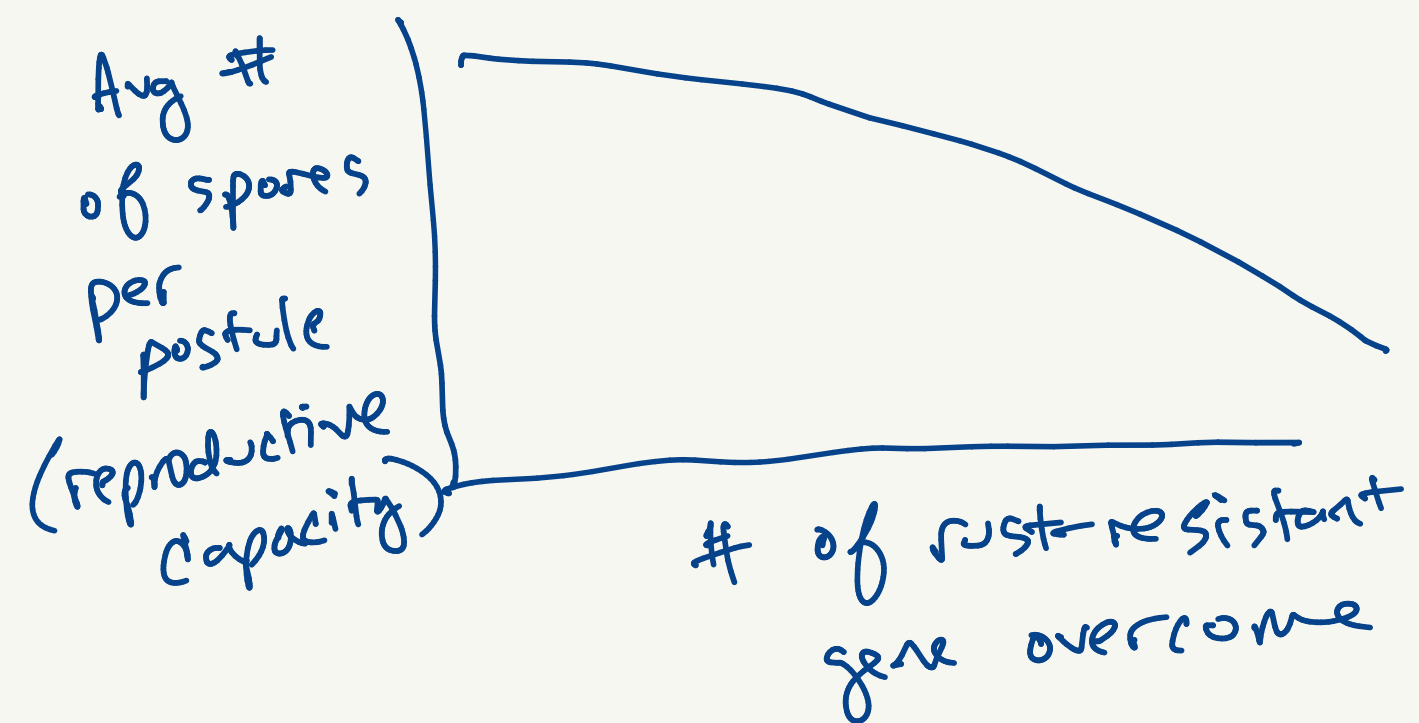


13.4

Host defenses and parasite counter-defenses have a cost

Wild Flax vs. Rust pathogen



Tradeoff between virulence and rate of reproduction

What are the ecological effects of ~~parasites~~ parasites?

- extinction

- reduced ranges

- Influence host population cycles

ex) American Chestnut Blight

1904 4 billion

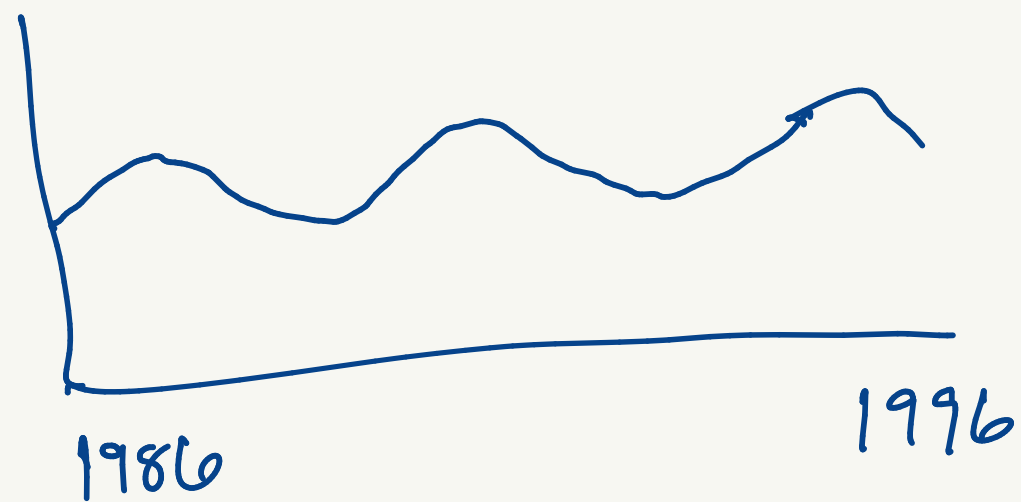
1940 a few individuals

↓ squirrel populations

extinction 7 moth spp.

↓ Deer, Coopers hawks, Coyars, bobcats

Grouse populations



w/nematodes



- elimination of nematode parasites does not eliminate cycles but changes their amplitudes

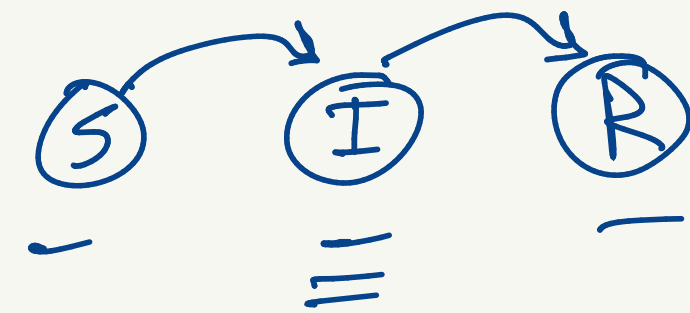
# Disease Dynamics

- Track the state of the host individuals w/in a population

Susceptible

Infected

Recovered ~ lifetime immunity



$$S + I + R = N$$

⊗ Assume that pathogen dynamics are much faster than host pop. dynamics

[  $S$  = Density of susceptible individuals  
 $I$  = Density of Infected individuals

- When should we expect a disease to spread within a population

- For a disease to spread,  $S$  individuals must encounter  $I$  individuals  
Encounter rate should be proportional to  $S \cdot I$

- Disease transmission is  $\beta SI$   
    ↖       $\beta$  is the transmission rate

If Disease transmission is  $\beta SI$

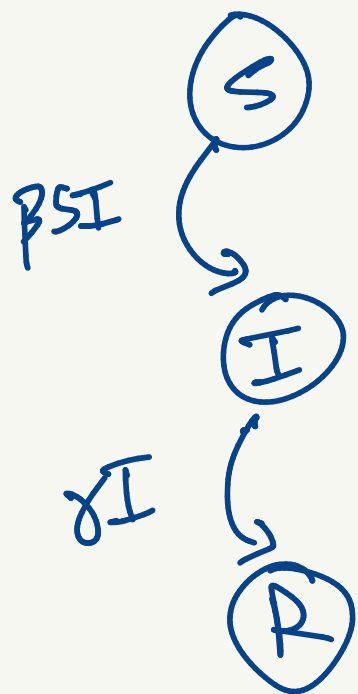
then ~~the~~ the density of infected individuals  $I$  should grow w/  $\beta SI$

$$\frac{dI}{dt} = \beta SI - \gamma I$$

$\uparrow$  Recovery rate

When should the disease be expected to spread?

$$\frac{dI}{dt} > 0?$$



$$S_T = \frac{\gamma}{\beta}$$

threshold value of the density of susceptible individuals

When  $S_T > \frac{\gamma}{\beta}$  the disease spreads

When  $S_T < \frac{\gamma}{\beta}$  the disease does not spread

$$\beta SI - \gamma I > 0$$

$$\beta S > \gamma$$

$$S > \frac{\gamma}{\beta}$$

$$\frac{dI}{dt} = \beta SI - \gamma I$$

$$S_T = \frac{\gamma}{\beta}$$

Disease growth:  $S_T > \frac{\gamma}{\beta}$

Disease decline:  $S_T < \frac{\gamma}{\beta}$

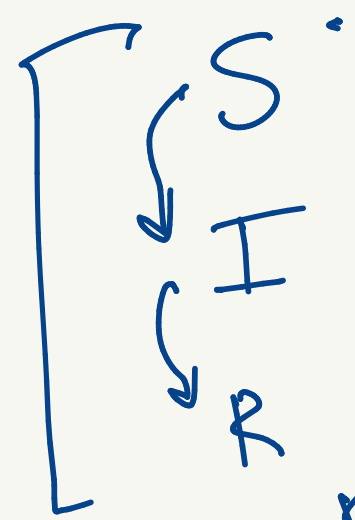
Recovery rate  
transmission rate

Social distancing

if recovery rate is higher, then  $S_T$  is larger

if the transmission rate is higher, then  $S_T$  is smaller

## Add some Realism



We track the size of compartments over time

become infected via contact

recover at a fixed rate

and have lifetime immunity

recovery rate

then the <sup>avg</sup> amount of time that individuals are infected is  $\frac{1}{\gamma}$

Total number of individuals is constant:

$$N = S + I + R$$

$\lambda = \underline{\text{the force of infection}}$

per-capita rate at which susceptible individuals acquire infection. ~~⊗⊗⊗~~  $\lambda$  is not constant... the more infected individuals there are, the greater the force of infection.  $\lambda(I)$

Let's consider the function  $\lambda(I)$

Composed of 1) transmission rate  $\beta \leftarrow \frac{1}{[\text{time}]}$

2) interaction term: proportion of infectious individuals  $\frac{I}{N} = \frac{\underline{I}}{S+I+R}$

$$\left[ \begin{array}{l} \frac{dS}{dt} = -\lambda(I)S = -\beta \frac{I}{N} S \\ \frac{dI}{dt} = \lambda(I)S - \gamma I = \beta \frac{I}{N} S - \gamma I \\ \frac{dR}{dt} = \gamma I \end{array} \right. \quad \lambda(I) = \beta \frac{I}{N}$$

pandemic