

$$3-1/ \quad R_0 \xrightarrow{\text{uniquify}} R_0 \xrightarrow{\text{flatten}} C_0 \xrightarrow{\text{select}} X_0^* \xrightarrow{\text{assign}} X_0 \xrightarrow{\text{fix}} X_0$$

$$R_0.e = \text{int} \mid (\text{read}) \mid (-e) \mid (+ e e) \mid \text{var} \mid (\text{let } x \text{ var } e e)$$

$$p = (\text{program } e)$$

$$C_0.p = (\text{program } (\text{var}^*) \text{ stmt}^* \text{ arg}) = \langle \text{var}^*, \text{stmt}^*, \text{arg} \rangle$$

$$\text{stmt} = (:= \text{var } \text{exp})$$

$$\text{exp} = \text{arg} \mid (\text{read}) \mid (- \text{arg}) \mid (+ \text{arg } \text{arg})$$

$$\text{arg} = \text{int} \mid \text{var}$$

$$\text{flatten} : R_0.p \rightarrow C_0.p$$

$$\text{flatten}_e : R_0.e \rightarrow C_0.p$$

$$F(\text{int}) = \langle \emptyset, \_, \text{int} \rangle$$

$$F(-e) =$$

$$\cancel{\langle \{nv\}, nv := (-e), nv \rangle}$$

$$\text{let } \langle vs, ss, \text{earg} \rangle = F(e)$$

$$\langle nv \uparrow\uparrow vs, ss \uparrow\uparrow (:= nv (- \text{earg})), nv \rangle$$

$$F(-(-8)) = \langle \emptyset, \_, \text{8} \rangle$$

$$\langle nv, (:= nv (-8)), nv \rangle$$

$$\langle nv_1, nv_2, (:= nv_1 (-8)) (:= nv_2 (-nv_1)), nv_2 \rangle$$

$$F(\text{read}) = \langle nv, (nv := (\text{read})), nv \rangle$$

$$F(+ e_1 e_2) = \langle vs_1, ss_1, \text{ea}_1 \rangle = F(e_1)$$

$$\langle vs_2, ss_2, \text{ea}_2 \rangle = F(e_2)$$

$$\langle vs_1 \uparrow\uparrow vs_2 \uparrow\uparrow av, ss_1 \uparrow\uparrow ss_2 \uparrow\uparrow (av := (+ e_1 e_2)), av \rangle$$

$$F(\text{var}) = \langle \{\text{var}\}, \_, \text{var} \rangle$$

$$F(\text{let } x \text{ } e_1 \text{ } e_2) = \langle vs_1 \uparrow\uparrow vs_2 \uparrow\uparrow \{x\},$$

$$ss_1 \uparrow\uparrow \text{ss}_2 \uparrow\uparrow (:= x \text{ } e_1) \uparrow\uparrow ss_2,$$

$$\text{ea}_2 \rangle$$

3-2/

$X_0$  = assembly

arg = int | reg | (reg, offset)

$X_{0.p}$  = instr +

$X_{0.instr}$  = (addg arg arg) (pushg arg)

(movg arg arg) (popg arg)

(callg label) (subg arg arg)

(negg arg)

(retg arg)

$X_0^* = X_0$  but arg = int | var | reg

\* program = var<sup>\*</sup>,  $X_{0.p}$

select : Co.p  $\Rightarrow X_{0^*,p}$

$S(<vs, ss, a>) = <vs, SS(ss)++(retg a)>$

$SS(mt) = mt$

$SS(stmt :: more) = S1(stmt)++SS(more)$

$S1 : Co.stmt \Rightarrow X_0^*.instr^*$

$S1(x := e) =$

match on e

arg  $\Rightarrow$  (movg arg, x)

read  $\Rightarrow$  (callg \_read)

(movg rax, x)

(- arg)  $\Rightarrow$  (movg arg, x)

(negg x)

(+ arg<sub>1</sub>, arg<sub>2</sub>)  $\Rightarrow$  (movg arg<sub>1</sub>, x)

(addg arg<sub>2</sub>, x)

3-3/

assign:  $X_0^x \rightarrow X_0$

$\langle \text{vars}^x, \text{instr}^+ \rangle \rightarrow \text{instr}^+$   
mention variables

$X_0^x, \text{arg} = \text{int} \mid \text{var} \mid \text{reg}$

$X_0, \text{arg} = \text{int} \mid \text{reg} \mid (\text{reg}, \text{offset})$

$\text{assign}(\langle \text{vars}, \text{instrs} \rangle) =$   
 $(\text{subq} \ (*8 \mid \text{vars}|) \text{rsp})$   
 ~~$\text{assign}(\text{instrs})$~~

$\text{aintr} \dots (\text{retq} \text{arg})$   
 $= \text{assign}^*(\text{instrs})$   
 $\sigma$

~~$\text{movq}$~~

$\text{aintr} \dots (\text{movq} \text{arg} \text{rax})$

$\sigma(\text{var}) = \text{offset}$

$(\text{addq} \ (*8 \mid \text{vars}|) \text{rsp})$

$(\text{retq} \text{rax})$

$\text{assign}^* : (\text{var} \rightarrow \text{offset}) \text{instr} \rightarrow \text{instr}$

$\text{assign}^*(\sigma, \text{var } v) = (\text{rsp}, -8 * \sigma(v))$

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fix:  $X_0 \rightarrow X_0$

$\leftarrow \begin{matrix} (+ + y \ (-10)) \\ (+ y \ 52) \end{matrix}$

movq 10, x  
negq x  
movq x, y  $\xRightarrow{\text{assign}}$  movq 10, rsp(-8)  
addq 52, y  
~~movq~~ retq y  
negq rsp(-8)  
movq rsp(-8), rsp(-16)  $\leftarrow$  illegal  
addq 52, rsp(-16)  
~~retq~~ movq rsp(-16), rax  
retq rax

cannot two memory references in one instruction

$\boxed{\begin{matrix} \text{movq} \\ \text{addq} \end{matrix}} \begin{matrix} a_1 & a_2 \end{matrix} \begin{matrix} \text{if} & a_1 = \text{rsp}(n) \\ & a_2 = \text{rsp}(m) \end{matrix}$

$\begin{matrix} \text{src} & \text{dest} \\ (0 & \text{rsp}(n) & \text{rsp}(m)) \\ \Rightarrow & (\text{movq} & \text{rsp}(n) & \text{rax}) \\ & (0 & \text{rax} & \text{rsp}(m)) \end{matrix}$