Quantization of ecological interactions yields insights into community assembly and dynamics

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Introduction

Amazing words. The best words.

Model Description

The ANIMe Model We examine assembly and dynamics of communities where we consider the interaction constraints that determine colonization and extinction of species in terms of presence/absence rather than population abundances. We assume that all species in a community at a given time have population steady states above the threshold required for persistence. In this context, we assume that the abundance of all species in a given community are > 0 and infer persistence based on the combination of interactions between species.

We aim to examine how interdependencies between species in communities either aid or inhibit both assembly and extinction over long timescales, and specifically how ecosystem engineers contribute to these dynamics. We approach these questions by considering both multiple types of interactions between species – including but not limited to trophic interactions – as well as indirect interactions between species and 'objects' that are introduced by the presence of ecosystem engineers. Such introduced objects are to be considered in the abstract, and serve to represent either resources, habitat, or environmental alterations that are introduced by the engineers that make them, and can be utilized by others.

The ANIMe model consists of four directed interactions: a: assimilate, which specifies a dependency involving biomass flow, n: need, which specifies a dependency that does not involve biomass flow, i: ignore, the null interaction, and m: make, which connects a species to an object that it engineers. Such objects are interactive components that are made by ≥ 1 species, and needed, assimilated, or ignored by the others. We also note that 'objects' are to be considered in the abstract, as they could represent actual things a species makes (e.g. an organic molecule), habitat it provides (e.g. as an elephant clears savannas of trees, facilitating shrubs), or even an abiotic condition (e.g. example).

The four directed interaction types describe specific dependencies that one species/object has on another, however it is the coupling of two opposing directed interactions that describe traditional and familiar ecological relationships (listed in Table 1). For example, an

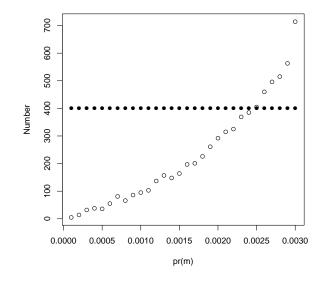


Figure 1: The number of species (closed circles; set to S = 400) and objects (open circles) in the interaction matrix as a function of pr(m).

 $a \leftrightarrow i$ interaction describes a typical predator-prey relationship, where species 1 assimilates species 2, and species 2 ignores species 1. Of course, a prey's abundance does not *ignore* predation, however the ANIMe model operates at the scale of presence-absence, rather than abundance. Both the $a \leftrightarrow n$ and $n \leftrightarrow n$ interactions describes mutualisms, with the former involving a trophic interaction (such as a plant-pollinator relationship), and the latter without (such as EXAMPLE). Uniquely, the $m \leftrightarrow n$ interaction describes ecosystem engineering, where a species makes an object, while the presence of the object 'needs' the presence of the species that makes it to exist. As pr(m) increases, the number of objects made by species increases, such that objects constitute a greater proportion of the interaction matrix compared to the species that create the objects (Fig. 1. Moreover, as pr(m) increases, the probability that multiple species makes the same object increases, but at a slower rate. A complete list of pairwise interactions is found in Table ??.

To establish an interaction matrix, we randomly assign interactions between species and the objects they create based on a set of directed interaction probabilities, which serve as model input. Given a species richness \mathcal{S} , the probability that a pair of species have an interaction as listed in Table 1 results from drawing an initial directed interaction pr(a, n, i, m), and the conditional probability of drawing the opposing directed interaction, which is constrained due to the fact that not every combination of [a, n, i, m] is feasible. The emergent $\mathcal{R} \times \mathcal{R}$ interaction matrix thus consists of a set of species S and objects \mathcal{O} , where $\mathcal{R} = S + O$. Three additional constraints introduce interaction structure to the model: 1) Species and objects behave differently: species can both assimilate and make, whereas objects ignore everything in the system except their 'makers'. 2) The distribution of assimilate interactions for a given species (i.e. the trophic degree) is drawn from an exponential distribution, such that the trophic interaction distribution among species is equivalent to that at the heart of the niche model. 3) We introduce a basal resource that can be assimilated by species, and those that consume this resource are identified as primary producers.

Ecological analogues: As pr(n) increases, so does the number of mutualistic interactions (direct and indirect). As pr(m) increases, so does the number of engineers (and indirect interactions). As pr(a) increases, so does the connectance of trophic interactions (show how this is related). As n_t increases, (this is the weird one), behavioral plasticity decreases in the sense that .

n-n: symbiont interaction

Colonization and extinction dynamics The interaction matrix above specifies how each species interacts with every other, however not all species are capable of coexisting in a given community at a given time. Assembly of a species community is thus the result of both colonization and extinction of species that are drawn from the larger interaction matrix, which essentially defines the species pool.

The colonization potential of a given species into a community is determined by two threshold conditions: 1) it must assimilate at least one species/object, which may include the basal resource if that species is a primary producer, and 2) it must satisfy a proportion of its need interactions, given by the threshold n_t ; higher values of n_t means that entry into the community is more difficult (a higher proportion of need interactions must be satisfied). If the assimilate and need threshold conditions are both satisfied, colonization is allowed.

Lotka-Volterra type interactions between k_i predators with respect to a resource density R_i leads to the steady state density $R_i^* \propto k_i^{-1}$. Although we do not model population densities explicitly, we make the simplifying assumption that the probability of extinction is increased from a background rate ω_b as a resource's population is depressed by the cumulative effects of k consumers as

$$\omega_i(t) = \frac{\omega_b + \epsilon k_i}{1 + \epsilon k_i},\tag{1}$$

where ϵ scales the effect of each consumer on extinction and is assumed to be small. Primary extinctions can trigger secondary extinctions, as elimination of prey – and any objects that an eliminated species uniquely makes – may then result in consumers falling below either of the above threshold conditions. Accordingly, extinctions cascade until the threshold conditions for every remaining species are satisfied.

I. METHODS

A. Generating the community pooled interaction matrix

Given the probabilities of assimilate (a), need (n), ignore (i), and make (m) directed interactions being inserted into the pooled interaction matrix, we calculate the probabilities of pairwise interactions between both species and objects as

$$\begin{aligned} p_{ai} &= p_i(p_a/(p_a + p_n + p_i)) + p_a(p_i/(p_a + p_i + p_n)), \\ p_{an} &= p_n(p_a/(p_a + p_n + p_i + p_m)) + p_a(p_n/(p_a + p_i + p_n)), \\ p_{aa} &= p_a(p_a/(p_i + p_n + p_a)), \\ p_{nn} &= p_n(p_n/(p_a + p_n + p_i + p_m)), \\ p_{ni} &= p_n(p_i/(p_a + p_n + p_i + p_m)) + p_i(p_n/(p_a + p_n + p_i)), \\ p_{mn} &= p_n(p_m/(p_a + p_n + p_i + p_m)) + p_m, \\ p_{ii} &= p_i(p_i/(p_a + p_n + p_i)). \end{aligned}$$

The size of the interaction matrix $(\mathcal{N} = \mathcal{S} + \mathcal{O})$ is obtained by first setting the desired number of species (\mathcal{S}) , where the expected number of objects is then estimated as $\mathrm{E}(\mathcal{O}) = \mathcal{S}(\mathcal{S}-1)p_{mn}$, though the final number of objects is stochastic and determined by a simulated annealing algorithm where interaction matrices are generated until \mathcal{S} is reached.

We build the community pool interaction matrix according to the following steps: 1) we first assume that all agents in the system are species, and assign trophic interactions based on a degree distribution estimated from the Niche Model (Williams and Martinez 2000). The degree distribution is based on the trophic connectance of the system, which in this case is calculated as

$$C = p_{ai} + p_{an} + p_{aa}. (3)$$

For large communities, the number of trophic interactions for a given species i in the Niche Model d_i is proportional to the niche range r_i , where $d_i = r_i * \mathcal{N}$ where $r_i = Xn_i$ where $X \sim \beta(1,1/2C-1)$ and n_i is drawn from a uniform distribution in [0,1]. However, because we do not stipulate which species are connected according to where the range falls on the niche axis, we incorporate the trophic interaction degree distribution of the Niche Model without the imposed interaction structure.

2) We next impose two post-hoc rules that keep the interaction matrix grounded in biological reality. We impose the rule that row/column 1 is the basal resource

Parameter	Definition	Value/Range
\overrightarrow{a}	assimilate	
$\frac{\overrightarrow{n}}{\overrightarrow{i}}$ \overrightarrow{m}	need	
\overrightarrow{i}	ignore	
\overrightarrow{m}	make	
$a \leftrightarrow i$	Asymmetric Predation	
$a \leftrightarrow a$	Symmetric predation	
$n \leftrightarrow a$	Trophic mutualism	
$n \leftrightarrow n$	Non-trophic mutualism	
$n \leftrightarrow i$	Commensalism	
$i \leftrightarrow i$	Null	
$m \leftrightarrow n$	Engineering	
$\mathcal N$	Number of species + objects	dyn.
$\mathcal S$	Number of species	dyn.
\mathcal{O}	Number of objects	dyn.
a_t	Assimilate threshold	0.0
n_t	Need threshold	0.2
k	Number of consumers interacting with species i	dyn.
$\omega_{ m b}$	Background probability of extinction at time t	
$\omega(t)$	Cumulative probability of extinction at time t	$\frac{\omega_b + \epsilon n}{1 + \epsilon n}$
$1/\epsilon$	Number of consumers of resource i at which $\omega_i(t) = \frac{1}{2}$	1000

Table I: Table of parameters, definitions, and assigned values or ranges.

(e.g. energy from the sun) from which primary producers derive their energy. Thus, an assimlate interaction in column 1 means that the consumer is capable of primary production; conversely, row 1 (the basal resources interactions) are 'ignore' throughout. The second post-hoc rule imposes a certain proportion of 'assimilate' interactions across agents that must be linked to the basal resource, such that a given proportion of agents are capable of primary production.

3) Finally, we declare that agents that 'make' other agents are species that are making objects. Thus, a certain proportion of the agents in the system are declared species if there is a 'make' interaction connecting them to another agent; the receiving agent is declared an object. When an agent is declared an object, its interactions are all set to 'ignore', expect with the species that is making it, which is retained as 'need', because its presence in the community requires the presence of the species that makes it. Objects are not allowed to 'make' other objects; if this occurs, the 'm' interaction will be randomly assigned to a declared species. Ultimately, species and objects are immediately distinguishable by the diagonal of the interaction matrix: a species has a 'need' interaction on the diagonal (a species needs itself to be present); an object has an 'ignore' interaction on the diagonal. Thus, species can interaction with objects (they may make, assimilate, or need them), however objects do not interact with anything. Moreover, multiple species can make the same object: for example, most plant species engineer O_2 , which is then used by other species. Because the

number of 'make' interactions is probabilistic, the number of species/objects is also probabilistic. To obtain the desired \mathcal{S} , we use a simulated annealing algorithm to generate multiple interaction matrices of different sizes until the desired \mathcal{S} is found.

B. Colonization and Extinction

Results & Discussion

Community assembly without extinctions In the context of community assembly, the niche space that is created by a given assemblage can be measured by evaluating the number of potential colonizers that can fit within the assemblage from the species pool, fulfilling required assimilation and need threshold conditions. Because colonization without extinction does not account for resource limitation due to ever-expanding trophic loads of species that serve as resources for higher-trophic consumers, niche space is not reduced by packing more species into the community. However, because colonization from the mainland is a zero-sum event, with each successful colonization the number of potential future colonizers is reduced by one. Importantly, if a successful colonizer increases the number of potential future colonizers, this can be interpreted as functionally expanding the niche space of the community.

Due to the competing effects of niche space expansion and species pool depletion, we find that the proportion of the species pool capable of successfully colonizing the assembling community is concave parabolic (Fig. 2a). Early in the assembly process, the proportion of potential colonizers is equal to the proportion of species that are primary producers without an abundance of n dependencies (too many need interactions precludes such primary producers from serving as initial colonizers). As assembly continues, niche space expands to a maximum, and then declines as the species pool diminishes and the community is filled.

For a species pool of 400, by changing the value of $\operatorname{pr}(m)$ from 0.0001 to 0.002, we alter the proportion of engineers from ca. 0 to ca. 700. As the number of engineers is increased, the number of objects that they create – and other species can interact with – is likewise increased. For example, a single realization where S=400 species and $\operatorname{pr}(m)=10^{-4}$ resulted in a 412×412 interaction matrix (400 species, 12 objects), while a realization with S=400 and $\operatorname{pr}(m)=0.003$ resulted in a 1100×1100 interaction matrix (400 species, 700 objects). The former example generated a small number of engineers, each producing a single object, whereas the latter example generated a large number of engineers, each producing between 1-6 objects, with some objects being produced by multiple engineers.

The effects of the proportion of engineers in the community on niche space expansion during assembly, and without the limiting forces of extinction, are substantial. While both limited-engineer and many-engineer systems resulted in a concave down niche expansion curve, the engineered system was different in three important ways. First, the many-engineer system began assembly with a smaller proportion of potential colonizers. This is due to the fact that there are many more interdependencies between species and objects, and as there are few objects carried over early in community development, the limitations on species are exaggerated. Second, the rate that niche space is expanded is higher for many-engineer communities Third, the production of objects by engineers nearly doubles the potential niche space (proportion of potential future colonizers) midway through assembly. Once there is a large enough base of colonizers in the assembling communities, there are enough objects present to facilitate rather than inhibit additional colonization opportunities. Thus, the influence of engineers during assembly - by creating more interdependencies between species and the objects they engineer - both constrains and promotes assembly at different stages of the process.

Every species must satisfy at least one assimilate interaction, i.e. it must eat at least one other present species or basal resource. Moreover, every species must fulfill a certain proportion of its 'need' interactions, set by the threshold parameter n_t . As n_t increases, the interdependencies between species become more rigid during the assembly process, and this will serve to limit niche expansion.

However, the trajectory of niche expansion is more complex when n_t is increased. Rather than simply low-

ering the proportion of potential colonizers, increasing n_t results in a qualitatively different assembly process where niche space is first lowered, increased, and lowered again as the community is filled (Fig. 2b). The initial niche space contraction results from a filling of the initial community with primary producers and their direct consumers. This lower trophic module fills without creating additional space for higher trophic level organisms due to the harsher restrictions given by a high n_t . Once a critical point in assembly is reached, the potential to add higher trophic level colonizers is attained, and niche space increases to a maximum, only to finally decrease as the species pool is used up. In some realizations, the community is never able to fill, resulting in a system without higher trophic levels.

Assembly where n_t is large, and with moderate engineering, follows a 2-stage process. First, the system is colonized by primary producers. Once the lower trophic levels are filled and reach a critical point, niche expansion permits the colonization of higher trophic level colonizers. [Need to explore this more by calculating trophic level for each species - in progress]

Assembly with extinctions Examination of the assembly process that is regulated by extinctions due to changes in trophic load results in saturation of species richness over time (Fig. 4). Accordingly, the colonization and extinction dynamic result in regular fluctuations around a steady state community richness, where the size of the fluctuations (relative to the steady state value) strongly depends on n_t and pr((a, n)).

The average diversity of the system after an initial assembly process increases as the number of need interactions and/or need threshold n_t are sufficiently low. This is intuitive because such a system has many more degrees of freedom and is free to expand to higher densities of species. Likewise, as $\operatorname{pr}(n)$ and n_t increase, species richness lowers nearly to zero, as does the average trophic level (check), resulting in a system dominated by primary producers and their immediate consumers.

The system conforms to an expected Taylor's law relationship for lower species richness (<100), however follow different rules for higher richness (also corresponding to low pr(n) and n_t . Here, species dependencies are low, such that primary extinctions due to predation will generally not result in a large number of secondary extinctions because the need threshold is not easily violated, and this reduces the magnitude of fluctuations. Accordingly, it is the same drivers that lead to high species richness (increased plasticity and/or fewer non-trophic dependencies) that also reduces the volatility of the system, thereby reducing variability.

The magnitude of oscillations around the steady state richness is a measure of community instability and turnover. Although modification of pr(n) and n_t reveals a smooth and expected influence on the mean species richness of the community, the effect on the magnitude of fluctuations around the mean richness is more complex, and this is most evident in the coefficient of variation

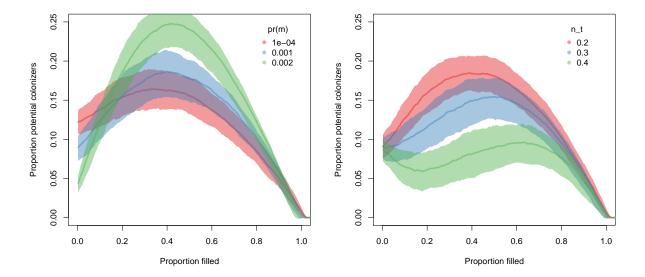


Figure 2: a) Expansion of niche space (by counting the proportion of species that are capable of colonizing from the larger species pool) over systems with increasing number of engineers (increasing pr(m)). b) Expansion of niche space over different need thresholds n_t .

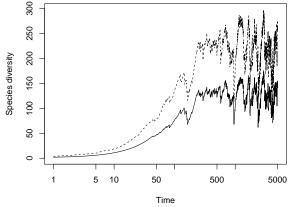


Figure 3: The colonization and extinction dynamics of a community over time. The solid line denotes species richness; the dashed line denotes species+object richness.

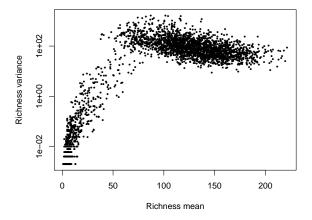


Figure 4: Relationship between mean species richness and the magnitude of fluctuations (SD) for communities with various values of pr(n) and n_t .

of community richness over time. The CV is maximized when n_t is intermediate and the number of non-trophic dependencies is large.

Effects of engineers on community dynamics We find that an increase in the number of engineers at time t results in the potential for marginally larger extinction cascades at time t+1 (positive but weak correlations, Fig 6a). This weak positive correlation between the number of objects at time t and extinction cascade size at time t+1 is due to the increasing interconnectedness that results

from the higher number of objects relative to species in the system. Because the existence of a given object is tied to the species that makes them (one or multiple), the effects of primary extinctions are magnified.

The number of objects in the system at time t (and by extension the number of engineers) is strongly positively correlated with the number of potential colonizers at time t+1. This correlation increases markedly with the proportion of engineers in the community. So from a species packing perspective, engineering enables suc-

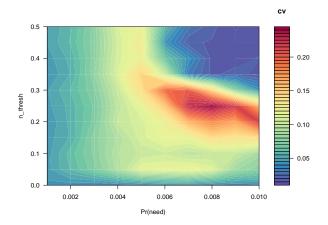


Figure 5: Changes in community richness CV as a function of pr(n) and n_t .

cessful colonization by increasing niche space, and this is particularly important for communities with a high proporiton of engineers. Colonization of engineers into a community both facilitates future colonization and increases the risks of larger extinction cas**cades**. This dual nature of ecosystem engineers may indicate short term/long term risks/gains?

Future things that I'm working on implementing (suggestions welcome!!!)

- 1. Calculate trophic level for each species
- 2. Object decay this is a big feature of engineered systems that the objects they engineer can last longer than the species
- 3. One potentially fruitful line of investigation would be to link this approach to random matrix theory inclusion of objects should modify species effects on one another. I'm currently tracking both direct trophic and mutualistic adjacency matrices (where if species 1 makes object 1, and species 2 eats object 1, we can say species 2 indirectly eats species 1 same for any other interaction type), but have not yet explored it this would probably be good for a stand-alone paper very little of engineering in food webs
- 4. Priority effects working on this what species traits alter assembly dynamics?

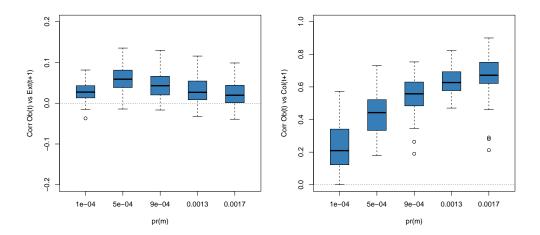


Figure 6: a) Correlations between objects at time t and extinction cascade size at time t + 1. b) Correlations between objects at time t and the number of potential colonizers at time t + 1.