

1. (a) Sets A and B are equal to each other.  
 (b)  $|A| = |B| = 3, |C| = 3, |D| = 3, |E| = 3, |F| = 3$   
 (c) i. True  
 ii. False  
 iii. True  
 iv. True  
 v. True
2. (a)  $V = \{-2, -1, 0, 1, 2, 3, 4, 5, 6\}, |V| = 9$   
 (b)  $V = \{t \in \mathbb{Z} | t < -3\} \cup \{t \in \mathbb{Z} | t > 7\}, |V| = \infty$   
 (c)  $B \times A = \{(x, p), (x, q), (x, r), (y, p), (y, q), (y, r)\}, |B \times A| = 6$
3. (a)  $A \times B = \{(m, g), (m, h), (n, g), (n, h), (o, g), (o, h), (p, g), (p, h)\}, |A \times B| = 8$   
 (b)  $B \times A = \{(g, m), (g, n), (g, o), (g, p), (h, m), (h, n), (h, o), (h, p)\}, |B \times A| = 8$   
 (c)  $A \times A = \{(m, m), (m, n), (m, o), (m, p), (n, m), (n, n), (n, o), (n, p), (o, m), (o, n), (o, o), (o, p), (p, m), (p, n), (p, o), (p, p)\}, |A \times A| = 16$   
 (d)  $B \times B = \{(g, g), (g, h), (h, g), (h, h)\}, |B \times B| = 4$
4. (a)  $A \times B = \{(10, 2), (10, 3), (10, 4), (11, 2), (11, 3), (11, 4), (12, 2), (12, 3), (12, 4)\}$   
 (b) i. No  
 ii. Yes  
 (c)  $R = \{(10, 2), (11, 3), (12, 4)\}$   
 (d) Domain of R is A and co-domain of R is B.  
 (e) R is a function because every element in A is related to exactly one element in B.
5. (a) i.  $p \wedge q$   
 ii.  $r \vee \neg q$   
 iii.  $\neg(p \wedge r)$   
 iv.  $\neg r \wedge \neg q$   
 (b) i. False  
 ii. True  
 iii. False  
 iv. True  
 v. False  
 vi. True

6. (a)

$p$	$q$	$r$	$p \vee (\neg q \wedge r)$
T	T	T	T
T	T	F	T
T	F	T	T
T	F	F	T
F	T	T	F
F	T	F	F
F	F	T	T
F	F	F	F

(b)

$p$	$q$	$r$	$(p \vee q) \wedge (\neg p \vee (q \wedge \neg r))$
T	T	T	T
T	T	F	T
T	F	T	T
T	F	F	F
F	T	T	T
F	T	F	T
F	F	T	F
F	F	F	F

(c)  $p \wedge (p \vee q)$  is equivalent to  $p$  because  $p \wedge (p \vee q) = p \wedge \top = p$

7.  $(p \oplus q) \wedge r = (p \wedge \neg q \vee \neg p \wedge q) \wedge r$  because the definition of Exclusive OR is  $p \oplus q = p \wedge \neg q \vee \neg p \wedge q$