Macro ML

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Introduction

In financial econometrics, numerous approaches have been developed to explain the returns of assets. It is often assumed that the excess returns are related to a given set of factors. The exposition of an asset to a factor must be compensated by a "risk premium". Therefore, the excess return of an asset depends on those risk premia multiplied by the exposition of the asset to each of the factors.

A key issue of financial factor models resides in the choice of the factors. Various models have been developed, using different sets of factors. For instance, the Fama-French three-factor model is based on market excess return, outperformance of small versus big companies and outperformance of high book-to-market versus low book-to-market companies.

Our article investigates how macro factors can be used in asset pricing models. As already shown in the literature, some macroeconomic variables (such as GDP growth, inflation, unemployment or housing prices) could generate risk premia. Nonetheless, the difficulty lies in the identification of the relevant macroeconomic variables among a very large set of macroeconomic indicators. Some previous papers have arbitrarily chosen one or two macroeconomic variables. Our article innovates by using machine learning techniques so as to construct a few factors out of a large set of macroeconomic variables. The central ML technique used here is **sparse Principal Component Analysis** (PCA). As we will see below, the main advantage of sparse PCA over PCA lies in the interpretability of the factors.

Once the principal components are extracted, we use them as factors in asset pricing models. The goal is to determine whether those factors are relevant and whether they generate significant risk premia. The estimation of the of the risk premia uses the **three-pass methodology** developed by Giglio and Xiu. Their methodology is designed to compute unbiased risk premia estimates under omission of relevant risk factors and measurement error. The concern about factor omission is indeed well founded. If we assume that the asset excess returns are only determined by the macro factors derived from the PCA, we might omit other relevant factors. The three-pass methodology solves this problem.

[reste de l'intro]

PCA and Sparse PCA

Our article performs a sparse PCA on a set of 120 macroeconomic variables from the FRED-MD database. Those variables cover various categories: output and income, labor market, housing, consumption, money and credit, interest and exchanges rates, and prices. Here are some examples of macroeconomic variables: real personal income, industrial production indices, civilian unemployment, number of employees by sector, number of housing permits, M1 money stock, commercial and industrial loans, fed fund rates, consumer price indices.

Before performing the sparse PCA, we need some treatment on the FRED-MD data. We use a csv file on which we reported metadata on the FRED-MD macroeconomic variables, in particular: whether they should be included in the analysis and what transformation should be performed on them (log, log growth, difference). These indications come from *Table 1* of the article. After selecting the relevant variables and performing the transformations, we restrict the dataset to the time period considered (1960:01 to 2019:12)

```
library(dplyr)
file <- "data/2020-11.csv"
data0 <- read.csv(file = file)</pre>
x <- data0$sasdate
# we drop the rows which have no date
data1 <- data0[(x!="Transform:" & nchar(x)>2),]
y<-data1[,1]</pre>
# extraction of variable names
varnames <- data.frame("FRED_ticker"=colnames(data1)[-1])</pre>
write.csv(varnames, "varnames.csv", row.names = F)
##### Keeping only relevant time series
# Importation of csv file with variables metadata
df <- read.csv("data/variables.csv",sep=";")</pre>
df <- filter(df,Inclusion==1)</pre>
var <- df$FRED_ticker</pre>
#on garde la date
var <- c("sasdate", var)</pre>
data <- data1[var]</pre>
### Transformation of the time series
var names <- colnames(data)</pre>
for(i in 2:length(var_names)){ # exclusion of 1st column (date)
  variable <- var_names[[i]]</pre>
  transfo <- df$Transformation[df$FRED_ticker==variable]</pre>
  if(!is.null(transfo)){
    if(transfo=="Log"){
      data[,i]<-log(data[,i])</pre>
    }
    if(transfo=="Difference"){
      data[,i] <-c(NA, diff(data[,i])) # length is decreased by 1 when we take the difference
    if(transfo=="Log growth"){
      tmp <- data[,i]</pre>
      tmp <- tmp/lag(tmp)</pre>
      tmp<-log(tmp)</pre>
      data[,i]<-c(tmp) # length is decreased by 1 when we take the difference
    }
  }
## Warning in log(tmp): Production de NaN
## Time interval
data$sasdate<-as.Date(data$sasdate, format = "%m/%d/%Y") # conversion to date
data <- filter(data, sasdate>="1960-02-01" & sasdate<"2020-01-01")
```

```
### Saving to RDS
saveRDS(data, "data/FRED_data.rds")
```

PCA

We first perform of traditional PCA on the 120 variables, and select 9 components. We use the same package as the authors

```
library(FactoMineR)
library(knitr)

data <- readRDS("data/FRED_data.rds")
data0 <- dplyr::select(data, -1) # we drop the date column
sum(is.na(data0))

## [1] 2
pca <- PCA(data0, ncp=9, graph=F)

## Warning in PCA(data0, ncp = 9, graph = F): Missing values are imputed by the
## mean of the variable: you should use the imputePCA function of the missMDA
## package
table1 <- pca$eig

kable(table1[1:9,], caption = "First 9 components of the PCA")</pre>
```

Table 1: First 9 components of the PCA

	eigenvalue	percentage of variance	cumulative percentage of variance
comp 1	20.741160	17.284300	17.28430
comp 2	17.368041	14.473368	31.75767
comp 3	7.985066	6.654221	38.41189
comp 4	6.449405	5.374504	43.78639
comp 5	4.896562	4.080468	47.86686
comp 6	3.668845	3.057370	50.92423
comp 7	3.122703	2.602253	53.52648
comp 8	2.785973	2.321644	55.84813
comp 9	2.704916	2.254097	58.10222

The first nine conventional PCs collectively explain 58.1022246% of the total variation in the macroeconomic variables.

The outcome of our PCA is somewhat different from the results presented in the article. Indeed, the weights of the components are different. This can be explained by modifications of the FRED-MD data between the redaction of the paper on our replication. We noticed that some variables do not have exactly the same name in our version of the FRED data and in the original article. Despite these differences, we are reassured by the fact that in the original article, the first nine PCs collectively explain 57% of the total variation.

We plot the principal components that we extracted from the 120 FRED-MD macroeconomic variables, as the authors do in **Figure 1** of their article.

```
pca_ts <- ts(data=pca$ind$coord, start = c(1960,1), frequency=12)
par(mfrow = c(3, 3), mar = c(5.1, 4.1, 4.1, 2.1))
for(i in 1:9){
   plot(pca_ts[,i],</pre>
```

```
main = paste0("PC",i),
    ylab="")
}
```

Sparse PCA

We now perform a sparse PCA, using the same R package as the authors. Before running the SPC function, we scale the variables (so that they have a unit variance). In the article, the authors set the shrinkage parameter so that only 108 weights are active. The set the parameter sumabsv to 3 to get a similar outcome.

Table 2: First 9 components of the SPCA

Component	Cumulative_percentage_of_variance
comp 1	0.0708785
comp 2	0.1325496
comp 3	0.1970411
comp 4	0.2583984
comp 5	0.3148364
comp 6	0.3680362
comp 7	0.4042698
comp 8	0.4335150
comp 9	0.4640008

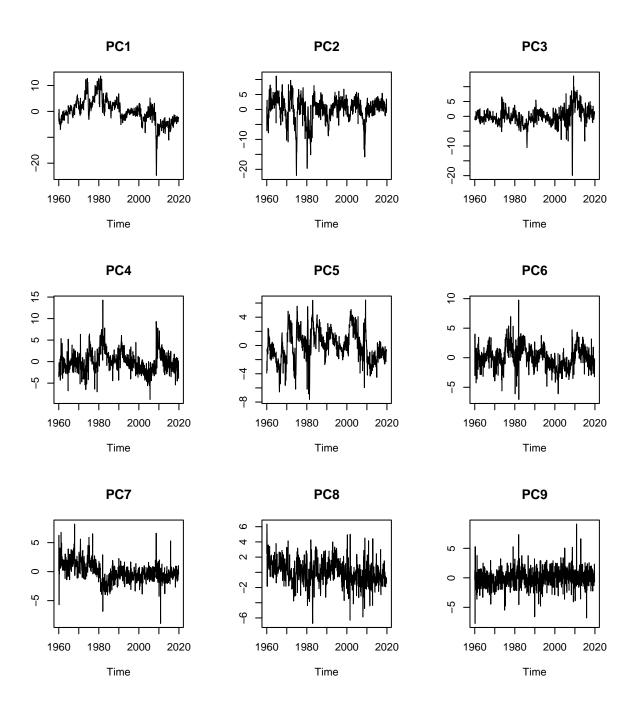


Figure 1: Conventional principal components

Sparse_ComponentenActiveneweights

```
S.P.div.yield; FEDFUNDS; CP3Mx; TB3MS; TB6MS; GS1; GS5; GS10; AAA;
  ProductionINDPRO; IPFPNSS; IPFINAL; IPCONGD; IPDCONGD; IPBUSEQ; IPMAT;
          IPDMAT; IPMANSICS; CUMFNS; MANEMP; DMANEMP
3
         WPSFD49207: WPSFD49502: WPSID61: CPIAUCSL: CPITRNSL: CUSR0000SAC
          ; CPIULFSL; CUSR0000SA0L2; CUSR0000SA0L5; PCEPI; DNDGRG3M086SBEA
  Housing
         HOUST; HOUSTNE; HOUSTMW; HOUSTS; HOUSTW; PERMIT; PERMITNE;
          PERMITMW; PERMITS; PERMITW; REALLN
         COMPAPFFx; TB3SMFFM; TB6SMFFM; T1YFFM; T5YFFM; T10YFFM;
  Spreads
          AAAFFM; BAAFFM; CPIMEDSL; CUSR0000SAS; DSERRG3M086SBEA
  EmploymeRAYEMS; USGOOD; USCONS; MANEMP; DMANEMP; NDMANEMP;
          SRVPRD; USTPU; USWTRADE; USTRADE; USFIRE
  Costs
          USFIRE; BUSINVx; M2REAL; S.P.div.yield; CPIAPPSL; CPIMEDSL;
7
          CUSR0000SAD; CUSR0000SAS; DDURRG3M086SBEA; DSERRG3M086SBEA;
          CES0600000008; CES2000000008; CES3000000008
  Money
          BUSINVx: M1SL: M2SL: M2REAL: BOGMBASE: TOTRESNS: WPSFD49207:
          WPSFD49502; WPSID61; WPSID62; OILPRICEx; PPICMM; MZMSL
          DPCERA3M086SBEA; CMRMTSPLx; RETAILx; IPNCONGD; IPNMAT;
  SPC9
          HWIURATIO; CE16OV; UNRATE; CLAIMSx; USCONS; CES0600000007;
          AWOTMAN; AWHMAN; AMDMNOx; ISRATIOx
```

The result of our sparse PCA is quite satisfactory, insofar as they are very similar to those represented in the article. As in the article, the nine components of the PCA explain 46% of the total variation in the 120 macroeconomic variables. By looking at the active weights of each component, we see that they do not exactly match those presented in *Table 3* of the article. We can nevertheless give them the same interpretation as in the article, except for the ninth component. The active weights of the ninth component diverge too much from those of the original article. In our results, it is difficult to interpret this component as an index for credit; we therefore keep the name "SPC 9".

```
spca_ts <- ts(data=spca$u, start = c(1960,1), frequency=12)
par(mfrow = c(3, 3), mar = c(5.1, 4.1, 4.1, 2.1))
for(i in 1:9){
    plot(spca_ts[,i],
        main = component_names[i],
        ylab="")
}</pre>
```

Even though our sparse components have similar interpretations as those derived by the authors, our plots are very different from those presented in **Figure 2** of the article

Innovations to the PCs

The set of macro factors is composed of the innovations to the principal components which have been extracted by the PCA. The innovations are computed by running a first-order vector autoregression (VAR(1)) on the principal components. For both the conventional and sparse PCAs, we run a VAR(1) on the PCs, we compute the residuals (which correspond to the innovations) and we then compute the correlations between those residuals.

Conventional PCA

We begin with the conventional PCA. pca\$ind\$coord contains the coordinates of each of the 120 macroeconomic variables in the space of the 9 PCs. We use the package vars to run the VAR(1).

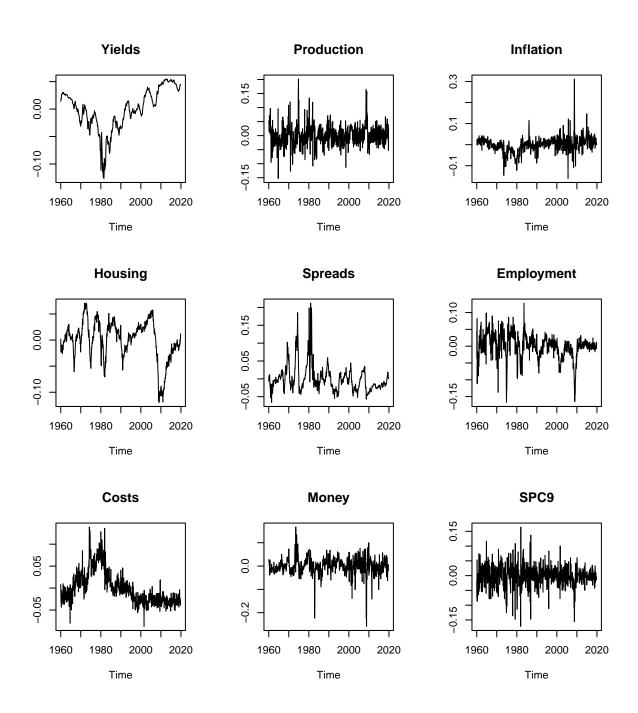


Figure 2: Sparse principal components

library(vars) ## Warning: le package 'vars' a été compilé avec la version R 4.2.2 ## Warning: le package 'strucchange' a été compilé avec la version R 4.2.2 data_pca <- pca\$ind\$coord row.names(data_pca) <- data\$date ar_pca <- VAR(data_pca, p=1) correlations_pca <- round(cor(residuals(ar_pca)),2) kable(correlations_pca, caption = "Innovation correlations to conventional PCs")</pre>

Table 4: Innovation correlations to conventional PCs

	Dim.1	Dim.2	Dim.3	Dim.4	Dim.5	Dim.6	Dim.7	Dim.8	Dim.9
Dim.1	1.00	0.39	0.79	0.07	0.14	-0.03	-0.07	-0.02	-0.05
Dim.2	0.39	1.00	0.09	0.70	-0.11	-0.18	-0.23	-0.12	-0.12
Dim.3	0.79	0.09	1.00	-0.15	0.45	-0.06	-0.03	0.01	0.04
Dim.4	0.07	0.70	-0.15	1.00	-0.09	-0.52	0.16	-0.11	0.03
Dim.5	0.14	-0.11	0.45	-0.09	1.00	-0.13	0.07	-0.05	-0.09
Dim.6	-0.03	-0.18	-0.06	-0.52	-0.13	1.00	-0.04	-0.21	-0.02
Dim.7	-0.07	-0.23	-0.03	0.16	0.07	-0.04	1.00	-0.19	0.09
Dim.8	-0.02	-0.12	0.01	-0.11	-0.05	-0.21	-0.19	1.00	0.05
Dim.9	-0.05	-0.12	0.04	0.03	-0.09	-0.02	0.09	0.05	1.00

The results of this correlation matrix are very close to the one displayed in **Table 4** of the original article.

Sparse PCA

We follow the same method with the sparse PCA. Here, the coordinates of each of the 120 macroeconomic variables in the space of the 9 sparse PCs are stored in spca\$u.

```
data_spca <- spca$u
row.names(data_spca) <- data$date
colnames(data_spca) <- component_names
ar_spca <- VAR(data_spca, p=1)
correlations_spca <- round(cor(residuals(ar_spca)),2)
kable(correlations_spca, caption = "Innovation correlations to sparse PCs")</pre>
```

Table 5: Innovation correlations to sparse PCs

	Yields	Production	Inflation	Housing	Spreads	Employment	Costs	Money	SPC9
Yields	1.00	0.14	0.12	0.08	-0.11	-0.10	-0.08	-0.20	-0.10
Production	0.14	1.00	0.03	-0.17	-0.03	-0.49	-0.10	-0.02	-0.58
Inflation	0.12	0.03	1.00	-0.07	-0.04	-0.09	-0.24	-0.58	-0.13
Housing	0.08	-0.17	-0.07	1.00	-0.04	0.19	0.00	-0.05	0.38
Spreads	-0.11	-0.03	-0.04	-0.04	1.00	0.04	-0.01	0.11	0.01
Employment	-0.10	-0.49	-0.09	0.19	0.04	1.00	0.08	0.07	0.42
Costs	-0.08	-0.10	-0.24	0.00	-0.01	0.08	1.00	0.07	0.00
Money	-0.20	-0.02	-0.58	-0.05	0.11	0.07	0.07	1.00	0.08
SPC9	-0.10	-0.58	-0.13	0.38	0.01	0.42	0.00	0.08	1.00

Once again, our results look quite similar to those of the original article, except for the ninth sparse PC.

However, for some correlations, the reported sign is the opposite of the one indicated in the original article.

Risk premia estimates

We now turn to the estimation of the risk premia of the sparse macro factors. The objective is to determine whether some of the macro factors generate some significant risk premia.

We import the data on portfolio returns and keep the same time period as the authors (1963:07 to 2019:12).

```
R <- readRDS("data/portfolios.rds")
R <- filter(R, date<='2019-12-01')
dates <- R$date
R<-dplyr::select(R,-1)</pre>
```

We need to compute the excess returns of each portfolios. This requires data on the risk-free rate at every period in time. The authors use the CRSP risk-free return. However, as these data are not freely available, we replace the risk-free rate by TB3MS variable from FREDMD (3-Month Treasury Bill Secondary Market Rate, Discount Basis).

```
data_rf <- read.csv(file = "data/TB3MS.csv")
data_rf <- dplyr::select(data_rf, -1) # we remove the date
for (i in 1:ncol(R)){
   R[,i] <- as.numeric(R[,i]) - data_rf[,1]
}</pre>
```

We demean the excess returns of each portfolio

1Q Median

##

Min

```
R_d <- R-t(as.matrix(colMeans(R))) # the result is != 0 due to approx errors
```

We run a PCA of the excess returns of our portfolios, to estimated the rotated fundamental factors (denoted ksi)

```
t <- nrow(R_d)
n \leftarrow ncol(R_d)
R_d <- t(as.matrix(R_d))</pre>
mat \leftarrow (t(R_d) %*% R_d)/(t*n)
r_pca <- PCA(mat, ncp=15,graph = F)</pre>
ksi <- t(r_pca$var$coord) #eigenvectors</pre>
V <- sqrt(t)*t(r pca$var$coord)</pre>
# estimator of beta (exposure to factors)
beta \leftarrow (1/t)*R_d%*\%t(V)
r_mean <- colMeans(R) #average return</pre>
gamma <- solve(t(beta)%*%beta) %*% t(beta) %*% as.matrix(r_mean) #0LS
# alternative : with OLS
lm1 \leftarrow lm(r_mean \sim -1 + beta)
summary(lm1)
##
## Call:
## lm(formula = r_mean \sim -1 + beta)
##
## Residuals:
```

Max

3Q

```
## -0.62699 -0.07578 0.00926 0.08367 0.36106
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## betaDim.1 -0.0285316 0.0001884 -151.410 < 2e-16 ***
## betaDim.2 -0.1425057 0.0029320 -48.604 < 2e-16 ***
## betaDim.3 -0.2647945 0.0115596 -22.907 < 2e-16 ***
## betaDim.4 0.0522575 0.0230164
                                      2.270 0.02382 *
## betaDim.5
             0.4417834 0.0281623 15.687 < 2e-16 ***
## betaDim.6 -0.2261978 0.0369536 -6.121 2.64e-09 ***
## betaDim.7 0.5512277 0.0657879 8.379 1.56e-15 ***
## betaDim.8 -1.0062995 0.0770880 -13.054 < 2e-16 ***
## betaDim.9
              0.0949227 0.0760880 1.248 0.21308
## betaDim.10 0.9460650 0.1055167 8.966 < 2e-16 ***
## betaDim.11 1.7915206 0.1258126 14.240 < 2e-16 ***
## betaDim.12 0.1629277 0.1537956
                                     1.059 0.29020
## betaDim.13 0.9970662 0.2213628
                                      4.504 9.26e-06 ***
## betaDim.14 0.6403207 0.2170883
                                      2.950 0.00341 **
## betaDim.15 -0.3667756 0.2448742 -1.498 0.13514
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1397 on 330 degrees of freedom
## Multiple R-squared: 0.9985, Adjusted R-squared: 0.9985
## F-statistic: 1.501e+04 on 15 and 330 DF, p-value: < 2.2e-16
\# R^2 proche de l'article avec intercept, mais erronné sans intercept (calcul du R^2 dans un modèle sans
The last step is to run a time-series regression of the observed factors on the rotated fundamental factors.
# we restrict the observed factors to the good time period
dates_pca <- data$sasdate</pre>
indices_dates <- dates_pca>="1963-07-01" & dates_pca<= "2019-12-01"
# residuals of the VAR(1)
res <- residuals(ar_pca)
G \leftarrow res[indices_dates[-1],] # we drop the first element of res (ar(1) has one obs less)
G \leftarrow t(G)
eta <- G %*% t(V) %*% solve(V %*% t(V))
gamma_g <- eta %*% gamma
df_pca <- data.frame(Factor = paste0("PC ", 1:9),</pre>
                    gamma_g=gamma_g)
```

Table 6: Estimators of the risk premia for the conventional PCA

kable(df_pca, caption = "Estimators of the risk premia for the conventional PCA")

	Factor	gamma_g
Dim.1	PC 1	-0.2045160
Dim.2	PC 2	-1.6692103
Dim.3	PC 3	0.2112325
Dim.4	PC 4	-1.1171945
Dim.5	PC 5	0.2812944

	Factor	gamma_g
Dim.6	PC 6	-0.0945888
Dim.7	PC7	-0.1963948
Dim.8	PC 8	0.4166464
Dim.9	PC9	0.1918584

```
# with tslm
library(forecast)
## Registered S3 method overwritten by 'quantmod':
##
     method
##
     as.zoo.data.frame zoo
G_ts <- ts(t(G))</pre>
ksi_ts <- ts(t(ksi))</pre>
lm3 <- tslm(G_ts~0+ksi_ts)</pre>
###### same for sparse PCA :
# residuals of the VAR(1)
res_spca <- residuals(ar_spca)</pre>
G_{spca} \leftarrow res_{spca}[indices_{dates}[-1],] # we drop the first element of res (ar(1) has one obs less)
G_spca <- t(G_spca)</pre>
eta_spca <- G_spca %*% t(V) %*% solve(V %*% t(V))
gamma_g_spca <- eta_spca %*% gamma
df_spca <- data.frame(Factor = component_names,</pre>
                       gamma_g=gamma_g_spca)
kable(df_spca, caption = "Estimators of the risk premia for the sparse PCA")
```

Table 7: Estimators of the risk premia for the sparse PCA

	Factor	gamma_g
Yields	Yields	0.0005209
Production	Production	0.0196118
Inflation	Inflation	-0.0048955
Housing	Housing	-0.0002049
Spreads	Spreads	0.0000608
Employment	Employment	-0.0177524
Costs	Costs	-0.0033390
Money	Money	0.0096273
SPC9	SPC9	-0.0093634

Biases without the three-pass methodology

What happens if we do not use the 3-pass methodology?

The authors have used the three-pass methodology due to concerns about potential omitted factors bias. We now go beyond the scope of the original article as we study whether there is evidence of such biases. To achieve this, we estimate the risk premia with a simple two-pass methodology, and then compare our results

to the outcome of the three-pass methodology.

Let us therefore assume that the true model for asset returns only depends on our macro factors. If this assumption is true, then we can derive unbiased estimates of the risk premia with a two-pass methodology. This methodology consists in two steps:

- 1. Time series regression of the demeaned asset excess returns on the innovations to the macro factors, to estimate the risk exposures of each asset (β)
- 2. Cross-sectional regression of the average returns of each asset on the asset' risk exposures

We run this estimation on the macro factors obtained with the conventional PCA, and then on the sparse macro factors.

```
R_1 <- t(R)
R_d_1 <- ts(t(R_d))
v_t <- ts(residuals(ar_pca)[indices_dates[-1],])

lm_pca <- tslm(R_d_1~0+v_t)
beta <- t(lm_pca$coefficients)

R_bar <- rowMeans(R_1)
lm_pca_2 <- lm(R_bar~0+beta)
summary(lm_pca_2)</pre>
```

Conventional PCA

```
##
## Call:
## lm(formula = R_bar ~ 0 + beta)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                            Max
                                    30
## -1.06088 -0.22810 -0.02091 0.19834
                                        1.21557
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## betav tDim.1
                  1.9593
                             0.2986
                                      6.561 2.02e-10 ***
                -0.7331
                                    -1.227 0.22062
## betav_tDim.2
                             0.5974
## betav_tDim.3
                  1.5329
                             0.3640
                                     4.211 3.26e-05 ***
## betav_tDim.4
                  1.7318
                             0.3731
                                      4.642 4.96e-06 ***
## betav_tDim.5
                  0.6746
                             0.2334
                                      2.890 0.00411 **
## betav_tDim.6
                -1.9331
                             0.3376
                                    -5.726 2.28e-08 ***
## betav_tDim.7
                 -0.8734
                             0.3330
                                     -2.623 0.00911 **
## betav_tDim.8
                  3.5981
                             0.2857
                                     12.596
                                             < 2e-16 ***
## betav_tDim.9
                  0.5887
                             0.2660
                                      2.213 0.02754 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3537 on 336 degrees of freedom
## Multiple R-squared: 0.9905, Adjusted R-squared: 0.9902
## F-statistic: 3872 on 9 and 336 DF, p-value: < 2.2e-16
R_2 \leftarrow t(R)
```

```
R_d_2 <- ts(t(R_d))
v_t_2 <- ts(residuals(ar_spca)[indices_dates[-1],])

lm_spca <- tslm(R_d_2~0+v_t_2)
beta_s <- t(lm_spca$coefficients)

R_bar <- rowMeans(R_2)
lm_spca_2 <- lm(R_bar~0+beta_s)
summary(lm_spca_2)</pre>
```

Sparse PCA

```
##
## Call:
## lm(formula = R_bar ~ 0 + beta_s)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -1.20054 -0.35413 0.05817 0.26402 1.15724
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
                        -0.0100697  0.0003732  -26.980  < 2e-16 ***
## beta_sv_t_2Yields
## beta_sv_t_2Production -0.0025171 0.0093614 -0.269
                                                        0.7882
## beta_sv_t_2Inflation -0.0026200 0.0059398
                                              -0.441
                                                        0.6594
## beta_sv_t_2Housing
                                   0.0019788
                                               -4.695 3.9e-06 ***
                        -0.0092895
                        -0.0045086 0.0051300 -0.879
## beta_sv_t_2Spreads
                                                        0.3801
## beta_sv_t_2Employment -0.0089420 0.0091957
                                               -0.972
                                                        0.3315
## beta_sv_t_2Costs
                        -0.0016906
                                   0.0053166
                                               -0.318
                                                        0.7507
## beta_sv_t_2Money
                        -0.0086009
                                   0.0067837
                                               -1.268
                                                        0.2057
## beta_sv_t_2SPC9
                         0.0141709 0.0081045
                                               1.749
                                                        0.0813 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.4432 on 336 degrees of freedom
## Multiple R-squared: 0.985, Adjusted R-squared: 0.9846
## F-statistic: 2453 on 9 and 336 DF, p-value: < 2.2e-16
```

Even though those estimates are biased, we find that the sparse components 1 and 4 (yield and housing) generate significant risk premia. This result is consistent with the result of the original article.