${\bf Lab2_BikeShared_Model1_LinearR}$

```
library(tinytex)
library(ggplot2)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(Hmisc)
## Loading required package: lattice
## Loading required package: survival
## Loading required package: Formula
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:dplyr':
##
##
       src, summarize
## The following objects are masked from 'package:base':
##
       format.pval, units
##
Get the Date
bike <- read.csv("hour.csv", header= TRUE )</pre>
Clear Data
bike$instant<- NULL
```

the temp in raw dataset have been divided by 100 in fahrenheit. Let's convert them by times 100 and then to Celsius.

```
library(weathermetrics)
bike <- mutate(bike, temp = fahrenheit.to.celsius(bike$temp *100 ))
bike <- mutate(bike, atemp = fahrenheit.to.celsius(bike$atemp *100 ))
bike$dteday <- as.POSIXct(bike$dteday)</pre>
```

the hum in the raw dataset have been divided by 100, let's convert them back.

```
bike <- mutate(bike, hum = bike$hum*100 )</pre>
```

the windspeed in the dataset have been divided by 67. let's convert them back.

```
bike <- mutate(bike, windspeed = bike$windspeed*67)</pre>
```

```
head(bike)
```

```
##
        dteday season yr mnth hr holiday weekday workingday weathersit temp
## 1 2011-01-01
                    1 0
                            1 0
                                      0
                                              6
                                                         0
                                                                    1 - 4.44
## 2 2011-01-01
                    1 0
                                              6
                                                         0
                                                                    1 - 5.56
                            1 1
                                      0
## 3 2011-01-01
                    1 0
                            1 2
                                      0
                                              6
                                                         0
                                                                    1 - 5.56
## 4 2011-01-01
                    1 0
                            1 3
                                      0
                                              6
                                                         0
                                                                    1 - 4.44
## 5 2011-01-01
                    1 0
                            1 4
                                       0
                                              6
                                                         0
                                                                    1 - 4.44
                            1 5
                                       0
                                                                    2 - 4.44
## 6 2011-01-01
                    1 0
    atemp hum windspeed casual registered cnt
                 0.0000
## 1 -1.78 81
                             3
                                      13 16
## 2 -2.63 80
                 0.0000
                             8
                                       32 40
## 3 -2.63 80
                 0.0000
                             5
                                      27 32
                 0.0000
                             3
## 4 -1.78 75
                                       10 13
## 5 -1.78 75
                 0.0000
                             0
                                        1
                                           1
## 6 -3.47 75
                 6.0032
```

use one year dataset for doing lenear Regression model

```
bike2012<- bike[8646:17379, ]

numeric_cols = sapply(bike2012, is.numeric)
bike_num_only = bike2012[, numeric_cols]

colnames(bike_num_only)

## [1] "season" "yr" "mnth" "hr" "holiday"</pre>
```

```
bike2012_sub= bike2012[ , c("season", "mnth", "hr" , "holiday", "weekday", "workingday", "weathersit", "
```

Determine correlation of each attributes to the counts of bike rent.

```
library(corrplot)
## corrplot 0.84 loaded
library(corrgram)
## Registered S3 method overwritten by 'seriation':
##
     method
                     from
     reorder.hclust gclus
##
## Attaching package: 'corrgram'
## The following object is masked from 'package:lattice':
##
##
       panel.fill
corrgram(bike2012_sub,order=TRUE, lower.panel=panel.shade,
  upper.panel=panel.pie, text.panel=panel.txt)
windspeed
        holiday
              weathersit
                                        workingday
                                                             weekday
```

cor(bike2012_sub)

```
0.1717043364 9.937272e-02 4.240457e-01 -0.041315974 0.051170585
## cnt
##
                 workingday
                              weathersit
                                                temp
                                                           atemp
              0.0136783682 -0.014102308 0.28080951 0.28702513
                                                                  0.107565722
## season
## mnth
              -0.0104470890
                             0.031844287
                                          0.14188811
                                                      0.14210589 0.139647261
## hr
              0.0007820535 - 0.024180977 \ 0.15614877 \ 0.15261088 - 0.305348400
## holiday
              -0.2568524234 -0.041803723 -0.03535751 -0.03573136 0.002675235
## weekday
              0.0531221871 -0.022220696 0.03759909 0.02685393 -0.023588523
## workingday 1.0000000000 0.019844039 0.05780063 0.05720205 0.005520906
## weathersit 0.0198440392 1.000000000 -0.11286550 -0.11410042 0.429349584
              0.0578006296 -0.112865503 1.00000000 0.98279969 -0.096547758
## temp
              0.0572020512 -0.114100422 0.98279969 1.00000000 -0.076590599
## atemp
              0.0055209055 \quad 0.429349584 \quad -0.09654776 \quad -0.07659060 \quad 1.0000000000
## hum
## windspeed -0.0342522129 0.002583501 -0.04066481 -0.07902589 -0.321941772
## cnt
              0.0458205736 - 0.148346392 \ 0.39962599 \ 0.39639356 - 0.344065069
##
                 windspeed
## season
              -0.145031296 0.17170434
## mnth
             -0.115398519 0.09937272
              0.149324399 0.42404571
## hr
## holiday
              0.007474693 -0.04131597
## weekday
              -0.016778200 0.05117058
## workingday -0.034252213 0.04582057
## weathersit 0.002583501 -0.14834639
              -0.040664811
                           0.39962599
## temp
## atemp
              -0.079025891 0.39639356
## hum
              -0.321941772 -0.34406507
             1.000000000 0.11115494
## windspeed
               0.111154939 1.00000000
## cnt
bike2012_sub = bike2012[ , c("season", "hr" , "holiday", "weekday", "workingday", "weathersit", "temp",
cor_result = rcorr(as.matrix(bike2012_sub))
corrplot(cor_result$r, type = "upper", order = "hclust", t1.col = "black", t1.srt = 45)
Attribute "mnth" has noticeable correlation with "season", "Holiday" and "hr". Remove mnth
as an attrubute. Attibute"temp" and "atemp" have very high correlation at 0.98. Remove
```

##

season

weekday

temp

hum

atemp

mnth

hr ## holiday season

-0.0174999989 7.797492e-03

mnth

workingday 0.0136783682 -1.044709e-02 7.820535e-04 -0.256852423 0.053122187 ## weathersit -0.0141023076 3.184429e-02 -2.418098e-02 -0.041803723 -0.022220696

windspeed -0.1450312963 -1.153985e-01 1.493244e-01 0.007474693 -0.016778200

1.0000000000 8.316577e-01 -2.270054e-04 -0.017499999 0.008735100

0.8316577130 1.000000e+00 7.990218e-05 0.007797492 0.008710095 -0.0002270054 7.990218e-05 1.000000e+00 0.001869484 -0.001436206

0.0087350995 8.710095e-03 -1.436206e-03 -0.126642035 1.000000000

0.2808095057 1.418881e-01 1.561488e-01 -0.035357509 0.037599087

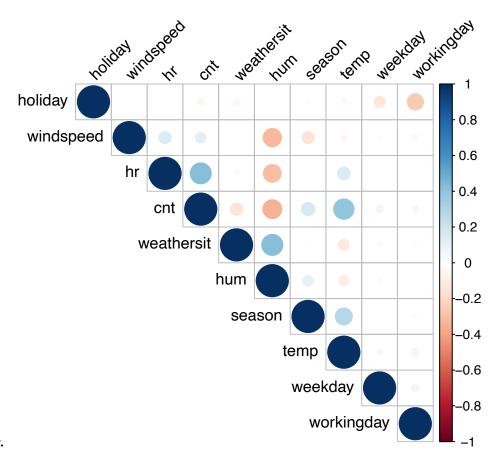
0.2870251337 1.421059e-01 1.526109e-01 -0.035731363 0.026853925

0.1075657222 1.396473e-01 -3.053484e-01 0.002675235 -0.023588523

holiday

1.869484e-03 1.000000000 -0.126642035

weekday



"atemp" to avoid intercollinearity.

Create Linear Regression Model

```
library(caTools)
bike2012.model <- lm(cnt ~ season + temp + hum + weathersit , data= bike2012_sub)
summary(bike2012.model)
##
## Call:
## lm(formula = cnt ~ season + temp + hum + weathersit, data = bike2012_sub)
##
## Residuals:
##
                10 Median
                                3Q
                                       Max
## -374.01 -124.50 -38.54
                             88.24
                                    667.88
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                            7.9222 40.899 < 2e-16 ***
## (Intercept) 324.0092
                21.3966
                            1.8207 11.752 < 2e-16 ***
## season
                            0.1944 35.124
                                           < 2e-16 ***
## temp
                6.8297
                            0.1141 -33.039 < 2e-16 ***
## hum
                -3.7695
## weathersit
              12.4860
                            3.4103
                                     3.661 0.000253 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 179 on 8729 degrees of freedom
## Multiple R-squared: 0.2663, Adjusted R-squared: 0.266
## F-statistic: 792.2 on 4 and 8729 DF, p-value: < 2.2e-16</pre>
```

We get pretty low Adjustered R_squared, which is 0.266. Let add "hr", "holiday".

```
colnames(bike2012_sub)
  [1] "season"
##
                    "hr"
                                 "holiday"
                                              "weekday"
                                                           "workingday"
  [6] "weathersit" "temp"
                                 "hum"
                                              "windspeed"
                                                           "cnt"
bike2012.model <- lm(cnt ~ season + temp + hum + weathersit + hr + holiday , data= bike2012_sub)
summary(bike2012.model)
##
## Call:
## lm(formula = cnt ~ season + temp + hum + weathersit + hr + holiday,
##
      data = bike2012_sub)
##
## Residuals:
               1Q Median
##
      Min
                               3Q
                                      Max
## -400.17 -112.97 -38.57
                           71.41 665.80
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                          8.7412 19.995 < 2e-16 ***
## (Intercept) 174.7804
## season
              21.2724
                           1.7146 12.407 < 2e-16 ***
## temp
                5.9548
                           0.1850 32.186 < 2e-16 ***
               -2.5543
                           0.1134 -22.519 < 2e-16 ***
                           3.2463 -0.863 0.388147
## weathersit -2.8016
                9.2813
                           0.2788 33.293 < 2e-16 ***
## hr
## holiday
              -35.8185
                          10.6140 -3.375 0.000742 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 168.5 on 8727 degrees of freedom
## Multiple R-squared: 0.3496, Adjusted R-squared: 0.3491
## F-statistic: 781.7 on 6 and 8727 DF, p-value: < 2.2e-16
```

Adjusted R-squared increase to 0.3491. "Weathersit" have shown to be not significant as p>0.05.

Remove weathersit and add weekday, windseppd and workingday for adjusting the model

```
bike2012.model <- lm(cnt ~ season + temp + hum + hr + holiday + weekday + workingday + windspeed, data
summary(bike2012.model)
##
## Call:
## lm(formula = cnt ~ season + temp + hum + hr + holiday + weekday +
##
       workingday + windspeed, data = bike2012_sub)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                       Max
## -413.57 -113.02 -39.03
                            71.62 657.48
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 143.8417
                          10.8331 13.278 < 2e-16 ***
               21.7921
                           1.7192 12.676 < 2e-16 ***
## season
## temp
                5.9477
                           0.1847 32.200 < 2e-16 ***
## hum
               -2.5173
                           0.1060 -23.746 < 2e-16 ***
## hr
                9.2175
                           0.2764 33.343 < 2e-16 ***
## holiday
              -23.7160
                          11.0243 -2.151 0.031484 *
                                     3.549 0.000388 ***
## weekday
                3.2183
                           0.9067
## workingday
               10.0245
                           4.0090
                                   2.500 0.012422 *
## windspeed
                0.5842
                           0.2363
                                   2.472 0.013449 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 168.3 on 8725 degrees of freedom
## Multiple R-squared: 0.3513, Adjusted R-squared: 0.3507
## F-statistic: 590.7 on 8 and 8725 DF, p-value: < 2.2e-16
The adjustered R-squred increases to 0.3507.P-values are all less than 0.05.
###let have a look if we build the model base on the original dataset, "hour.csv" (renamed as "bike"), for
2011 and 2012.
bike_subset = bike[ , c("season", "hr" , "holiday", "weekday", "workingday", "temp", "hum", "windspee
bike.model <- lm(cnt ~ season + temp + hum + hr + holiday + weekday + workingday + windspeed, data= bi
summary(bike.model)
##
## Call:
## lm(formula = cnt ~ season + temp + hum + hr + holiday + weekday +
       workingday + windspeed, data = bike_subset)
##
##
## Residuals:
##
      Min
               1Q Median
                                3Q
                                       Max
## -335.82 -96.77 -30.46 54.01 691.14
```

```
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 132.53273
                            6.50831
                                     20.364
                                             < 2e-16 ***
## season
                19.63438
                            1.08840
                                     18.040
                                              < 2e-16 ***
                                     47.060
                 5.27017
                            0.11199
                                             < 2e-16 ***
## temp
                            0.06339 -35.162
## hum
                -2.22902
                                              < 2e-16 ***
                                              < 2e-16 ***
## hr
                 7.47914
                            0.17018
                                     43.947
## holiday
               -21.62282
                            6.95442
                                     -3.109
                                             0.00188 **
## weekday
                 1.57787
                            0.56159
                                      2.810
                                             0.00496 **
## workingday
                 3.49010
                            2.48953
                                      1.402 0.16096
## windspeed
                 0.23108
                            0.14396
                                      1.605
                                             0.10848
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 147.6 on 17370 degrees of freedom
## Multiple R-squared: 0.3384, Adjusted R-squared: 0.3381
## F-statistic: 1110 on 8 and 17370 DF, p-value: < 2.2e-16
```

We get less Adjusted R-squared which is 0.3381. Attributes "workingday" and "windspeed" have shown to be not significant as P-value <0.05. We will continue use bike2012.model to train and test the model.

Interpret bike2012.model

```
coef(bike2012.model)
## (Intercept)
                     season
                                   temp
                                                 hum
                                                               hr
                                                                      holiday
## 143.8417033
                21.7920637
                              5.9476594
                                          -2.5172664
                                                       9.2175063 -23.7160157
##
       weekday
                workingday
                              windspeed
     3.2183018
                10.0244554
                              0.5841525
```

Explaine the model manually —If every attribute are "zero", the intercept is 143.842. —add one if it is in winter, (times 2 if it is in spring, times 3 if it in autumns). — add 5.948 if temp increase one Celsius; — minus 2.217 if humidity increase 1/100 measurement; — add 9.218 or minus 9.218 base on the time period and if it is on

workingday or not. for example if it is on Tuesday 8am, then add 8*9.218, which is 73.744; — minus 23.716 if it is on holiday(people might drive more in holidays); — add one unit of 3.218 from Monday to Friday then reduce to Monday; —add 10.024 if it is workingday (minus 10.024 if it is none working day); —The values of windspeed have been divided by 67 in the raw dataset. add 0.5841 if wind speed increase 1/100 k/h degree, or minus 0.5841 if it is reduced 1/100 k/h.

Base on the data visualization, we adjust the number accordinly.

Model prediction

Because this dataset is base on datetime. It is not necessary to train the model. We just use the coefficient result to predict the future numbers of bike rented.

Let's say on April 12 2020, the Weather of Washington USA forecast for the time of 23pm: temp is 19C, Cloudy,hum 66%, wind speed is 27 k/h, Sunday. (We have not yet consider the growth rate of the number of bike rental from 2012 to 2019)

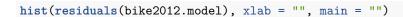
```
We can estimate that the number of bike will be rent are:
```

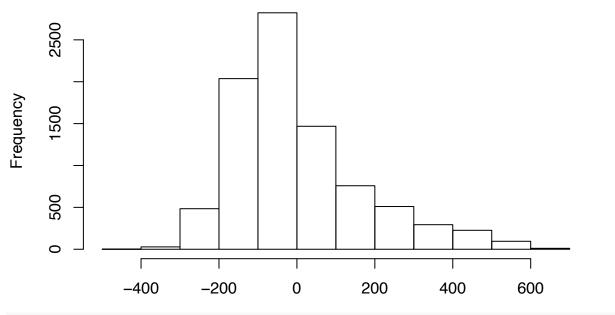
```
143.84 + 21.7922 + 5.94819 - 2.51766 + (109.217 - 890217) - 23.716 + (3.2184 - 3.2182) - 10.024 + (0.58427) = 141.212 ### The median of the residuals is -30.46 Estimate numbers will be 110.752.
```

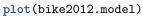
```
143.84 + (21.792*2) + (5.948*19) -( 2.517*66) + (10*9.217- 8*9.217) - 23.716 + (3.218*4 - 3.218*2) -10.
caculate manually:
## [1] 141.212
141.212 - 30.46
## [1] 110.752
Evaluate the Model
library(MASS)
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
fit <- lm(cnt ~ season + temp + hum + hr + holiday + weekday + workingday + windspeed, data= bike2012_
step <- stepAIC(fit, direction = "both", trace = FALSE)</pre>
step$anova
## Stepwise Model Path
## Analysis of Deviance Table
## Initial Model:
## cnt ~ season + temp + hum + hr + holiday + weekday + workingday +
##
       windspeed
##
## Final Model:
## cnt ~ season + temp + hum + hr + holiday + weekday + workingday +
##
       windspeed
##
##
##
    Step Df Deviance Resid. Df Resid. Dev
```

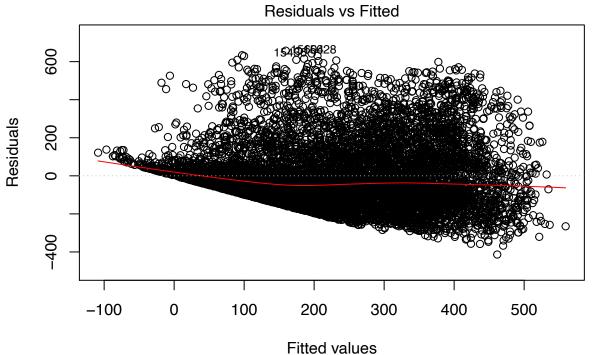
8725 247233352 89549.05

1

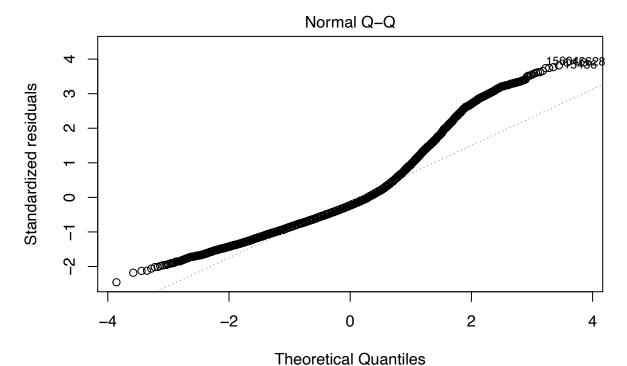




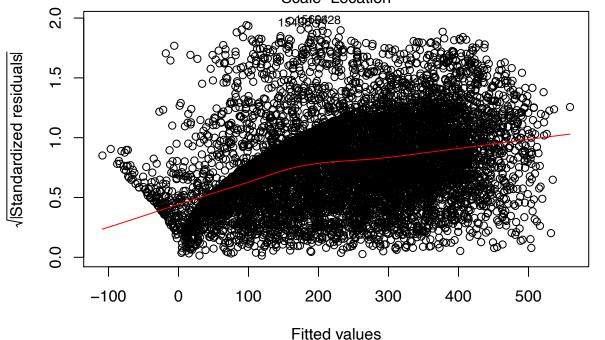




Im(cnt ~ season + temp + hum + hr + holiday + weekday + workingday + windsp ...

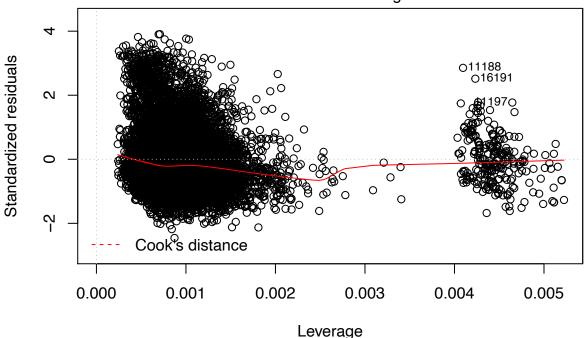


Im(cnt ~ season + temp + hum + hr + holiday + weekday + workingday + windsp ... Scale-Location



Im(cnt ~ season + temp + hum + hr + holiday + weekday + workingday + windsp ...

Residuals vs Leverage



Im(cnt ~ season + temp + hum + hr + holiday + weekday + workingday + windsp ...

Let's see if we use the train/test/split model to check any diffirent

```
set.seed(99)
sample<- sample.split(bike2012_sub$cnt, SplitRatio = 0.7)</pre>
train<- subset(bike2012_sub, sample==TRUE)</pre>
test <- subset(bike2012_sub,sample== FALSE)</pre>
biketrain.model <- lm(cnt ~ season + temp + hum + hr + holiday + weekday + workingday + windspeed, dat
summary(biketrain.model)
##
## Call:
  lm(formula = cnt ~ season + temp + hum + hr + holiday + weekday +
##
       workingday + windspeed, data = train)
##
##
## Residuals:
##
       Min
                10 Median
                                 3Q
                                        Max
  -416.38 -114.57
                    -38.85
                              72.01
                                     658.29
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                            12.8920 11.745
                                            < 2e-16 ***
## (Intercept) 151.4166
## season
                20.7392
                             2.0775
                                      9.983 < 2e-16 ***
                             0.2227 27.152 < 2e-16 ***
## temp
                 6.0457
```

```
## hum
                -2.5475
                           0.1270 -20.057 < 2e-16 ***
## hr
                9.1360
                           0.3343
                                   27.328 < 2e-16 ***
## holiday
               -20.2911
                          12.9535
                                   -1.566 0.117294
                                    3.512 0.000448 ***
## weekday
                3.8218
                           1.0882
## workingday
               11.5705
                           4.8133
                                    2.404 0.016253 *
## windspeed
                           0.2834
                                    0.675 0.499587
                0.1913
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 169.7 on 6113 degrees of freedom
## Multiple R-squared: 0.3494, Adjusted R-squared: 0.3485
## F-statistic: 410.3 on 8 and 6113 DF, p-value: < 2.2e-16
```

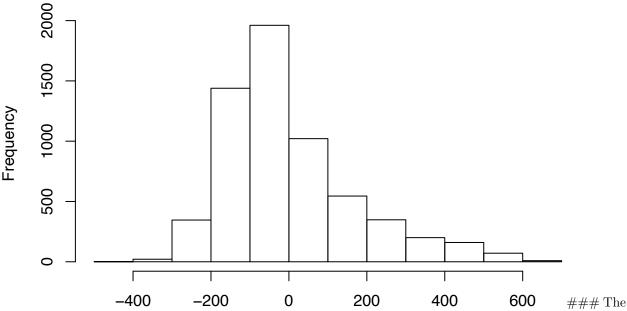
Adjustered R_squared is 0.3485. in this train model "holiday" and "windspeed" have no significant as p < 0.05.

```
res <- residuals(biketrain.model)
```

head(as.data.frame(res))

```
## res
## 8646 30.559900
## 8647 64.702289
## 8648 78.184470
## 8650 17.922822
## 8651 5.595775
## 8652 30.358775
```

hist(residuals(biketrain.model), xlab = "", main = "")



residuals has the same as bike2012 sub.model, aslo shows normally distributaion.

Predition future bike counts by the bike.copy2012 model.

```
cnt.pred <- predict(biketrain.model,test)</pre>
results <- cbind(cnt.pred,test$cnt)
colnames(results) <- c("predicted", "actual")</pre>
results <- as.data.frame(results)</pre>
head(results)
##
         predicted actual
## 8649 -13.496755
## 8653 -18.839447
                        7
                        14
## 8654
         4.816501
## 8656 51.795132
                       70
## 8660 206.644692
                       267
## 8662 224.916784
                       215
```

```
to_zero <- function(x){
  if (x<0){
    return(0)
  }else{
    return(x)
  }
}</pre>
```

```
results$predicted <- sapply(results$predicted,to_zero)
head(results)</pre>
```

It is no sense if there is -13 or any minus zoro number of bike rented. Adjuste munus number to zero.

```
## predicted actual
## 8649 0.000000 52
## 8653 0.000000 7
## 8654 4.816501 14
## 8656 51.795132 70
## 8660 206.644692 267
## 8662 224.916784 215
```

Basily the model is not that bad so far. However we will see if other kind of model will have a better results.