

DAY-1 - 04/05/2021 - Introduction

#include - Preprocessors

<iostream>, <cmath> - Headers

using namespace std - Avoid name conflicts

main() - The most prioritised function and start point of program

cin - input function in CPP

Syntax: cin >> a >> b; [a,b are any type of variables declared]

cout - output function in CPP

Syntax: cout << a << b; [a,b are any type of variables]

endl - It is used after cout to give a new line in place
of \n in strings

Syntax: cout << "a" << endl << "b"; [Prints a and b on two lines]

// - Used to comment a single line

/* */ - Used to comment multiple lines [must end]

Variable - It is a container to store data in it.

Data types

int → 4 bytes → 10

float → 4 bytes → 2.51

char → 1 byte → 'a'

String → (as required) → "Hello"

bool → 1 byte → true/false

When we print bool, true-1 and false-0 will be printed

return 0; - Shows that work is completed in the (task) program

DAY-2 - 05/05/2021 - Operators

NameSpace - It is used to avoid the name conflicts.

Using NameSpace std; - It is used to call the cout and cin from the namespace std created in the iostream module.

Without using this, we have to use std:::cin, std:::cout, std:::endl in place of cin, cout, endl etc.

Operators:

1. Arithmetic operators: +, -, *, /, %

2. Assignment operators: =, +=, *=, -=, /= etc..

3. Comparison or Relation operators: >, >=, <, <=, ==, !=

4. Bitwise operators: &, |, ^, <<, >>

and

$$5 - 0101$$

$$\& 10 - 1010$$

(both 1's gives 1) 0000 - 0

$$\& 5 - 0101$$

$$10 - 1010$$

(all zeros 0) 1111 - 15

ex-or

$$8 - 1000$$

$$112 - 1100$$

(diff bits?) 0100 - 4

left shift

$\ll \Rightarrow$ Shifts every bit ^{to left} by given number [Shifts 2^n if given n]

$$2 \rightarrow 0010 \ll 1 \text{ gives } 4 \rightarrow 2 \times 2^1 = 4 - 0100$$

$$\text{right shift} \quad 2 \rightarrow 0010 \ll 2 \text{ gives } 8 \rightarrow 2 \times 2^2 = 8 - 1000$$

$\gg \Rightarrow$ Shifts every bit to right by given number [divide by 2^n]

$$5 \rightarrow 0101 \gg 1 \rightarrow 0010 \text{ gives } 5/2^1 \text{ [Floor].}$$

$$10 \rightarrow 1010 \gg 2 \rightarrow 0010 \text{ gives } 10/2^2 \text{ [Floor]}$$

DAY-3 06/05/2021 - Operators and Modules

Left shift and right shift formulas:

$$\text{num} \gg k = \text{num}/2^k \quad [\text{right shift}]$$

$$\text{num} \ll k = \text{num} * 2^k \quad [\text{left shift}]$$

Count the set bits of a number:

To check set bits of 10:

$$\begin{array}{rcl} 10 = 1010 & \Rightarrow \text{right shift of } 10 \Rightarrow 0101 \\ \begin{array}{r} \cancel{1} \\ \cancel{0} \\ \hline 0001 \end{array} & & \begin{array}{r} \cancel{1} \\ \cancel{0} \\ \hline 0001 \end{array} \\ \text{unset} & & \text{set} \\ \text{set bits} = 0 & & \text{set bits} = 1 \end{array}$$

$$\begin{array}{rcl} \text{right shift again } \Rightarrow 0010 & \text{again } \Rightarrow \Rightarrow 0001 \\ \begin{array}{r} \cancel{1} \\ \cancel{0} \\ \hline 0000 \end{array} & & \begin{array}{r} \cancel{1} \\ \cancel{0} \\ \hline 0001 \end{array} \\ \text{unset} & & \text{set} \\ \text{set bits} = 1 & & \text{set bits} = 2 \end{array}$$

again right shift gives 0. So set bits of 10 = 2.

Process:

1. We have to check the $\&$ with 1 such that $n \& 1$, if we get 1, the last bit is setbit else it is not a setbit.
2. Now right shift n and again repeat the above process until we get $n=0$.

Ex-OR formula:

$$\begin{array}{l|l|l} 1 \rightarrow 1 & 1^{\wedge} 2^{\wedge} 3^{\wedge} 4^{\wedge} 5 \rightarrow 1 & 1^{\wedge} 2^{\wedge} \dots ^{\wedge} 9 \rightarrow 1 \\ 1^{\wedge} 2 \rightarrow 3 & 1^{\wedge} 2^{\wedge} \dots ^{\wedge} 6 \rightarrow 7 & 1^{\wedge} 2^{\wedge} \dots ^{\wedge} 10 \rightarrow 11 \\ 1^{\wedge} 2^{\wedge} 3 \rightarrow 0 & 1^{\wedge} 2^{\wedge} \dots ^{\wedge} 7 \rightarrow 0 & 1^{\wedge} 2^{\wedge} \dots ^{\wedge} 11 \rightarrow 0 \\ 1^{\wedge} 2^{\wedge} 3^{\wedge} 4 \rightarrow 4 & 1^{\wedge} 2^{\wedge} \dots ^{\wedge} 8 \rightarrow 8 & 1^{\wedge} 2^{\wedge} \dots ^{\wedge} 12 \rightarrow 12 \end{array}$$

So to find exor upto n numbers, if $n=1$:

like $1^{\wedge} 2^{\wedge} 3^{\wedge} \dots ^{\wedge} n \Rightarrow$

- = if $n \% 4 = 0$, answer will be n
- if $n \% 4 = 1$, answer will be 1
- if $n \% 4 = 2$, answer will be $n+1$
- if $n \% 4 = 3$, answer will be 0

* Note: $n \& n = 0$ always. This is used to find the unique elements.

5. Logical Operators &&, ||, !

String: We can use the string in C++. We can include the string library using `#include <string>`

Math: To do mathematical tasks, we have to include the cmath library. We can do sqrt, power, etc.

Powerful header

```
( #include <bits/stdc++.h> )
```

The above header includes all the libraries like iostream, vector, list, map, dynamic functions and all using the same header file.

Conditions: The condition can be either true or false.

Here '0' will be considered as false and any other number is considered as true because there will be atleast one '1' in the binary digits of the number except '0'. Zero has only 0's in its binary representation so it is considered as false.

The conditions can be combined with logical operators to compare two or more conditions.

if: The body of if will be executed when condition is true else it is not executed.

else It must be an extension for if and it has no specific condition. If the condition of "if" is false, automatically "else" part will be executed.

else-if: It is followed by "if" and will be skipped if the first condition is true. It is an extension of else including a condition for it.

Loops:

(i) Infinite loops + The loops that are iterated over a ^{finite} range of values
or for

(ii) Indefinite loops Loops that run until a condition is checked and it is false
or while, do-while

When there is a syntaxical error, the loop runs based on logic and if the logic leads to a non-ending point and leads to infinite loop.

Find sum - To find the sum of elements of n^{th} row of the Pascal triangle, sum is 2^n [n starts from 0]

The first ^{column} of pascal triangle are 1's and remaining can be obtained by

$$a[\text{row}][\text{col}] = a[\text{row}-1][\text{col}-1] + a[\text{row}-1][\text{col}]$$

Pascal Triangle

1

1 1

1 2 1

1 3 3 1

1 4 6 4 1

1 5 10 10 5 1

$$\left[a[1][1] = 1 = a[0][0] \right] \\ \left[a[0][0] \right] \\ (\text{Hence})$$

It gives our binomial expressions like:-

$$(a+b) = (a+b)$$

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$$

⋮

LCM

To find faster, we can start loop from big number of two and run it upto product of 2 numbers & increment by big num.

big = num1 > num2 ? num1 : num2;

for(int i = big; i <= num1 * num2; i = big)

{ if(i % num1 == 0 & i % num2 == 0)

3 3 --- break; // save i value or print here

Day - 6 - 10/05/2021

- LCM & HCF (GCD)

Pseudo code for LCM = (optimized).

```

yes = 1, r = 2
if (num1 % r == 0 & num2 % r == 0)
{
    num1 = num1 / r;
    num2 = num2 / r;
    yes = yes * r;
}
else
{
    r++;
}
if (num1 < r || num2 < r)
{
    res = res * num1 * num2;
    break;
}

```

x value

$$\begin{array}{r}
 2 \overline{) 12, 24} \\
 2 \overline{) 6, 12} \\
 3 \overline{) 3, 6} \\
 1, 2
 \end{array}$$

Pnum1 num2
final.

LCM = (res * r in loop)

Pseudo code for GCD =

Euclid's algorithm

$$\begin{aligned}
 GCD(a, b) &= (a-b, b) \\
 &\Rightarrow a > b \text{ (swap)} \\
 &\quad (a-b, b) \\
 &\text{until 1st becomes zero, } b \text{ is GCD.}
 \end{aligned}$$

$$\begin{aligned}
 GCD(30, 24) &\ni (30-24, 24) \\
 &= (6, 24) \\
 &\xrightarrow{\text{swap}} (24, 6) \\
 &\quad (24-6, 6) = (18, 6) \\
 &= (18-6, 6) = (12, 6) \\
 &\quad \vdots (12-6, 6) = (6, 6) = (6, 0) \\
 &= (6, 0) \ni 6 \text{ is GCD of } 30, 24
 \end{aligned}$$

More optimized

$$\begin{aligned}
 GCD(a, b) &\ni (a \%, b, b) \\
 &\quad \text{loop until 1st digit one becomes 0, } b \text{ is GCD}
 \end{aligned}$$

loop

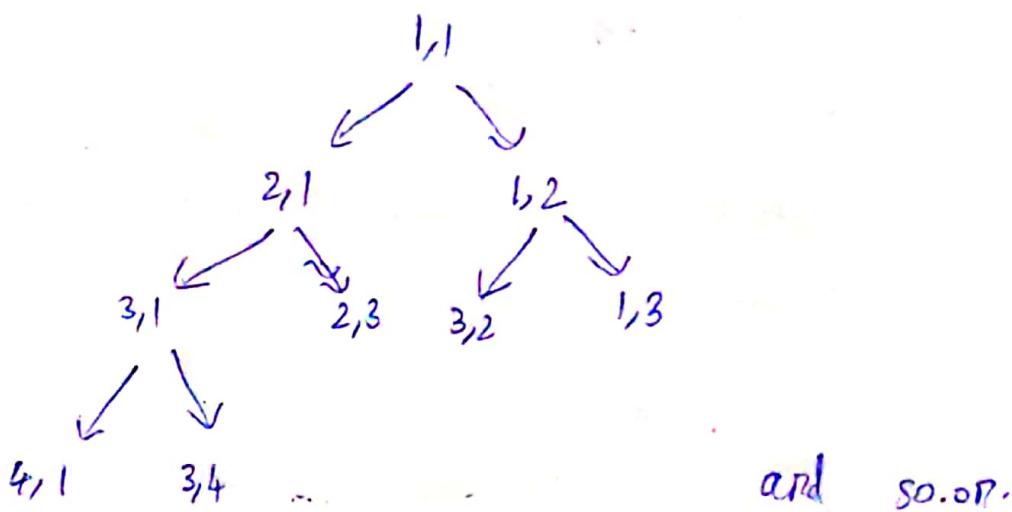
24) 30 (1

$$\begin{array}{r}
 24 \\
 6) 24 (4 \\
 \underline{24} \\
 0
 \end{array}$$

6 is GCD of 30, 24

Question given in AWS Frame of co-ordinates.

A person start from $(1,1)$, input will be given to us like $(2,3)$, $(5,4)$, $(3,3)$ Point "Yes" or "No" if he can move to that point or not. He can move in two directions, $(a+b, b)$, $(a, b+a)$



* By applying reverse formula, from $(4,1)$ to $(3,1)$ is

(i) $(3,4)$ to $(3,1)$ is $\underline{(a, b-a)}$ which is $\underline{\text{gcd}}$ formula $\underline{(a-b, a)}$

* So the GCD of any coordinate is finally 1 because GCD of $(1,1)$ is 1. So if the GCD of two numbers is 1, it is Yes.

* If the GCD of two given input numbers, equals to 1, then he can reach to point given as input starting from $(1,1)$. If the GCD is not 1, then the answer is "No".

- (i) GCD of $2,3$ is 1 so print "Yes"
- (ii) GCD of $5,4$ is 1 so print "Yes"
- (iii) GCD of $3,3$ is 3 so print "No"

Reverse of a number

→ Num $y = \text{Num} \% 10$
→ Yes=0 $\text{Num} = \text{Num} / 10$ } until $\text{Num} = 0$ (while(n))
 Yes = Yes * 10 + Y because every num is true except 0

Palindrome or Not

check reverse of a number equals to actual number.

Even and odd digits

We can increment even or odd variables in reverse of number program and neglect result part.

Even strongly even or Strongly odd or mixed

In the above program if odd=0, strongly even or even=0, strongly odd else mixed.

Happy number

Sum of squares of digits until it becomes single digit

$$13 \rightarrow 1^2 + 3^2 \rightarrow 1 + 9 \rightarrow 10 \rightarrow 1^2 + 0^2 = 1 \rightarrow \text{happy number}$$

$$19 \rightarrow 1^2 + 9^2 \rightarrow 82 \rightarrow 8^2 + 2^2 = 68 \rightarrow 6^2 + 8^2 = 100 \rightarrow 1^2 + 0^2 + 0^2 = 1$$

7, 1 are single digit happy numbers.

Happy Number

1. Check as prime or not

- (i) Check from 1 to n [n operations]
- (ii) Check from 2 to n-1 [n-2 operations]
- (iii) Check from 2 to $n/2+1$ [Optimised]
- (iv) Check from 2 to \sqrt{n} [Very optimised]

2. To get last digit of power of any number

Ex: 2^{137} , $2^1 = 2$, $2^2 = 4$, $2^3 = 8$, $2^4 = 16$, $2^5 = 32$.

Repeatedly we get [2, 4, 8, 6]

$$\therefore 137 \div 4 = 1 \quad [2 \rightarrow 0] \quad [4 \div 4 = 0]$$

Last digit of $2^{137} = 2$

Note: We have to divide the exponent part with the length of the array formed by the repeating values.

In program, we can take [6, 2, 4, 8] and by taking the index of array as $137 \div 4$, we can get the last digit.

1. Find factors of a number :-

(i) Optimized :- Iterate upto $n/2$ times

(ii) Very optimized :- Iterate upto \sqrt{n} times and can find factors as $num/factor = \text{another associated factor.}$

ex:- 100

1) ② 4 5 10 20 25 ⑤ (100)
Sqrt.

The above are related by one before and one after the square root. So we can find them easily.

Handling larger numbers \div Continued in advanced topics //

Long long int range is upto 10^{18}

CPP arrays Limits

10^6 for int & 10^7 for char, bool arrays.
 10^7 if declared globally.

So we can store them in arrays discussed later.
(using vectors)

Prime factors

$$30 \Rightarrow 2 \times 3 \times 5$$

* After dividing any number with 2 for all possible times, then any other multiples of 2 can't divide that number. Similarly all other numbers.

No of factors using prime factors

$$\text{Num} = a^p \times b^q \times c^r \times \dots \quad [a, b, c, \dots \text{are prime factors}]$$

$$\text{No. of factors} = (p+1)(q+1)(r+1) \dots$$

Factorial

Factorial of a number is a product of numbers from 1 to that number.

To find the no. of zeroes at last (leading)

(i) We can find by using prime factors as no. of zeroes will be as equal to ~~no.~~ pairs of (2,5) available.

Always no. of 5's will be less than no. of 2's. So the no. of 5's will be answer.

(ii) The no. of 5's in prime factors of solution of factorial will be, in the factorial [optimized]

$$5-24 = 1 \quad \therefore \text{No. of zeroes} = \frac{1}{5} + \frac{1}{25} + \frac{1}{125} + \dots$$

$$25-124 = 2 \text{ increased.} \quad \therefore 5! = 2^3 \times 3 \times 5 \quad [\text{One } 5.]$$

$$125- = 3 \text{ increased.} \quad 10! = 2^8 \times 3^4 \times 5^2 \times 7 \quad [\text{Two } 5's.]$$

Since no. of 5's change according to those numbers.
At every interval of 5, 10, 15, 20, ..., by 1 but at 25, 125 etc, the no. of 5's increase one or two excess.

Bit Magic

To check whether a bit at position p is set or not
 $num = num \gg (pos-1)$, now check $num \& 1$

Unset the p^{th} position bit:

$x = 1 \ll (p-1)$, perform $num \wedge x$.

Set the p^{th} position bit:

$x = 1 \ll (p-1)$, perform $num | x$

Best way to check prime or not :-

(I) Most of the numbers are divisible by 2 & 3.

(II) Check from 5 to n , increment 6, check x_1, x_{i+2} ($i=5, i+2=7$) x_3, x_{i+6} ($i=11, i+2=13$) x_5, x_{i+8} ($i=17, i+2=19$), ...

So the code will be,

if ($n == 1$)

 return false

if ($n == 2 \text{ || } n == 3$)

 return true

if ($n \% 2 == 0 \text{ || } n \% 3 == 0$)

 return false

for (int $i = 5$; $i < n$; $i += 6$)

 if ($n \% i == 0 \text{ || } n \% (i + 2) == 0$)

 return false

 return true

Problem: If a bucket has 7 chocolates, and we can take 1 or 3 chocolates at a time. In how many ways, we can empty the bucket?

To remove 1 chocolate $\rightarrow (1) \rightarrow 1$ way.

2 $\rightarrow (1,1) \rightarrow 1$ way

3 $\rightarrow (1,1,1), (3) \rightarrow 2$ ways

4 $\rightarrow (1,1,1,1), (3,1), (1,3) \rightarrow 3$ ways

5 $\rightarrow (1,1,1,1), (1,3,1), (3,1,1), (1,1,3)$

$\rightarrow 4$ ways

From above,

To give 4, it takes value from 3 & 1

Similarly for 5, it takes values from 4 & 2.

$$\therefore \text{ways}(4) = \text{ways}(3) + \text{ways}(1)$$

$$\text{ways}(5) = \text{ways}(4) + \text{ways}(2).$$

$$\therefore \text{ways}(n) = \text{ways}(n-1) + \text{ways}(n-3)$$

Problem: If we are finding $n \& (n-1) \& (n-2) \& \dots \& 1$, print number when it becomes 0.

Normally we iterate from n-1 and perform the & operation and break if it becomes 0.

But,

$$1 \& 2 = 0$$

$$2 \& 3 = 2; 2 \& 3 \& 4 = 0$$

$$4 \& 5 = 4, \dots, 4 \& 5 \& 6 \& 7 = 4, \dots, 4 \& 5 \& 6 \& 7 \& 8 = 0$$

$$8 \& 9 = 8, \dots, 8 \& 9 \& \dots \& 15 = 8, \dots, 8 \& 9 \& 10 \& \dots \& 15 \& 16 = 0$$

when we reach the 2^n , we get 0. $\begin{bmatrix} 2 \& 1 = 0 \\ 4 \& 3 = 0 \\ 8 \& 7 = 0 \\ 16 \& 15 = 0 \end{bmatrix}$ $\begin{bmatrix} 32 \& 31 = 0 \\ 64 \& 63 = 0 \end{bmatrix}$

So, we can find the least nearest 2^n value and return the 2^{n-1} value, it will be the result.

To make 17 as 0, we get 5 right shifts. So to get 16, we make (count-1) left shift of 1.

Similarly 5 as 0, we get 3 right shifts, so to get 4, we get (count-1) left shifts of 1.

$$\text{for } 17, 5 \text{ count } \Rightarrow 1 \gg\ll(5-1) = 16$$

$$\text{for } 5, 3 \text{ count } \Rightarrow 1 \gg\ll(3-1) = 4$$

Then return $16-1$ or $4-1$ as required.

Problem: If a large array is given and only one element will be present single and all other will be even pairs.

ex:- 1 2 2 3 3 4 4 5 5

By applying all elements with "AND" we get the result.

Problem: To calculate the power of a number, to represent it into the powers of multiples of 2

$$3^{19} = 3^{16} \times 3^2 \times 3^1$$

write the binary of 19 \Rightarrow 10011
 $\begin{array}{r} 10011 \\ 1010 \\ 3^8 3^4 3^2 3^1 \\ \downarrow \\ \text{base at base applied.} \end{array}$

Take $3^{10} = 3^8 * 3^2$

binary of 10 \Rightarrow 1010
 $\begin{array}{r} 1010 \\ 3^8 3^4 3^2 3^1 \end{array}$

We take base, exp and by using above formula, we solve the power.

\therefore while (exp)

{ if (exp & 1) // To check the bit set or not

yes = yes * base;

~~do~~

exp >> 1; // to shift to check the next bit

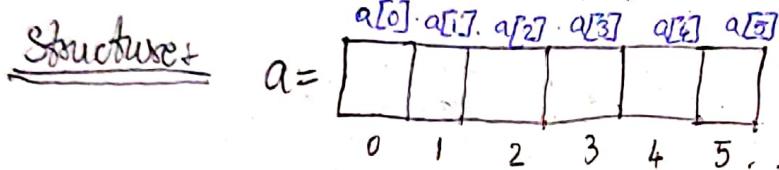
base *= base; // base is changing from position to position [3¹, 3², 3⁴, 3⁸ second]

Here if there is a set bit, result will be multiplied with base value and every time exponent will be right shifted. base will be multiplied by itself to satisfy the exponent value of base power.

Array: * An array is a data structure where we can store multiple data of same datatype.

* Array has an index value from 0 to n-1 where n is size of array.

* We can access elements of an array by index value of the element like $a[0]$, $a[1]$, etc.



* If we declare an array globally, you will get more space to store elements than declared locally and not needed to pass it as arguments.

* `for(auto it: arr)` - is a new way of accessing all elements.

Problem: To get the most visited customer details based on the id of the customer.

* We can write a loop in loop.

Normal

* We can get a max element from array and increase its value by taking that ^{id} value as index and the frequency will be the element of the array and we can print the elements of the index of the maximum element of the frequency to get the customer id.

Optimized

* We can use a map data structure to reduce the memory usage of the frequency array by ~~as~~ key,value pair

- * There are two types of arrays - static and dynamic.
- * For static arrays, we declare int arr[10] and it won't increase its size upon adding more than 10 elements.
- * For dynamic arrays, we use vector in which we can push elements. We declare as vector<datatype> v; and we have to include `#include <vector>`. It contains the dtos for vector.
- * `#include <vector>`

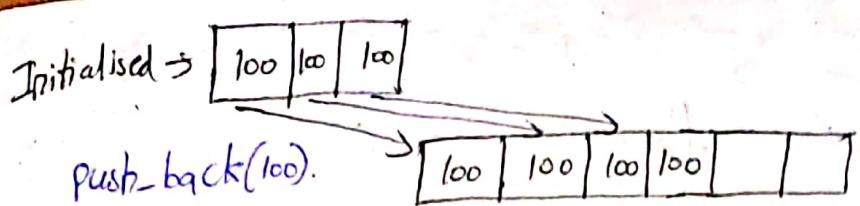
This header file contains all the functions of a vector like search, sort, merge etc.

- * `v.push_back(x)` - push x to vector v.
- * `emplace_back(x)` - Similar to push-back.
- * `size()` - returns the size of the vector.
- * `pop_back()` - deletes the last inserted value.
- * If we want to declare same number of elements and length to be n [like arr {100,100,100} 3 hundreds], we can declare `vector<int> arr(3,100)`, 3 is the length of vector and 100 is the element to be appeared 3 times after initialized.
- * If we didn't give second parameters, all zeros will be given.

`vector<int> arr(5,100);` - {100,100,100,100,100}

`vector<int> arr(5);` - {0,0,0,0,0}

Note If we declare size like this, after we append another element, the size will be doubled and inserted at the position after initialized.



Like this, it always doubles the size of the vector when we push an elements.

* `vector<int> arr(v)` - Copies ve elements to arr during the initialisation.

* We can access the elements of a vector using iterator.

`vector<int>::iterator it;`

^ iterator name

We can use arr.begin() & arr.end() to access the first and last elements.

`arr.begin()` points to 1st element of arr.

`arr.end()` points to the last elements next address.

We can take `it = arr.begin();`

To print address `cout << ⁢`

`cout << *it;` gives the element at that position.

Giving `cout << it;` throws an error where it is iterator.

To move to another element, we can increment the it to get the next value. `[it++]`

We can use auto keyword instead of `vector<int>::iterator`.

Later it is updated again.

* `for(vector<int> :: iterator it = arr.begin(); it != arr.end(); it++)`
`cout << *(it);`



* `for(auto it = arr.begin(); it != arr.end(); it++)`
`cout << *(it);`



* `for(auto dit : arr)`

`cout << it;` // doesn't require *



it returns the value but not address.

* To find an element in a vector,
(must be defined) `it = find(vec.begin(), vec.end(), element);`

`cout << it - ve.begin();`



address of starting address of
element vector.

Because all elements are stored in continuous locations,
the difference of these two will give the index value.

ex element at 1st position.

`starting address - ve.begin() - ve.begin()` giving index 0

1. To find the index of an element if it is present in vector or not.

auto it = find(arr.begin(), arr.end(), x)

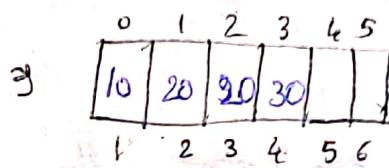
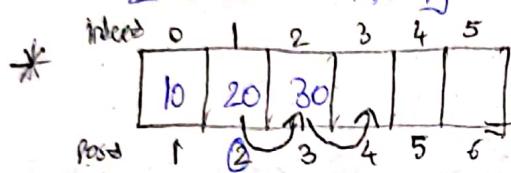
* Now we can find the memory address by &it and element by *it.

* But we know that the difference of continuous indices of an array or vector is 1. So we can get the index by it - arr.begin().

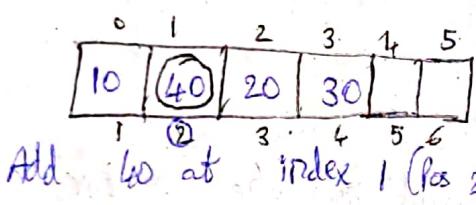
* If the element is not found in the vector, our it will be at the arr.end(). By this, we can write a condition such that if it != arr.end(), we can print the index. If not, we can print -1 in else condition.

1. Insert an element at the position "pos" of an array.

- * To insert an element at position, we have to move the elements from pos to n from left to right by one step. [pos = index-1]



Insert 40 at 2nd position



element copied.

⇒ 40 inserted at 2nd position

2. Insert an element at the position "pos" of a vector.

- * To insert an element into a vector, we can use insert method to insert an element.

SYNTAX : v.insert(v.begin() + pos-1, n) //insert(position, value)

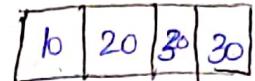
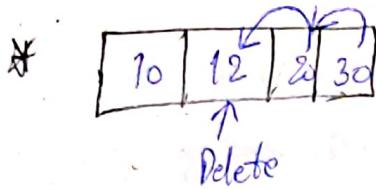
n is the element, pos = position to be inserted.

v.begin + pos-1 gives the index of the element's position at which element to be inserted.

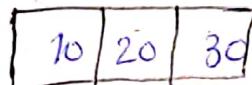
- * We can pass multiple values as value, to insert into vector.

1. Delete an element from an array:

- * Find the index of the element in the array.
- * Shift all the elements from index to left by 1.



↑ Replace with INT_MIN
and decrease n by 1.



* We will get the final array after deletion.

2. Delete an element from a vector:

- * We can use ve.erase(itr).
- * If index is given, $itr = ve.begin() + index$.
- * If element is given, $itr = ve.find(ve.begin(), ve.end(), element)$

3. Find the second largest element of array:

val1 = a[0], val2 = INT_MIN.

for loop {

 if ($a[i] > val1$)

 {

 val2 = val1;

 val1 = a[i];

 }

 else if ($val2 < a[i]$)

 {

 val2 = a[i];

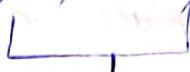
 }

}

Day-23 - 29/05/2021 - Arrays

1. To check whether array is sorted or not.
 - * We can search using two for loops by checking each element with the remaining array.
 - * We can use a single for loop by taking or comparing adjacent (side-by-side) elements.

1. sort() - $\text{sort}(\text{v.begin}(), \text{v.end}())$



can take any two iterators.

Sort in descending order: $\text{sort}(\text{v.begin}(), \text{v.end}(), \text{greater<int>})$

* Bubble Sort:

Let elements = 2, 6, 4, 3

pass 1

② ⑥ 4, 3, 1

2, ⑥ ④, 3, 1 (swap)

2, 4, ⑥ ③, 1 (swap)

2, 4, 3, ⑥, 1 (swap)

2, 4, 3, 1, 6

pass 2

②, ④, 3, 1, 6

2, ④, ③, 1, 6 (swap)

2, 3, ④, 1, 6 (swap)

2, 3, 1, 4, 6

pass 3

②, ③, 1, 4, 6

2, ③, ①, 4, 6 (swap)

2, 1, 3, 4, 6

pass 4

②, ①, 3, 4, 6 (Stop)

1, 2, 3, 4, 6

∴ Finally the sorted array is 1, 2, 3, 4, 6.

We can ignore last element every iteration as they will be occupied with their actual positions

Without return type :-

We cannot return values and it is of type void and we can't get values back to the main().

With return type :-

We can return values by declaring return type as its data type and we can get those in the main().

void: The function doesn't return anything is void type.

Note: The function must be declared above the function call.

Call by reference:

use the '&' before variables in function argument.

Function with &

While we are using '&' before function name, we cannot create and modify a local variable but we can only change the argument passed to it.

Return array

```
Using int * fun()
{
    int* arr = { ... };
    return arr;
}
```

In main, `int *p = fun();` we can get the array.

By using pointers, we can get the array to be returned by the function.

Most of the times, vector is used instead of `int*` to return an array.

Recursion:

Function that calls itself. We must give a base case to stop.

<u>ex:-</u> int fact(int n) { if (i == 1) return n * fact(n-1); return 1; }	int fact(int n) { if (i <= 1) return 1; return n * fact(n-1); }
--	--

The if case is base case where the recursion stops.

Day - 28 - 05/06/2021 - Explanation on recursion.

Day - 29 - 07/06/2021 - Explanation on recursion

1. Check prime or not using recursion.

bool is_prime(int n, int i)

{

 if ($n \leq 2$)

 {

 if ($n = 2$)

 return true;

 return false;

 }

 if ($n \% i == 0$)

 return false;

 if ($i * i > n$)

 return true;

 is_prime(n, i + 1)

}

2. Print n^{th} fibonacci.

int fib(int n)

{

 if ($n == 1$)

 return 0;

 else if ($n == 2$)

 return 1;

 return fib(n - 1) + fib(n - 2);

}

if ($dp[n] == -1$)

 return dp[n];

 return dp[n] = fib(n - 1) + fib(n - 2);

The dp array is declared globally so that to reduce the time complexity and storing each value at respective positions.

Day-30 - 08/06/2021 - Explanation on recursion

1. Print n to 1

```
Void print(int n)
```

```
{
```

```
if (n == 0)
```

```
return;
```

```
cout << n << " ";
```

```
print(n-1);
```

```
}
```



Tail recursion



After child call, nothing to do with parent call.

Less

complex

2. Print 1 to n

We can take two parameters but by changing n to 1 function, we can get..

```
print(n-1);
```

```
cout << n << " ";
```

} changing this, we can print 1 to n numbers.



Non-Tail recursion



After child call, there is something to do in parent calls.



More complex

1. To print all the combinations of a given number.

N=4 \Rightarrow [1,1,1,1 1,1,2 1,2,1 2,1,1 2,2 1,3 3,1 4]

We can use recursion to get this by decreasing N one by one in each recursion and in each we can take another two recursive calls. Base case is $N=0$ & then we have to print.

We have to fix element in loop because we have to remove the last element when back tracking.

Task:

There is a rope, of length N, we have to cut that into parts using lengths given as input a, b, c. Find maximum value of parts, we can get.

$$N=5, \quad a=2, \quad b=5, \quad c=1.$$

$$\text{for } a=2, \quad 5 = 2, 2, 1 \quad [3 \text{ parts}] \quad (or) \quad 2, 1, 1, 1 \quad [4 \text{ parts}]$$

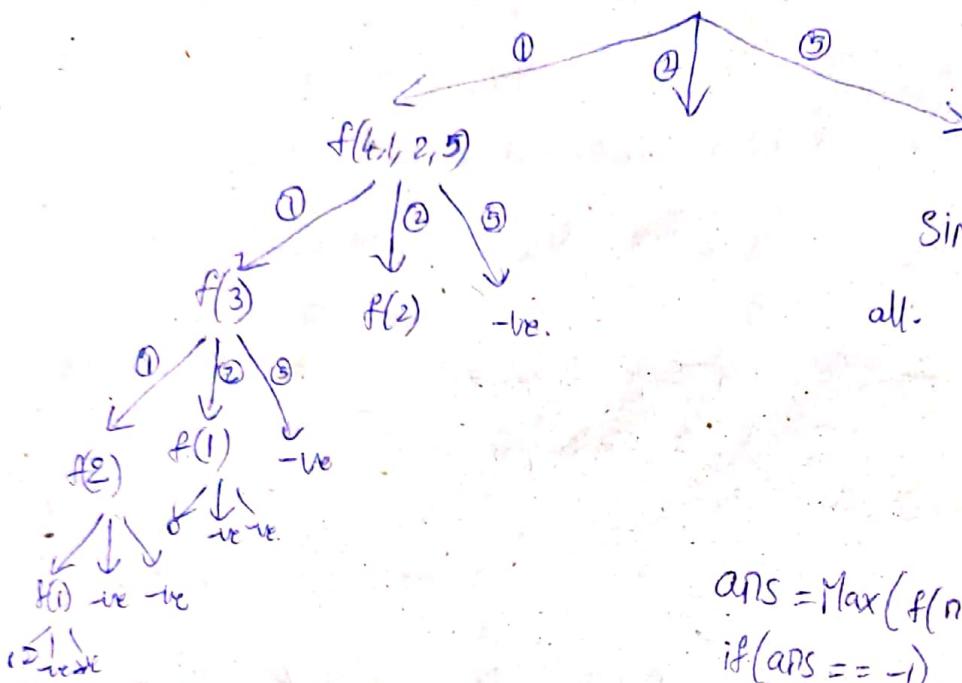
$$b=5, \quad 5 = 5 \quad [1 \text{ part}]$$

$$c=1, \quad 5 = 1, 1, 1, 1, 1 \quad [5 \text{ parts}] \quad \text{maximum} = 5 \text{ parts.}$$

Day-33 - 12/06/2021. - Task explanation, Sub array, Subset

Hope cut+ Let $n=5$, $a=1$, $b=2$, $c=5$.

$$f(5, 1, 2, 5)$$



Similarly we see for all.

```

if ( $n==0$ )
    return 0;
if ( $n<0$ )
    return -1;

```

$ans = \max(f(n-a), f(n-b), f(n-c));$
 $\text{if } (ans == -1)$
 return -1;
 return $ans + 1;$

For $f(1)$, $f(0)$ returns 1 because 0 is present, and 0 is 1 and at $f(2)$, $f(1)$ returns 1+1 since 1 is max of all. Thus returns max to fp by returning 5 from 1.

Sub-array

The sub-arrays are the contiguous parts of the array.

Ex Let $a = \{1, 2, 3\}$,

Sub arrays are

1	2	3	1
1 2		3	
1 2 3			

No. of subarrays of array of length n are,

$$\text{Sub arrays} = \frac{n(n+1)}{2}$$

Sub-sets

The every possible combinations of array elements even non-contiguous continuous elements.

Ex:	$a = \{1, 2, 3\}$	1	2
		1 2	2 3
		1 3	3
		1 2 3	[]

$$\therefore \text{Sub-set count} = 2^n$$

We can get these using power-set.

Let $a = \{1, 2, 3\} \rightarrow 2^{\cancel{n}} = 8$.

Index	2	1	0	
0	0	0	0	$\rightarrow []$
1	0	0	1	$\rightarrow [1]$
2	0	1	0	$\rightarrow [2]$
3	0	1	1	$\rightarrow [1, 2]$
4	1	0	0	$\rightarrow [3]$
5	1	0	1	$\rightarrow [1, 3]$
6	1	1	0	$\rightarrow [2, 3]$
7	1	1	1	$\rightarrow [1, 2, 3]$

We write two loops, 1st loop to run for 2^n times and inner loop runs for n times. [$\because 2^{n-1} \ll (n-1)$ or $n < 2^{n-1}$]

```
for (int num=0; num<(1<<3); num++)
```

```

    vector<int> ans; // We are getting indices, so we
    for (i=0; i<n; i++) // have to left shift with 1 so
        if (num&(1<<i)). // we get multiples of 2 to
    {                         check.
    }
```

we push the elements.

Note: Time complexity is $O(2^n * n)$.

Day-34 - 14/06/2021 - Subsets using recursion

$n=3$ $a=\{1, 2, 3\}$

$f(ind, n, a, [])$

Pick Non-Pick.

$f(ind+1, n, a, [1])$

$f(ind+1, n, a, [])$

N

$f(2, n, a, [1, 2])$ $f(2, n, a, [1])$

P N

$f(3, n, a, [1, 2, 3])$

P N

↓

base case

$if(ind == n)$

print ds;

It is not necessary
because base case
already checks.

$\rightarrow if(ind < n)$

```
{  
    ds.push_back(a[ind]);  
    printSubset(ind+1, n, a, ds);  
    ds.pop_back();  
}
```

$\rightarrow printSubset(ind+1, n, a, ds);$

Note: The complexity of this recursion is 2^n . This code is optimised by n times.

Combinations vs Permutations

Combinations are selections and permutations are ordered.

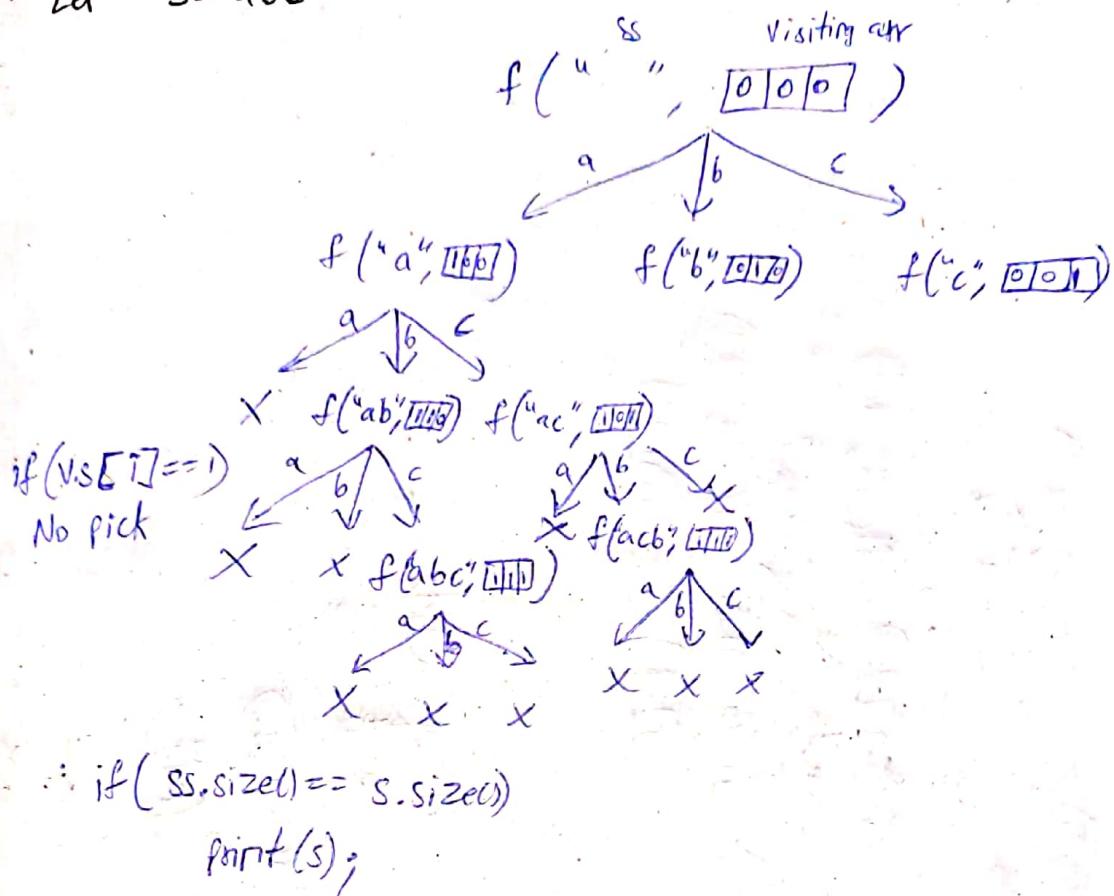
Recursion

① Clarity on parameters

② Base case

To print all permutations of a string

Let $s = "abc"$



for($i=0; i < n; i++$)

{

if ($vis[i] == 0$)

{

$ss += s[i];$

$vis[i] = 1;$

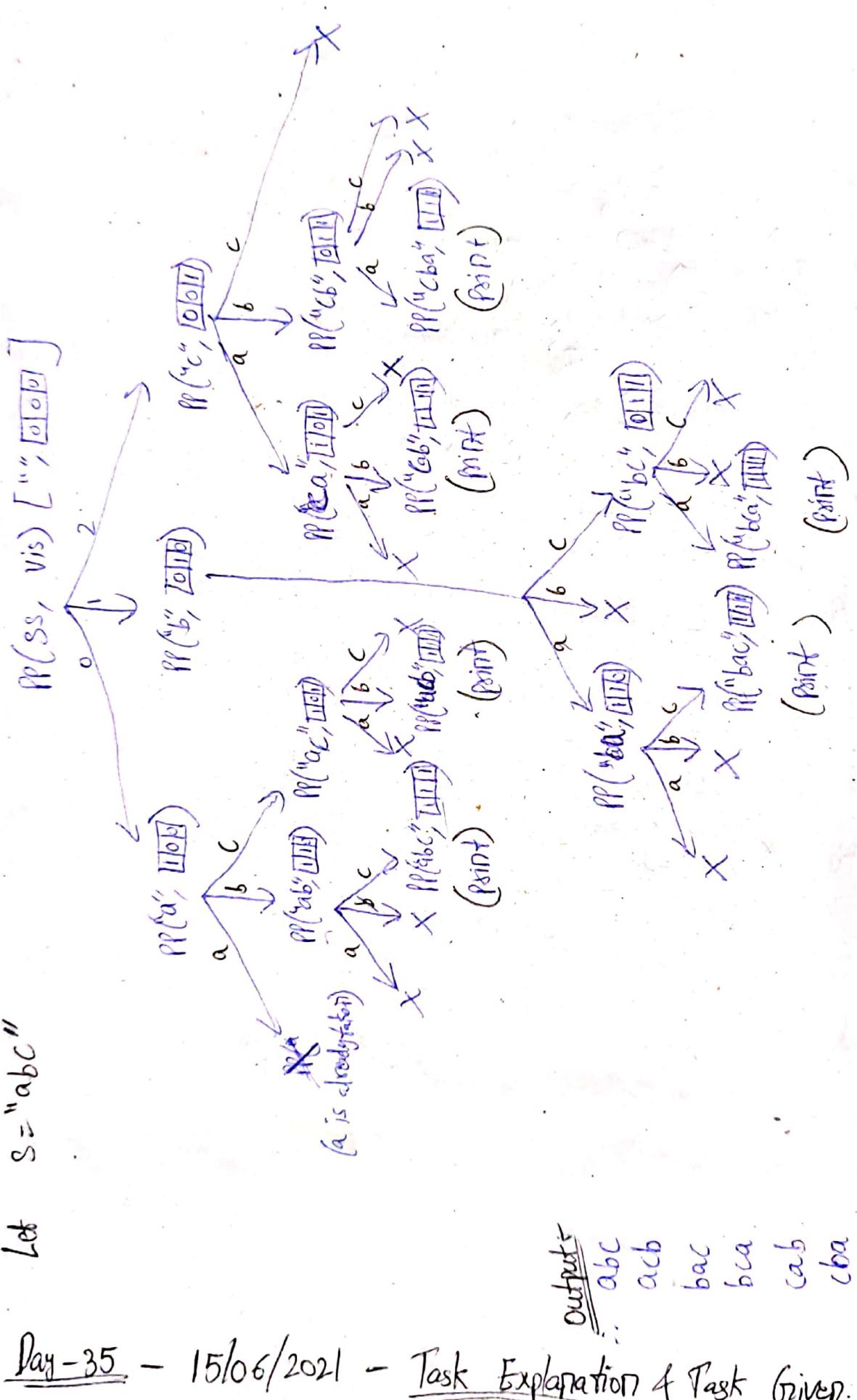
$func(ss, vis);$

$vis[i] = 0;$

}

}

Let $S = "abc"$



Day-35 - 15/06/2021 - Task Explanation & Task Given

Day-36 - 16/06/2021 - Kadane's Algorithm

1. Task explanation (Maximum Subarray - LeetCode)

ex: [-1, 2, -3, 4, -5]

To find in $O(n)$ using single loop (Kadane's algorithm)

Taking two variables

Max_so_far = INT_MIN

Tracing

Max_up_to = 0

index	0	1	2	3	4
Max_up_to (before i)	-1	2	-1	4	-1
Max_so_far	-1	2	2	4	4
Max_up_to (after i)	0	2	0	4	0

Loop \rightarrow i to n

$\text{Max_upto} += a[i];$

if $\text{Max_upto} > \text{Max_so_far}$

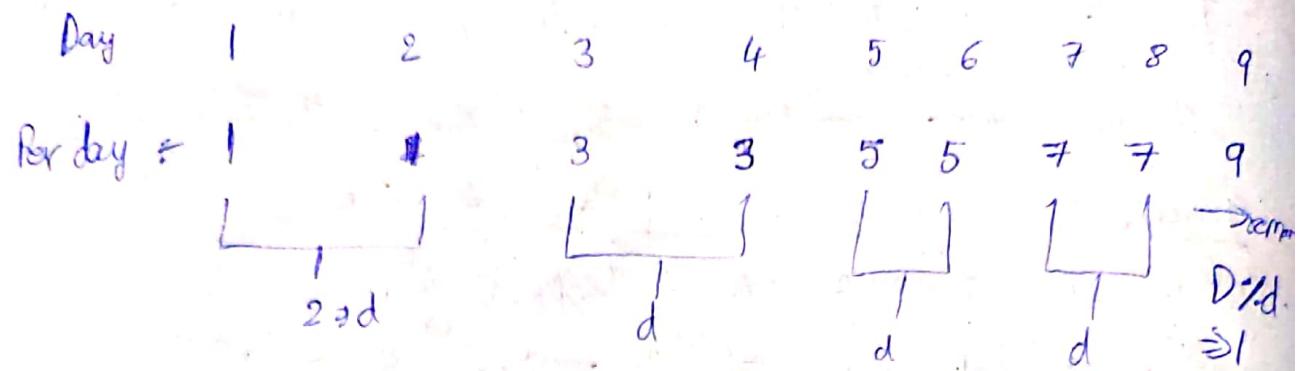
$\text{Max_so_far} = \text{Max_upto}$

if $\text{max_upto} < 0$

$\text{Max_upto} = 0$

Codective task

Let $D=9$, $d=2$, $P=1$, $Q=2$.



$$d \times [P + (P+Q) + (P+2Q) + (P+3Q)] / D/d$$

Series in AP \Rightarrow sum of series $\Rightarrow \frac{n}{2} (2a + (n-1)d)$

$D = D/d$: we have D/d distinct series.

$$\therefore \text{res} = d * [D/d * (2*P + (D/d-1)*Q)] / 2;$$

but there is remaining 9th day.

\therefore For remaining days, $\text{res} = (D-d) * (P+n*Q)$;

\therefore Complete formula is

$$\text{res} = d * [n * (2*P + (n-1)*Q) / 2] + [(D-d) * (P+n*Q)]$$

or we can write on if condition for D/d to check equals to 0 or not and we can reduce time.

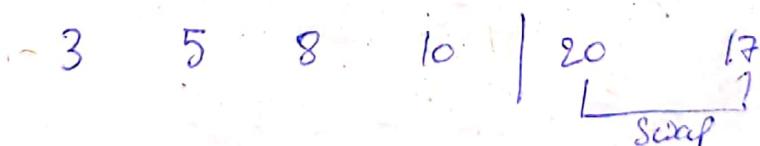
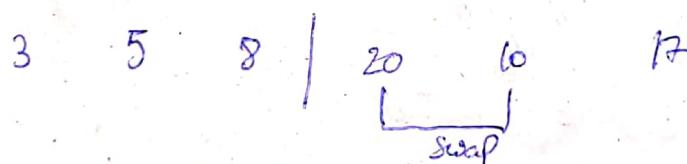
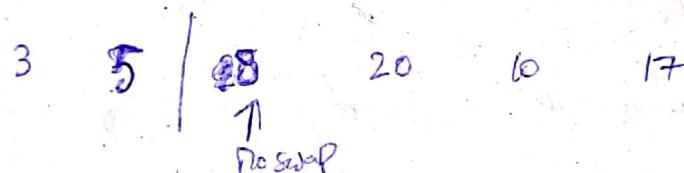
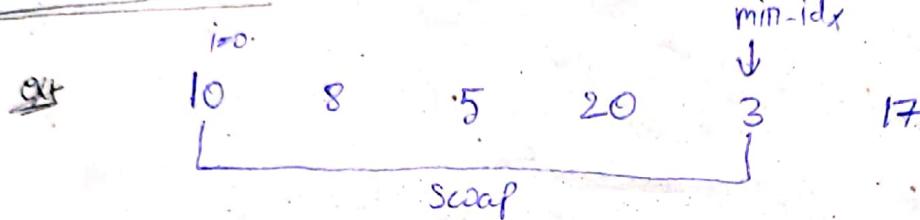
Day-38 - 18/06/2021 - Sorting

* Bubble Sort: Explained on Day 24.

Bubble sort is the stable sort.

Ex: 6 6 6 8 , then these are equal elements and it doesn't swaps.

* Selection Sort:



3 5 8 10 17 20

Pseudo-code

```
for (i=0 → n-1)  
    min-idx = i  
    for (j = i+1 → n)  
        if (arr[j] < arr[min-idx])  
            min-idx = j  
    swap(arr[i], arr[min-idx])
```

* Selection sort is not stable since it changes the positions are changed for repeated elements.

Day-39 - 19/06/2021 - Sorting.

*Insertion Sort:

Ques $a = \{20, 5, 40, 60, 10, 30\}$

unsorted

20 5 40 60 10 30
Sorted

Step.

5 20 40 60 10 30
Sorted

5 20 40 60 10 30
Sorted unsorted

5 20 40 60 10 30
Sorted unsorted

By checking 20 with all, we move 20 to 60 to right.

5 10 20 40 60 30
Sorted unsorted

5 10 20 30 40 60.

Pseudo code

```
for (int i=1; i<n; i++)
```

```
    int key = arr[i];
```

```
    int j = i-1;
```

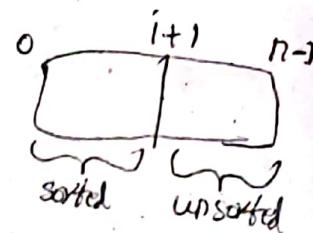
```
    while (j >= 0 && arr[j] > key)
```

```
        arr[j+1] = arr[j];
```

```
        j--;
```

```
    arr[i+1] = key.
```

Note: It is also a stable sort.



Merge Sort

It follows Divide & Conquer algorithm.

ex:-

arr = {2, 1, 5, 6, 3}

o 1 2 3 4

DAC

l=0

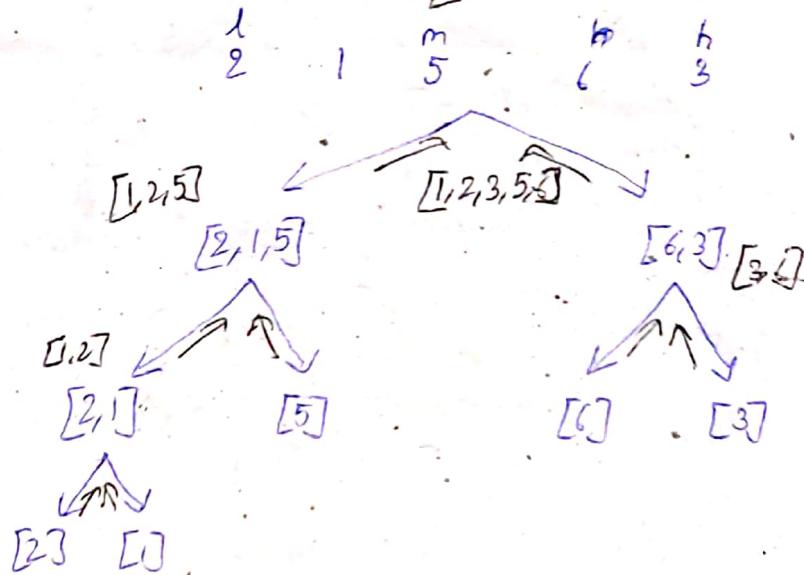
h=n-1

m=(l+h)/2

Complexity

divide into two $\Rightarrow O(\log_2 n) \Rightarrow O(n \log n)$

To merge n elements $\Rightarrow O(n)$



Then by checking left pointer and right pointer values, we can conquer after dividing.

Merge function

// Starting points for two sub arrays

left = low, right = mid+1.

while (left <= mid && right <= high)

if (arr[left] < arr[right])

vector.push_back(arr[left])

left++;

else

vector.push_back(arr[right])

right++;

// To copy remaining elements if
while (left <= mid) | remaining
remaining

vec.push_back(arr[left])

left++;

while (right <= high)

vec.push_back(arr[right])

right++;

Sort function

if (low = high)

return;

mid = (low+high)/2

sort (low, mid, arr)

sort (mid+1, high, arr)

merge (low, mid, high, arr)

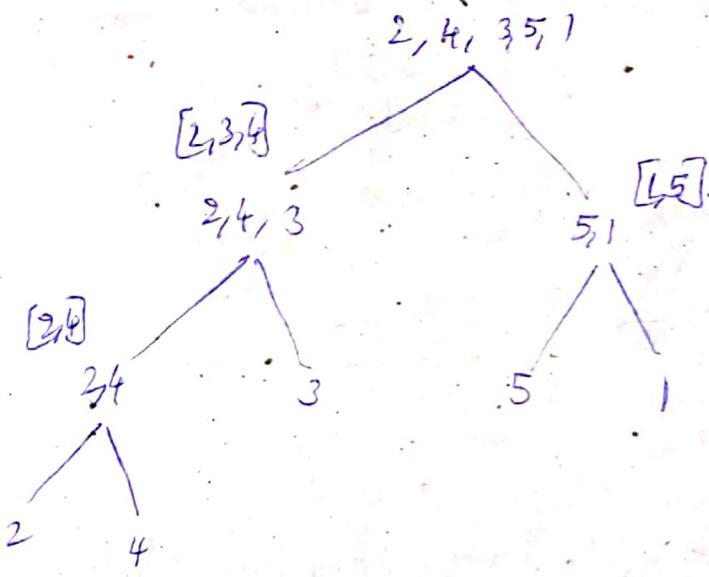
// Finally insert sorted elements to array.

for (int i=low; i<=high; i++)

arr[i] = vector[i-(low)].

1. Leetcode - ~~reverse fix~~ Local and global conversions.

Take $2, 4, 3, 5, 1$



At first, 2, 4 and 3, 2 < 3 & latter.

$4 > 3$ \Rightarrow count = 1.

Similarly.

$\frac{L}{2, 3, 4}$ mid

R
1, 5

* Here

$2 > 1 \Rightarrow 2, 3, 4$ are sorted array now and all can form a pair with 1. \Rightarrow we add the $\boxed{\text{mid-left} + 1}$ to count.

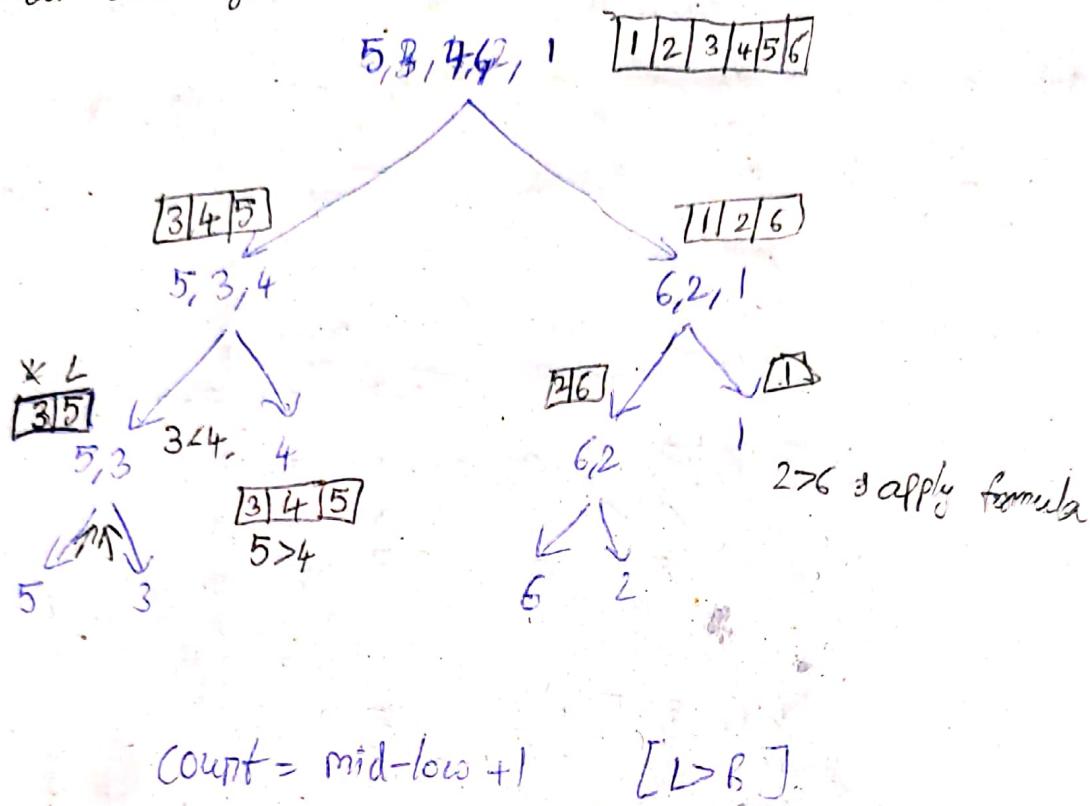
\Rightarrow count $\leftarrow 3$ [Value equals].

* Now we compare with R+1, i.e. 5 and check until we get the less than within loop.

* By using conditions, we can increase either local or global. Now if global = 0, then return true else false.

Day-41 - 23/06/2021 - Problems on MergeSort

1. Local and global conversions



At final,



$L > R \Rightarrow$ all in left array would be greater as it is sorted.



similar to above.



Here $3 < 6 \Rightarrow L++$, $4 < 6 \Rightarrow L++$, $5 < 6$ (no change)

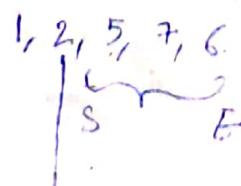
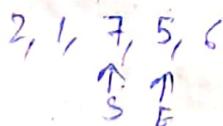
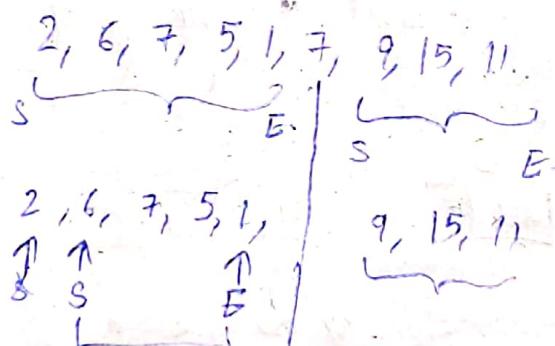
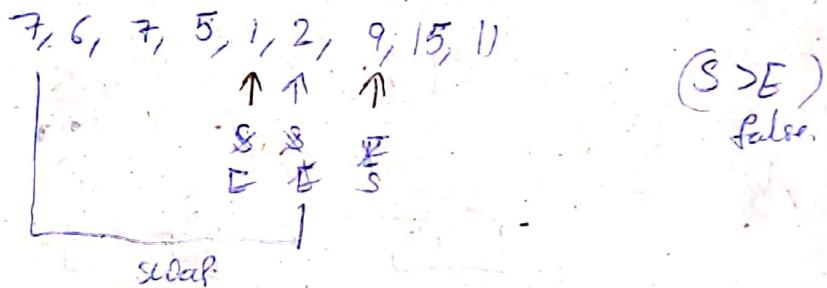
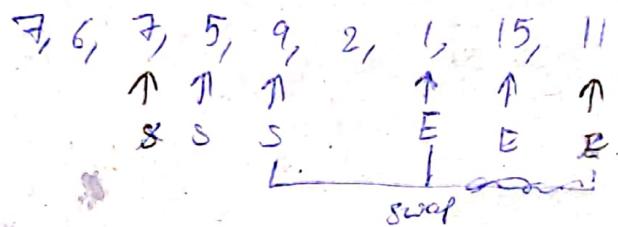
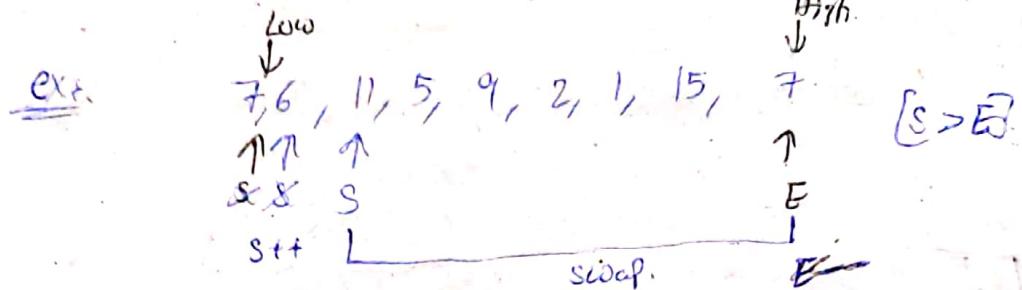
Finally sorted. and count will be 11.

Contd...

Quick Sort

$$Q.S = \{10, 12, 2, 3, 8, 15, 11\}$$

We take one element as pivot. and sort using it.



Similarly works in the recursion.

* Linear Search

Loop from 0 to $n-1$ elements.

Loop $i \rightarrow 0$ to n

if ($a[i] == \text{target}$)

break;

Complexity is $O(n)$. But can be applied on any type.

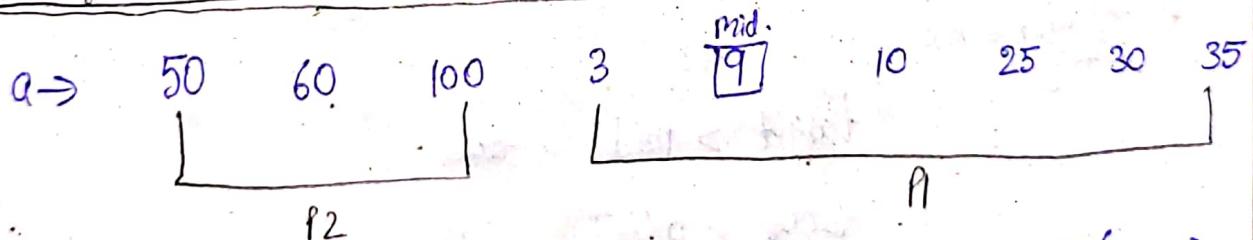
* Binary Search

By taking mid values and checking.

Complexity is $O(\log n)$ but can be applied on sorted array.

We can take $\text{low} + \frac{(\text{high}-\text{low})}{2}$ [$\gg 1$].

Because of very large numbers.

* Binary search on Rotated Sorted array

if ($a[\text{mid}] == \text{target}$) return mid ;

else if ($a[\text{mid}] > a[\text{low}]$) // exists in part 1.

if ($a < 50$)

if

else if ($\text{target} > a[\text{mid}] \text{ || target} < a[\text{low}]$) // in part 2

$\text{high} = \text{mid} + 1;$

if ($\text{target} \geq a[0]$) // in part 2 [also] // $\text{target} < a[\text{mid}]$

$\text{high} = \text{mid} - 1;$

else

$\text{low} = \text{mid} + 1;$

Day -43

- 25/06/2021 - Binary Search for rotated sorted array

	Part-1				Part-2				
index	0	1	2	3	4	5	6	7	8
array	50	60	100	3	9	10	25	30	35

Low

mid

High

$$\text{mid} = ((\text{Low} + \text{High})/2),$$

if ($\text{arr}[\text{mid}] == \text{target}$) return mid;

check target with mid if target > mid

check target with 0th element if target < 0th elem.

So target is in part 2 because the element less than 0th will be at right of part.

if (target > arr[mid]) if target < arr[0]

$$\text{low} = \text{mid} + 1;$$

② target > 0

$$\text{Now, } \text{mid} = (5+8)/2 = 6$$

arr[mid] = target [found at pos 6]

* Target = 100

target > mid true

target < arr[0] false.

$$\text{high} = \text{mid} - 1 = 3$$

$$\text{mid} = (0+3)/2 = 1.$$

Here they are at same part

$$\text{low} = \text{mid} + 1.$$

$$\text{mid} = (2+3)/2 = 2$$

arr[mid] = target.

* Target = 3 :

target \geq mid

high = mid - 1. = 3.

mid = 1

if (target \geq mid & target $<$ a[0]) abo.

loc = mid + 1.

mid = 2

target \geq mid & target $<$ a[0]

loc = mid + 1.

mid = 3

arr[3] = target

found at pos 3.

Day-44 26/06/2021 - Task Explanation

1. Leet code Sort colors

* By counting 1's & 2's & 0's and append to a new array or vector and add those using while loop.

2 1 1 2 0 1 0
L
m
h

if $m > 2$

swap(m, h)

$h--;$

$m=0$

swap(m, L)

$m++;$

$L++;$

$m=1$

$m++;$

swap(m, L)

0 1 1 2 0 1 2

m

L

h

0 1 1 2 0 1 2

L $\xrightarrow{m \rightarrow m}$ h

0 1 1 0 2 2

L m h

m++

0 1 1 0 2 2

L m h

0 0 1 1 1 2 2

2. Task n^{th} magical number in leetcode.

$a=2, b=4, n=5$. 2, 4, 6, 8, 10, 12.

L m h

The seq will be from $\text{low}(a, b)$ to $\text{min}(a, b)$.

If $a=4$, $b=6$, $n=4$.

in the loop.

$$\begin{array}{ccccccc} 4 & 6 & 8 & 12 & 16 \\ \downarrow & & & & & & \end{array} \quad | \quad c = \frac{mid}{a} + \frac{mid}{b} - \frac{mid}{\text{lcm}(a,b)}$$

Here $c = 3 \Rightarrow \text{nums}[c] = 12$.

$$\text{Mid} = (l+h)/2 = 10.$$

if ($c == n$)

 if ($m \% a == 0 \text{ || } m \% b == 0$)

 return mid;

 else if ($c < n$)

 low = mid + 1;

 else

 high = mid - 1;

* Allocation of books: The maximum pages allocated should be minimum.

Rules:

- * A book will be allocated to only one student.
- * Each student min of 1 book.
- * Allocation should be in a continuous order.

exs $n=4$, $a = \{12, 34, 67, 90\}$, $sf=2$.

<u>S1</u>	<u>S2</u>	
12	34, 67, 90	if $\max = 191$
12, 34	67, 90	if $\max = 157$
12, 34, 67	90	if $\max = 113$ minimum possible

Pseudo code:

int low = min(array)

int high = max(array)

int ans = -1

while (low <= high)

mid = (low+high) // 2;

if (is possible (array, mid, students))

ans = mid;

high = mid-1;

else .

low = mid+1;

return ans;

bool is possible (array[], barrier, std)

{ int count = 0;

int sumalloc = 0;

for (int i=0; i<n; i++)

{ if (sumalloc + array[i] > barrier)

count++;

sumalloc = array[i];

if (sumalloc > barrier)

return false;

}

else {

sumalloc += array[i];

}

if (count > std)

return false;

return true;

* Range problem

If $a = \{20, 15, 17, 34, 67\}$

If we give queries (number) and low & high,

$$\begin{array}{ll} \text{Low} & \text{High} \\ 1 & 3 \end{array} = 66 \quad [\text{sum}]$$

$$\begin{array}{ll} 0 & 4 \end{array} = 153$$

$$\begin{array}{ll} 2 & 3 \end{array} = 51$$

Brute force

* To use this algorithm, complexity is $O(n^2)$, in worst case, $n=10^6$, $2=10^6 \Rightarrow O(n^2) \Rightarrow O(10^{12}) \Rightarrow \text{TLE}$

Fittle optimised

* We can solve using binary search but it also gives TLE.

Highly optimised (Using Prefix Sum)

By creating prefix array = $\{20, 35, 52, 86, 153\}$

Now to get sum from 2 to 3, we have to

remove 0th sum because our sum should contain element at 1.

But we have to check for 0th index because 0th is first, so if we remove 1 from 0, it becomes -1.

\therefore if ($\text{low} == 0$)

return prefix[high];

return prefix[high] - prefix[low-1];

In worst, $O(2 \times n)$

$\Theta(O(n+2))$

Day-47 - 07/07/2021 - Prefix Sum Algorithm

$$a = \{2, 6, 1, 4, 8, 7\}$$

Queries + left right num

iOS-base:: sync-with-stream
cin.tie(NULL);
Use to make fast input.

$$0 \quad 4 \quad 2 \text{ [add]} \quad [4, 8, 3, 6, 10, 7]$$

$$1 \quad 3 \quad 5 \quad [4, 13, 8, 11, 10, 7]$$

$$4 \quad 5 \quad 1 \quad [4, 13, 8, 11, 11, 8]$$

Adding the number from left to right to all each like above example.

By using brute force, we will get a TLE.

Optimized:

2	5			-4	-3	-2	-1
0	1	2	3	4	5	6	

add K at arr[left], -K at arr[right+1]

∴ To get prefix array,

2	7	7	7	3	1	0
0	1	2	3	4	5	6

So by adding this prefix array to array, we get the resultant array.

Day -48 - 02/07/2021 - GFG Equilibrium Point

If $a = \{1\}^{n=1}$, output = 1 [only one element, position returned]

If $a = \{1, 3, 5, 2, 2\}^{n=5}$, op = 3 [$1+3=4, 2+2=4$ & return 5 pos]

Brute force

If $n \neq 1$, the 1st element and last element cannot be the equilibrium points.

in for $i \rightarrow 1$ to $n-1$

for $j \rightarrow 0$ to i

Left sum += arr[j];

for $j \rightarrow i+1$ to n

Right sum += arr[j];

if (Left sum == Right sum)

return $i+1$;

return -1;

Optimized: (Prefix Sum)

Prepare a prefix array.

if ($n=1$) return 1
if ($n=2$) return -1;

for (int $i=1$; $i < n-1$; $i++$)

if (prefix[i] == prefix[n-1] - prefix[i])

return $i+1$;

return -1;

Prefix.

Here if 1, 3, 5, 2, 2 is array, 1, 4, 9, 11, 13

Here if $i=2$, prefix[$i-1$] = 4 [sum upto $i-1$],

prefix[n-1] - prefix[i] = 13 - 9 = 4 [sum from $i+1$ to n]

Day-49 - 03/07/2021 - GFG Explanation (Coding Contest)

Day-50 - 05/07/2021 - Subarray Sums equals k (Prefix sum)

4	-2	-1	1	-2	3	-3
---	----	----	---	----	---	----

Prefix 4 2 1 2 0 3 0 $a=0$.

$$x=4$$

$$x-a =$$

Take a map with

key as elements of prefix and
value as count.

if (Prefix[i]-k) is in dict(map).

count += dic[^{Prefix[i]}Prefix-k]

dic[Prefix]++;

Day - 51 - 06/07/2021 - Subarray sum divisible by k (prefix sum)

Let $\{4, 5, 0, -2, -3, 1\}$. $k = 5$.

$4 \rightarrow 4$	$5 \rightarrow \underline{5}$	$0, -2, -3 \rightarrow \underline{-5}$
$4, 5 \rightarrow 9$	$5, 0 \rightarrow \underline{5}$	$0, -2, -3, \cancel{1} \rightarrow -4$
$4, 5, 0 \rightarrow 9$	$5, 0, -2 \rightarrow 3$	$-2 \rightarrow -2$
$4, 5, 0, -2 \rightarrow 7$	$5, 0, -2, -3 \rightarrow \underline{0}$	$-2, -3 \rightarrow \underline{-5}$
$4, 5, 0, -2, -3 \rightarrow 4$	$5, 0, -2, -3, 1 \rightarrow 1$	$-2, -3, 1 \rightarrow 4$
$4, 5, 0, -2, -3, 1 \rightarrow 5$	$0 \rightarrow \underline{0}$	$-3, 1 \rightarrow -2$
	$0, -2 \rightarrow -2$	$-3 \rightarrow -3$
		$1 \rightarrow 1$

count = 7.

Brute force :-

By writing three loops, we can calculate each subarray sum and check if it is divisible by k.

* It gives TLE.

optimised (Prefix sum) :-

Prefix array is 4 9 9 7 4 5. $k = 5$.

count = 0/3/6/7

$4 \% 5 = 4$ $9 \% 5 = 4$ $9 \% 5 = 4$ $7 \% 5 = 2$ $4 \% 5 = 4$ $5 \% 5 = 0$

$dic[\text{sum}]++;$

$\left. \begin{array}{l} \text{equal} \\ 9-4=5 \end{array} \right\} 5 \times 5=0 \text{ divisible}$

key	value
0	12
4	1234
2	1

$4 \% 5 = 4$.

$4 \% 5 = 4$. \Rightarrow incn.

$5 \% 5 = 0$

Count + = $\text{Prefix}[\text{sum}]$.

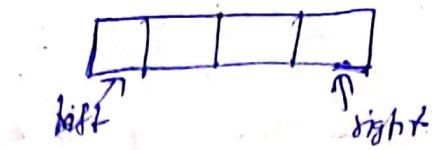
Note:-

In CPP, if we execute $-9 \% 5$ gives -4 & $-1 \% 5 = -1$
But in Python, $-9 \% 5$ is 1 & $-1 \% 5$ is 4 .

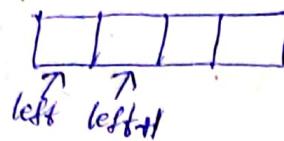
So we have to do $(-9 \% 5) + 5$ because we have to get the positive keys for our map. $\boxed{[x \% K] + K}$

Day-51 - 07/07/2021 - Two pointer

Opposite direction +



Uni direction +



Day-52 - 09/07/2021 - Two pointer

Move zeroes (Leetcode) +

Let $\text{nums} = \{0, 1, 0, 3, 12\}$

we have to move all zeroes to last without changing order of others.

$\text{nums} = \{1, 3, 12, 0, 0\}$ will be output

\boxed{b}

0, 1, 0, 3, 12

\boxed{s}

\boxed{t}

[E - for zero elements]
[S - for non-zero elements]

swap (E, S).

\boxed{E}

1, 0, 0, 3, 12

\boxed{S}

\boxed{T}

swap

\boxed{E}

1, 3, 0, 0, 12

\boxed{S}

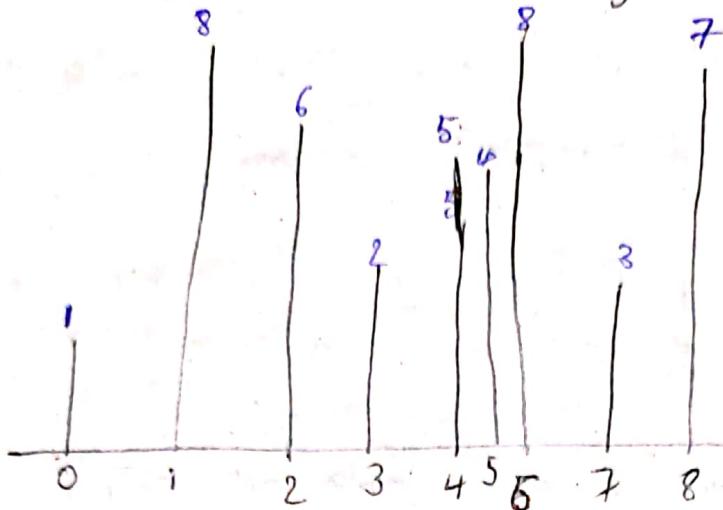
\boxed{T}

swap

1, 3, 12, 0, 0 . result.

Container with most water (Leetcode).

$$\{1, 8, 6, 2, 5, 4, 8, 3, 7\}$$



$$\text{formula} = (l - o) \times \min(l, o). \text{ like that.}$$

We can take start at 0^{th} , end at 8^{th} .

$$\therefore \text{formula} = (E - S) \times \min(\text{nums}[E], \text{nums}[S]).$$

if $\text{nums}[E]$ is less

$E--$

else

$S++$

$$\text{We get } \max(8-1) \times 7 = 49.$$

To get all primes less than n

Create an array of length $n+1$. (ex $n=25$).

$a[0], a[1] = 0$. [\because not prime] all are 1's.

0	0	1	1	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24

We check from 2 and make all of multiples 0.

3 and make all $3 \cdot \dots \cdot 0$.

4 is already 0 so ignore.

5 and make all of multiples 0.

until \sqrt{n} ; here $\sqrt{25} = 5$ so we can stop.

Now we get, 2 3 5 7 11 13 17 19 23
are primes.

2. Take vector<bool> sieve($N+1$, true) [$\because N$ is number, initially all are prime]

sieve[0] = false

sieve[1] = false

for(int i=2; i*i <= N; i++) {

if (sieve[i]) {

for(int j=i*i; j <= N; j+=i) {

sieve[j] = false;

}

}

}

Note: We take $j = i*i$ but for 3*2 is already false, 5*2, 5*3 will already be false, so we check from $i*i$.

Number of Primes (HackerEarth)

We can create a prefix, we can count easily if given queries. else we can count in Sieve array.

Day - 55 - 14/07/2021 - Finding Prime factors.

Create Sieve

	2		2	2	3	2	2	2	3	2	2	2	2	2	2	2
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16

↑ ↑

We change all like this.

Now for $100 \rightarrow \text{sieve}[100] = 2$. add 2 to factors,

$$100/\text{sieve}[100] = 50 \quad " 2.$$

$$50/\text{sieve}[100] = 25 \quad " 5 \text{ at } [25]$$

$$25/\text{sieve}[100] = 5 \quad " 5 \text{ at } [5].$$

$$5/\text{sieve}[100] = 1.$$

we get 1 so get out of loop.

$2 \times 2 \times 5 \times 5$ are factors

$$\text{sieve}[0] = \text{sieve}[1] = 0.$$

```
for(int i=2; i<=N; i++) sieve[i] = i;
```

```
for(int i=2; i<=sqrt(N); i++)
    if(sieve[i] == i) {
        for(int j=i*i; j<=N; j+=i) //only primes can be inserted.
            if(sieve[j] != i) //if not equal, we can't change it
                sieve[j] = i;
```

Day - 56 - 15/07/2021 - Sieve problems

I. Sum of primes

We can generate sieve and also a prefix array taking $\text{sums}[0] = \text{sums}[1] = 0$.

for $i \rightarrow 2$ to N

if ($\text{sieve}[i]$)

$\text{sums}[i] = \text{sums}[i-1] + i;$

else

$\text{sums}[i] = \text{sums}[i-1];$

$\text{sums}[i] = \text{sums}[i-1];$

(ii)

for $i \rightarrow 2$ to N

$\text{sums}[i] = \text{sums}[i-1]$

+ $i * \text{sieve}[i]$

if sieve is 0, not added.

Now we can return

$\text{sums}[\text{end}] - \text{sums}[\text{start}-1]$

where start is starting prime ; end is ending prime.

We take $\text{start}-1$ because we have to use start value also in the sum to get complete sum [inclusive $[\text{start}, \text{end}]$]

Day - 57 - 16/07/2021 - Strings

Day - 58 - 17/07/2021 - Strings

Day - 59 - 18/07/2021 - Strings

Day - 60 - 19/07/2021 - Strings

Day - 61 - 20/07/2021 - Strings

Array :-

array < int, len > a;

a.fill(10); // inserts 10 at all index values of a.

We can access elements using the methods of vector.

Day-63 - 27/07/2021

Set: Collection of unique elements in a sorted order.

set < int > st;

* We can use insert(), emplace() [faster]. We cannot use index.

* We can iterate as same as vector.

* st.erase(iterator1, iterator2); both are inclusive iterators.

* st.clear(); clears the set completely.

* Any set function takes $O(\log n)$.

Unordered set :-

* Same as set but unsorted set.

* unordered_set < int > st;

Multiset:

* multiset < int > mt;

* Stores multiple occurrences in a sorted manner.

* mt.count(item) // to find no. of occurrences of an element.

Map :-

* Key \rightarrow Value pairs. [sorted keys and unique keys]

* can insert using mp.emplace(key, val);

* Time complexity $O(\log n)$

Unordered Map

- * Same as map but unsorted. $\text{unordered_map} < \text{int, int} \text{ data}$
- * Time complexity in most case $O(1)$ but in worst $O(n)$

Multimap

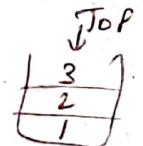
- * Same as map but takes duplicate keys. $\text{multimap} < \text{int, int} \text{ data}$

Pair class

- * $\text{pair} < \text{int, int} \rangle \quad \text{pr} = \{1, 2\};$
- * $\text{pr}.first;$ $\text{pr}.second;$
- * We can nest a pair inside a pair.

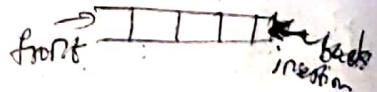
Stack

- * $\text{stack} < \text{int} \rangle \text{ stk}; \rightarrow \text{Last In First Out}$
- * st.push(val);
- * st.pop();
- * $\text{st.top();} \rightarrow \text{returns last inserted.}$
- * $\text{st.empty();} \rightarrow \text{returns empty or not.}$



Queue

- * $\text{queue} < \text{int} \rangle \text{ qu}; \rightarrow \text{First In First Out}$
- * qu.push(val);
- * $\text{qu.pop();} \rightarrow \text{removes front.}$
- * qu.front();



Priority Queue

- * $\text{priority_queue} < \text{int} \rangle \text{ pq}; \rightarrow \text{Stores in reverse.}$
- * pq.push(val);
- * pq.pop();
- * pq.top();



Day-65 - 29/07/2021 - Stack & Queue implementation.

Day-66 - 31/07/2021 - Queue implementation

Day-67 - 02/08/2021 - BFS Algorithm

BFS Algorithm

① Implement Queue

② Try out all the combinations

③ When reach the end, stop.

Problem

1. Given start, end, array.

The least combination of multiplication of numbers to get from start to end. use $\times 10000$ to get limited values.

Let start = 2, end = 24, arr = {2, 3, 4, 6}.

$$2 \times 2 = 4$$

$4 \times 6 = 24$ \rightarrow opt 2 [= least steps]

BFS

①

12,1
9,1
6,1
4,1
2,0

↑ ↑ step

$2 \times$ all elements, push to queue and make visited.

check all. if not visited, add to queue.
finally we get after 2, next queue front

Take Visited array

is 4.

0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	

already start

Now all combinations with 4, we get $4 \times 6 = 24$. is end.

now we reached end, steps at 24 are 2 is opt 2.

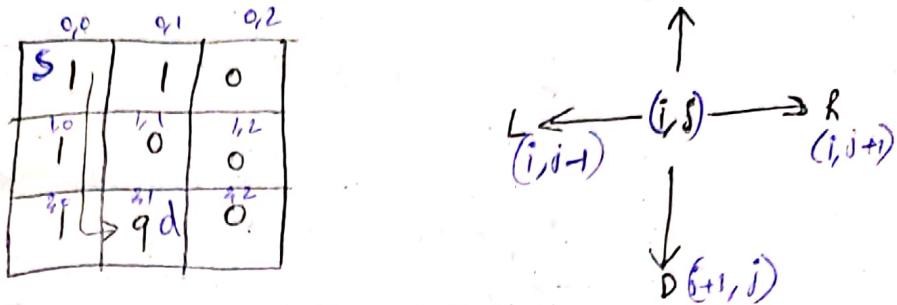
Code \rightarrow contd :-

```

int BFS(int start, int end, int arr[], int n) // n is length of arr
{
    int visited[100000] = {0};
    visited[start] = 1;
    queue<pair<int, int>> Q;
    Q.push({start, 0});
    while (!Q.empty())
    {
        int newstart = Q.front().first, steps = Q.front().second;
        Q.pop();
        for (int i=0; i<n; i++)
        {
            int res = (newstart + arr[i]) % 100000;
            if (res == end)
                return steps+1;
            if (!vis[res])
            {
                Q.push({res, steps+1});
                vis[res] = 1;
            }
        }
    }
    return -1;
}

```

Problem: To find the minimum path from store to home.
 If there is a store, there will be 1 else 0. destination is 9.



One can move in 4 ways. Top, bottom, left, right.

Now we will take a bool function isvalid to check whether the coordinate lies in grid or not and if the position is valid to move (1) or not. Then return true or false to make it valid path.

Then check if visited or not. if not visited, add to queue and make it visited.

Code:

```
Void amazon() // we can pass parameters here taking hard coded values
{
```

```
int matrix[3][3] = {{1, 0, 0}, {1, 1, 0}, {1, 9, 0}}, n=3, m=3;
```

```
queue < pair< pair< int, int>, int >> Q; [ Queue { {{1, 0, 0}, 1} } ]
```

```
if (matrix[0][0] == 0)
```

rate count

```
{
```

```
cout << -1;
```

```
return;
```

```
}
```

```
if (matrix[0][0] == 9)
```

```
{
```

```
cout << 0;
```

```
return;
```

```
{
```

```
Q.push({{0, 0, 0}, 0});
```

```
int vis[m][n];
```

```
memset(vis, 0, sizeof vis);
```

```

vis[0][0] = 1;
int di[] = {-1, 0, 1, 0};
int dj[] = {0, 1, 0, -1};
while (!Q.empty())
{
    int i = Q.front().first, first, j = Q.front().second, second;
    int steps = Q.front().second;
    Q.pop();
    for (int k = 0; k < 4; k++) // 4 ways T B L R
    {
        int newi = i + di[k];
        int newj = j + dj[k];
        if ((isValid(newi, newj, matrix) & !vis[newi][newj]))
        {
            cout << steps + 1;
            return;
        }
        vis[newi][newj] = 1;
        Q.push({{newi, newj}, steps + 1});
    }
}
cout <-1;
}

bool isValid(int i, int j, int matrix[3][3])
{
    if (i >= 0 & i < 3 & j >= 0 & j < 3 & matrix[i][j] != 0)
        return true;
    return false;
}

```

Day-69 - 05/08/2021 - Circle Broken

Find intersection points of two circles.



point all the possible points in the intersection region of two circles even on border.