

12.1a

$$\frac{da_{ij}}{dt} = b_i a_{ij} \left( \overset{\text{energy gain per unit effort}}{e_{ij} f_{ij} X_j} - \overset{\text{Avg profitability}}{\sum_{k \neq i} a_{ik} e_{ik} f_{ik} X_k} \right)$$

Assumes that there is a single condition that determines foraging effort

- Physiology: how close individuals are from starvation
- Ecology: landscape heterogeneity
- Stochasticity: the likelihood of finding/acquiring food
- life history: Risk is treated differently as a function of organismal age.

state-dependent foraging  
stochastic (random) influences.

## 12.1b Canonical Equation for Activity Choice

- Consider animal during a nonbreeding season where only survival matters



- Challenge: Avoid starvation & Predation

$X(t)$  = energetic reserves @ time  $t$

$X_c$  = critical level: fall below  $X_c$  and you die

$X_{max}$  = Maximum level

"Patches" ~ choices of activity (not necessarily spatial)  
 have individual characteristics: RISK / REWARD

### Risk

$d_i = \text{Pr}\{\text{killed in one visit to patch } i\}$

$s_i = \text{Pr}\{\text{finding food in one visit to patch } i\}$

### Reward

$c_i$  = Cost of one visit to Patch  $i$

$p_i$  = Reward for one visit to Patch  $i$

Patch	<u>Risk</u>		<u>Reward</u>		
	$d$	$s$	$p$	$c$	
1	0	1	0	1	} Tradeoffs
2	0.004	0.4	3	1	
3	0.02	0.6	5	1	



@ last time step, you are

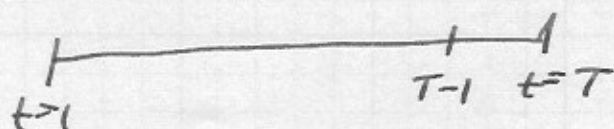
$$\left. \begin{array}{l} \text{alive: } X(T) > x_c \\ \text{dead: } X(T) \leq x_c \end{array} \right\} \text{ known for } t=T$$

⊛ Go backward one step @ a time  $(t-1)$  to calculate

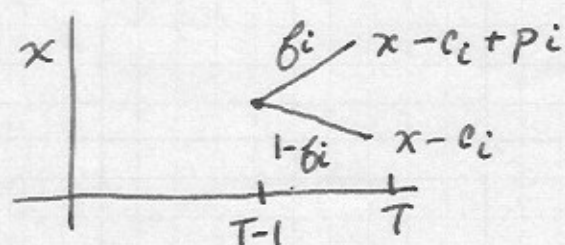
$S(x, t)$  = maximum probability of survival from  $t \rightarrow T$   
given  $X(T) = x$

$$S(x, t=T) = \begin{cases} 0 & \text{if } x \leq x_c \\ 1 & \text{if } x > x_c \end{cases}$$

Now for  $t=T-1$



$$S_i(x, T-1) = \Pr \{ \text{Surviving from } t=T-1 \text{ to } t=T \mid X(T-1)=x \}$$



if activity/patch  $i$  is chosen,   
 food is found   
 new  $x$  is  $x - c_i + p_i$    
 food is NOT found   
 new  $x$  is  $x - c_i$

at patch  $i$ : Max. prob. of survival from  $T-1$  to  $T$

$$\begin{aligned} S_i(x, T-1) &= (1 - d_i) \cdot f_i \cdot S(x - c_i + p_i, T) \\ &\quad + (1 - d_i) \cdot (1 - f_i) \cdot S(x - c_i, T) \\ &\quad + d_i \cdot 0 \end{aligned}$$

[We can calculate this for each patch  $i$ ]



We calculate

$$S_1(x, T-1)$$

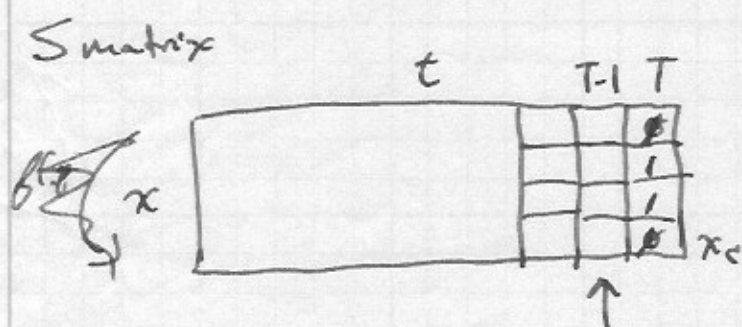
$$S_2(x, T-1)$$

$$S_3(x, T-1)$$

\* Max. survival prob. from  $T-1$  to  $T$   
in patch/activity 1, 2, 3

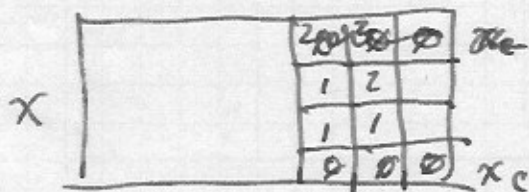
We will assume the individual has evolved to maximize its survival

$\hookrightarrow \max_i \{S_i(x, T-1)\} \rightarrow$  will tell you which patch/activity to choose  
GIVEN current current  
1) energetic state  $x$   
2) time  $T-1$



we are calculating survival probabilities for each prior timestep assuming the patch that maximizes survival is chosen.

$i^*$  matrix



When we are done, we have computed the maximum probability of survival for previous timesteps

$$S(x, t) \text{ is } \max_i \{S_i(x, t)\}$$

$$S(x, t) = \max_i \left\{ (1 - d_i) f_i S(x - c_i + p_i, t+1) + (1 - d_i)(1 - f_i) S(x - c_i, t+1) \right\}$$

w/ boundary conditions

$$S(x, t) = 0 \text{ if } x \leq x_c \text{ and } x = x_{\max} \text{ if } x > x_{\max}$$

Calculate for patches  $i = 1, 2, 3$  @  $t = T-1$  for  $x = 6$   
given  $x_c = 5$ ,  $x_{\max} = 10$

$$\text{and } S(x, t=T) = 0 \text{ if } x \leq x_c, 1 \text{ if } x > x_c$$

$$S_1(x=6, T-1) = (1 - 0)(1) \cdot S(6 - 1 + 0, t+1) + (1 - 0)(0) S(6 - 1, t+1) \\ = S(5, t+1) = S(5, T) = 0$$

$$S_2(x=6, T-1) = (1 - 0.004)(0.4) S(6 - 1 + 3, t+1) \\ + (1 - 0.004)(1 - 0.4) S(6 - 1, t+1) \\ = (0.39) S(8, t+1) + 0 = 0.39$$

$$S_3(x=6, T-1) = (1 - 0.02)(0.6) S(6 - 1 + 5, t+1) \\ + (1 - 0.02)(1 - 0.6) S(6 - 1, t+1) \\ = (0.58) S(10, t+1) + (0.39) S(5, t+1) \\ = 0.58$$

Ex 40

$$S(x=6, t=T-1) = \max \left\{ \overset{1}{0}, \overset{2}{0.39}, \overset{3}{0.58} \right\}$$

So given that energetic state, and that time interval,  
activity/patch 3 maximizes the Prob(Surviving from  $t=T-1$  to  $t=T$ )

## The Pseudo Code

## ① Define Constants

$$xc = 3$$

$$x_{max} = 10$$

$$T_{max} = 20$$

## ② Create Patch-specific vectors

~~xxx~~ 
$$E[3]$$

$$P[3]$$

$$f[3]$$

$$d[3]$$

$$V[3] \leftarrow \text{final values over which we maximize}$$

$\alpha$  input values

## ③ Create Survival matrix &amp; Decision matrix

$$S[10, 20]$$

$$\begin{matrix} \uparrow & \uparrow \\ x & t \end{matrix}$$

$$D[10, 20]$$

$$\begin{matrix} \uparrow & \uparrow \\ x & t \end{matrix}$$

## ④ Define end condition (terminal fitness function)

$$\Phi = 0 \text{ for } x=1 \text{ to } x=3$$

$$= 1 \text{ for } x=4 \text{ to } x=10$$



### 13.1 General

$$S(x, t) = \max_i \left[ (1-d_i) f_i S(x - c_i + p_i, t+1) + (1-d_i)(1-f_i) S(x - c_i, t+1) \right]$$

$$S(x, T) = \Omega(x) = \frac{x - x_c}{x - x_c + \bar{x}}$$

Matrix

$S(x, t)$ : Survival from  $t$  to  $t=T$  given @ energy level  $x$

$i^*(x, t)$ : Survival-maximizing decision @  $t, x$

$$S(x, t) \leq S(x, t+1)$$

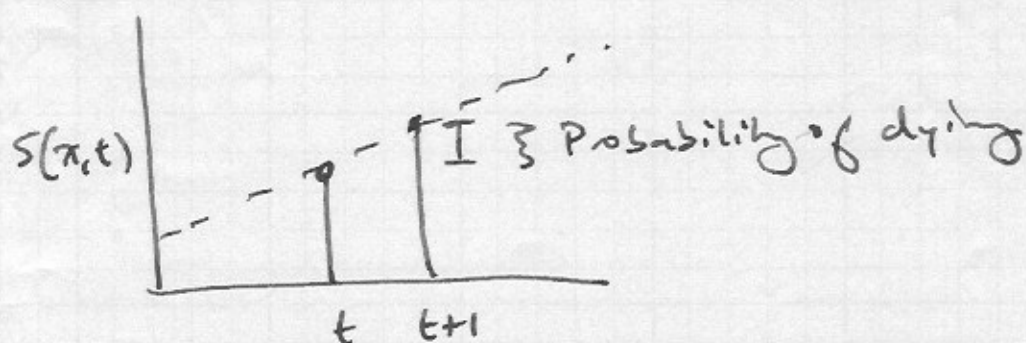
What is the probability of dying? in timestep  $t$ ?

$$1 - S(x, t+1) \sim \text{Dying from } t+1 \rightarrow T$$

$$1 - S(x, t) \sim \text{Dying from } t \rightarrow T$$

$$1 - S(x, t+1) - (1 - S(x, t))$$

$$(1 - S(x, t)) - (1 - S(x, t+1)) = S(x, t+1) - S(x, t)$$



Behavioral Predictions via Monte-Carlo Forward Simulations

- Many inds in computer simulation =  $N$

$X_n(t)$  = state of  $n$ th individual @ start of period  $t$

where  $x_c \leq x_n(1) \leq x_{max}$

$$X_n(t) \Rightarrow i^*(x_n(t), t)$$

Possible states @  $t = t+1$

$$x_n(t+1) = \cancel{x_c \text{ w/prob } d_i^*(x_n, t)} + \underbrace{x_c \text{ w/prob } d_i^*(x_n, t) + (1-d_i^*(x_n, t))(1-f_i^*(x_n, t))}_{\text{and } \{x_n(t) - c_i^*(x_n, t) \leq x_c\}}$$

$$x_n(t) + x_i^*(x_n, t) - c_i^*(x_n, t) \\ \text{w/prob. } (1-d_i^*(x_n, t))(f_i^*(x_n, t))$$

$$x_n(t) - c_i^*(x_n, t) \\ \text{w/prob } (1-d_i^*(x_n, t))(1-f_i^*(x_n, t)) \\ \text{and } \{x_n(t) - c_i^*(x_n, t) > x_c\}$$

-Determine dead/alive

$U \sim \text{unif}$

if  $U_d < d_i$ , then dead

if  $U_d > d_i$ , then alive and we want to know probability of finding food

if  $U_f < f_i$ , then find food  
 $> f_i$ , then you don't



## Pseudo Code

⑥ Solve SDP, get  $i^*(x, t)$

① Put in all parameters incl.  $x_n(t)$  & dims.

② Generate initial conditions for individuals

③ Go forward in time until  $t=T$

@ each  $t$ , cycle over all individuals

if  $x_n(t) = x_c$  set  $x_n(t+1) = x_c$

if  $x_n(t) > x_c$  draw  $U_d$  and  $U_f$

if  $U_d \leq di^*(x_n(t), t)$  then  $x_n(t+1) = x_c$

if  $U_d > di^*(x_n(t), t)$  &  $U_f \leq fi^*(x_n(t), t)$   
then  $x_n(t+1) = \min \left[ x_{max}, x_n(t) + \frac{f_i^*(x_n(t), t) - c_i^*(x_n(t), t)}{p_i^*(x_n(t), t)} \right]$

if  $U_d > di^*(x_n(t), t)$  &  $U_f > fi^*(x_n(t), t)$

then  $x_n(t+1) = \max[x_c, x_n(t) - c_i^*(x_n(t), t)]$

④ Summarize

⑤ Miller Time