

# Homework 1

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**Problem 6.2:**

Compute the Fourier transform of  $\exp(-a|x|^2)$ ,  $a > 0$ , directly for  $x \in \mathbb{R}$ .

**Solution****Problem 6.3:**

If  $f \in L^1(\mathbb{R}^d)$  and  $f > 0$ , show that for every  $\xi \neq 0$ ,  $|\hat{f}(\xi)| < \hat{f}(0)$ .

**Solution****Problem 6.4:**

If  $f \in L^1(\mathbb{R}^d)$  and  $f(x) = g(|x|)$  for some  $g$ , show that  $\hat{f}(\xi) = h(|\xi|)$  for some  $h$ . Can you relate  $g$  and  $h$ ?

**Solution****Problem 6.6:**

Show that the Fourier transform  $\mathcal{F} : L^1(\mathbb{R}^d) \rightarrow C_v(\mathbb{R}^d)$  is not onto. Show that  $\mathcal{F}(L^1(\mathbb{R}^d))$  is dense in  $C_v(\mathbb{R}^d)$ .

**Solution**