Arrays & Linked Lists Introduction to Recursion

CS 311 Data Structures and Algorithms Lecture Slides Monday, September 18, 2023

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Unit Overview Advanced C++ & Software Engineering Concepts

Topics: Advanced C++

- Expressions
- Parameter passing I
- Operator everloading
- ✓ Simple class example
- Parameter passing
- ✓ Invisible rec. 18
- Managing esou ces class
- ContainersLerators
- Invisible functions II
- ✓ Error handling
- ✓ Using exceptions

Topics: S.E. Concepts

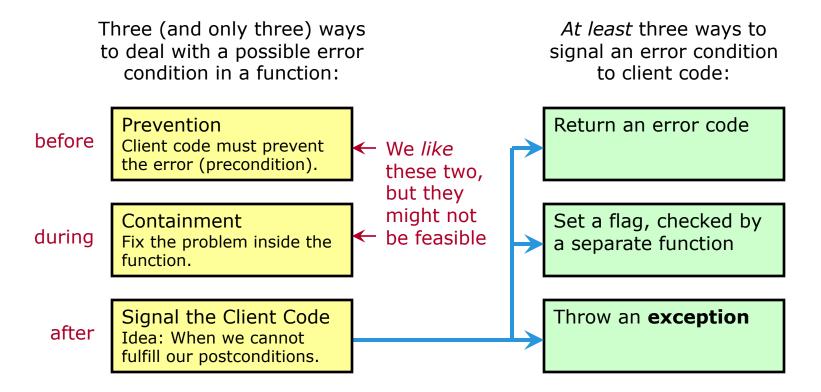
- ✓ Abstraction
- Assertions
- sting
- √ ariants

Review

Error Handling Summary

An **error condition** (often *error*) is a condition occurring during runtime that cannot be handled by the normal flow of execution.

- Not necessarily a bug or a user mistake.
- Example: Could not read file.



Exception: an object that is **thrown** to signal an error condition. To handle an exception, **catch** it using try ... catch.

```
Foo * p;
bool success = true;
                      new throws
try {
                     std::bad alloc
    p = new Foo; (<new>) or a derived
                      class, if memory
                      allocation fails.
catch (std::bad alloc & e) {
     success = false:
    cerr << "Alloc. failed: "</pre>
           << e.what() << endl;
```

How It Works

- When an exception is thrown inside a try-block, control passes to the catch-block that is associated with the smallest possible enclosing try-block that catches the proper type. Derived classes are handled as usual.
- In all other circumstances, a catch-block is not executed.
- An uncaught exception terminates the program.

Catch—when you can handle an error signaled by a function you call.

```
catch (std::out_of_range & e) {
```

Throw—when your function is unable to fulfill its postconditions.

```
if (ix >= arrsize) throw std::out_of_range("bad index");
```

Catch all & re-throw—when you call a throwing function, and you cannot handle the error, but your function must clean up before exiting.

```
try { ... } The code contains
three dots.

catch (...) {
    [Clean up here]
    throw; }
```

```
We typically only write one of the three: catch, throw, or catch all & re-throw.
```

Another might be written by someone else.

Destructors should not throw.

It is okay for constructors to throw.

Why? Destructors are called when an automatic object goes out of scope due to an exception. If the destructor throws in this context, then the program terminates.

Because of this, generally the destructors in your classes are implicitly marked noexcept, unless you specify otherwise. (To specify otherwise: "noexcept (false)". But this is EVIL. ②)

If a noexcept function throws, then the program terminates.

Some people do not like exceptions. Some of these people are very vocal about their dislike. But I think that *some* of them dislike exceptions for the wrong reasons.

A bad reason to dislike exceptions is that they require lots of work.

- Dealing with error conditions is work. Writing software that works is work. Exceptions are one tool we can use to achieve this goal.
- Handling exceptions properly is hard work because writing correct, robust software is hard work.

Software is **robust** if it can gracefully handle any input or situation.

What *might* be a good reason to dislike exceptions is that they add hidden execution paths. But remember that other error-handling methods have their own downsides—which is why exceptions were invented.

Unit Overview Recursion & Searching

This ends the introductory material.

We now begin a unit on recursion and searching.

Topics

- Arrays & Linked Lists
- Introduction to recursion
- Search algorithms I
- Recursion vs. iteration
- Search algorithms II
- Eliminating recursion
- Search in the C++ STL
- Recursive backtracking

There will be a number of topics like this one—typically at the end of our coverage of some data structure or algorithmic idea.

After this, we will cover Algorithmic Efficiency & Sorting.

Arrays & Linked Lists

Arrays & Linked Lists Arrays

This unit covers recursion and searching. In-depth coverage of data structures will wait until later in the semester. But if we are taking about searching, then we need data structures to search.

The simplest container data structure is the **array**. This stores a sequence of items, placing them one after the other in a contiguous block of memory.

Array 3 1 5 3 5 2

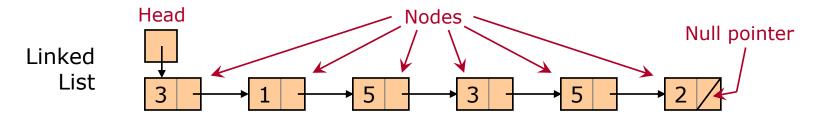
An array is a random-access structure. Since we know where in memory each item lies, we can look up an item quickly by its index, typically using a bracket operator: cout << arr[1000];

In C++, the following hold arrays: std::vector, std::array,
 std::basic string (basis of std::string), and built-in arrays.

Arrays & Linked Lists Linked Lists — Basics [1/2]

Another container data structure is the **Linked List**. Like an array, a Linked List stores a sequence of items.

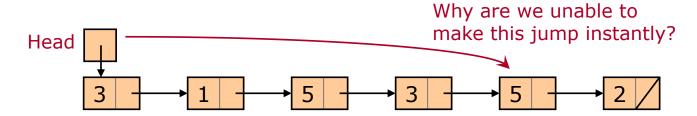
A Linked List is made of **nodes**. Each has a single data item and a pointer to the next node, or a null pointer at the end of the list. We keep track of a Linked List using its **head** pointer.



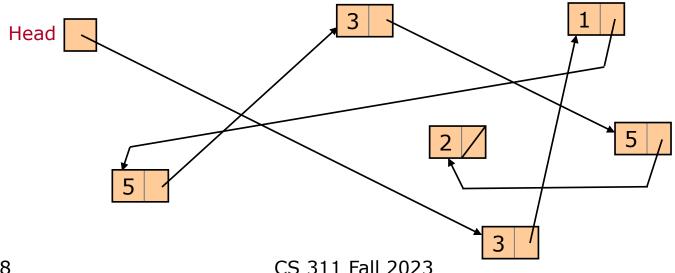
A Linked List is a forward-only sequential-access structure. To find items, we follow pointers though the list. We cannot quickly find the 100,000th item. Nor can we quickly find the previous item.

Arrays & Linked Lists Linked Lists — Basics [2/2]

We cannot quickly find a Linked List item, given only its index. Why not? It certainly looks as if we could.



But the above picture can be deceptive. A Linked List might actually be arranged in memory more like this:



Arrays & Linked Lists Linked Lists — Advantages

Why not always use (smart) arrays?

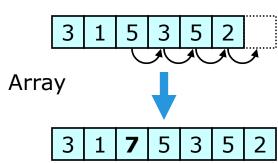
One reason: Linked Lists support fast insertion.

Suppose we have a sequence 3, 1, 5, 3, 5, 2. We wish to insert a 7 before the first 5.

Linked

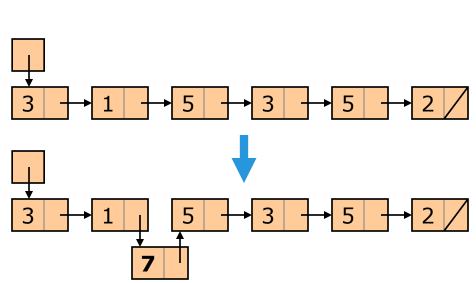
List

With an array, we move all later items up. For a large array this can be very slow.



With a Linked List, if we know the location, insertion is fast.

For large datasets, the speed-up can be huge.



Arrays & Linked Lists Linked Lists — Implementation [1/2]

Here is one possible implementation of a Linked List node.

```
The data members are public??!?!?
template <typename ValType>
                                       In practice, only the Linked List package deals
                                       with this struct, so these are not a problem.
struct LLNode {
    ValType data; // Data for this node
     LLNode * next; // Ptr to next node, or nullptr if none
     // The following simplify creation & destruction
     explicit LLNode (const ValType & data,
                                                             data
                                                                         next
                         LLNode * next = nullptr)
          : data(data), next(next)
     { }
                                If next points to a node, then delete calls that
                                node's destructor, which will delete its next pointer,
     ~LLNode()
                                which calls the destructor of the node after that, etc.
     { delete next; }
                                So this destructor calls itself; it is recursive. This is
};
                                convenient! However, it can be problematic if there
                                are lots of nodes. More on this later in the semester.
```

The head of our Linked List would hold an (LLNode<...> *).

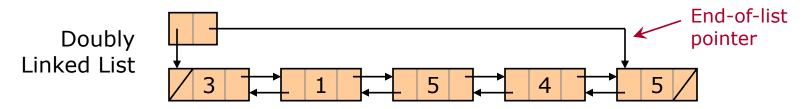
Arrays & Linked Lists Linked Lists — Implementation [2/2]

TO DO

 Write a function to find the size (number of items) of a Linked List, given its head pointer (LLNode<...> *).

See use_list.cpp.
The llnode.hpp header
defines LLNode.

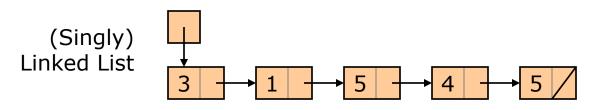
In a **Doubly Linked List**, each node has two pointers: next-node (null at the end) and previous-node (null at the beginning).



Doubly Linked Lists typically have not only a beginning-of-list pointer, but also an end-of-list pointer.

A Doubly Linked List is a bidirectional sequential-access structure.

To make it clear what we are talking about, the one-pointer-pernode Linked List has a more precise name: **Singly Linked List**.



We cover Linked Lists in more detail later in the semester.

Introduction to Recursion

Introduction to Recursion Basics — Definitions

A **recursive** algorithm is one that makes use of itself.

- An algorithm solves a problem. If we can write the solution of a problem in terms of the solutions to **smaller** problems of the same kind, then recursion may be called for.
- There must be a smallest problem, which we solve directly. This is a base case.
 Others are recursive cases.

Similarly, a **recursive** function is one that calls itself.

- Such calls are typically direct, but may be indirect.
- When a function calls itself, it is making a recursive call. We also say it recurses.

```
int mult(int a, int b)
                                Base case
              (a <= 1)
               return a ==
                            Direct recursion
           int ax = (a \gg 1);
Recursive
           int m1 = mult(ax,
    case
           return m1 + [m2(a, ax, b)];
                           Indirect recursion
      int m2 (int a, int ax, int b)
           return mult(a-ax, b);
```

Introduction to Recursion Basics — Four Questions

When designing a recursive algorithm or function, consider the following four questions*:

- 1. How can we solve the problem using solutions to one or more smaller problems of the same kind?
- 2. How much does each recursive call reduce the size of the problem?
- 3. What instances of the problem can serve as base cases?
- 4. As the problem size shrinks, will a base case always be reached?
 ♠

This is critical!

Every call to a recursive function must eventually reach a base case.

*Adapted from Frank M. Carrano, *Data Abstraction and Problem Solving with C++: Walls and Mirrors*, 4th ed., 2004.

Introduction to Recursion Fibonacci Numbers — Definitions [1/2]

The **Fibonacci numbers** are the sequence 0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, 233, 377, 610, 987, 1597, 2584, 4181, ... To get the next Fibonacci number, *do what???*

The Fibonacci numbers (F_n , for n = 0, 1, 2, ...):

- $F_0 = 0.$ $F_1 = 1.$
- For $n \ge 2$, $F_n = F_{n-2} + F_{n-1}$.

An equation defining a sequence of numbers in terms of itself, as above, is a **recurrence relation** (often simply **recurrence**). The values for the start of the sequence are **initial conditions**.

A recurrence often translates nicely into a recursive algorithm.

Let's do such a translation for the Fibonacci numbers: we write a recursive function fibo that takes an integer n and returns the nth Fibonacci number F_n .

Introduction to Recursion Fibonacci Numbers — Four Questions

- How can we solve the problem using solutions to one or more smaller problems of the same kind?
- 2. How much does each recursive call reduce the size of the problem?
 ???
- 3. What instances of the problem can serve as base cases? ???
- 4. As the problem size shrinks, will a base case always be reached?

Introduction to Recursion Fibonacci Numbers — Design Decisions

fibo takes an integer n and returns the nth Fibonacci number F_n . I will write F_n as F(n) in source-code comments.

What should the parameter and return types for fibo be?

- The parameter can be int.
- As n grows, F_n will grow very quickly. We may wish to guard against numeric overflow. Let's use a 64-bit unsigned integer for the return type: std::uint fast64 t. A type alias could be helpful:

```
using bignum = uint fast64 t;
```

What pre- and postconditions does fibo have?

- Pre: ???
- Post: ???

Introduction to Recursion Fibonacci Numbers — CODE

When we write a recursive function, we usually want to check for the base case(s) first. If we are not in a base case, then we are in a recursive case.

TO DO

Write recursive function fibo, as described.

See fibo_first.cpp.

Function fibo turns out to be extremely slow for anything other than small parameters. But do not conclude that recursion is slow! We will revisit fibo, rewriting it in various ways—including fast recursive versions.