$T: \mathbb{R}^n \to \mathbb{R}^m$ : linear transformation

<u>Def1</u> if (⊕ T(ü)+T(v)=T(ü+v) ∀ ü, v ∈ IR" (⊕ rT(ü)=T(rü) ∀ re IR

Deta if rT(u)+sT(v)=T(ru+sv) Vu, ver Yr.ser

 $T: \mathbb{R}^n \to \mathbb{R}^m : [\text{inear transformation}, Given <math>\mathcal{B} = \{\vec{b}_1, \vec{b}_2, ..., \vec{b}_n\} : \text{basis for } \mathbb{R}^n$ 

⇒ Y V ∈ IR", T(V) is uniquely determined by T(b,), T(b,)..., T(b,)

Def.  $T: \mathbb{R}^n \to \mathbb{R}^m$ : linear transformation, A is the s.m.r. of T

if Yver, T(v): Av

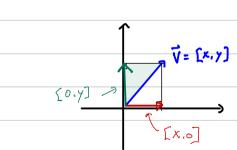
Moreover, A = T(ë,) T(ë,) -... T(ë,

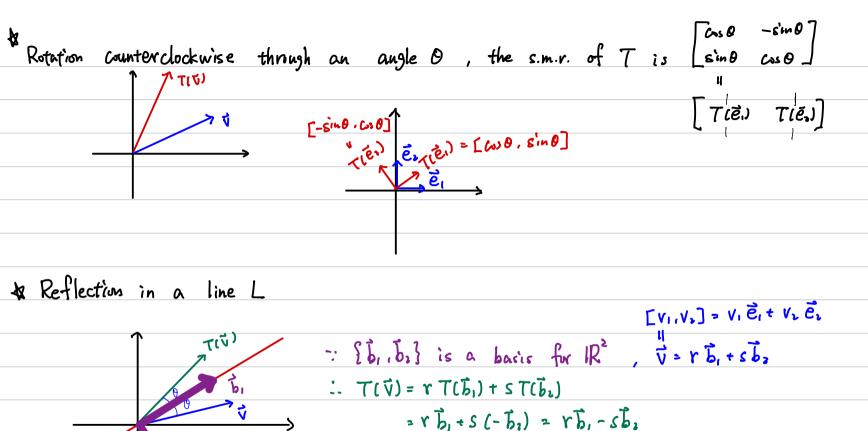
=> T[IR"] has basis {T(b,), T(b)}, ..., T(bn)}

Def. kernel of T = nullspace of A

Def.  $T: \mathbb{R}^n \to \mathbb{R}^m$ : invertible linear transformation if A is the s.m.r. of T and A is invertible

in 
$$\mathbb{R}^2$$
, s.m.r. is  $\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} 1$ 





e.g. 
$$\left[\begin{array}{c|c} y_{2} & 2X \\ \end{array}\right] \Rightarrow \left[\begin{array}{c|c} \overline{b}_{1} & \overline{c}_{1} \\ \end{array}\right] \Rightarrow \left[\begin{array}{c|c} \overline{b}_{1} & \overline{c}_{1} \\ \end{array}\right] \Rightarrow \left[\begin{array}{c|c} \overline{c}_{1} & \overline{c}_{2} \\ \end{array}\right] \Rightarrow \left[\begin{array}{c|c} \overline{c}$$

2-4.CK2

$$= \begin{bmatrix} -\frac{1}{1} \\ \frac{1}{1} \end{bmatrix}$$

$$= \begin{bmatrix} \frac{1}{1} \\ \frac{1}{1} \end{bmatrix}$$

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$$= \frac{1}{5} \left[ \left( V_1 + 2 V_2 \right) \overline{b}_1 + \left( 2 V_1 - V_2 \right) \overline{b}_2 \right]$$

$$= \frac{1}{5} \left[ \left( V_1 + 2 V_2 \right) \left[ \frac{1}{2} \right] + \left( 2 V_1 - V_2 \right) \left[ \frac{1}{2} \right] \right] = \left[ \frac{-3 \left( 5 - 4 \right) \left( 5 - 4 \right)}{4 \left( 5 - 3 \right) \left( 5 - 4 \right)} \left[ \frac{V_1}{V_2} \right]$$

\* invertible linear transformation

Recall: every invertible matrix is a product of elementary matrices.

