

1. Yes, since $(CDE)^+ \rightarrow (CDEFABGHIJ)$ which is the entire set of attributes in R.
2. No, since $CD \subseteq CDE$ determines every attribute in RHS.
3. Consider $K = ABCDEFGHIJ$,
 $(K - J)^+ = R$, remove J from K
 $(K - I)^+ = R$, remove I from K
 $(K - H)^+ = R$, remove H from K
 $(K - G)^+ = R$, remove G from K
 $(K - F)^+ = R$, remove F from K
 $(K - E)^+ = R$, remove E from K
 $(K - A)^+ = R$, remove A from K
 $(K - B)^+ = R$, remove B from K
 $(K - C)^+ \neq R$, cannot remove C
 $(K - D)^+ \neq R$, cannot remove D
Hence, CD is a key.
4. Set of attributes not in RHS in G, $X = (C, D)$. Every Key of R w.r.t G constraints C and D.
Is (CD) a key? YES. We don't need to examine other combinations.

Observation In G, C^+ and D^+ determine two disjoint sets and together, they determine E , hence covering R.

Minimal FD

1. Singleton RHS

$F \rightarrow A$

$F \rightarrow B$

$CD \rightarrow E$

$C \rightarrow F$

$C \rightarrow G$

$H \rightarrow I$

$H \rightarrow J$

$D \rightarrow H$

2. Extraneous LHS attributes : None, since $C^+ = (F,G,A,B)$ and $D^+ = (H,I,J)$ are disjoint sets.

3. Remove Redundant FDs.

$CD \rightarrow E$ (non-redundant since $(CD)^+$ does not cover E if we remove the FD from G).

$C \rightarrow F$

$C \rightarrow G$

$H \rightarrow I$

$H \rightarrow J$

$D \rightarrow H$

$F \rightarrow A$

$F \rightarrow B$

5. C, D are prime attributes of R.
6. It is not in BCNF since LHS for every F in G is not a superkey. (Eg: $H \rightarrow IJ$)

7. It is not in 3NF since LHS for every F in G is not a superkey or the RHS is not always a prime attribute. (Eg: $H \rightarrow IJ$ and IJ are not prime attributes either.)
- 8 Let $D1 : CDE, D2 : CFG, D3 : DH, D4 : HIJ$, and $D5 : FAB$

In D1, $CD \rightarrow E$ is preserved. Similarly, in D2 : $C \rightarrow FG$, D3: $D \rightarrow H$, D4 : $H \rightarrow IJ$ and D5: $F \rightarrow AB$ are preserved. Considering the UNION of all these preserved dependencies, we get set G. Hence, the decomposition is dependency preserving in nature.

Table 1: Lossless Decomposition Check

	A	B	C	D	E	F	G	H	I	J
D1	a	a	a	a	a	a	a	a	a	a
D2	a	a	a			a	a			
D3				a				a	a	a
D4								a	a	a
D5	a	a				a				

Using the algorithm (1) as described in class, we observe a row with all distinguished variables after iteration 1 is in red and iteration 2 is in blue. Hence, the decomposition is lossless too.

Finally,

D1 is in BCNF since CD is a superkey.

D2 is in BCNF since C is a superkey.

D3 is in BCNF since D is a superkey.

D4 is in BCNF since H is a superkey.

D5 is in BCNF since F is a superkey.