

不可使用手機、計算器，禁止作弊!

1. Check if  $\{[2x, x + y, y] \mid x, y \in \mathbb{R}\}$  is a subspace of  $\mathbb{R}^2$ .

**Solution :**

No, since  $\{[2x, x + y, y] \mid x, y \in \mathbb{R}\}$  is not in  $\mathbb{R}^2$ .

2. Check if the line  $y = mx$  is a subspace of  $\mathbb{R}^2$ . (Hint: write the line as  $W = \{[x, mx] \mid x \in \mathbb{R}\}$ )

**Solution :**

Yes, check 1-6 problem 11.

3. Given  $A, B$  are two singular (i.e. not invertible) matrices. Prove or disprove (證明或反證) that if  $C = AB$ , then  $C$  is also a singular matrix.

**Solution :**

1-5, problem 23 (d).