UT Austin CSE 386C

A fun problem 2

Jonathan Zhang

Your task in this problem is to establish a relationship between *pairs* of natural numbers and natural numbers. The *set of natural numbers* is the set $\{1,2,3,4,\dots\}$, not including zero. A *pair* of natural numbers is denoted (i,j) where i and j are both natural numbers. The first few pairs of natural numbers are (1,1),(1,2),(2,1), and so on. It turns out that there is a natural paring between the natural numbers and the pairs of natural numbers.

Your task is to **find** a formula that takes a pair of natural numbers (i, j) and associates a single, unique, natural number k. For example, you may start like

$$\begin{array}{cccc} (1,1) & \rightarrow & 1 \\ (2,1) & \rightarrow & 2 \\ (1,2) & \rightarrow & 3 \\ (3,1) & \rightarrow & 4 \\ \vdots & \vdots & \vdots \end{array}$$

Once you have done so, can you do the reverse? That is, given a natural number k, find the unique pair of natural numbers (i, j) that are associated with it?

Oden Institute 1