$T: \mathbb{R}^n \to \mathbb{R}^m$: linear transformation

<u>Def1</u> if (0 T (ũ) + T (ῦ) = T (ũ + ῦ) ∀ ũ, ũ ∈ IRⁿ
(② rT (ũ) = T (rũ) ∀ re IR

$$T:\mathbb{R}^n\to\mathbb{R}^m:$$
 linear transformation, Given $\mathcal{B}=\{\vec{b}_1,\vec{b}_2,...,\vec{b}_n\}$: basis for \mathbb{R}^n

Dof. $T: \mathbb{R}^n \to \mathbb{R}^m$: linear transformation, A is the s.m.r. of T if Yvelp", T(v): Av Moreover, A = T(ë,) T(ë,) -... T(ë,)

$$= \begin{bmatrix} (e_i) & (e_i) & \cdots & (e_n) \\ \vdots & \vdots & \ddots & \vdots \\ v_n \end{bmatrix}$$

$$= \begin{bmatrix} T(\vec{e}_i) & T(\vec{e}_i) & \cdots & T(\vec{e}_n) \end{bmatrix} \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix}$$

$$= \begin{bmatrix} T(\vec{e}_i) & T(\vec{e}_i) & \cdots & T(\vec{e}_n) \\ \vdots & \ddots & \ddots \\ \end{bmatrix} \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix}$$

$$\int_{a} \{\tilde{x} \in \mathbb{R}^{n} \mid T(\tilde{x}) = \tilde{o}\}$$
Def. kernel of $T = \text{null space}$ of A

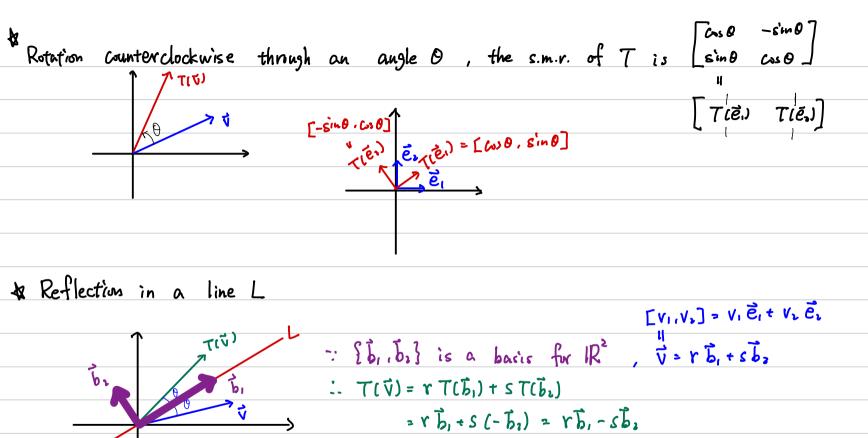
in \mathbb{R}^2 , s.m.r. is $\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} x \\ 0 \end{bmatrix}$ i.e. projection on x-axis

S.m.r. is $\begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$ $\Rightarrow \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ y \end{bmatrix}$ i.e. projection on y-axis

Def.
$$T: \mathbb{R}^n \to \mathbb{R}^n$$
: invertible linear transformation



2-4



e.g.
$$\left[\begin{array}{c|c} y_{2} & 2X \\ \end{array}\right] \Rightarrow \left[\begin{array}{c|c} \overline{b}_{1} & \overline{c}_{1} \\ \end{array}\right] \Rightarrow \left[\begin{array}{c|c} \overline{b}_{1} & \overline{c}_{1} \\ \end{array}\right] \Rightarrow \left[\begin{array}{c|c} \overline{c}_{1} & \overline{c}_{2} \\ \end{array}\right] \Rightarrow \left[\begin{array}{c|c} \overline{c}$$

2-4.CK2

$$= \begin{bmatrix} -\frac{1}{1} \\ \frac{1}{1} \end{bmatrix}$$

$$= \begin{bmatrix} \frac{1}{1} \\ \frac{1}{1} \end{bmatrix}$$

$$= \begin{bmatrix} \frac{1}{1} \\ \frac{1}{1} \end{bmatrix}$$

$$= \begin{bmatrix} \frac{1}{1} \\ \frac{1}{1} \end{bmatrix}$$

$$= \frac{1}{5} \left[\left(V_1 + 2 V_2 \right) \overline{b}_1 + \left(2 V_1 - V_2 \right) \overline{b}_2 \right]$$

$$= \frac{1}{5} \left[\left(V_1 + 2 V_2 \right) \left[\frac{1}{2} \right] + \left(2 V_1 - V_2 \right) \left[\frac{1}{2} \right] \right] = \left[\frac{-3 \left(5 - 4 \right) \left(5 - 4 \right)}{4 \left(5 - 3 \right) \left(5 - 4 \right)} \left[\frac{V_1}{V_2} \right]$$

* invertible linear transformation

Recall: every invertible matrix is a product of elementary matrices.

