5 and 5
- 7 and 2
- 7 and 5

Now is obvious that 5 and 5 can't be a solution to [X](#) and [Y](#). If any of the other pair solutions were true we'd be able to remove those solutions from the candidates in all the other yellow squares. The strategy asks us to look at all the bi-value cells [X](#) and [Y](#) can 'see'. Cells marked [A](#), [B](#) and [C](#) containing 2/7 and 3/5 and 5/7 match some of the options we have for [X](#) and [Y](#). Any of these pairs would remove ALL candidates from one of [A](#), [B](#) or [C](#) which is illogical, captain. This means we can exclude them from possible solutions for [X](#) and [Y](#). This leaves us with a shorter list:

- 3 and 2 (in X and Y)
- 5 and 2

What are we left with? According to our new list [Y](#) can only take the value 2 so we can remove 5. We can also remove the 7 from [X](#). This helps us solve the Sudoku.

Credits - Rod Hagglund first popularised this method. A good thread with a double example and walk-through is [here](#)

3	9	8	1 4 5	6	4 5	1 4	2	7
5	4 7	1	4 7	8	2	9	6	3
4 7	6	2	1 4 7	9	3	8	5	1 4
2 7 A	1	3 5 B	9	4	6	3 5 7 X	8	2 5 Y
2 4 7 6 9	4 7	5 6 9	8	3	1	5 7 C	4 9	2 5 6
4 6 9	8	3 6 9	2	5	7	1 3	4 9	1 6
6 9	2	6 9	3	1	8	4 5	7	4 5
1	5	4	6	7	9	2	3	8
8	3	7	4 5	2	4 5	6	1	9

APE 1: [Load Example](#) or : [From the Start](#)

Aligned Pair Exclusion - Type 2

The **Extended Aligned Pair Exclusion** includes tri-values spread over two cells as part of the attack. **APE 2** Says that any two cells with only **abc** excludes combinations **ab**, **ac** and **bc** from the pair under consideration.

This example is very clear since the two-cell tri-value is conveniently 4/5/6 in both cells. (see next example for alternative tri-value formations).

Lets consider all the possible pairs of numbers in **X** and **Y** first. These are:

- 1 and 4 (in X and Y)
- 1 and 6
- 1 and 8
- 4 and 4 (impossible)
- 4 and 6
- 4 and 8
- 6 and 4
- 6 and 6 (impossible)
- 6 and 8

Cell R5C6 marked **C** removes a 1/4 pair.

Now the tri-value: These are 4/5, 4/6 and 5/6. Removing these from the possibles for **X** but **Y** leaves us:

1/4/6 remains in **X** but **Y** is reduced to 6/8. Why should this work? Well, 5 is not really part of the tri-value that effects our APE. The key combination is 4/6 and that does the damage. Pretend that **X** is 4 and **Y** is 6 (or the other way round). This would leave **A** and **B** both equalling 5. Thats illegal which is why 4/6 is a combination we can remove from possible pairs in **X** and **Y**.

- 1 and 6 (in X and Y)
- 1 and 8
- 4 and 8
- 6 and 8

	1	2	3	4	5	6	7	8	9
1	7	^{1 2} 5 6	^{1 2} 4 5	¹ 5 8	A 4 5 6	3	² 4 6 8	4 6	9
2	8	^{1 3} 6	¹ 4	9	4 5 6	¹ 4 6 8	X 5	³ 4 6	7
3	³ 4 5 6	^{2 3} 5 6	9	7	B 4 5 6	⁴ 4 6 8	Y ² 4 6 8	1	³ 8
4	9	7	¹ 4 5	2	3	⁴ 4 6 8	4 6	^{4 5 6}	¹ 5 8
5	4 5	8	6	¹ 5	7	¹ 4 C	3	9	2
6	³ 4 5	^{1 2 3} 5	^{1 2} 5	⁵ 8	4 5 6	9	⁴ 4 6 8	7	¹ 8
7	2	4	8	6	9	7	1	³ 5	³ 5
8	1	9	3	4	8	5	7	2	6
9	^{5 6}	^{5 6}	7	3	1	2	9	8	4

APE 1: [Load Example](#) or : [From the Start](#)

Our one tri-value which matches these is 7/8. If we remove 7/8 from our list Y is reduced to 5 and 9. We get a naked pair and the rest of the Sudoku solves.

	1	2	3	4	5	6	7	8	9
1	4 5 8 9	7	6	4 2 8 9	4 2 8 9	4 2 8 9	2 5 9	3	1
2	4 8 9	4 8	3	5	4 2 8 9	1	2 7 9	4 7	6
3	4 5 9	1	2	7	6	3	5 9	4 5	8
4	2 6 7 8	2 5 8	1	4 2 8 9	4 5 2 7 8 9	4 6 7 8 9	3	5 6 7 8	4 5 7 9
5	6 7 8	9	5 7 8	1	3	4 6 7 8	5 6 7	2	4 5 7
6	2 6 7 8	3	4	2 8 9	2 5 7 8 9	6 7 8 9	1	5 6 7 8	5 7 9
7	3	2 8	X 7 8	6	1	5	4	9	2 7
8	1	4 5	Y 5 7 9	4 3 8 9	4 7 8 9	2	5 6 7	5 6 7	3 5 7
9	2 7	B 6	5 9	4 3 9	4 7 9	4 7 9	8	1	2 3 5 7

Credits: Myth Jellies came up with the insight for Type 2 (see bottom of [this page](#))

2		
8		6
		3

	3	6
5		7

If I take that literally in the first example... X in the first example can see the bivalues 25 and 37. It cannot duplicate the contents of those cells.

Therefore... it can't be 2,5,3 or 7? Obviously that's not what was meant.

Or is it... if the two aligned cells see some bivalue cells, and they both mutually share a certain candidate [that's part of those bivalue cells] then that shared candidate can go? But no, that's not it either.

If either if the cells see two bivalue cells, and those two bivalue cells both share a candidate with the cell under consideration... that shared one goes?

Does one actually have to enumerate the possibilities? This seems like something that can be spotted with a glance, if only it can be made clear the exact conditions needed.

Wednesday 30-Sep-2009

... by: Bernard Gervais

align pair type 2

I found more than one numerical solution for this example.

Best regards.

BG

Wednesday 30-Sep-2009

... by: Bernard Gervais

Excellent site, thank you.

for example 1, I use the unicity concept which pinpoints A4 = 1.

Best regards.

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