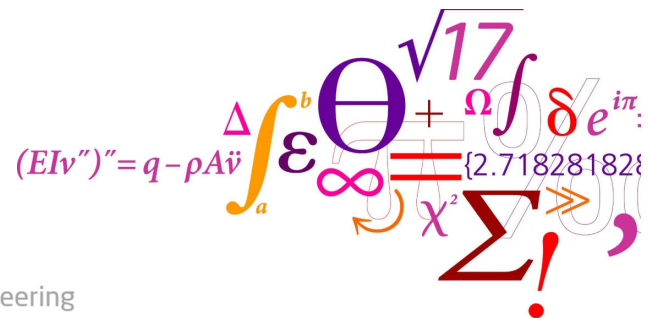


Lattice defects

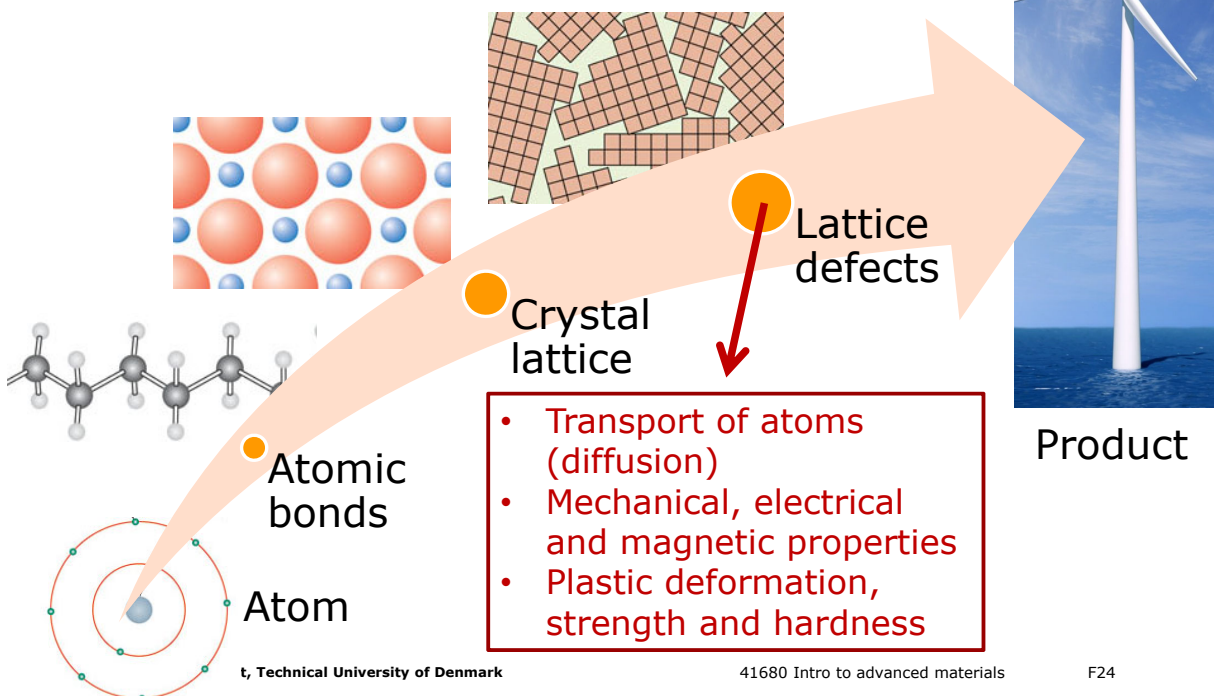
Is order everything?

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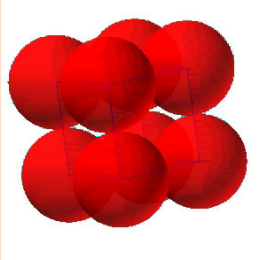
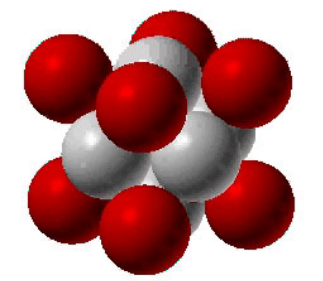
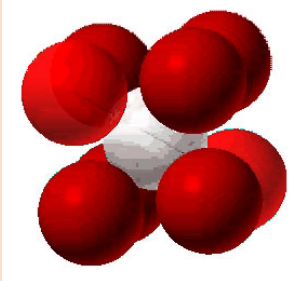


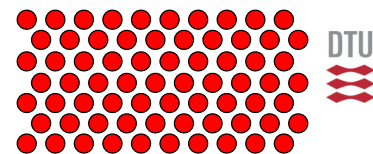
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Advanced materials Atoms - Microstructure - Properties



Cubic lattices

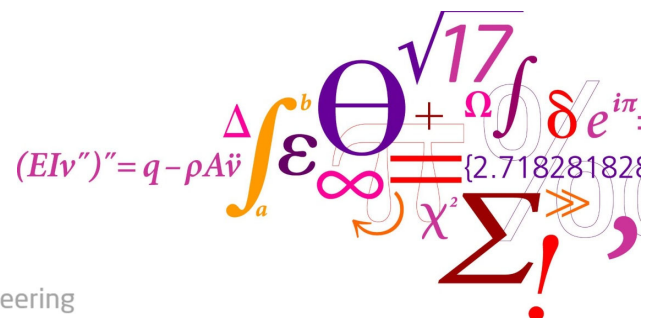
Simple cubic (sc)	Face-centered cubic (fcc)	Body-centered cubic (bcc)
		
Elements	Al, Cu, Ni, Ag, Au, Pt, γ -Fe	α -Fe, V, Nb, Ta, Cr, Mo, W, K
Atomic packing factor	74 %	68 %
Packing of planes	Close-packed planes	Less dense planes

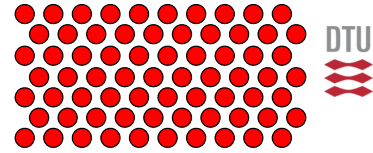


Lattice defects

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„Crystals are like people, it is the defects in them, which make them interesting!“
(Colin Humphreys)





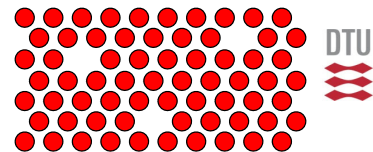
Lattice defects

0-dimensional: **point defects**
 vacancies, interstitials, substitutional atoms

1-dimensional: **line defects**
 dislocations

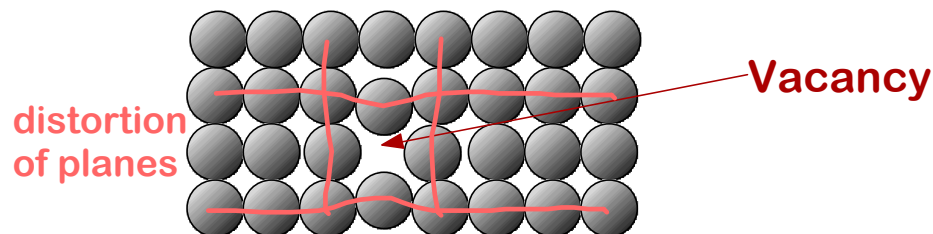
2-dimensional: **area (planar) defects**
 interfaces (stacking faults,
 grain-, phase-, twin-boundaries, surfaces)

3-dimensional: **volume (bulk) defects**
 voids, pores, precipitates, inclusions, cracks



Point defects Vacancies

- Vacant lattice site in a lattice



- Vacancies exist in thermal equilibrium
- Equilibrium density of vacancies

$$c_v = \frac{N_v}{N} = e^{-\frac{Q_v}{kT}}$$

N_v number of vacancies

N number of lattice sites

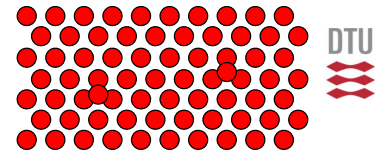
Q_v vacancy formation energy (G_v)

$k = 1.38 \cdot 10^{-23}$ J/K Boltzmann constant

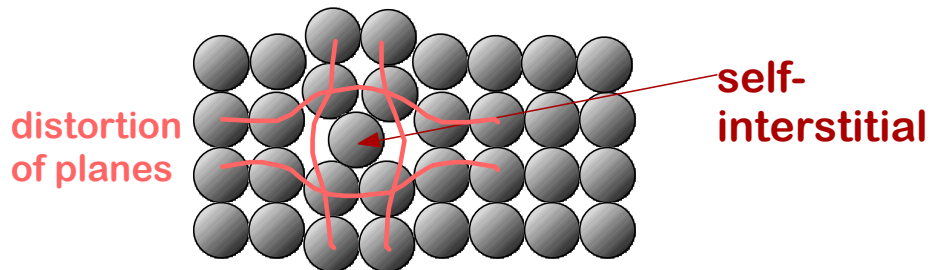
- Concentration at melting point 10^{-4}

Point defects

Self-interstitial atoms (SIA)



- Atoms sitting on an interstitial site (between lattice sites)



- High formation energy:
No self-interstitial atoms in thermal equilibrium in metals
- High mobility

Lattice defects

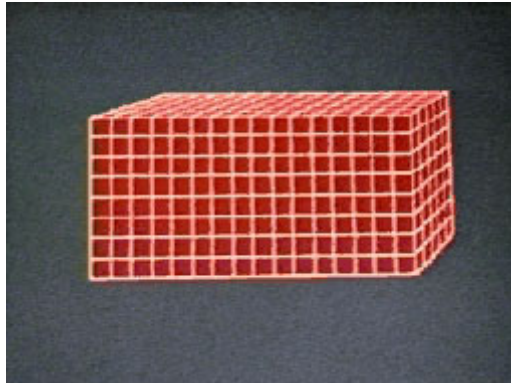
0-dimensional: point defects
vacancies, interstitials, substitutional atoms

1-dimensional: line defects
dislocations

2-dimensional: area (planar) defects
interfaces (stacking faults,
grain-, phase-, twin-boundaries, surfaces)

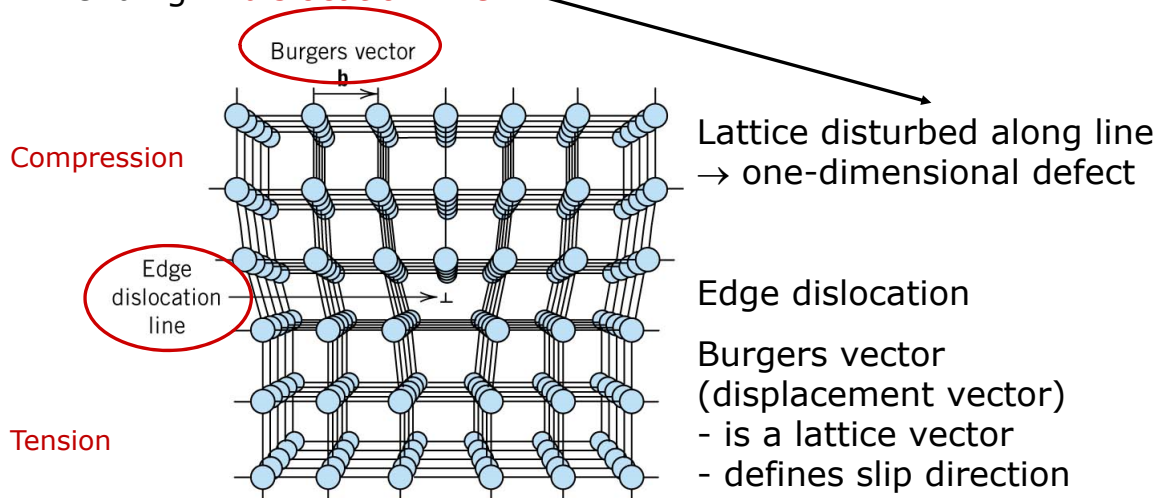
3-dimensional: volume (bulk) defects
voids, pores, precipitates, inclusions, cracks

Motion of (edge) dislocation



Line defects Dislocations

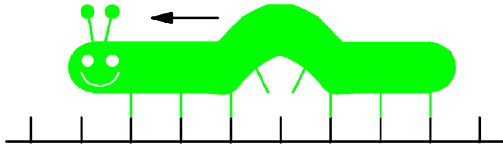
Extra lattice plane inserted in crystal,
not extending through all of the crystal (half-plane),
ending in **dislocation line**



Line defects

Dislocations as carrier of plastic deformation

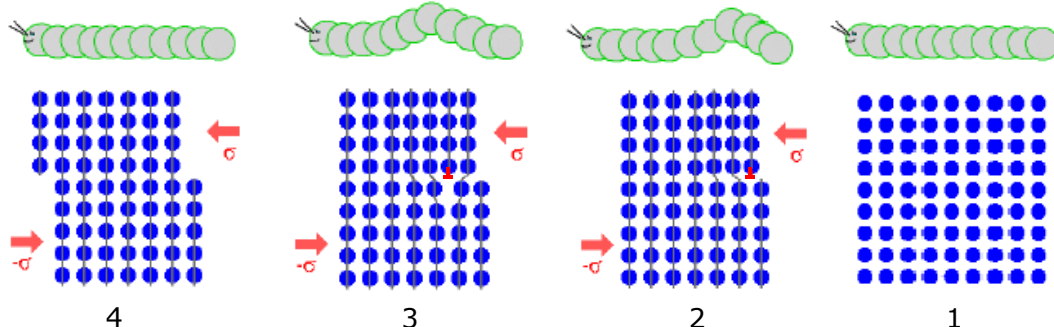
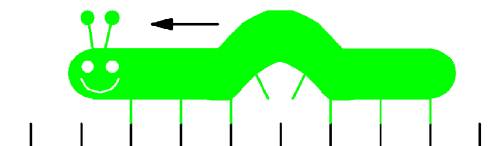
- Caterpillar technique



Line defects

Dislocations as carrier of plastic deformation

- Caterpillar technique
- same trick as moving a carpet



plastic deformation proceeds

- atomic step by atomic step
- by movement of dislocations

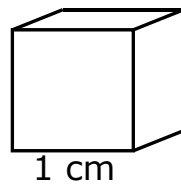
Line defects

Dislocation density

- Definition (dislocation line length per volume)

$$\rho = \frac{L}{V}$$

- SI unit $\text{m}/\text{m}^3 = \text{m}^{-2}$
- Whiskers containing a single (screw) dislocation
- Si wafers 10^4 m^{-2}
- Undeformed metals 10^{10} m^{-2}
- Highly deformed metals $10^{16} \text{ m}/\text{m}^3$
 - Illustration: 10 million km in a cm^3



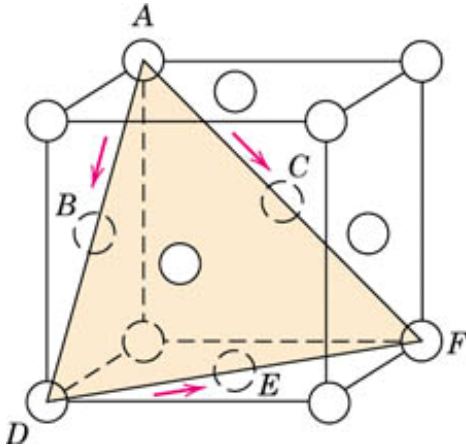
1000 x



Dislocations and crystalline lattice

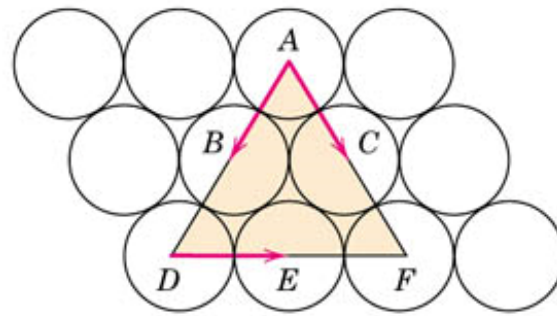
Slip systems in metals

- plastic deformation = dislocation motion = **slip (or glide)**
- **slip system**: slip plane $\{hkl\}$ + slip direction $\langle uvw \rangle$
 closest packed plane + closest packed direction
 planes with largest distance + Burgers vector



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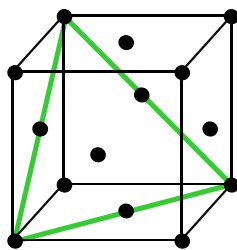
Example: fcc lattice



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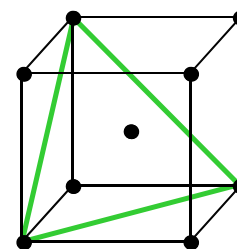
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Close-packed planes (hkl) and directions [uvw]

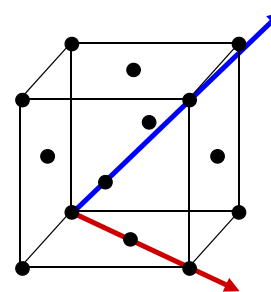


fcc

(111) plane: close-packed in fcc,
but not in bcc

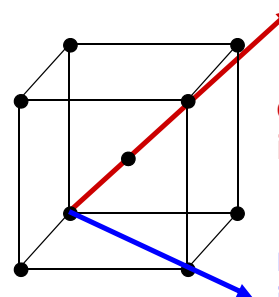


bcc



[111] =
not close-packed
in fcc

[110] =
close-packed
in fcc



[111] =
close-packed
in bcc

[110] =
not close-packed
in bcc

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Slip systems in metals

- plastic deformation = dislocation motion = **slip (or glide)**
- **slip system**: slip plane $\{hkl\}$ + slip direction $\langle uvw \rangle$
 closest packed plane + closest packed direction
 planes with largest distance + Burgers vector

Lattice	Examples	Close(st) packed planes (hkl)	Close(st) packed directions [uvw]	Slip systems
fcc	Al, Cu, Ag, Au, Ni, γ -Fe, ...	$\{111\}$ = close-packed	$\langle 110 \rangle$ face diagonals	$4 \times 3 = 12$
bcc	Cr, W, α -Fe, ...	$\{110\}$ = not close-packed	$\langle 111 \rangle$ volume diagonals	$6 \times 2 = 12$

Lattice defects

0-dimensional: **point defects**
vacancies, interstitials, substitutional atoms

1-dimensional: **line defects**
dislocations

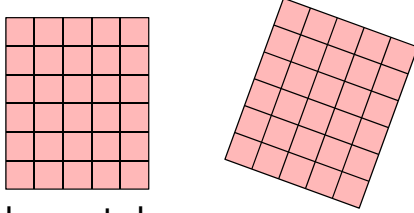
2-dimensional: **area (planar) defects**
interfaces (stacking faults, grain-, phase-, twin-boundaries, surfaces)

3-dimensional: **volume (bulk) defects**
voids, pores, precipitates, inclusions, cracks

Microstructure – grains from solidification

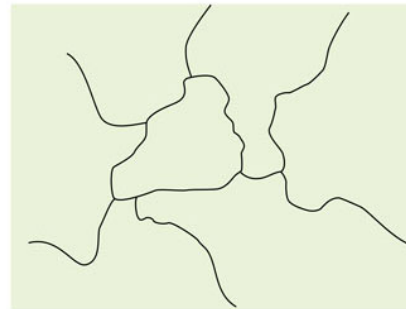
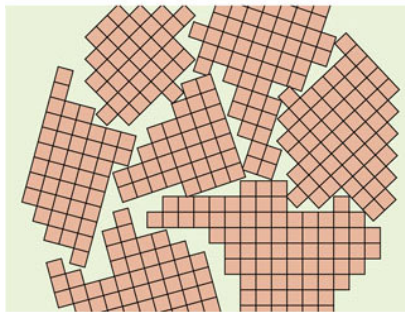
- Single crystals

from a single nucleus

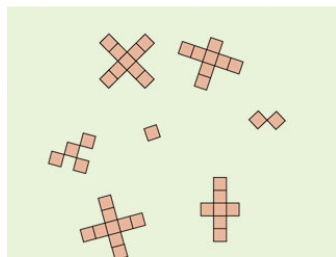
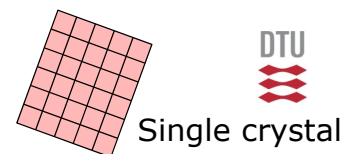


- Polycrystals

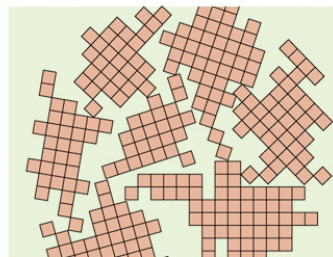
from many nuclei



Planar defects Grain boundaries in polycrystals

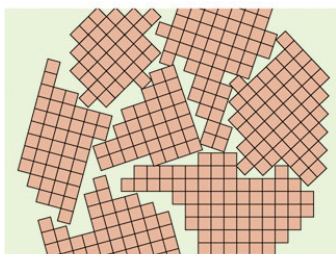


(a)



(b)

Nuclei form during solidification in melt



(c)

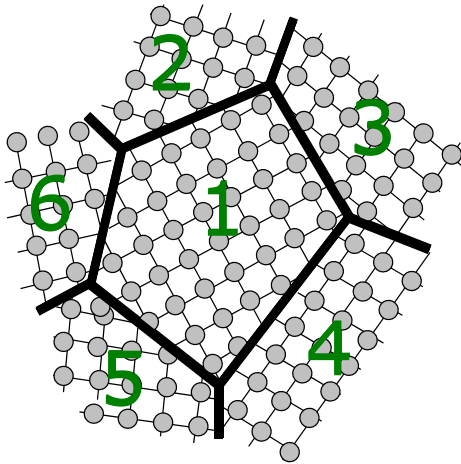


(d)

Nuclei grow and form grains

Planar defects

Grain boundaries

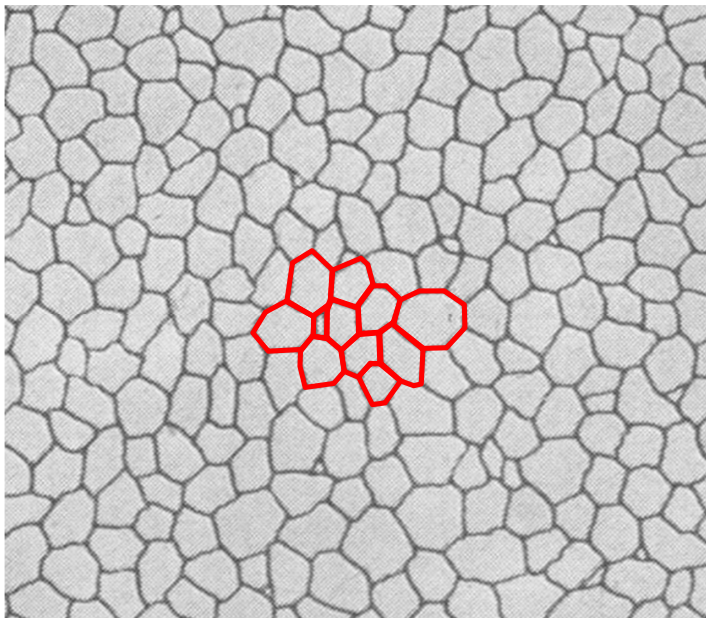


Grain boundaries

- Separate two grains
i.e. two regions of same
crystal structure, but of
different crystallographic
orientation

Planar defects

Grain boundaries



Grain size D

Surface area S

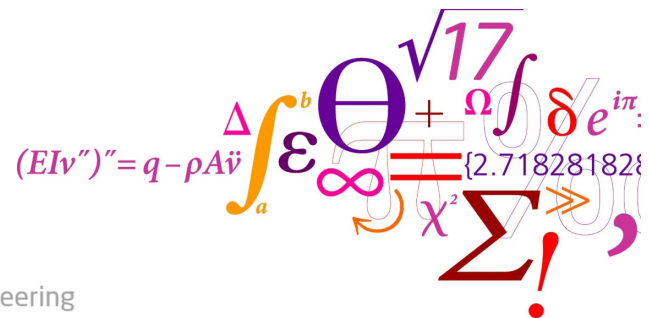
Volume V

Boundary density

$$S_v = \frac{S}{V} \approx \frac{2}{D}$$

Intermezzo

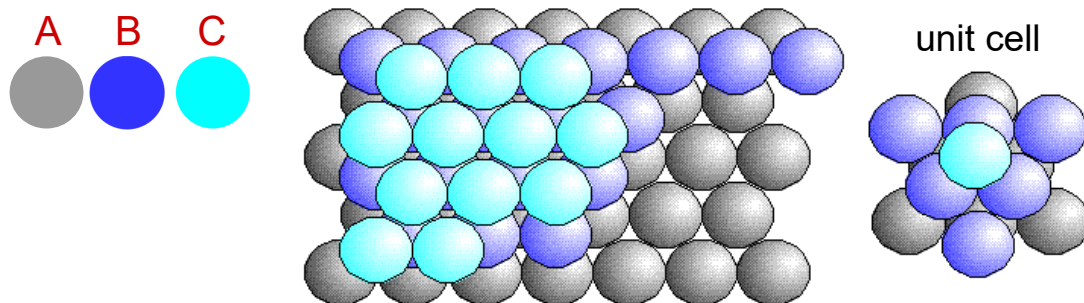
Stacking of close-packed planes



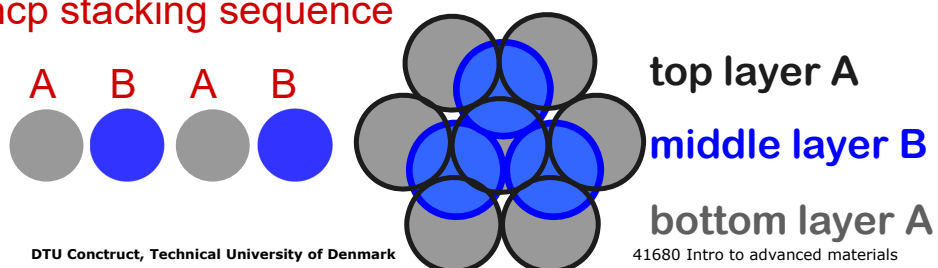
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Stacking sequences

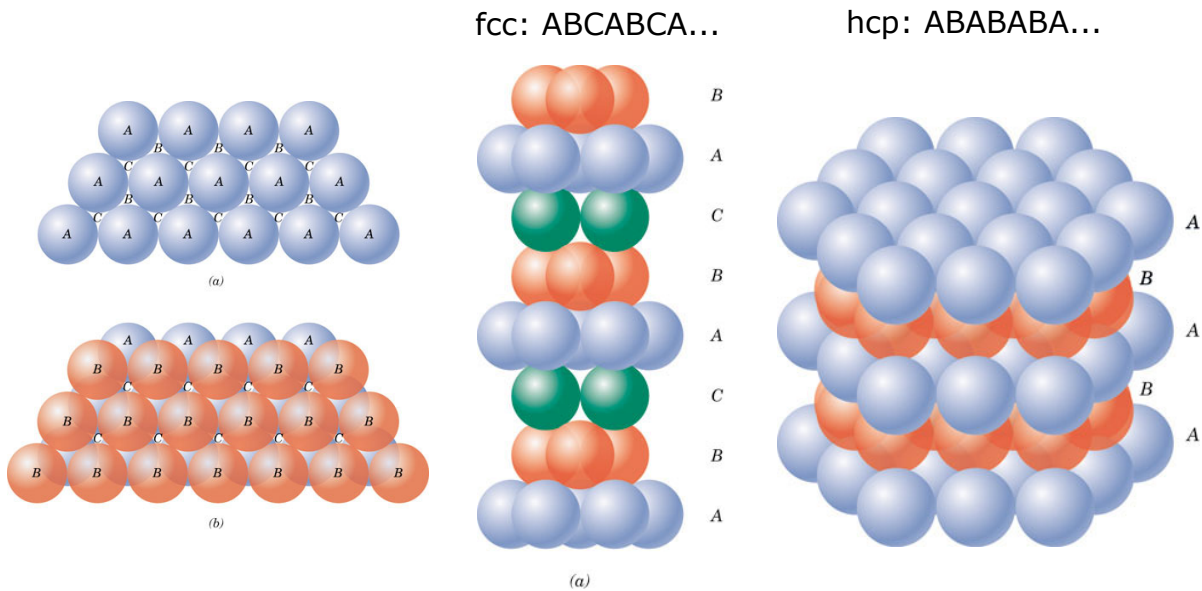
fcc stacking sequence



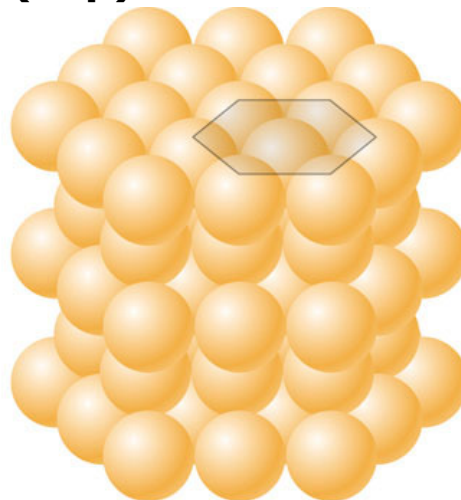
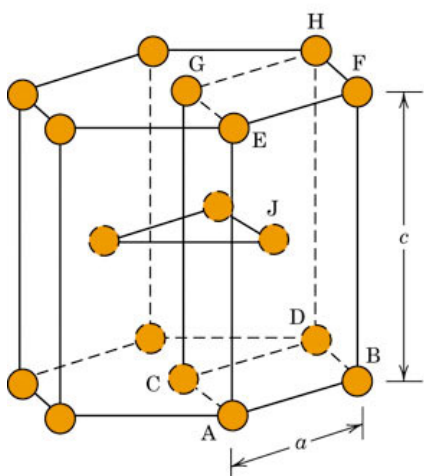
hcp stacking sequence



Stacking sequences



Hexagonal close-packed (hcp)



- Atomic packing factor 0.74
- Coordination number 12
- Examples: Mg, Co, Ti

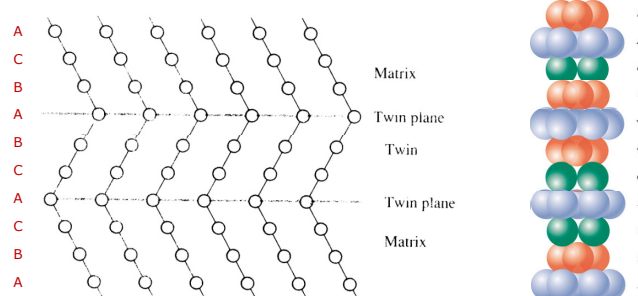
Elements – crystal structures

H																	He
Li <i>hcp</i>	Be											B	C <i>cub</i>	N	O	F	Ne
Na <i>hcp</i>	Mg											Al	Si	P	S	Cl	Ar
K	Ca <i>bcc</i>	Sc <i>fcc</i>	Ti <i>bcc</i>	V	Cr	Mn	Fe <i>fcc</i>	Co <i>fcc</i>	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
Rb	Sr <i>bcc</i>	Y <i>bcc</i>	Zr <i>bcc</i>	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn <i>ttg</i>	Sb	Te	I	Xe
Cs	Ba	L	Hf <i>bcc</i>	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl <i>bcc</i>	Pb	Bi	Po	At	Rn
Fr	Ra	A	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	Fl	Mc	Lv	Ts	Og
		L	La <i>fcc</i>	Ce <i>fcc</i>	Pr <i>bcc</i>	Nd <i>bcc</i>	Pm <i>bcc</i>	Sm <i>hcp</i>	Eu	Gd <i>bcc</i>	Tb <i>bcc</i>	Dy <i>bcc</i>	Ho	Er	Tm	Yb <i>bcc</i>	Lu
		A	Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr
	Cubic primitive						Face-centered cubic						Diamond (cubic)				
	Body-centered cubic						Hexagonal						Nonmetals				

Planar defect

Twin boundaries in polycrystals

- Twin = mirrored crystalline lattice

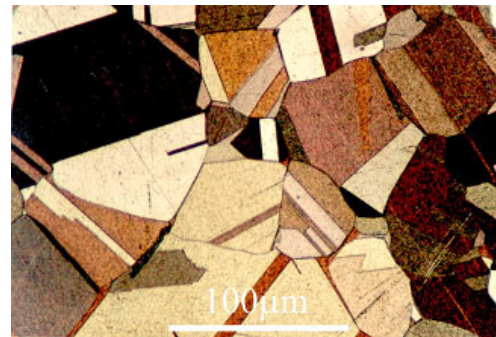
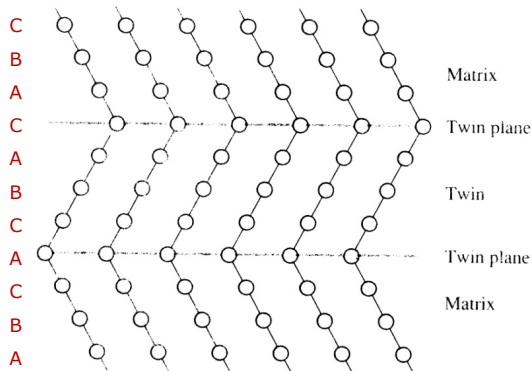


- Coherent boundaries on well-defined lattice planes (fcc {111})
- Twin formation causes shear
- Plastic deformation in non-cubic lattices ("tin cry")

Planar defects

Twin boundaries

- Twin = mirror symmetry



Cu70-Zn30 wt%, α -phase,
annealing twins

Lattice defects

0-dimensional: point defects

vacancies, interstitials, substitutional atoms

1-dimensional: line defects

dislocations

2-dimensional: area (planar) defects

interfaces (stacking faults,
grain-, phase-, twin-boundaries, surfaces)

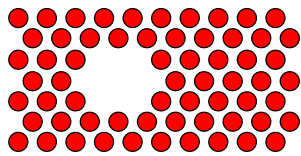
3-dimensional: volume (bulk) defects

voids, pores, precipitates, inclusions, cracks

Volume defects

Self defects

- Clusters of point defects
- Pore = agglomerate of vacancies



- Requires many missing atoms!

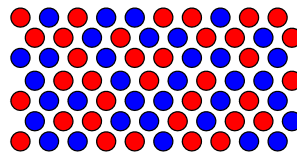
Alloys

mixture of two or more elements with metallic bonding

A complex, colorful mathematical expression featuring various symbols like integrals, Greek letters, and numbers. The expression includes symbols such as Δ , \int_a^b , ε , Θ , $\sqrt{17}$, Ω , $\delta e^{i\pi}$, ∞ , χ^2 , Σ , and $!$. The expression is written in a stylized, overlapping manner with various colors.

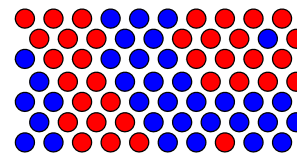
Alloys – three principle types

- Solid solutions
= foreign atoms in
crystal lattice



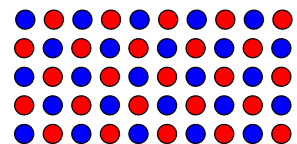
- Atoms unordered
in same lattice

- Mixture of different
metallic phases



- Distinct phases
with different
composition and
possibly different
lattices

- Intermetallic
compounds



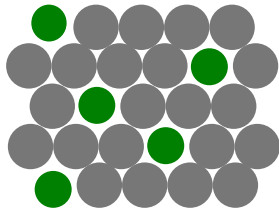
- Atoms ordered in
possibly different
lattice

Point defects in alloys

- **Solid solution** = foreign atoms (impurities) in
the crystal lattice of host atoms
- **Interstitial** atoms
 - ⇒ sitting between lattice sites
 - ⇒ interstitial solid solution
- **Substitutional** atoms
 - ⇒ substitute atoms on latt. sites
 - ⇒ substitutional solid solution
- **Crystal structure maintained for solid solutions**
- **Alternatives**
 - immiscibility
 - intermetallic compounds
(new phase of own structure)

Point defects in alloys

Substitutional atoms
substitutional solid solution
(e.g. Ni in Cu)



Hume-Rothery rules

Complete miscibility for substitutional solid solution requires:

- Same crystal structure
- Difference in atomic radius not more than 15%
- Similar electronegativity
- Same valence

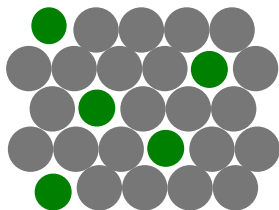
Example: Cu and Ni

Otherwise

- Partial miscibility
- Immiscibility

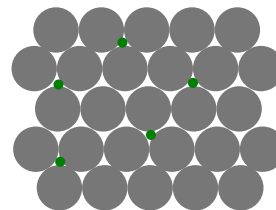
Point defects in alloys

Substitutional atoms
substitutional solid solution
(e.g. Ni in Cu)



- Foreign atoms on regular lattice sites
- Hume-Rothery rules

Interstitial atoms
interstitial solid solution
(e.g. C in Fe)



- Foreign atoms on interstitial sites
- Only small atoms in holes (as B, C, N, O)

Composition of binary alloys containing A and B

- Composition
(weight percentage)

- Proper term: mass fraction

$$C_A = \frac{m_A}{m_A + m_B}$$

$$C_B = \frac{m_B}{m_A + m_B}$$

- Conversion

$$m_A = n_A \mu_A$$

$$C_A = \frac{n_A \mu_A}{n_A \mu_A + n_B \mu_B} = \frac{C_A^* \mu_A}{C_A^* \mu_A + C_B^* \mu_B}$$

- Composition
(atomic percentage)

- Proper term: amount fraction

$$C_A^* = \frac{n_A}{n_A + n_B}$$

$$C_B^* = \frac{n_B}{n_A + n_B}$$

- Conversion

$$\mu_A = m_A / n_A$$

$$C_A^* = \frac{C_A / \mu_A}{C_A / \mu_A + C_B / \mu_B}$$

m mass

n amount of substance (number of atoms)

μ molar mass (atomic mass, atomic weight)

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o to advanced materials

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Composition of binary alloys Applications

- Density

$$\rho = \frac{m}{V} = \frac{m_A + m_B}{V}$$

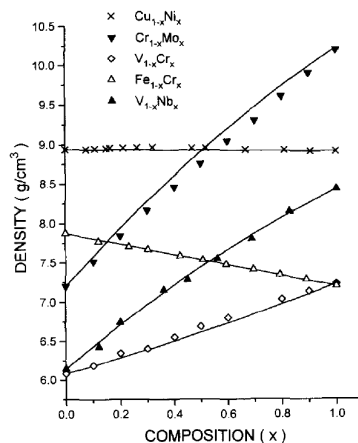
- Naïve estimate:
additivity of volumes

$$V = \frac{m_A + m_B}{\rho}$$

$$\approx V_A + V_B$$

$$\approx \frac{m_A}{\rho_A} + \frac{m_B}{\rho_B}$$

$$\rho \approx \frac{1}{\frac{C_A}{\rho_A} + \frac{C_B}{\rho_B}}$$

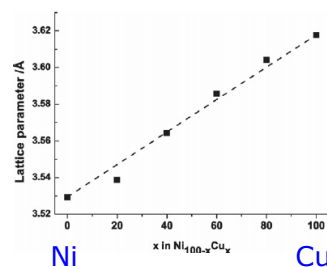


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- Lattice constant a of
solid solutions
– Vegard's rule

$$a_{ss} = C_A^* a_A + C_B^* a_B$$

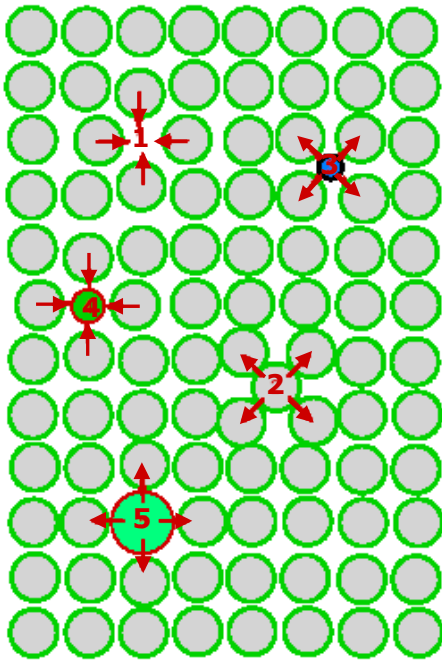
- Limited validity
- Example CuNi



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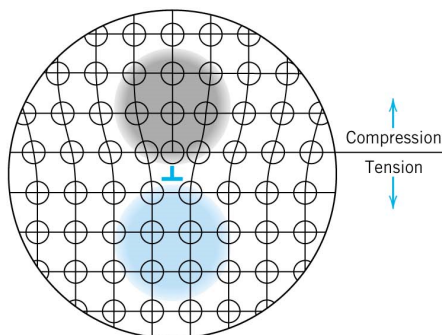
F24

Points defects



- local distortion of the lattice
 - interaction
 - external stress
1. Vacancy
 2. self-interstitial
 3. interstitial impurity
 4. small substitutional impurity
 5. large substitutional impurity

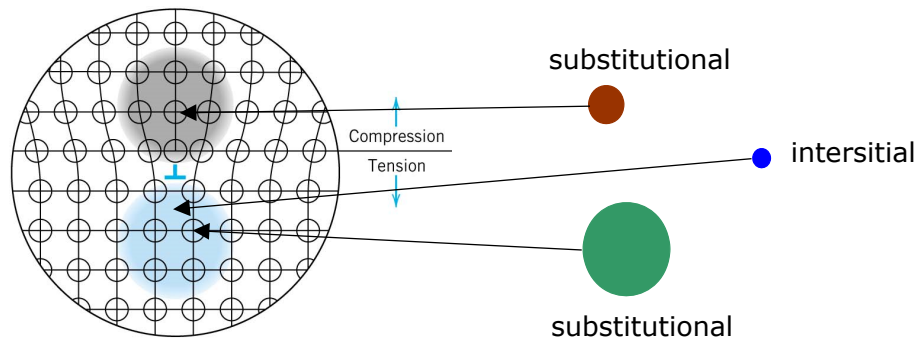
Interaction: dislocations and point defects



Which position is likely to be occupied by

- an interstitial atom
- a substitutional atom larger than the host ones
- a substitutional atom smaller than the host ones ?

Interaction: dislocations and point defects



Which position is likely to be occupied by

- an interstitial atom
- a substitutional atom larger than the host ones
- a substitutional atom smaller than the host ones ?

Lattice defects

0-dimensional: point defects

vacancies, interstitials, substitutional atoms

1-dimensional: line defects

dislocations

2-dimensional: area (planar) defects

interfaces (stacking faults,
grain-, phase-, twin-boundaries, surfaces)

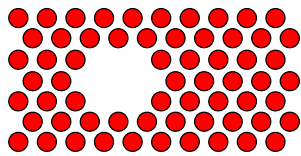
3-dimensional: volume (bulk) defects

voids, pores, precipitates, inclusions, cracks

Volume defects

Self defects

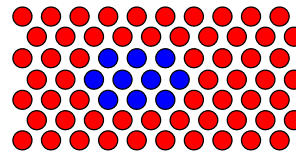
- Clusters of point defects
- Pore = agglomerate of vacancies



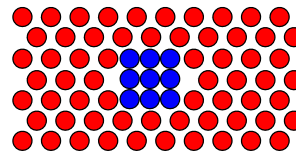
- Requires many missing atoms!

Alien defects

- Particles of second phase
- Precipitates
 - coherent

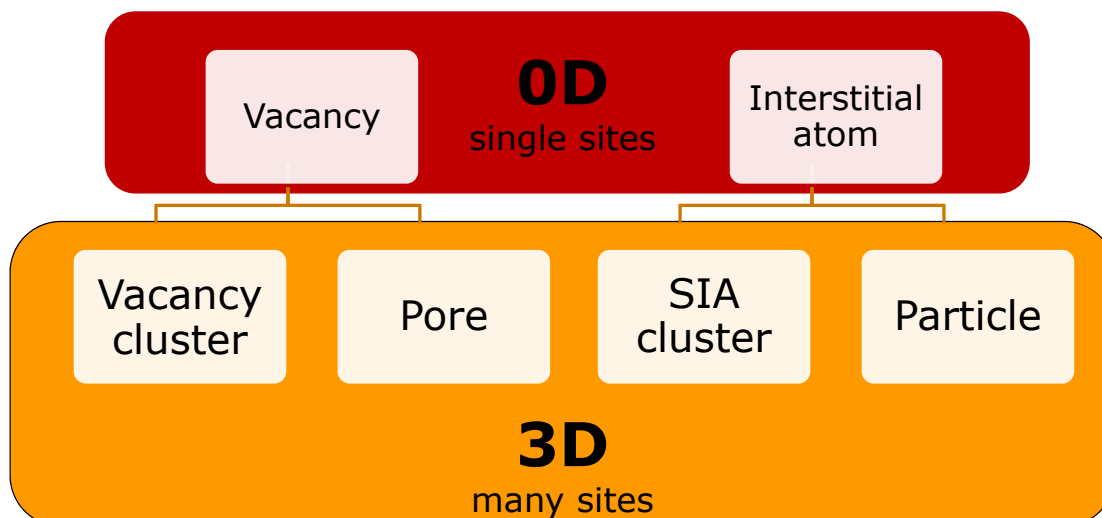


– incoherent



- Requires many atoms!

Overview

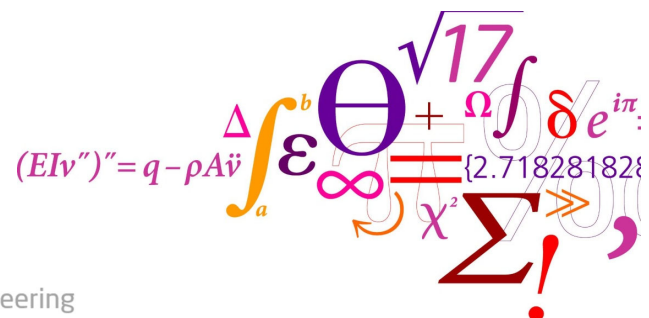


Rôle of defects

- diffusion
- mechanical properties
- electrical properties
- magnetic properties
- plastic deformation
- strengthening mechanisms !!!
- various interactions
e.g. interstitial atoms = obstacles to dislocation movement

Interstitial lattice sites

Where is space for foreign atoms?



Cubic lattices - comparison

	* Close-packed direction	Neighbor closest to origin	Atomic diameter $2R$	Atomic packing factor	Coordination number	Examples
sc	1 $\langle 100 \rangle$	$[100]a$	a	0.52	6	only α -Po
bcc	2 $\langle 111 \rangle$	$[111]a/2$	$\sqrt{3}a/2$	0.68	8	Cr, W, V, Ta, α -Fe
fcc	4 $\langle 110 \rangle$	$[110]a/2$	$\sqrt{2}a/2$	0.74	12	Al, Cu, Ag, Au, Ni, γ -Fe

* Number of atoms in unit cell

Lattice parameter a

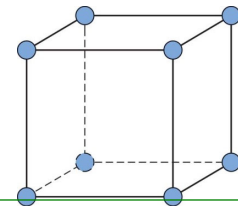
Random close-packed spheres	0.64		
Ordered close-packed spheres	0.74		

Only fcc is close-packed !

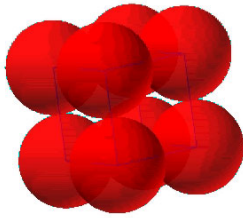
Wanted Simple cubic lattice

I	<ul style="list-style-type: none"> Atoms in unit cell Coordination number (# nearest neighbors) 	<div>1</div> <div>6</div>
III	<ul style="list-style-type: none"> Ratio between edge length and atomic radius Atomic packing factor Closest packed direction Closest packed planes 	<div>$a/R = 2$</div> <div>$APF = \frac{\pi}{6} \approx 0.52$</div> <div>$\langle 100 \rangle$</div> <div> <div>$\{100\}$</div> <div> <ul style="list-style-type: none"> ○ Close-packed ✗ Not close-packed </div> </div>

II	<ul style="list-style-type: none"> Along edges <ul style="list-style-type: none"> ✗ Atoms touch each other ○ Atoms do not touch each other <ul style="list-style-type: none"> Distance between centers a Distance between neighbors 0 Along face diagonals <ul style="list-style-type: none"> ○ Atoms touch each other ✗ Atoms do not touch each other <ul style="list-style-type: none"> Distance between centers $\sqrt{2}a$ Distance between neighbors $\sqrt{2}a - 2R$ Along volume diagonals <ul style="list-style-type: none"> ○ Atoms touch each other ✗ Atoms do not touch each other <ul style="list-style-type: none"> Distance between centers $\sqrt{3}a$ Distance between neighbors $\sqrt{3}a - 2R$
----	--



Simple cubic lattice – Interstitial site



- Hard sphere model

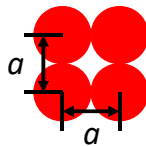
- Interstitial site (hexahedral site)

$$2r_H = \sqrt{3}a - 2R_{at} = 2R_{at}(\sqrt{3} - 1)$$

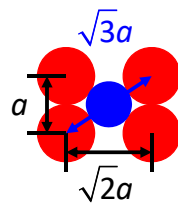
$$r_H/R_{at} = 0.73$$

- Crystallographic planes

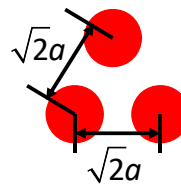
(100)



(110)

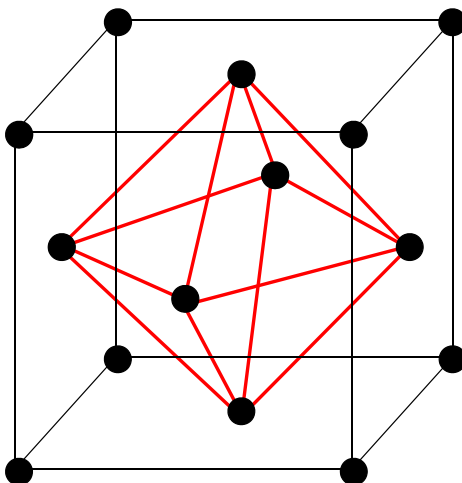


(111)

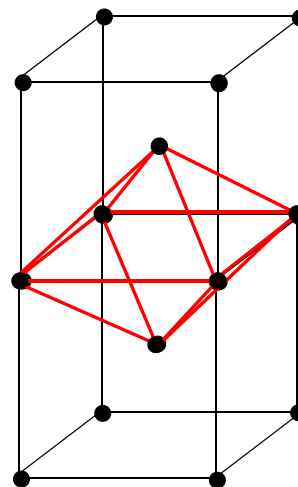


Interstitial sites - octahedral sites

fcc

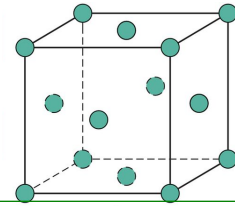


bcc



Radius of interstitial site r
Radius of host atoms R_{at}

Wanted Face centered cubic lattice



- I
- Atoms in unit cell 4
 - Coordination number (# nearest neighbors) 12

- III
- Ratio between edge length and atomic radius

$$a/R = 4/\sqrt{2}$$

- Atomic packing factor

$$APF = 4 \frac{4\pi}{3} \left(\frac{\sqrt{2}}{4} \right)^3 = \frac{\pi\sqrt{2}}{6} \approx 0.74$$

- Closest packed direction

$$\langle 110 \rangle$$

- Closest packed planes

$$\{111\}$$

☒ Close-packed

☐ Not close-packed

- II
- Along edges

☐ Atoms touch each other

☒ Atoms do not touch each other

– Distance between centers

$$a$$

– Distance between neighbors

$$a - 2R$$

- Along face diagonals

☒ Atoms touch each other

☐ Atoms do not touch each other

– Distance between centers

$$\sqrt{2}a/2$$

– Distance between neighbors

$$0$$

- Along volume diagonals

☐ Atoms touch each other

☒ Atoms do not touch each other

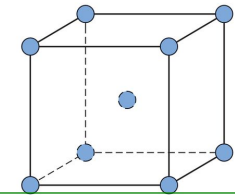
– Distance between centers

$$\sqrt{3}a$$

– Distance between neighbors

$$\sqrt{3}a - 2R$$

Wanted Body centered cubic lattice



- I
- Atoms in unit cell 2
 - Coordination number (# nearest neighbors) 8

- III
- Ratio between edge length and atomic radius

$$a/R = 4/\sqrt{3}$$

- Atomic packing factor

$$APF = 2 \frac{4\pi}{3} \left(\frac{\sqrt{3}}{4} \right)^3 = \frac{\pi\sqrt{3}}{8} \approx 0.68$$

- Closest packed direction

$$\langle 111 \rangle$$

- Closest packed planes

$$\{110\}$$

☐ Close-packed

☒ Not close-packed

- II
- Along edges

☐ Atoms touch each other

☒ Atoms do not touch each other

– Distance between centers

$$a$$

– Distance between neighbors

$$a - 2R$$

- Along face diagonals

☐ Atoms touch each other

☒ Atoms do not touch each other

– Distance between centers

$$\sqrt{2}a$$

– Distance between neighbors

$$\sqrt{2}a - 2R$$

- Along volume diagonals

☒ Atoms touch each other

☐ Atoms do not touch each other

– Distance between centers

$$\sqrt{3}a/2$$

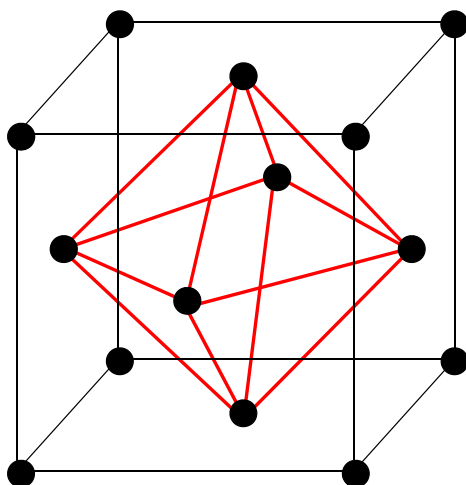
– Distance between neighbors

$$0$$

Group exercises

Interstitial sites in fcc

octahedral

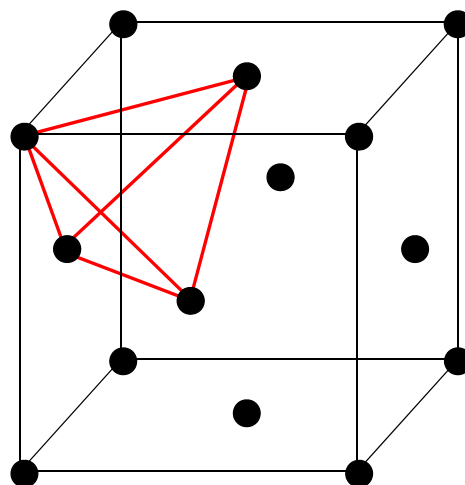


number: 4

$$r_o/R_{at} = 0.414$$

Radius of interstitial site r
Radius of host atoms R_{at}

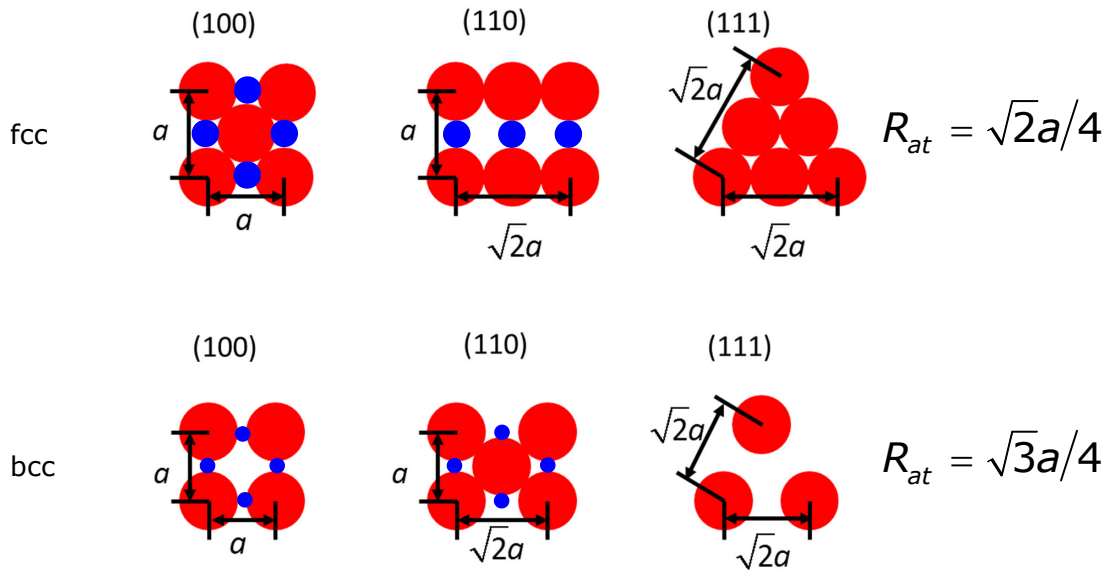
tetrahedral



number: 8

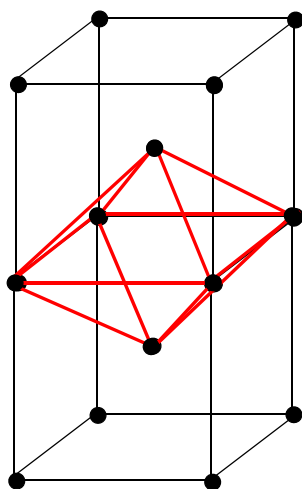
$$r_t/R_{at} = 0.230$$

$$a = 2R_{at} + 2r_o \rightarrow r_o = \frac{a}{2} - R_{at}$$



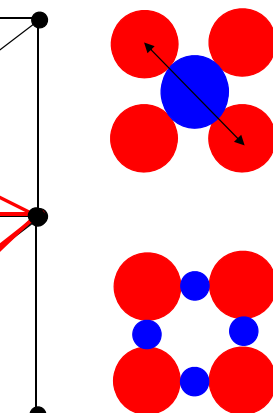
Interstitial sites in bcc

octahedral

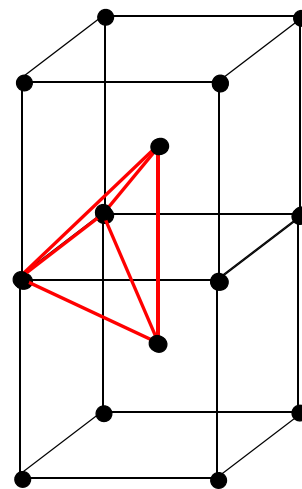


number: 6

$$r_o/R_{at} = 0.150$$



tetrahedral



number: 12

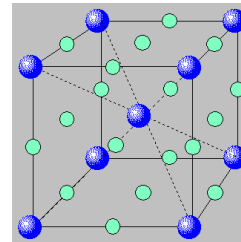
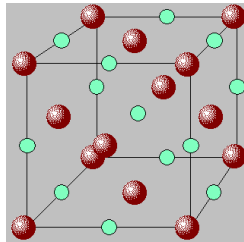
$$r_T/R_{at} = 0.290$$

Radius of interstitial site r
Radius of host atoms R

Interstitial lattice sites

Octahedral interstitial sites

- Face-centered cubic
- Body-centered cubic



- Number of sites in unit cell
 $1 + 12/4 = 4$
- Number of atoms in unit cell
4
- Number of sites in unit cell
 $6/2 + 12/4 = 6$
- Number of atoms in unit cell
2

Interstitial lattice sites

Overview

Lattice	Simple cubic	Body-centered cubic	Face-centered cubic
Atoms in uc	1	2	4
Coordination	6	8	12
APF	52 %	68 %	74 %
Type	Hexahedral	Octahedral	Octahedral
-relative size	0.732	0.150	0.414
-number in uc	1	6	4
Sites/atom	1	3	1
	