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葉均承 應數一線性代數

學號: \_\_\_\_\_

### Quiz 9

考試日期: 2020/06/04

不可使用手機、計算器，禁止作弊!  
背面還有題目

1. Find an unitary matrix  $U$  and a diagonal matrix  $D$  such that  $D = U^{-1}AU$ , where

$$A = \begin{bmatrix} 0 & i & 0 \\ -i & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

9.3 ✕ 5.

$$U = \frac{1}{\sqrt{2}} \begin{bmatrix} -\bar{\lambda} & 0 & \bar{\lambda} \\ 1 & 0 & 1 \\ 0 & \sqrt{2} & 0 \end{bmatrix}$$

$$D = \begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

2. Find  $A^{-1}$  if  $A = \begin{bmatrix} 1 & i \\ 1+i & 2+i \end{bmatrix}$

9.2 ✕ 5

$$\frac{1}{3} \begin{bmatrix} 2+\bar{\lambda} & -1 \\ -1-\bar{\lambda} & 1 \end{bmatrix}$$

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應數—線性代數

3. Using the Gram-Schmidt process to transform the basis  $\{[2+i, 1+i], [1+i, i]\}$  into an orthogonal basis.

~~9.2~~ ~~27~~

$$\{[2+\bar{i}, 1+\bar{i}], [1-\bar{i}, -2+\bar{i}]\}$$