## Homework 2

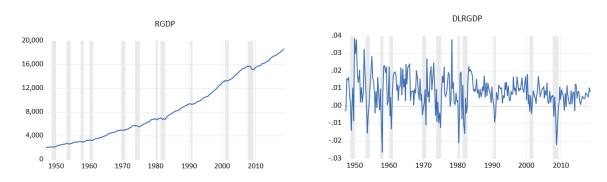
Eco 4306 Economic and Business Forecasting Spring 2019

Due: Wednesday, February 13, before the class

## Problem 1 (70 points)

Visit again the website of the Federal Reserve Bank in St. Louis (http://research.stlouisfed.org) and download the following data:

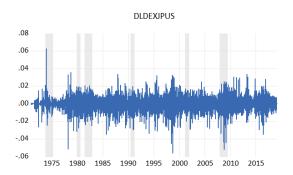
- (a) (10 points) U.S. real GDP., time series GDPC1:
- definition: real gross domestic product is the inflation adjusted value of the goods and services produced by labor and property located in the United States
- units: billions of chained 2009 dollars, seasonally adjusted annual rate
- frequency: quarterly



Time series is not weakly stationary, because it is growing over time, so mean and variance can not be constant. To obtain weakly stationary data we transform the time series by taking log and then calculating the first differences. The resulting series approximates the growth rate (percentage change) and fluctuates around mean with roughly same volatility over the sample period.

- (b) (10 points) The exchange rate of the Japanese yen against the U.S. dollar., time series DEXJPUS:
  - definition: Noon buying rates in New York City for cable transfers payable in foreign currencies.
  - units: Japanese yen to one U.S. dollar, not seasonally adjusted
  - frequency: daily

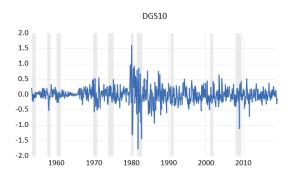




Time series might be weakly stationary, if we only consider the period since 1990, but before that it was gradually declining in 1970s and 1980s. To obtain weakly stationary data we transform the time series by taking log and then calculating the first differences. The resulting series approximates the growth rate (percentage change) and fluctuates around its mean, though the volatility appears to be changing, with calmer periods interrupted by period of larger volatility.

- (c) (10 points) The 10-year U.S. Treasury constant maturity yield., time series GS10:
- definition:
- units: percent, not seasonally adjusted
- frequency: monthly

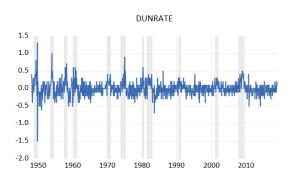




Time series was gradually growing in 1960s and 1970s, but was since then gradually declining, so it is hard to tell whether it is weakly stationary or not. The first difference appears first order weakly stationary but not second order weakly stationary, since its volatility is changing over time.

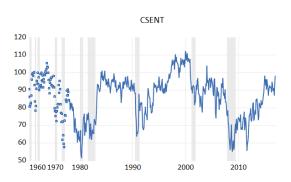
- (d) (10 points) The U.S. unemployment rate., time series UNRATE:
  - definition: Number of unemployed as a percentage of the labor force. Labor force data are restricted to people 16 years of age and older, who do not reside in institutions (e.g., penal and mental facilities, homes for the aged), and who are not on active duty in the Armed Forces.
  - units: percent, seasonally adjusted
  - frequency: monthly

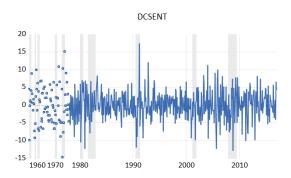




Time series might be weakly stationary, since it is not growing and instead it fluctuates around its mean, but it shows a lot of persistence. The time series for first differences also fluctuates around its mean, with roughly constant volatility, and with much smaller persistence.

- (e) (10 points) Index of Consumer Sentiment:, time series UMICH/SOC1
- definition:
- units: index, 1966Q1=100, not seasonally adjusted
- frequency:

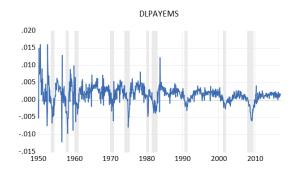




Time series appears to be weakly stationary, since it fluctuates around its mean, but this time series also shows high persistence. The time series for first differences also fluctuates around its mean, with roughly constant volatility, and with much smaller persistence.

- (f) (10 points) All Employees, Total Nonfarm Payrolls, time series PAYEMS
- definition: Total Nonfarm Payroll, is a measure of the number of U.S. workers in the economy that excludes proprietors, private household employees, unpaid volunteers, farm employees, and the unincorporated self-employed. This measure accounts for approximately 80 percent of the workers who contribute to Gross Domestic Product (GDP).
- units: thousands of persons, seasonally adjusted
- frequency: monthly

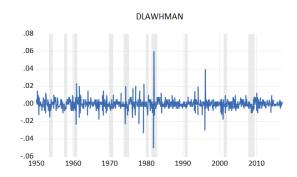




Time series is not weakly stationary, because it is growing over time, so mean and variance can not be constant. To obtain weakly stationary data we transform the time series by taking log and then calculating the first differences. The resulting series approximates the growth rate (percentage change) and fluctuates around mean with roughly same volatility over the sample period.

- (g) (10 points) Average Weekly Hours of Production and Nonsupervisory Employees: Manufacturing:, time series AWHMAN
  - definition: Average weekly hours are the total weekly hours divided by the employees paid for those hours. Nonsupervisory employees include individuals who are not above the working-supervisor level.
  - units: hours, seasonally adjusted
- frequency: monthly





Time series appears to be weakly stationary, since it fluctuates around its mean. The time series for first differences also fluctuates around its mean.

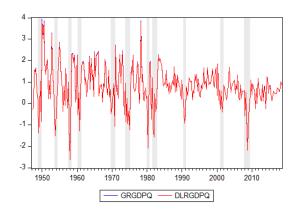
## Problem 2 (30 points)

(a) (10 points) There is almost no noticeable difference between the the quarter-over-quarter growth rate (percentage change) of the real GDP

$$grGDPQ_t = 100 \times \frac{Y_t - Y_{t-1}}{Y_{t-1}}$$

and the first log-differences of the real GDP

$$dlrGDPQ_t = 100 \times (y_t - y_{t-1}) = 100 \times (\log Y_t - \log Y_{t-1})$$

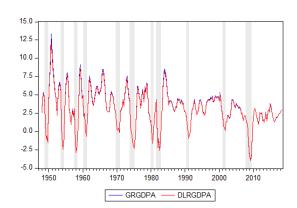


(b) (10 points) There is almost no noticeable difference between the year-over-year growth rate (percentage change) of the real GDP

$$grGDPA_t = 100 \times \frac{Y_t - Y_{t-4}}{Y_{t-4}}$$

and the first log-differences at lag 4 of the real GDP

$$dlrGDPA_t = 100 \times (y_t - y_{t-4}) = 100 \times (\log Y_t - \log Y_{t-4})$$



(c) (10 points) The ACF and PACF for  $dlrGDPA_t$  show that there is more linear dependence (higher autocorrelation coefficients) than in  $dlrGDPQ_t$ . The AC coefficients are statistically different from zero for first two lags in case of  $dlrGDPQ_t$  and for first three lags in case of  $dlrGDPA_t$ .

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Date: 02/12/19 Time: 18:54 Time Series: Sample: 1947Q1 2018Q3 Included observations: 286

DLRGDPQ

Date: 02/12/19 Time: 18:54 Sample: 1947Q1 2018Q3 Included observations: 283

Time Series:

DLRGDPA

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob
- 🗀		1	0.360	0.360	37.451	0.000
· 🗀		2	0.227	0.112	52.384	0.000
(1)	<b>d</b> -	3	0.019	-0.110	52.486	0.000
ı <b>d</b> ı	1 11	4	-0.059	-0.069	53.499	0.000
<b>□</b> ·	1 11	5	-0.126	-0.077	58.124	0.000
10		6	-0.032	0.067	58.422	0.000
1 <b>(</b> 1	1 (1)	7	-0.042	-0.021	58.942	0.000
40	1 (1)	8	-0.013	-0.017	58.991	0.000
· <b>b</b> i	•  b	9	0.079	0.099	60.862	0.000
· þr		10	0.095	0.043	63.568	0.000
1 1 1	III	11	0.020	-0.066	63.682	0.000
<b>4</b> ·	ļ <b></b>	12	-0.112	-0.156	67.433	0.000
<b>@</b> •	1 11	13	-0.114	-0.019	71.349	0.000
ı <b>l</b> i ı	ļ i	14	-0.055	0.084	72.258	0.000
·Щ ·	ļ ( <b>Q</b> )	15	-0.078		74.114	0.000
1 <b>j</b> i	·	16	0.054	0.078	74.998	0.000
1 <b>j</b> i)	1 11	17	0.052	0.012	75.826	0.000
· þ	·    -	18	0.106	0.064	79.248	0.000
· <b>j</b> ii	1 11	19		-0.015	80.647	0.000
· <b>j</b> ir	1 1	20		-0.006	82.209	0.000
ı <b>ii</b> i	u  -	21	-0.068		83.641	0.000
1(1)	i  i	22	-0.048	0.030	84.371	0.000
<b>(</b>	1 10	23	-0.093	-0.036	87.102	0.000
1(1)		24	-0.015	0.031	87.173	0.000
(1)	<b> </b>   -	25	0.035	0.047	87.554	0.000
( <b>)</b> ))	1 10	26	0.026	-0.037	87.770	0.000
1 <b>j</b> i	1 10	27	0.064	0.027	89.054	0.000
· þ	1 1	28	0.084	0.053	91.320	0.000
, <b>j</b> i	1 1	29		-0.003	91.879	0.000
· · ·	. I I I I I I I I I I I I I I I I I I I	30	-0.097		94.927	0.000
· <b>(</b> ) ·	·    -	31	-0.055	0.051	95.898	0.000
ι <b>ά</b> ι	·	32	-0.053	0.051	96.818	0.000
1)1	-   <b> </b>  -	33	0.020	0.050	96.951	0.000
٠ <u>١</u> ٠	1 1)1	34	0.072	0.008	98.647	0.000
ı <b>j</b> ı	ļ ( <b>d</b> )	35	0.045	-0.050	99.314	0.000
1 <b>j</b> ) 1	1 1 1	36	0.025	-0.004	99.517	0.000

Autocorrelation	Partial Correlation	,	AC	PAC	Q-Stat	Prob
1		1 0	).851	0.851	207.24	0.00
ı <b>——</b>	<b>=</b>	2 0	.587	-0.498	306.29	0.00
· <b> </b>	<b>□</b>  -	3 0	.288	-0.181	330.13	0.00
(1)	1 10	4 0	0.025	-0.022	330.31	0.00
<b>₫</b> ,		5 -0	0.085	0.366	332.41	0.00
<b>d</b> :	📺 -	6 -0	0.100	-0.130	335.35	0.00
ı <b>d</b> ı	idi-	7 -0	0.059	-0.079	336.37	0.00
1   1	1 1	8 0	0.002	-0.018	336.37	0.00
( <b>þ</b> )		9 0	0.046	0.150	337.00	0.00
(1)	<b>□</b> '	10 0	0.039	-0.200	337.45	0.00
1   1	10 1	11 -0	0.005	-0.060	337.46	0.00
ı <b>d</b> ı	11 1	12 -0	0.075	-0.043	339.12	0.00
<b>d</b> :		13 -0	).111	0.292	342.77	0.00
₫:	•	14 -0	0.101	-0.112	345.83	0.00
ı <b>d</b> ı	1 1	15 -0	0.050	-0.009	346.57	0.00
( <b>)</b> )	1 1)	16 0	0.036	0.018	346.97	0.00
ı þi		17 0	0.103	0.129	350.16	0.00
· 🗀	<b>□</b>  -	18 0	).129	-0.156	355.21	0.00
, <b>þ</b> i	11 -	19 0	0.110	-0.027	358.94	0.00
· <b>þ</b> i	1 10	20 0	0.051	-0.016	359.75	0.00
40		21 -0	0.019	0.131	359.86	0.00
( <b>d</b> )	1 11	22 -0	0.058	-0.026	360.90	0.00
<b>₁₫</b> -	id -	23 -0	0.068	-0.070	362.32	0.00
( <b>1</b> )		24 -0	0.037	0.040	362.74	0.00
1 <b>)</b> 1		25 0	0.016	0.103	362.83	0.00
· þi	10 -	26 0	0.058	-0.052	363.87	0.00
ı þo	<b>d</b>  -	27 0	0.077	-0.107	365.72	0.00
· <b>þ</b> i	<b>    </b>	28 0	0.061	0.044	366.92	0.00
r <b>j</b> ir		29 0	0.016	0.041	367.00	0.00
ı <b>ğ</b> ı		30 -0	0.033	0.004	367.35	0.00
1 <b>(</b> )	·   jp ·	31 -0	0.045	0.067	368.00	0.00
· <b>(</b> )	141	32 -0	0.029	-0.039	368.27	0.00
r <b>j</b> ir		33 0	0.013	-0.001	368.33	0.00
( <b>þ</b> )	<u> </u>			-0.089	369.11	0.00
ı <b>j</b> ı	141	35 0	0.043	-0.042	369.72	0.00
1   1		36 0	0.006	-0.005	369.73	0.00