

Texas Tech University  
Department of Economics  
Spring 2018  
Eco 4306: Economic and Business Forecasting  
**Midterm 2**

Name:

ID:

Short questions (45 points)

**Q1.** 7.5 points

**Q2.** 7.5 points

**Q3.** 7.5 points

**Q4.** 7.5 points

**Q5.** 7.5 points

**Q6.** 7.5 points

Applied problems (60 points)

**Q7.** 10 points

**Q8.** 10 points

**Q9.** 10 points

**Q10.** 10 points

**Q11.** 10 points

**Q12.** 10 points

**Good luck!**

**Question 1** (7.5 points)

Explain the difference between in-sample evaluation and out-of-sample evaluation.

**Question 2** (7.5 points)

Explain how Mean Squared Error and Mean Loss are used in the assessment of forecasts.

**Question 3** (7.5 points)

Give an example of a deterministic trend  $g(t)$  other than a linear trend and plot its graph. Write the equation of a model with this trend.

**Question 4** (7.5 points)

Explain the difference between a trend stationary time series and a difference stationary time series.

**Question 5** (7.5 points)

Explain what it means for a time series process to be  $I(1)$ , and what it means for a process to be  $I(0)$ .

**Question 6** (7.5 points)

Write down the equation for a pure seasonal S-AR(1) model. Describe how its AC and PAC functions look like.

## Question 7 (10 points)

Consider two candidate models for change in monthly private residential construction spending, AR(1) and AR(2)+SAR(1), the results for which are below. Evaluate the adequacy of these models based on the correlograms of residuals, AIC and BIC, and statistical significance of coefficients.

Dependent Variable: DCONST  
Method: ARMA Maximum Likelihood (BFGS)  
Date: 04/11/18 Time: 16:28  
Sample: 1993M02 2013M12  
Included observations: 251  
Convergence achieved after 3 iterations  
Coefficient covariance computed using outer product of gradients

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	34.02301	284.5681	0.119560	0.9049
AR(1)	0.503787	0.082472	6.108569	0.0000
SIGMASQ	4263658.	311155.6	13.70266	0.0000

R-squared	0.254386	Mean dependent var	49.44223
Adjusted R-squared	0.248373	S.D. dependent var	2396.078
S.E. of regression	2077.314	Akaike info criterion	18.12859
Sum squared resid	1.07E+09	Schwarz criterion	18.17072
Log likelihood	-2272.138	Hannan-Quinn criter.	18.14554
F-statistic	42.30579	Durbin-Watson stat	2.030264
Prob(F-statistic)	0.000000		

Date: 04/11/18 Time: 16:30  
Sample: 1993M01 2013M12  
Included observations: 251  
Q-statistic probabilities adjusted for 1 ARMA term

Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob
1	0.196	-0.016	-0.016	0.0654	
2	0.196	0.196	0.196	9.8361	0.002
3	-0.156	-0.156	-0.156	16.045	0.000
4	-0.152	-0.202	-0.202	21.954	0.000
5	-0.073	-0.014	-0.014	23.343	0.000
6	-0.437	-0.430	-0.430	72.819	0.000
7	-0.077	-0.174	-0.174	74.368	0.000
8	-0.167	-0.097	-0.097	81.652	0.000
9	-0.141	-0.424	-0.424	86.868	0.000
10	0.174	-0.055	-0.055	94.847	0.000
11	-0.004	-0.168	-0.168	94.852	0.000
12	0.928	0.873	0.873	323.74	0.000
13	-0.022	0.004	0.004	323.87	0.000
14	0.191	-0.179	-0.179	333.60	0.000
15	-0.170	-0.052	-0.052	341.37	0.000
16	-0.138	0.000	0.000	346.48	0.000
17	-0.073	-0.027	-0.027	347.93	0.000
18	-0.426	0.036	0.036	397.29	0.000
19	-0.074	0.040	0.040	398.77	0.000
20	-0.181	-0.046	-0.046	407.75	0.000
21	-0.107	0.110	0.110	410.89	0.000
22	0.145	-0.070	-0.070	416.75	0.000
23	0.014	-0.017	-0.017	416.81	0.000
24	0.859	-0.003	-0.003	623.42	0.000
25	-0.023	0.005	0.005	623.56	0.000
26	0.187	-0.009	-0.009	633.38	0.000
27	-0.183	-0.013	-0.013	642.88	0.000
28	-0.128	-0.051	-0.051	647.55	0.000
29	-0.074	-0.018	-0.018	649.09	0.000
30	-0.408	0.052	0.052	696.98	0.000
31	-0.070	-0.020	-0.020	698.38	0.000
32	-0.203	-0.115	-0.115	710.36	0.000
33	-0.069	0.028	0.028	711.77	0.000
34	0.118	-0.001	-0.001	715.82	0.000
35	0.035	-0.014	-0.014	716.18	0.000
36	0.783	-0.102	-0.102	897.23	0.000

Dependent Variable: DCONST  
Method: ARMA Maximum Likelihood (BFGS)  
Date: 04/11/18 Time: 16:26  
Sample: 1993M02 2013M12  
Included observations: 251  
Convergence achieved after 7 iterations  
Coefficient covariance computed using outer product of gradients

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	214.4219	1374.109	0.156044	0.8761
AR(1)	0.497140	0.054595	9.105947	0.0000
AR(2)	0.116143	0.052147	2.227211	0.0268
SAR(12)	0.944592	0.013249	71.29646	0.0000
SIGMASQ	373960.6	26485.07	14.11968	0.0000

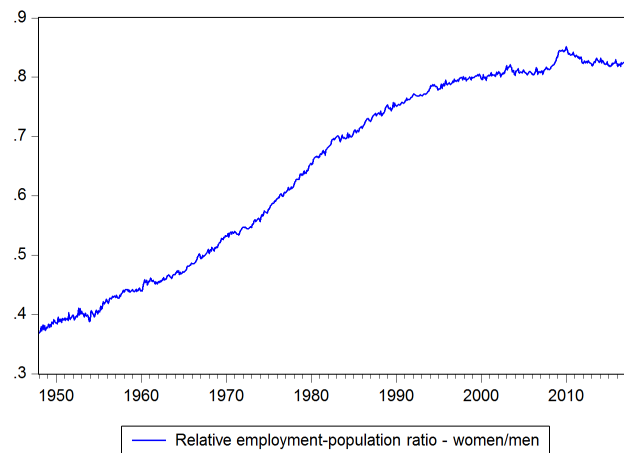
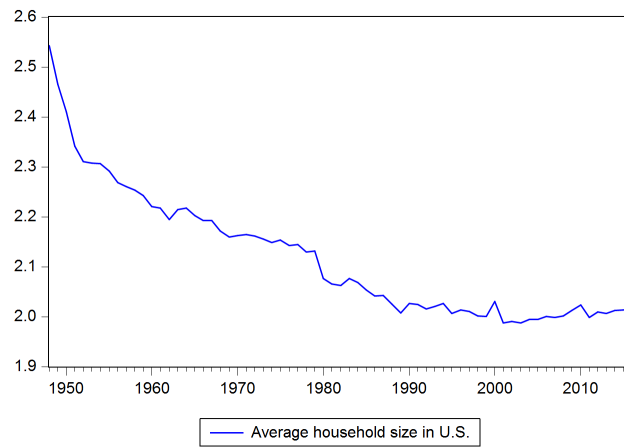
R-squared	0.934603	Mean dependent var	49.44223
Adjusted R-squared	0.933540	S.D. dependent var	2396.078
S.E. of regression	617.7066	Akaike info criterion	15.81783
Sum squared resid	93864109	Schwarz criterion	15.88805
Log likelihood	-1980.137	Hannan-Quinn criter.	15.84609
F-statistic	878.9103	Durbin-Watson stat	1.975678
Prob(F-statistic)	0.000000		

Date: 04/11/18 Time: 16:26  
Sample: 1993M01 2013M12  
Included observations: 251  
Q-statistic probabilities adjusted for 3 ARMA terms

Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob
1	0.011	0.011	0.011	0.0322	
2	0.054	0.054	0.054	0.7743	
3	-0.054	-0.056	-0.056	1.5282	
4	-0.032	-0.034	-0.034	1.7972	0.180
5	0.042	0.049	0.049	2.2539	0.324
6	-0.091	-0.092	-0.092	4.3953	0.222
7	-0.081	-0.089	-0.089	6.1091	0.191
8	0.112	0.132	0.132	9.3965	0.094
9	-0.073	-0.078	-0.078	10.799	0.095
10	-0.031	-0.065	-0.065	11.048	0.137
11	-0.041	-0.009	-0.009	11.501	0.175
12	-0.005	-0.001	-0.001	11.507	0.243
13	-0.013	-0.053	-0.053	11.553	0.316
14	-0.007	0.014	0.014	11.565	0.397
15	0.006	0.021	0.021	11.575	0.480
16	0.019	-0.024	-0.024	11.670	0.555
17	0.040	0.045	0.045	12.109	0.598
18	-0.095	-0.096	-0.096	14.580	0.482
19	0.042	0.037	0.037	15.068	0.520
20	0.070	0.082	0.082	16.416	0.495
21	-0.041	-0.061	-0.061	16.875	0.532
22	0.010	-0.006	-0.006	16.904	0.596
23	-0.005	0.036	0.036	16.912	0.659
24	0.158	0.146	0.146	23.933	0.296
25	0.008	-0.038	-0.038	23.952	0.350
26	-0.075	-0.038	-0.038	25.527	0.324
27	-0.033	-0.021	-0.021	25.837	0.362
28	0.024	0.018	0.018	25.999	0.408
29	-0.044	-0.047	-0.047	26.564	0.432
30	-0.043	-0.024	-0.024	27.097	0.459
31	-0.037	-0.000	-0.000	27.498	0.491
32	0.064	0.024	0.024	28.673	0.482
33	0.022	0.028	0.028	28.816	0.527
34	0.044	0.058	0.058	29.388	0.549
35	-0.016	-0.004	-0.004	29.459	0.596
36	-0.071	-0.119	-0.119	30.955	0.569

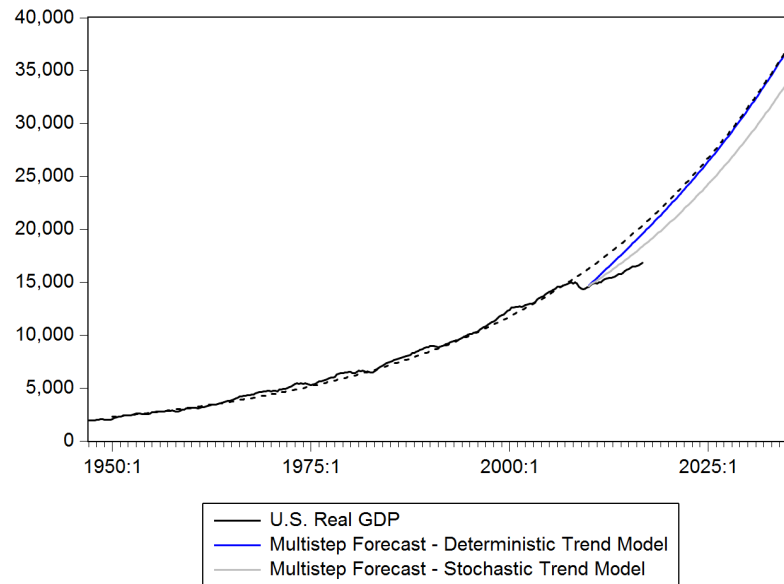
**Question 8** (10 points)

Which deterministic trends would you use when developing models for the two series plotted below?



**Question 9** (10 points)

The following figure shows the multistep forecasts for the U.S. real GDP, from the deterministic model and from the stochastic trend model, both for the period 2010Q1-2035Q4. Discuss the main difference in the behavior of the two forecasts and explain the reason for this difference.

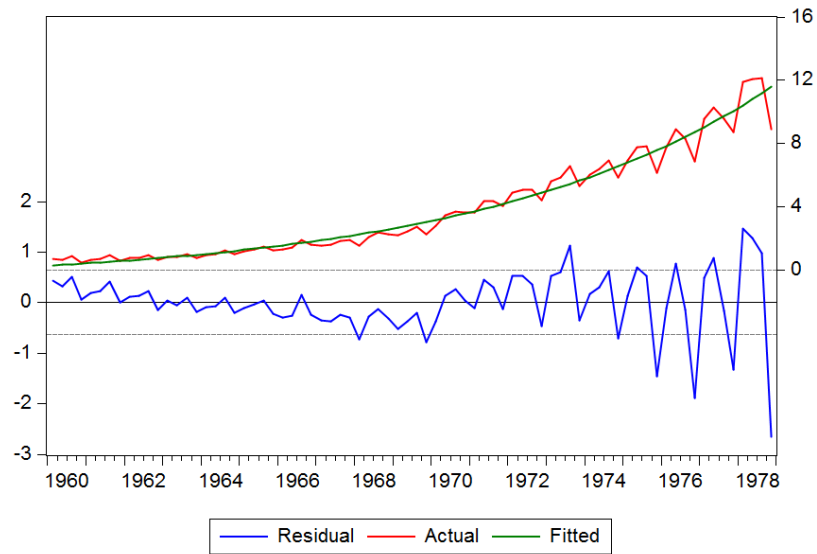


**Question 10** (10 points)

Consider a model for quarterly earnings per share of the Johnson and Johnson company

$$JNJ_t = \beta_0 + \beta_1 e^{\beta_2 t} + \varepsilon_t$$

Given the plot with actual values, fitted values, and residuals below, explain how you would proceed with modifying/developing the model further.





**Question 11** (10 points)

Below are the results for the Augmented Dickey-Fuller unit root test for log transformed earnings per share  $\log JNJ_t$ , and for the first difference of the log transformed earnings per share  $\Delta \log JNJ_t$ .

Interpret the results, and determine whether  $\log JNJ_t$  is  $I(0)$  or  $I(1)$ .

Null Hypothesis: LJNJ has a unit root		
Exogenous: Constant, Linear Trend		
Lag Length: 3 (Automatic - based on SIC, maxlag=11)		
		t-Statistic      Prob.*
<u>Augmented Dickey-Fuller test statistic</u>		<u>-1.696535      0.7428</u>
Test critical values:	1% level	-4.090602
	5% level	-3.473447
	10% level	-3.163967
*Mackinnon (1996) one-sided p-values.		

Null Hypothesis: D(LJNJ) has a unit root		
Exogenous: Constant, Linear Trend		
Lag Length: 2 (Automatic - based on SIC, maxlag=11)		
		t-Statistic      Prob.*
<u>Augmented Dickey-Fuller test statistic</u>		<u>-19.93554      0.0001</u>
Test critical values:	1% level	-4.090602
	5% level	-3.473447
	10% level	-3.163967
*Mackinnon (1996) one-sided p-values.		

**Question 12** (10 points)

Consider two models for U.S. real GDP, used to construct forecast for the period 2010Q1-2016Q4:

- model A: deterministic trend model for which the sequence of 1-step ahead forecasts has RMSE=103.45 and the multistep forecast has RMSE=1649.06
- model B: stochastic trend model for which the sequence of 1-step ahead forecasts has RMSE=77.32 and the multistep forecast has RMSE=905.18.

The 1-step ahead forecasts are then used to perform the test of equal predictive ability by estimating

$$\Delta L_{t+j,1} = \beta_0 + u_{t+j} \quad \text{with } j = 0, 1, 2, \dots, T - t - 1$$

where  $\Delta L_{t+j,1} = (e_{t+j,1}^A)^2 - (e_{t+j,1}^B)^2$ , and  $e_{t+j,1}^k$  is the one step ahead forecast error for forecast from model  $k$  in period  $t + j$ . Explain the idea behind this test and interpret its results below. Discuss how we would use it together with above RMSE values in model selection process.

Dependent Variable: DL\_TREND

Method: Least Squares

Date: 04/09/17 Time: 18:34

Sample (adjusted): 2010Q1 2016Q4

Included observations: 28 after adjustments

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	5454.311	1293.939	4.215275	0.0002
R-squared	0.000000	Mean dependent var		5454.311
Adjusted R-squared	0.000000	S.D. dependent var		6846.884
S.E. of regression	6846.884	Akaike info criterion		20.53604
Sum squared resid	1.27E+09	Schwarz criterion		20.58361
Log likelihood	-286.5045	Hannan-Quinn criter.		20.55058
Durbin-Watson stat	2.683486			