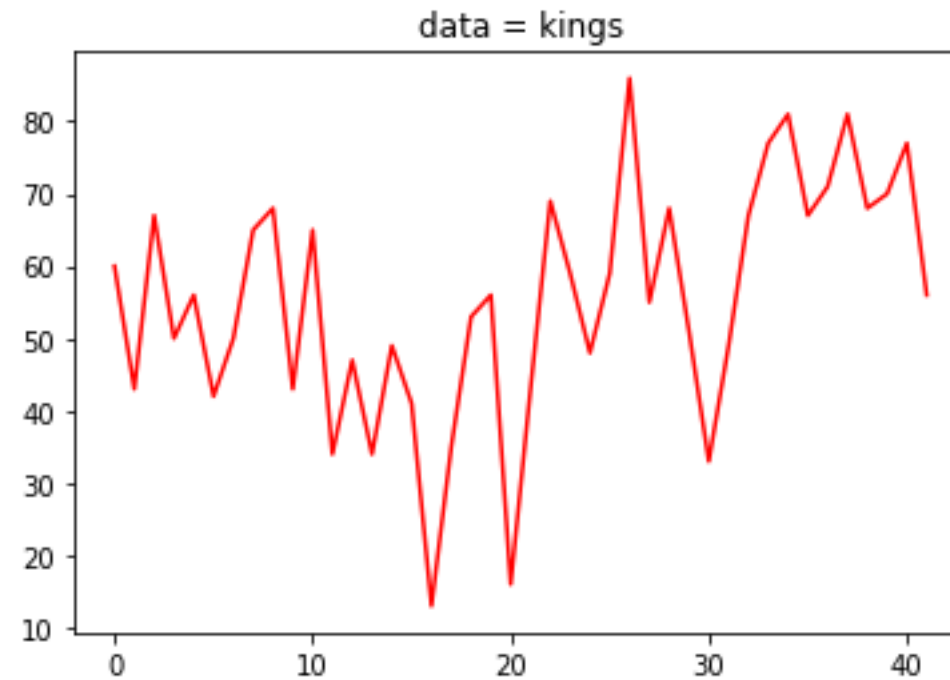
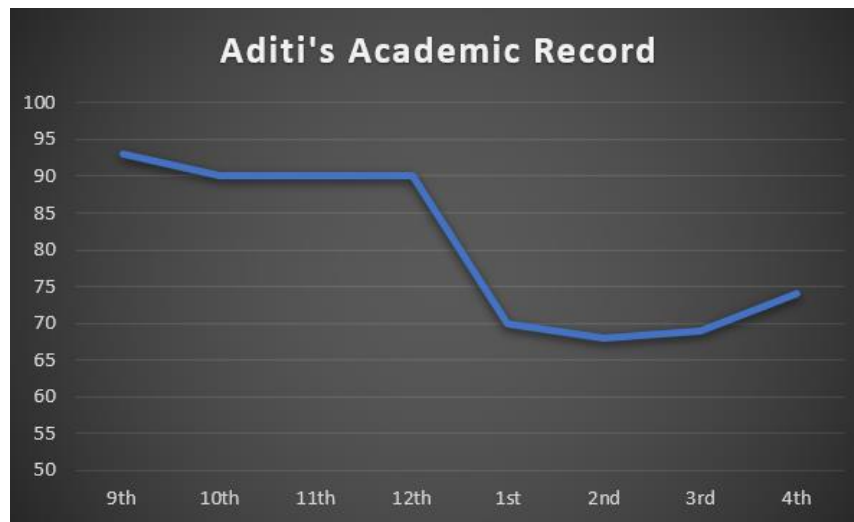


Time Series Concepts

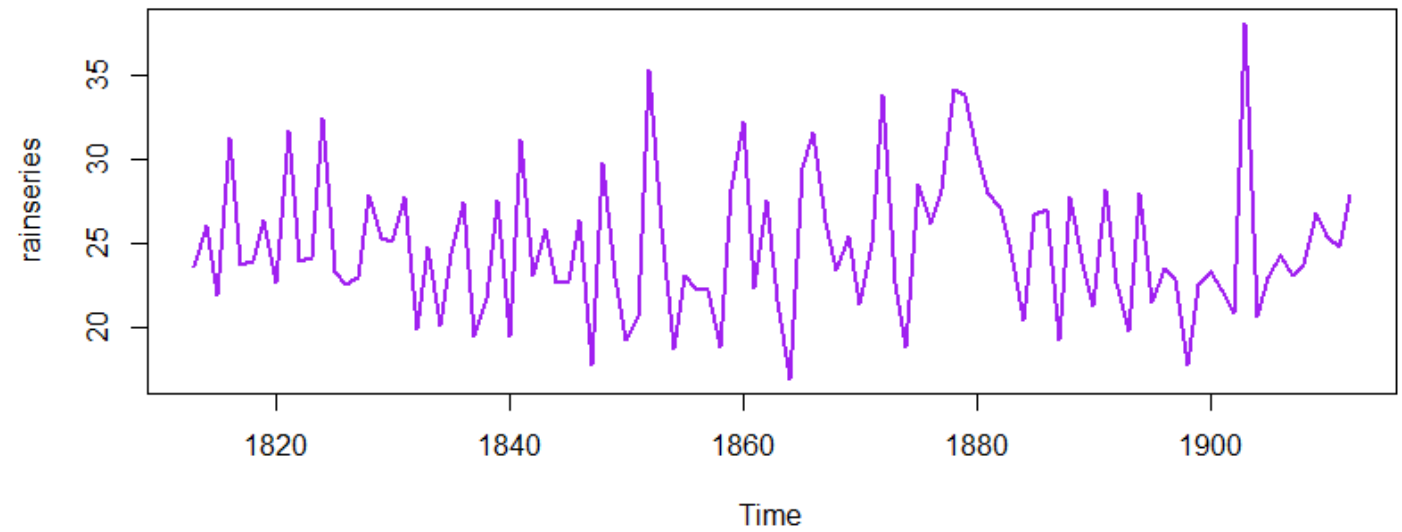
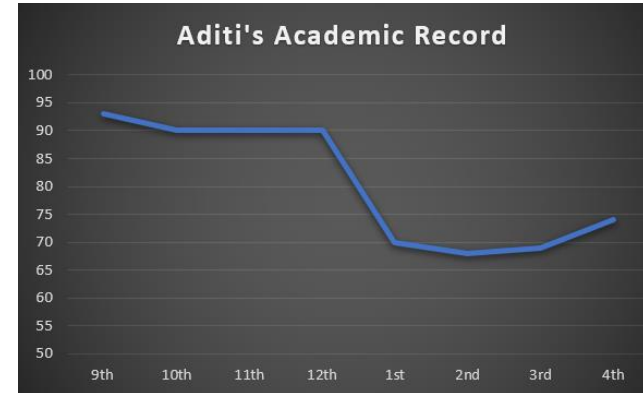
Data sets: kings, rain, births, skirts, sovenir

[illegible]

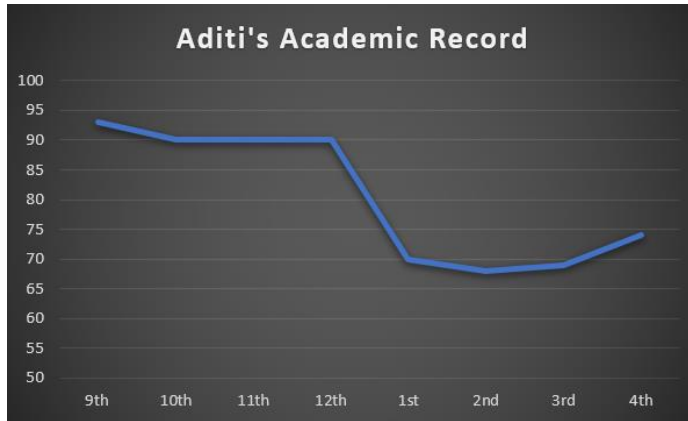
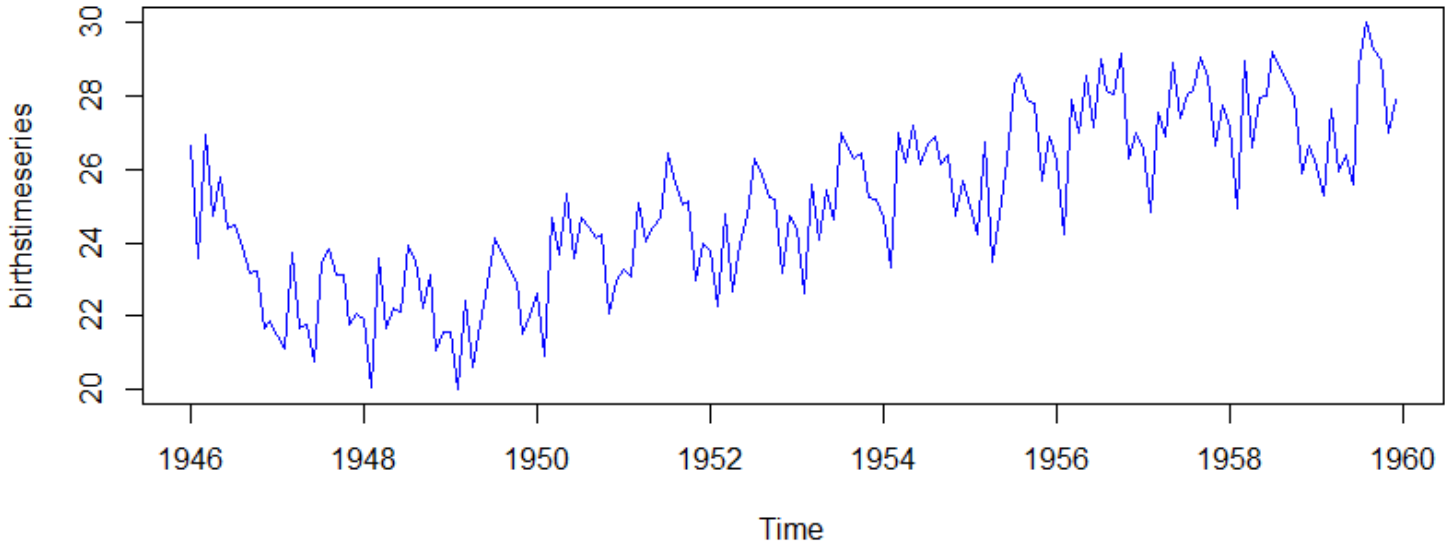
Data: kings



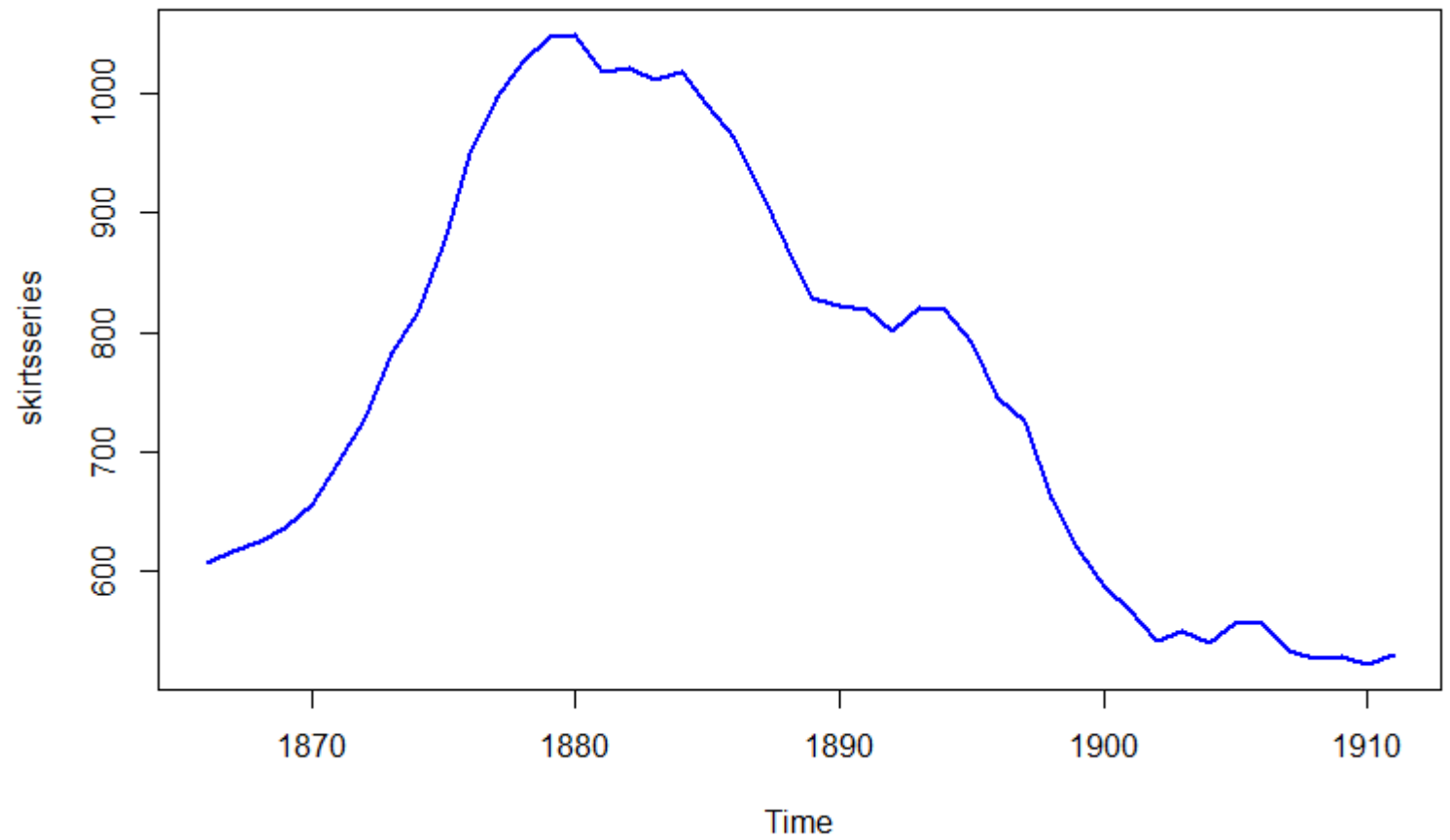
Data: rain

[illegible]

Data: births

[illegible]

Data: skirts

[illegible]

The graph displays the 'souveniritmeseries' over time. The y-axis, labeled 'souveniritmeseries', uses scientific notation ranging from 0e+00 to 1e+05. The x-axis, labeled 'Time', spans from 1987 to 1994. The series exhibits a clear upward trend with several prominent peaks. Notable spikes occur around 1988, 1990, 1991, 1992, and 1993. A particularly sharp and high peak is visible at the end of the period shown, around early 1994, reaching a value of approximately 1e+05.

Five data sets have been provided to you for applying the learnt concepts and see the difference in the results of different approaches!

Kings



Libraries

```
# Jesus is King of Kings!
import os
os.chdir('C:\\Users\\Dr Vinod\\Desktop\\WD_python')
import pandas as pd
pd.set_option('display.max_columns', None)
import numpy as np
import matplotlib.pyplot as plt
import statsmodels.api as sm
import statsmodels.formula.api as smf
from statsmodels.tsa.stattools import adfuller
%matplotlib inline
from math import sqrt
from statsmodels.tsa.arima_model import ARIMA
from sklearn.metrics import mean_squared_error
```



Import Data

```
kings = pd.read_csv('kings.csv')
kings.info() # 42
kings = kings.drop('obsno', axis=1)
kings.info()
kings.index #RangeIndex(start=0, stop=42, step=1)
```

```
In [7]: kings.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 42 entries, 0 to 41
Data columns (total 2 columns):
#   Column  Non-Null Count  Dtype
---  -
0   obsno   42 non-null      int64
1   age     42 non-null      int64
dtypes: int64(2)
memory usage: 800.0 bytes
```

```
In [9]: kings.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 42 entries, 0 to 41
Data columns (total 1 columns):
#   Column  Non-Null Count  Dtype
---  -
0   age     42 non-null      int64
dtypes: int64(1)
memory usage: 464.0 bytes
```

```
In [10]: kings.index #RangeIndex(start=0, stop=42, step=1)
Out[10]: RangeIndex(start=0, stop=42, step=1)
```



Plots

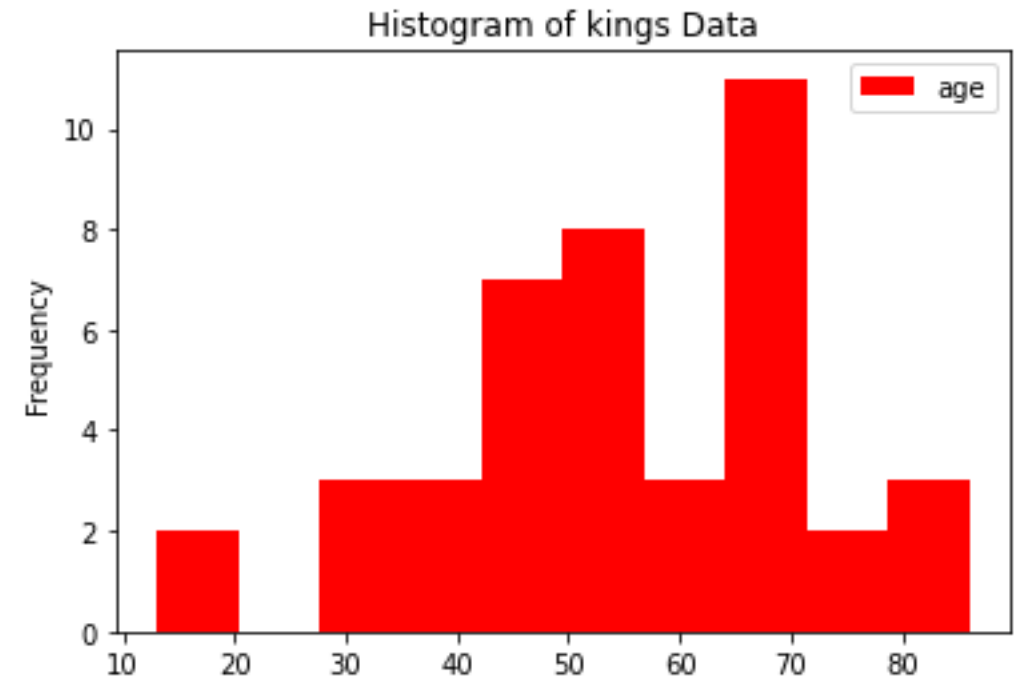
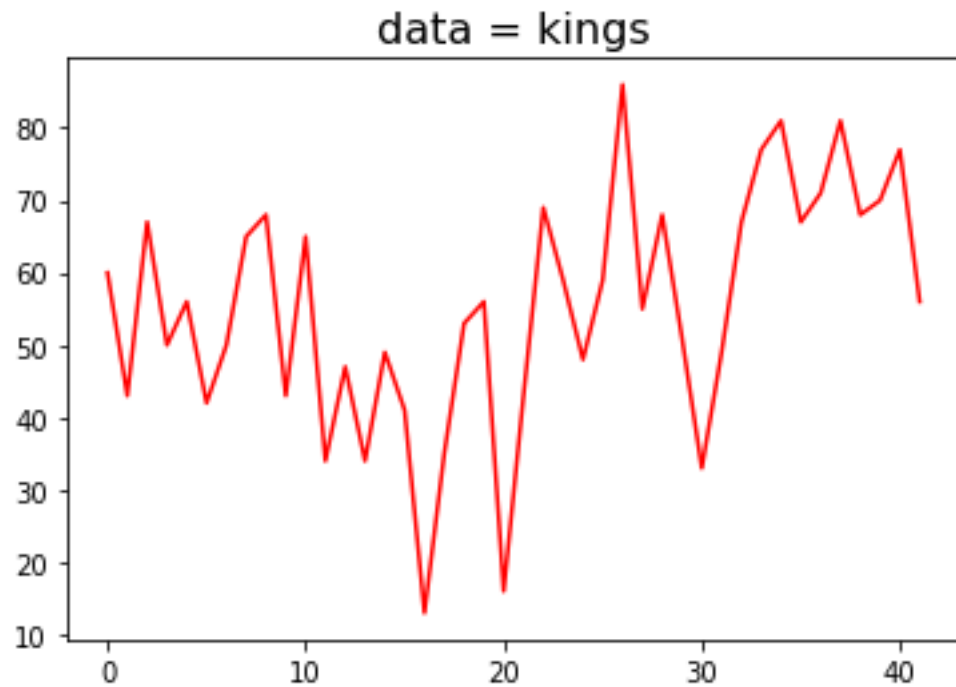


#lineplot

```
plt.plot(kings, 'r')  
plt.title('data = kings', fontsize=16)
```

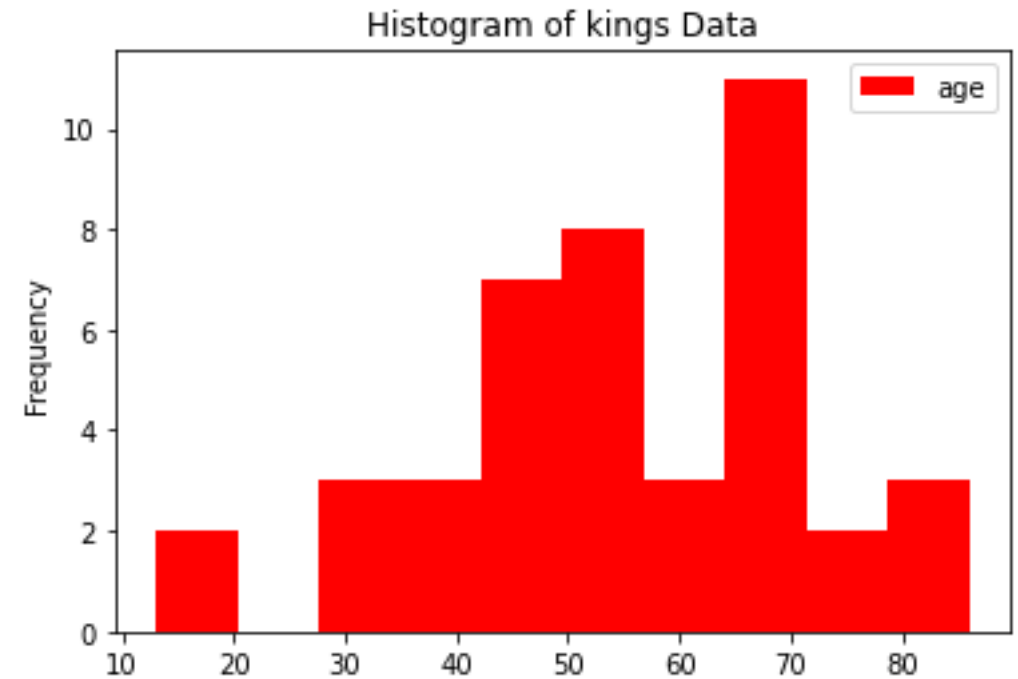
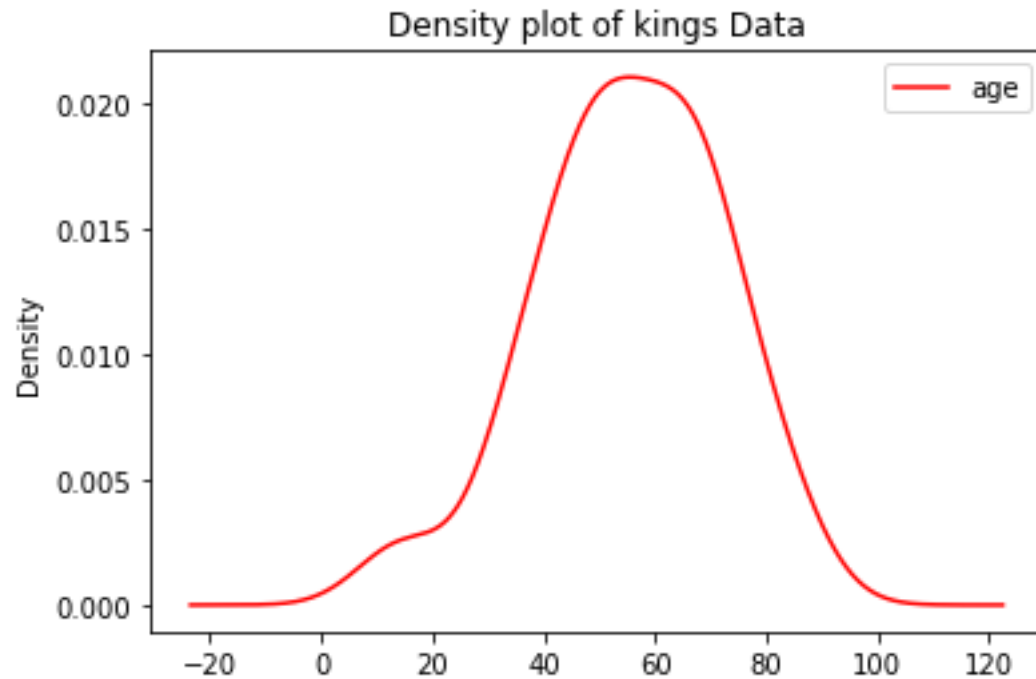
#Histogram

```
kings.plot(kind='hist', facecolor = 'r')  
plt.title('Histogram of kings Data')
```



Plots

```
#Density plot  
kings.plot(kind='kde', color = 'r')  
plt.title('Density plot of kings Data')
```

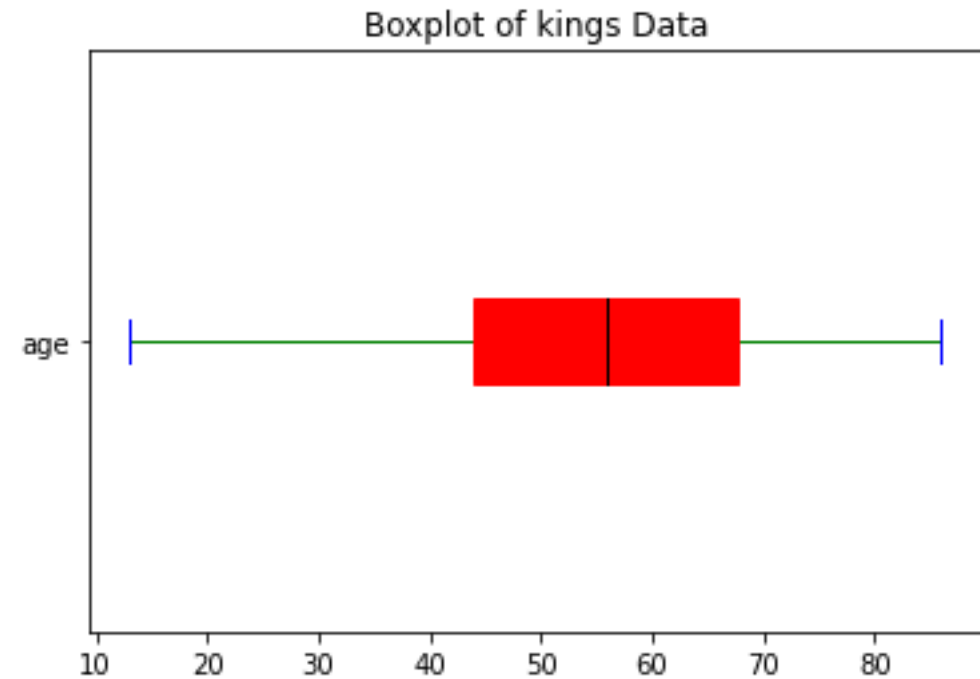
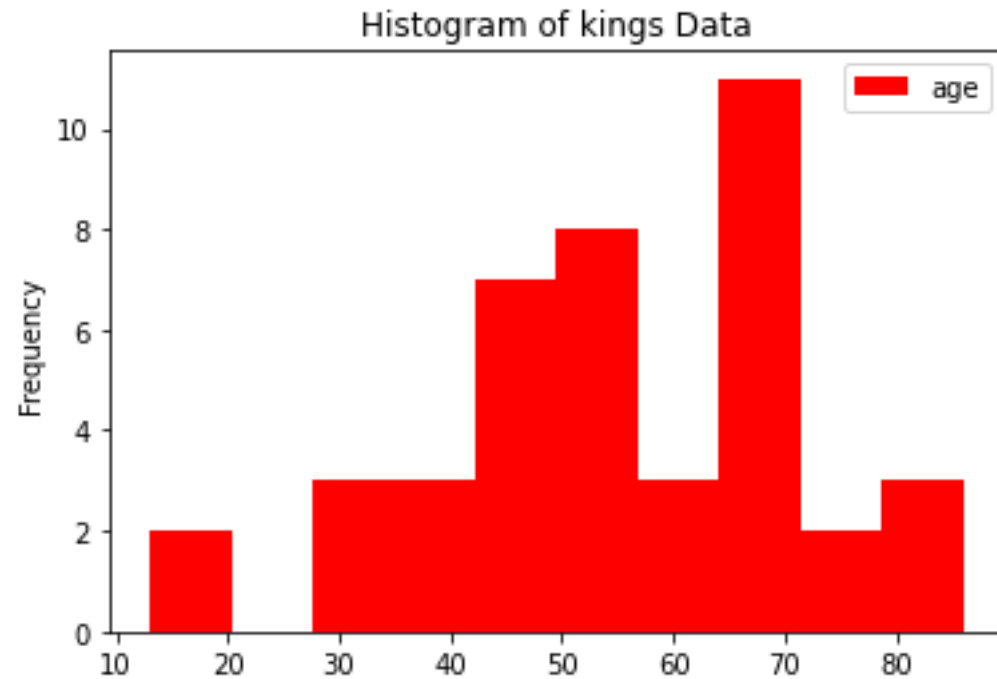


Box Plot



#Boxplot

```
props2 = dict(boxes = 'red', whiskers = 'green', medians = 'black', caps = 'blue')  
kings.plot.box(color = props2 , patch_artist = True, vert = False)  
plt.title('Boxplot of kings Data')
```



Decompose

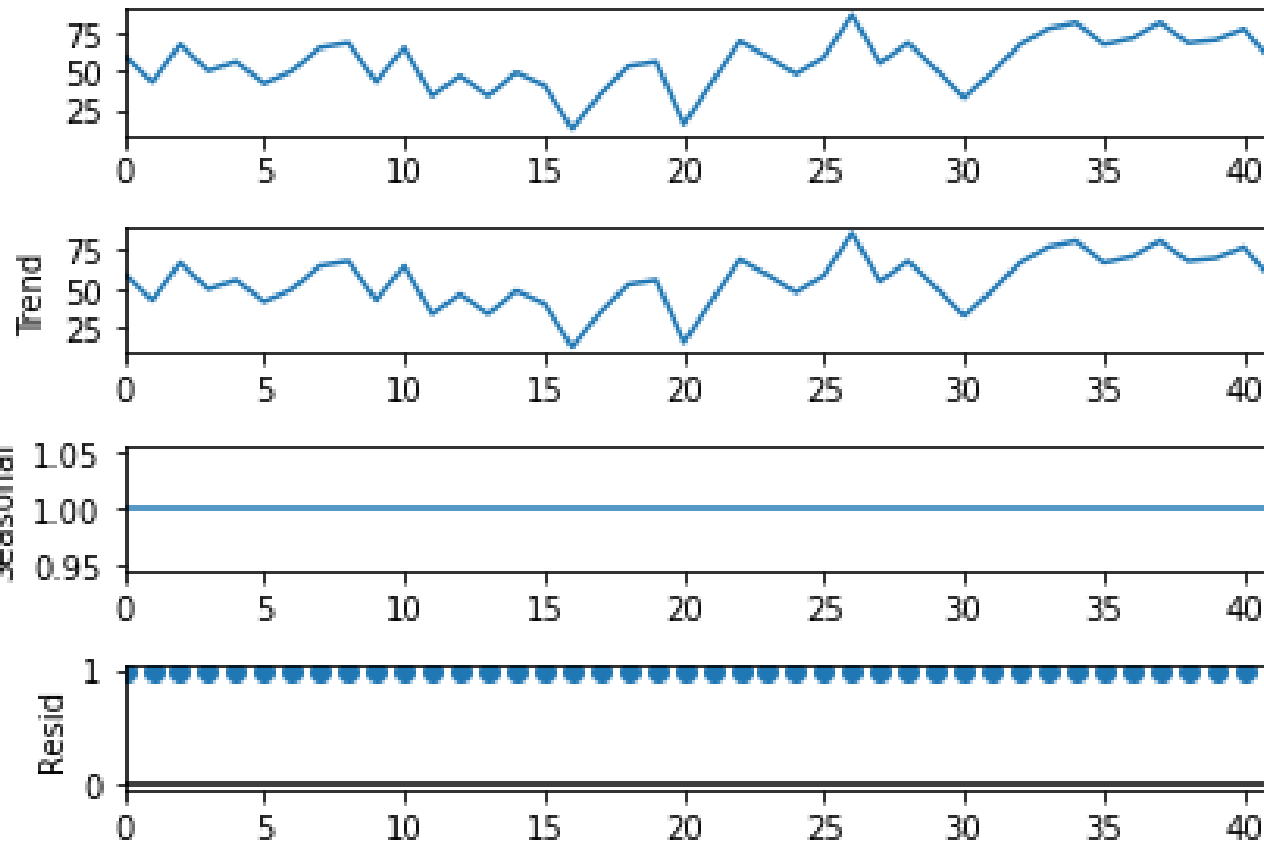


$Ts = t*s*r$
No seasonality
 $S = 1$

$Ts = t+s+r$
No seasonality
 $S = 0$

```
#Decompose with multiplicative
from statsmodels.tsa.seasonal import seasonal_decompose
kings_decomp_m = seasonal_decompose(kings, period=1, model='mul')
#Period is specified being the data is not having date as index
```

```
kings_decomp_m.plot() #No Trend & no seasonality; note 1
```



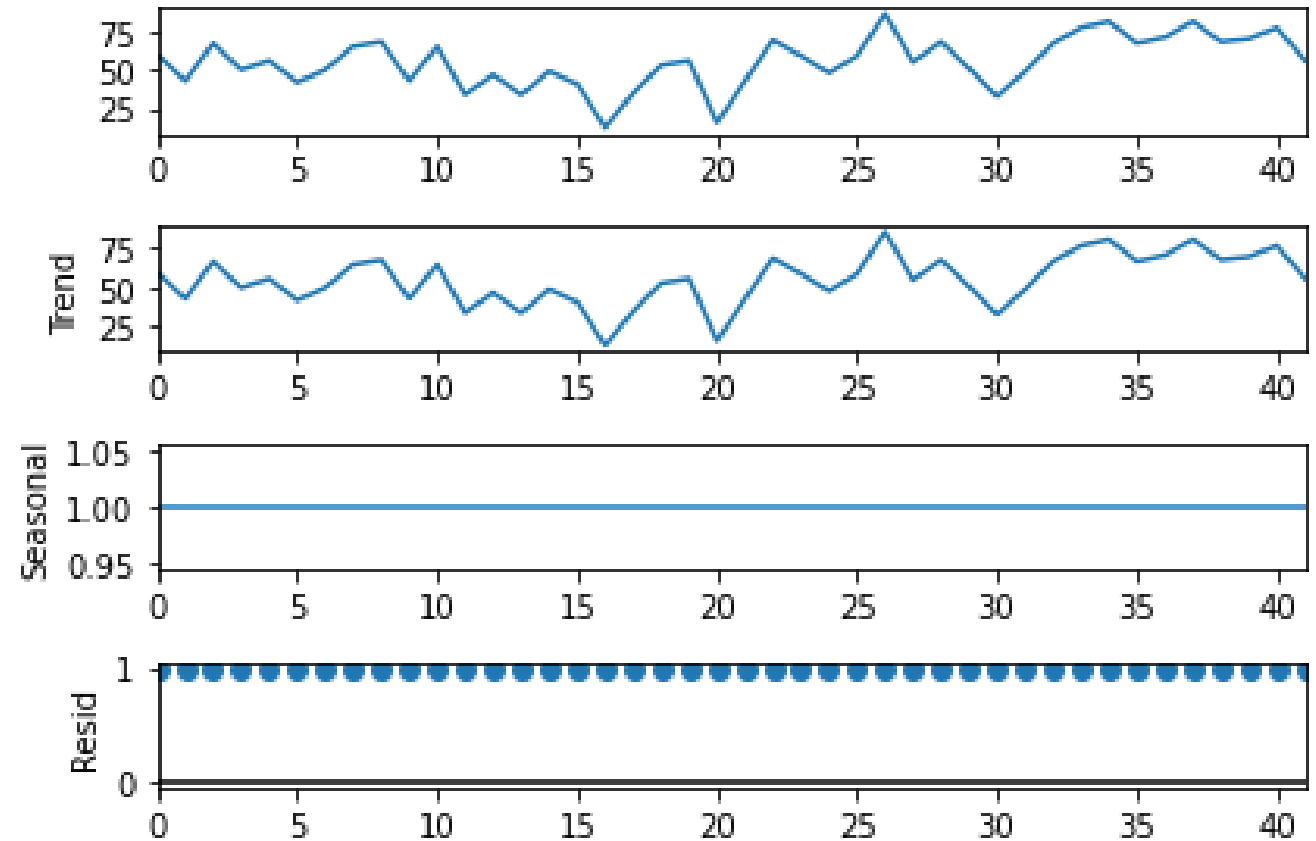
Observed

```
In [36]: kings_decomp_m.observed
```

```
Out[36]:
```

| | | | |
|----|------|----|------|
| 0 | 60.0 | 21 | 43.0 |
| 1 | 43.0 | 22 | 69.0 |
| 2 | 67.0 | 23 | 59.0 |
| 3 | 50.0 | 24 | 48.0 |
| 4 | 56.0 | 25 | 59.0 |
| 5 | 42.0 | 26 | 86.0 |
| 6 | 50.0 | 27 | 55.0 |
| 7 | 65.0 | 28 | 68.0 |
| 8 | 68.0 | 29 | 51.0 |
| 9 | 43.0 | 30 | 33.0 |
| 10 | 65.0 | 31 | 49.0 |
| 11 | 34.0 | 32 | 67.0 |
| 12 | 47.0 | 33 | 77.0 |
| 13 | 34.0 | 34 | 81.0 |
| 14 | 49.0 | 35 | 67.0 |
| 15 | 41.0 | 36 | 71.0 |
| 16 | 13.0 | 37 | 81.0 |
| 17 | 35.0 | 38 | 68.0 |
| 18 | 53.0 | 39 | 70.0 |
| 19 | 56.0 | 40 | 77.0 |
| 20 | 16.0 | 41 | 56.0 |

```
dtype: float64
```



Trend

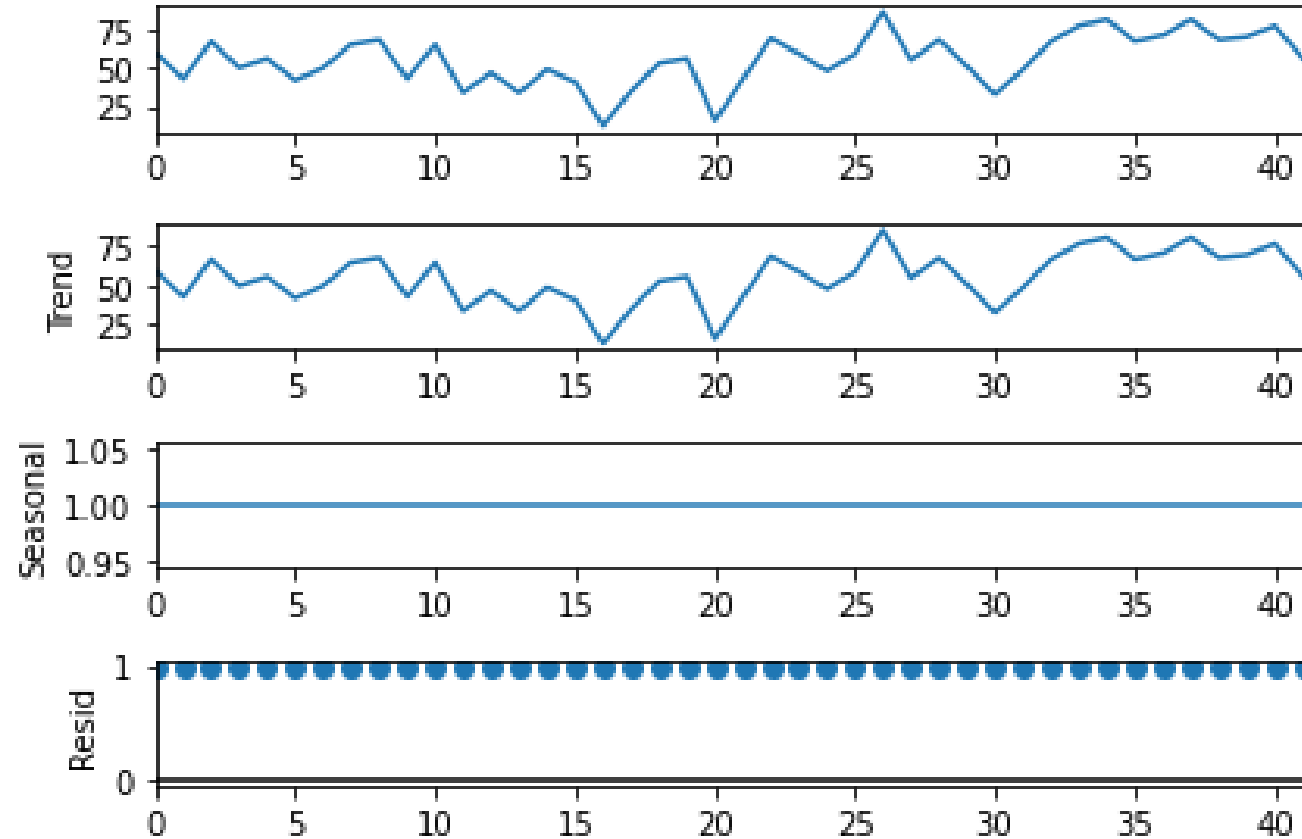


```
In [37]: kings_decomp_m.trend
```

```
Out[37]:
```

| | | | |
|----|------|----|------|
| 0 | 60.0 | 21 | 43.0 |
| 1 | 43.0 | 22 | 69.0 |
| 2 | 67.0 | 23 | 59.0 |
| 3 | 50.0 | 24 | 48.0 |
| 4 | 56.0 | 25 | 59.0 |
| 5 | 42.0 | 26 | 86.0 |
| 6 | 50.0 | 27 | 55.0 |
| 7 | 65.0 | 28 | 68.0 |
| 8 | 68.0 | 29 | 51.0 |
| 9 | 43.0 | 30 | 33.0 |
| 10 | 65.0 | 31 | 49.0 |
| 11 | 34.0 | 32 | 67.0 |
| 12 | 47.0 | 33 | 77.0 |
| 13 | 34.0 | 34 | 81.0 |
| 14 | 49.0 | 35 | 67.0 |
| 15 | 41.0 | 36 | 71.0 |
| 16 | 13.0 | 37 | 81.0 |
| 17 | 35.0 | 38 | 68.0 |
| 18 | 53.0 | 39 | 70.0 |
| 19 | 56.0 | 40 | 77.0 |
| 20 | 16.0 | 41 | 56.0 |

```
Name: trend, dtype: float64
```



Seasonal

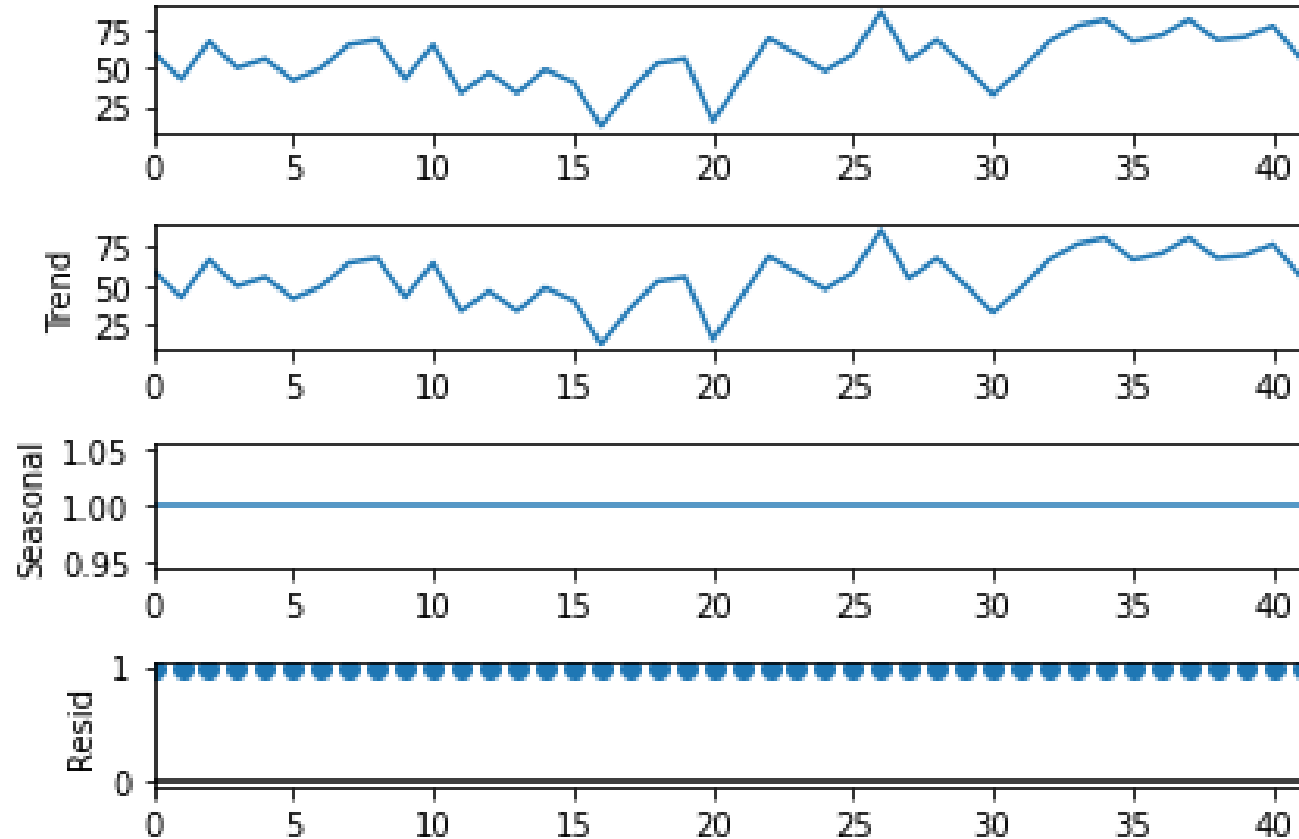


```
In [38]: kings_decomp_m.seasonal
```

```
Out[38]:
```

| | | | |
|----|-----|----|-----|
| 0 | 1.0 | 21 | 1.0 |
| 1 | 1.0 | 22 | 1.0 |
| 2 | 1.0 | 23 | 1.0 |
| 3 | 1.0 | 24 | 1.0 |
| 4 | 1.0 | 25 | 1.0 |
| 5 | 1.0 | 26 | 1.0 |
| 6 | 1.0 | 27 | 1.0 |
| 7 | 1.0 | 28 | 1.0 |
| 8 | 1.0 | 29 | 1.0 |
| 9 | 1.0 | 30 | 1.0 |
| 10 | 1.0 | 31 | 1.0 |
| 11 | 1.0 | 32 | 1.0 |
| 12 | 1.0 | 33 | 1.0 |
| 13 | 1.0 | 34 | 1.0 |
| 14 | 1.0 | 35 | 1.0 |
| 15 | 1.0 | 36 | 1.0 |
| 16 | 1.0 | 37 | 1.0 |
| 17 | 1.0 | 38 | 1.0 |
| 18 | 1.0 | 39 | 1.0 |
| 19 | 1.0 | 40 | 1.0 |
| 20 | 1.0 | 41 | 1.0 |

```
Name: seasonal, dtype: float64
```



Residuals

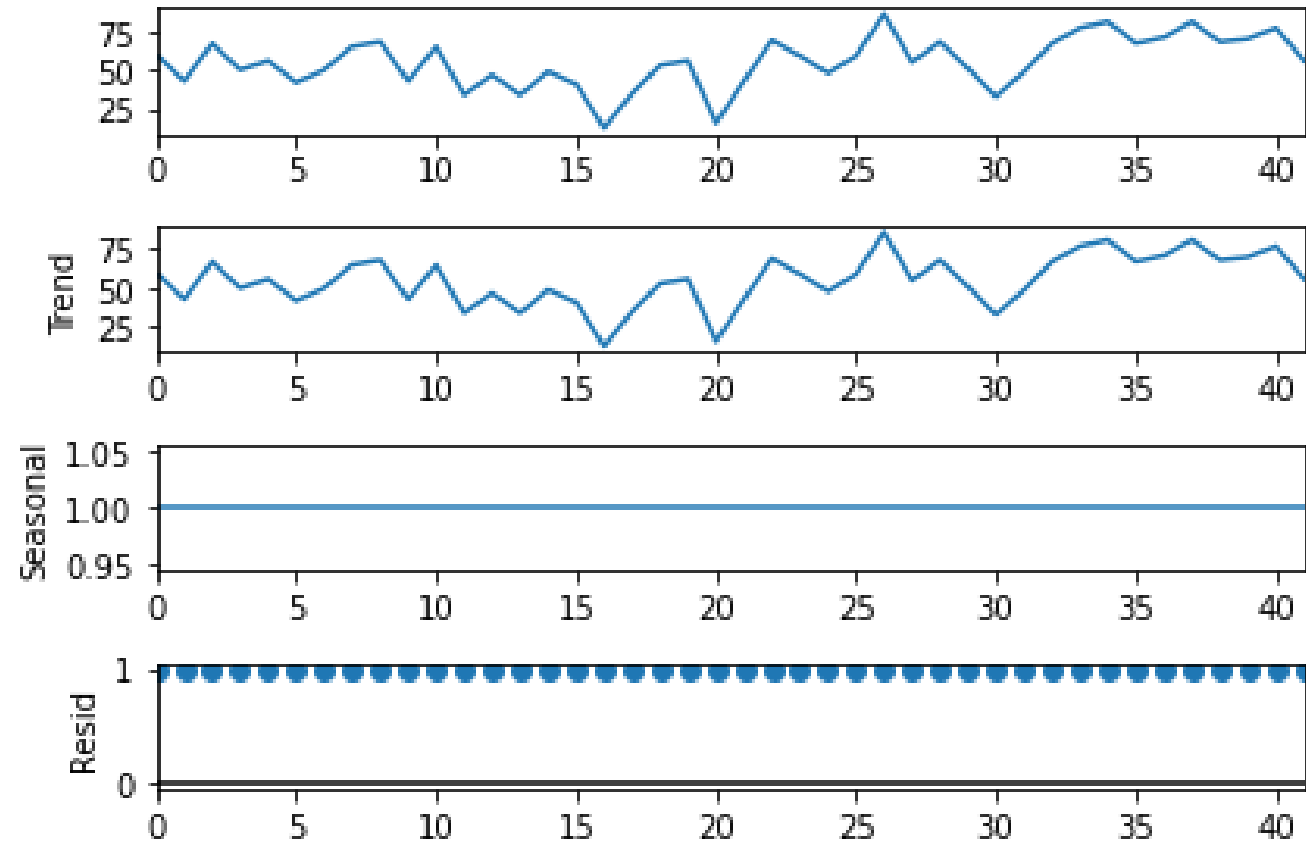


```
In [39]: kings_decomp_m.resid
```

```
Out[39]:
```

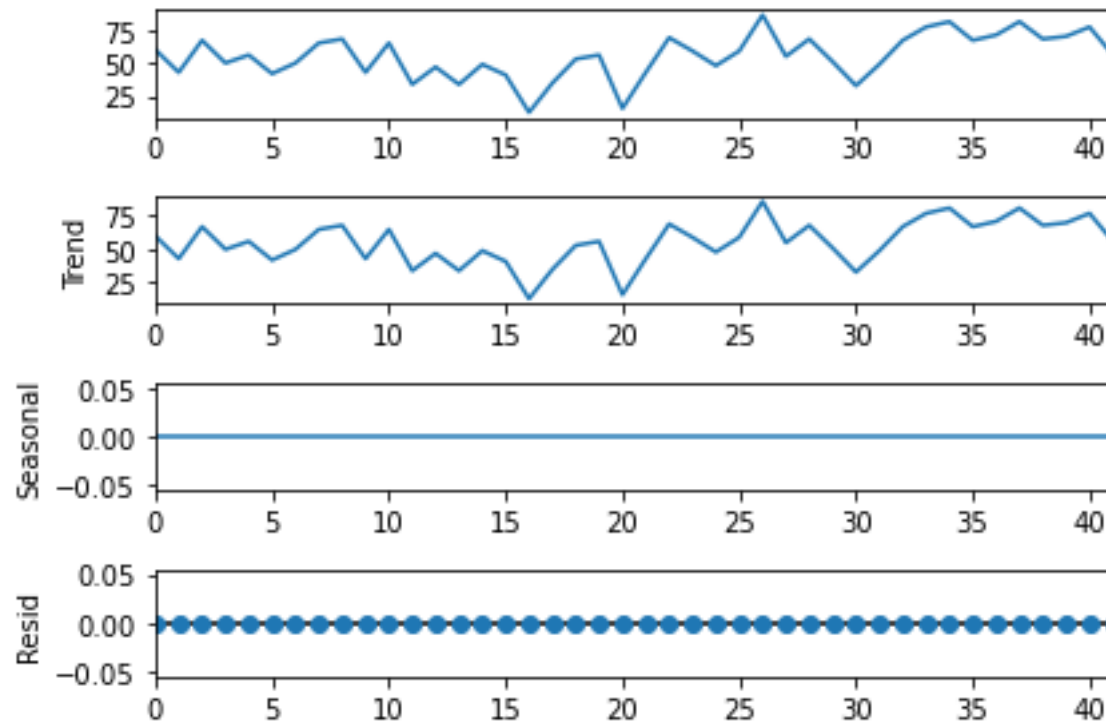
| | | | |
|----|-----|----|-----|
| 0 | 1.0 | 21 | 1.0 |
| 1 | 1.0 | 22 | 1.0 |
| 2 | 1.0 | 23 | 1.0 |
| 3 | 1.0 | 24 | 1.0 |
| 4 | 1.0 | 25 | 1.0 |
| 5 | 1.0 | 26 | 1.0 |
| 6 | 1.0 | 27 | 1.0 |
| 7 | 1.0 | 28 | 1.0 |
| 8 | 1.0 | 29 | 1.0 |
| 9 | 1.0 | 30 | 1.0 |
| 10 | 1.0 | 31 | 1.0 |
| 11 | 1.0 | 32 | 1.0 |
| 12 | 1.0 | 33 | 1.0 |
| 13 | 1.0 | 34 | 1.0 |
| 14 | 1.0 | 35 | 1.0 |
| 15 | 1.0 | 36 | 1.0 |
| 16 | 1.0 | 37 | 1.0 |
| 17 | 1.0 | 38 | 1.0 |
| 18 | 1.0 | 39 | 1.0 |
| 19 | 1.0 | 40 | 1.0 |
| 20 | 1.0 | 41 | 1.0 |

```
Name: resid, dtype: float64
```



```
#Decompose with Additive  
from statsmodels.tsa.seasonal import seasonal_decompose  
kings_decomp_add = seasonal_decompose(kings, period=1, model='add')  
  
kings_decomp_add.plot() #No Trend & no seasonality
```

Decompose _additive



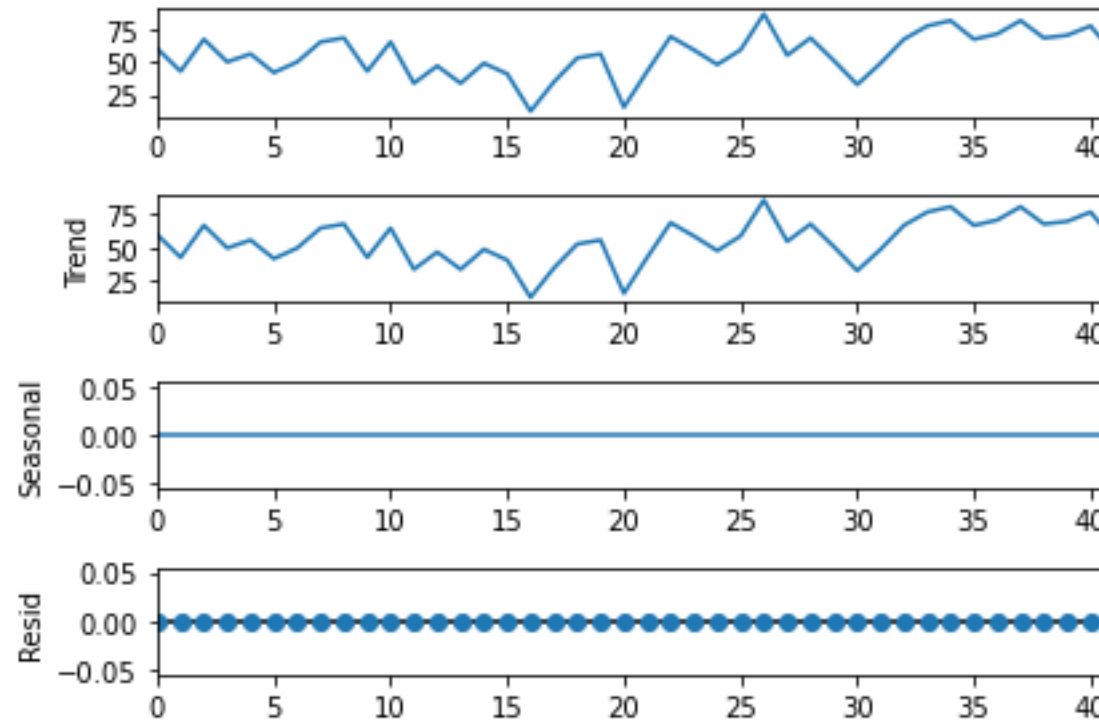
Decompose_additive Observed

```
In [43]: kings_decomp_add.observations
```

```
Out[43]:
```

| | | | |
|----|------|----|------|
| 0 | 60.0 | 21 | 43.0 |
| 1 | 43.0 | 22 | 69.0 |
| 2 | 67.0 | 23 | 59.0 |
| 3 | 50.0 | 24 | 48.0 |
| 4 | 56.0 | 25 | 59.0 |
| 5 | 42.0 | 26 | 86.0 |
| 6 | 50.0 | 27 | 55.0 |
| 7 | 65.0 | 28 | 68.0 |
| 8 | 68.0 | 29 | 51.0 |
| 9 | 43.0 | 30 | 33.0 |
| 10 | 65.0 | 31 | 49.0 |
| 11 | 34.0 | 32 | 67.0 |
| 12 | 47.0 | 33 | 77.0 |
| 13 | 34.0 | 34 | 81.0 |
| 14 | 49.0 | 35 | 67.0 |
| 15 | 41.0 | 36 | 71.0 |
| 16 | 13.0 | 37 | 81.0 |
| 17 | 35.0 | 38 | 68.0 |
| 18 | 53.0 | 39 | 70.0 |
| 19 | 56.0 | 40 | 77.0 |
| 20 | 16.0 | 41 | 56.0 |

dtype: float64



Decompose_additive Trend

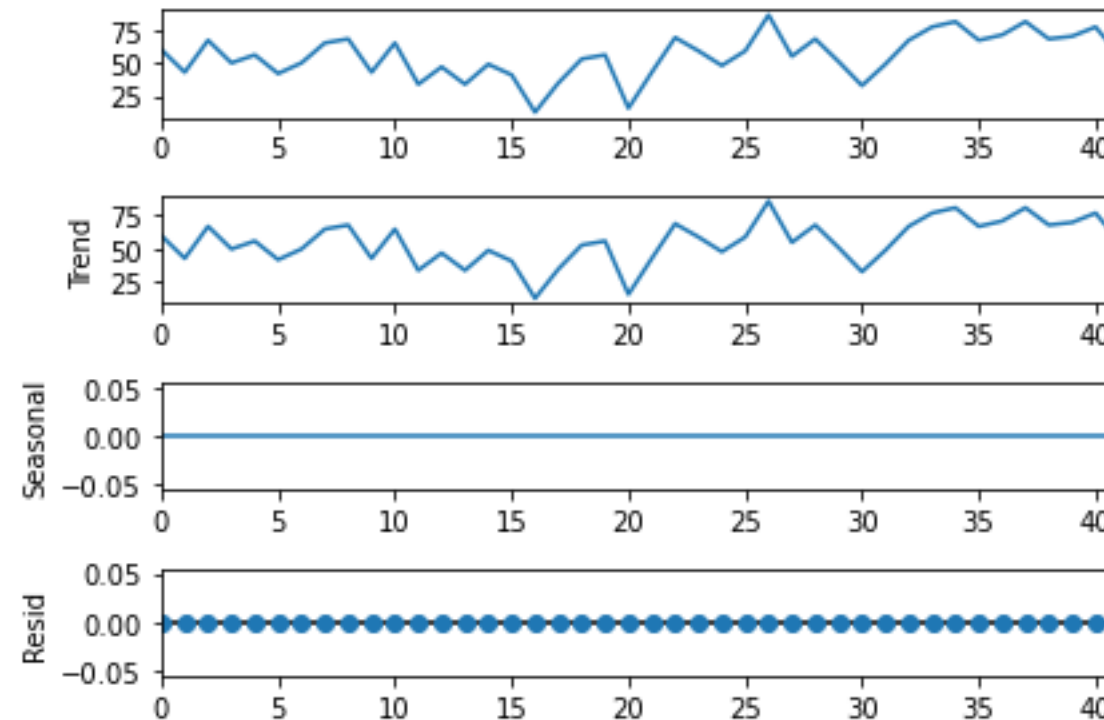


```
In [44]: kings_decomp_add.trend
```

```
Out[44]:
```

| | | | |
|----|------|----|------|
| 0 | 60.0 | 21 | 43.0 |
| 1 | 43.0 | 22 | 69.0 |
| 2 | 67.0 | 23 | 59.0 |
| 3 | 50.0 | 24 | 48.0 |
| 4 | 56.0 | 25 | 59.0 |
| 5 | 42.0 | 26 | 86.0 |
| 6 | 50.0 | 27 | 55.0 |
| 7 | 65.0 | 28 | 68.0 |
| 8 | 68.0 | 29 | 51.0 |
| 9 | 43.0 | 30 | 33.0 |
| 10 | 65.0 | 31 | 49.0 |
| 11 | 34.0 | 32 | 67.0 |
| 12 | 47.0 | 33 | 77.0 |
| 13 | 34.0 | 34 | 81.0 |
| 14 | 49.0 | 35 | 67.0 |
| 15 | 41.0 | 36 | 71.0 |
| 16 | 13.0 | 37 | 81.0 |
| 17 | 35.0 | 38 | 68.0 |
| 18 | 53.0 | 39 | 70.0 |
| 19 | 56.0 | 40 | 77.0 |
| 20 | 16.0 | 41 | 56.0 |

Name: trend, dtype: float64



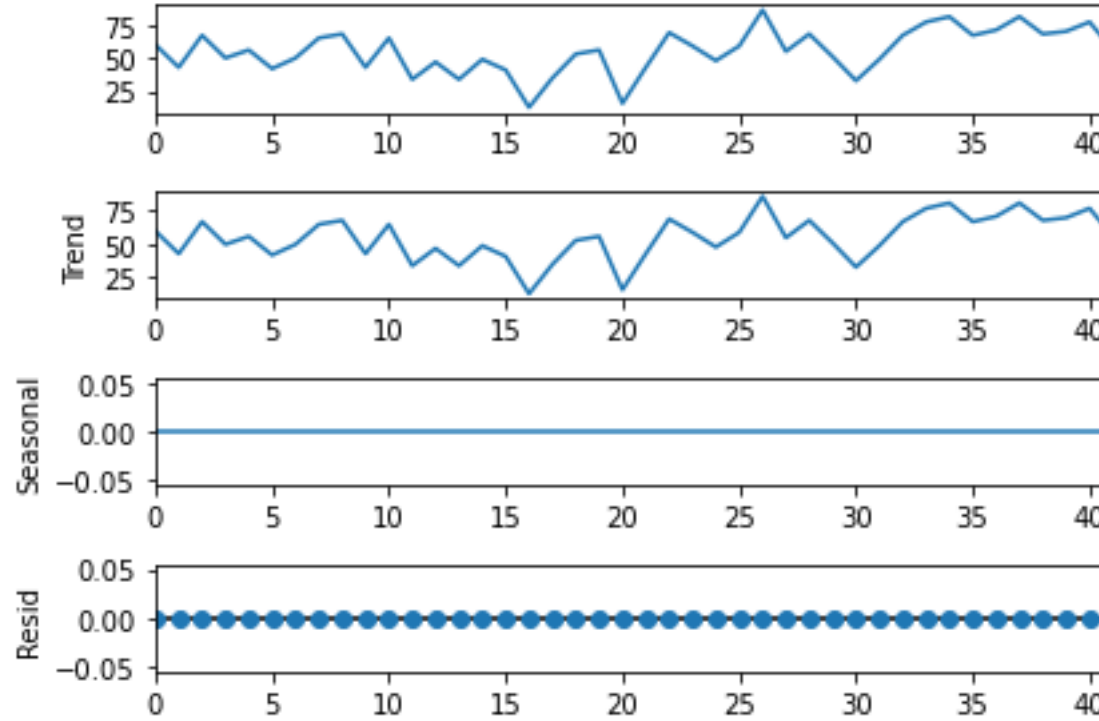
Decompose_additive Seasonal

```
In [45]: kings_decomp_add.seasonal
```

```
Out[45]:
```

| | | | |
|----|-----|----|-----|
| 0 | 0.0 | 21 | 0.0 |
| 1 | 0.0 | 22 | 0.0 |
| 2 | 0.0 | 23 | 0.0 |
| 3 | 0.0 | 24 | 0.0 |
| 4 | 0.0 | 25 | 0.0 |
| 5 | 0.0 | 26 | 0.0 |
| 6 | 0.0 | 27 | 0.0 |
| 7 | 0.0 | 28 | 0.0 |
| 8 | 0.0 | 29 | 0.0 |
| 9 | 0.0 | 30 | 0.0 |
| 10 | 0.0 | 31 | 0.0 |
| 11 | 0.0 | 32 | 0.0 |
| 12 | 0.0 | 33 | 0.0 |
| 13 | 0.0 | 34 | 0.0 |
| 14 | 0.0 | 35 | 0.0 |
| 15 | 0.0 | 36 | 0.0 |
| 16 | 0.0 | 37 | 0.0 |
| 17 | 0.0 | 38 | 0.0 |
| 18 | 0.0 | 39 | 0.0 |
| 19 | 0.0 | 40 | 0.0 |
| 20 | 0.0 | 41 | 0.0 |

Name: seasonal, dtype: float64



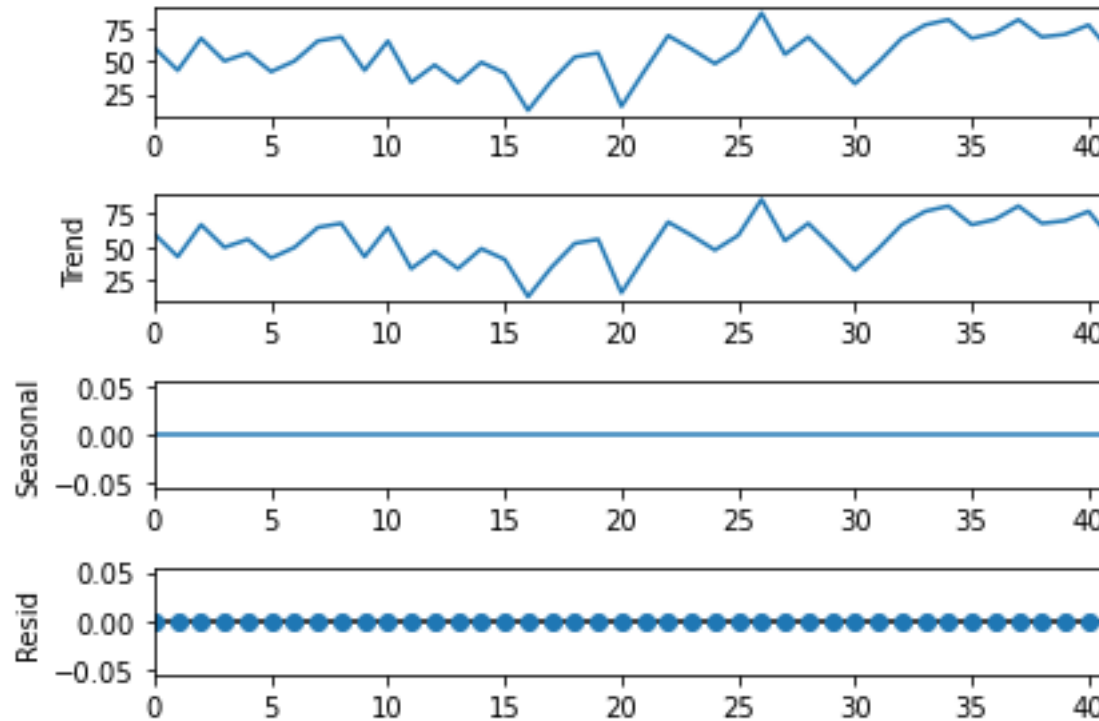
Decompose_additive Residuals

```
In [46]: kings_decomp_add.resid
```

```
Out[46]:
```

| | | | |
|----|-----|----|-----|
| 0 | 0.0 | 21 | 0.0 |
| 1 | 0.0 | 22 | 0.0 |
| 2 | 0.0 | 23 | 0.0 |
| 3 | 0.0 | 24 | 0.0 |
| 4 | 0.0 | 25 | 0.0 |
| 5 | 0.0 | 26 | 0.0 |
| 6 | 0.0 | 27 | 0.0 |
| 7 | 0.0 | 28 | 0.0 |
| 8 | 0.0 | 29 | 0.0 |
| 9 | 0.0 | 30 | 0.0 |
| 10 | 0.0 | 31 | 0.0 |
| 11 | 0.0 | 32 | 0.0 |
| 12 | 0.0 | 33 | 0.0 |
| 13 | 0.0 | 34 | 0.0 |
| 14 | 0.0 | 35 | 0.0 |
| 15 | 0.0 | 36 | 0.0 |
| 16 | 0.0 | 37 | 0.0 |
| 17 | 0.0 | 38 | 0.0 |
| 18 | 0.0 | 39 | 0.0 |
| 19 | 0.0 | 40 | 0.0 |
| 20 | 0.0 | 41 | 0.0 |

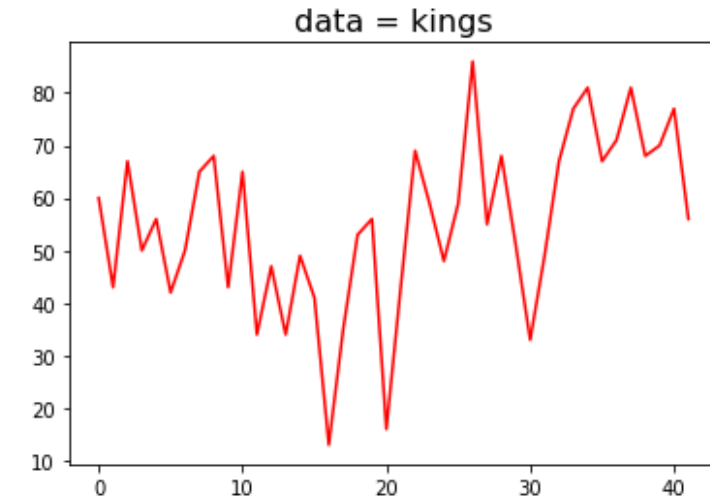
```
Name: resid, dtype: float64
```



Stationarity Test

```
#Test for stationarity
from statsmodels.tsa.stattools import adfuller
kings_adf = adfuller(kings)
kings_adf
```

```
In [49]: kings_adf
Out[49]:
(-4.090229860104913,
 0.0010051728027032974,
 0,
 41,
 {'1%': -3.60098336718852,
  '5%': -2.9351348158036012,
  '10%': -2.6059629803688282},
 263.5882454953018)
```



#H0: Data is not stationary

#p-value: 0.001005 ie ≤ 0.05 , Null Hypothesis rejected, so, the data is stationary

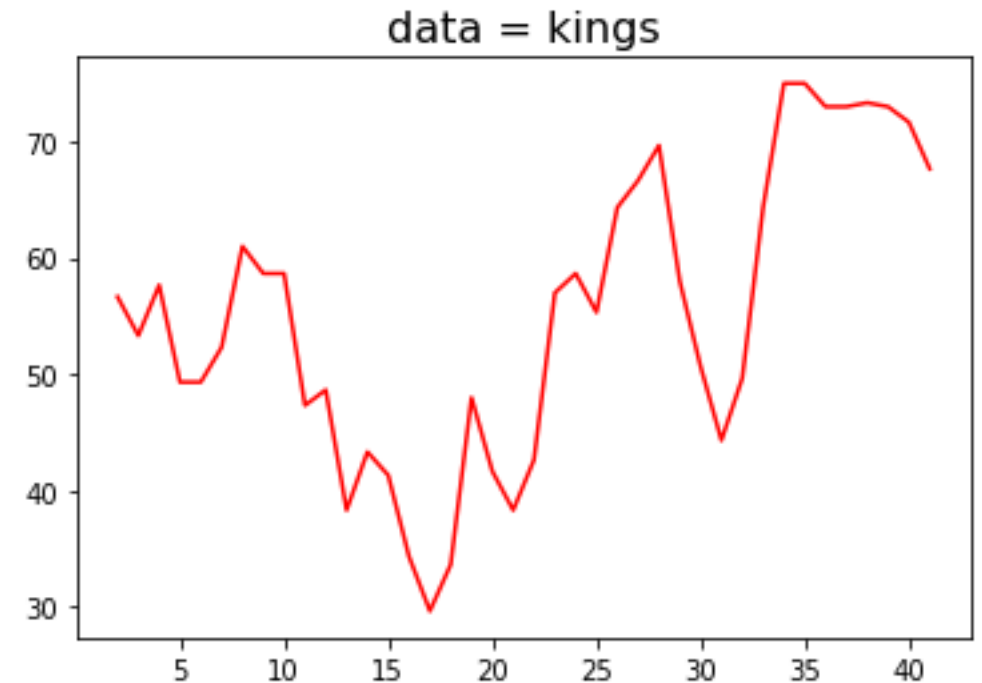
Moving Average 3



```
#Moving average/Rolloing average @3  
kings_ma3 = kings.rolling(window=3).mean()  
kings_ma3.head(10) # 1st & 2nd obs will be na
```

```
#lineplot  
plt.plot(kings_ma3, 'r')  
plt.title('data = kings', fontsize=16)
```

| | age |
|---|-----------|
| 0 | NaN |
| 1 | NaN |
| 2 | 56.666667 |
| 3 | 53.333333 |
| 4 | 57.666667 |
| 5 | 49.333333 |
| 6 | 49.333333 |
| 7 | 52.333333 |
| 8 | 61.000000 |
| 9 | 58.666667 |



Moving Average 3

#Residuals / errors

```
kings_ma3_res = kings - kings_ma3  
kings_ma3_res.head()  
kings_ma3_res = kings_ma3_res.dropna()  
kings_ma3_res.head()
```



```
In [65]: kings_ma3_res.head()  
Out[65]:
```

| | age |
|---|-----------|
| 0 | NaN |
| 1 | NaN |
| 2 | 10.333333 |
| 3 | -3.333333 |
| 4 | -1.666667 |

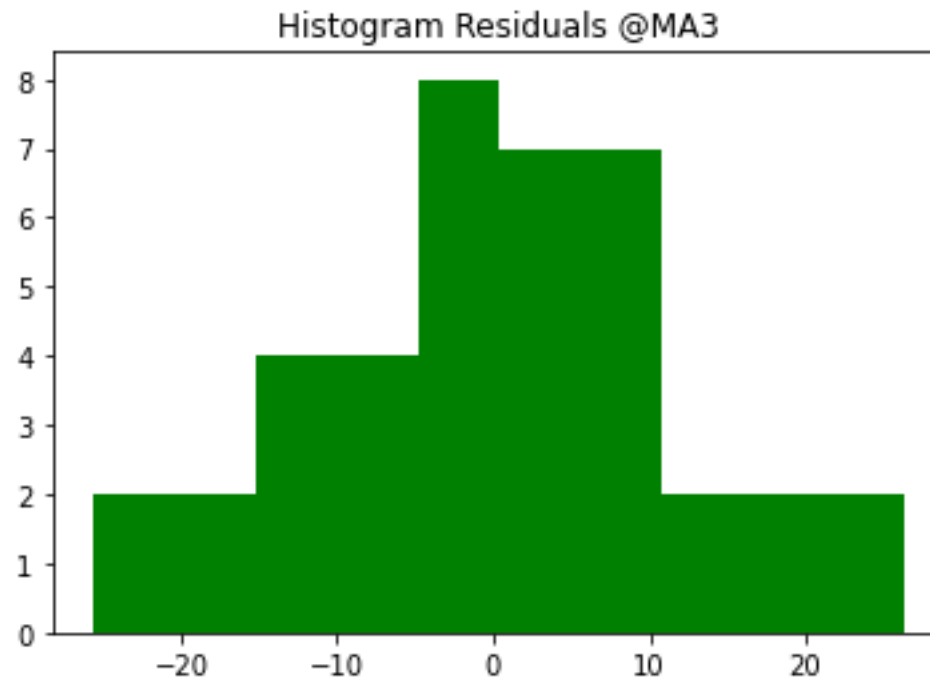
```
In [66]: kings_ma3_res = kings_ma3_res.dropna()  
  
In [67]: kings_ma3_res.head()  
Out[67]:
```

| | age |
|---|-----------|
| 2 | 10.333333 |
| 3 | -3.333333 |
| 4 | -1.666667 |
| 5 | -7.333333 |
| 6 | 0.666667 |



Moving Average 3

```
#Plotting histogram for residuals  
plt.hist(kings_ma3_res, facecolor = 'g')  
plt.title('Histogram Residuals @MA3')
```



RMSE_ma3

```
#  
#Squaring residuals/ errors  
kings_ma3_se = pow(kings_ma3_res,2)  
kings_ma3_se.head()
```

```
In [65]: kings_ma3_res.head()  
Out[65]:  
      age  
0      NaN  
1      NaN  
2  10.333333  
3  -3.333333  
4  -1.666667
```

```
In [85]: kings_ma3_se.head()  
Out[85]:  
      age  
2  106.777778  
3   11.111111  
4    2.777778  
5   53.777778  
6    0.444444
```



```
#average/mean of squared residuals/ errors  
kings_ma3_mse = (kings_ma3_se.sum())/len(kings_ma3_se)  
print(kings_ma3_mse) #128.752777777778
```

```
In [87]: print(kings_ma3_mse)  
age      128.752778  
dtype: float64
```

```
#Root of average/mean of squared residuals/ errors  
kings_ma3_rmse = sqrt(kings_ma3_mse)  
print(kings_ma3_rmse) #11.346928120763689
```

```
In [89]: print(kings_ma3_rmse)  
11.346928120763689
```

births



Libraries

```
# Jesus is King of Kings!
import os
os.chdir('C:\\Users\\Dr Vinod\\Desktop\\WD_python')
import pandas as pd
pd.set_option('display.max_columns', None)
import numpy as np
import matplotlib.pyplot as plt
import statsmodels.api as sm
import statsmodels.formula.api as smf
from statsmodels.tsa.stattools import adfuller
%matplotlib inline
from math import sqrt
from statsmodels.tsa.arima_model import ARIMA
from sklearn.metrics import mean_squared_error
```



Import Data

```
births = pd.read_csv('births.csv', date_parser=True)
births.info()
births.head()
```

```
In [4]: births.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 168 entries, 0 to 167
Data columns (total 3 columns):
#   Column      Non-Null Count  Dtype
---  -
0   obsno       168 non-null   int64
1   month_year  168 non-null   object
2   births      168 non-null   float64
dtypes: float64(1), int64(1), object(1)
memory usage: 4.1+ KB
```

```
In [5]: births.head()
Out[5]:
```

| | obsno | month_year | births |
|---|-------|------------|--------|
| 0 | 1 | Jan-46 | 26.663 |
| 1 | 2 | Feb-46 | 23.598 |
| 2 | 3 | Mar-46 | 26.931 |
| 3 | 4 | Apr-46 | 24.740 |
| 4 | 5 | May-46 | 25.806 |



2 digit
year

births - DataFrame

| Index | obsno | month_year | births |
|-------|-------|------------|--------|
| 0 | 1 | Jan-46 | 26.663 |
| 1 | 2 | Feb-46 | 23.598 |
| 2 | 3 | Mar-46 | 26.931 |
| 3 | 4 | Apr-46 | 24.74 |
| 4 | 5 | May-46 | 25.806 |
| 5 | 6 | Jun-46 | 24.364 |
| 6 | 7 | Jul-46 | 24.477 |
| 7 | 8 | Aug-46 | 23.901 |
| 8 | 9 | Sep-46 | 23.175 |
| 9 | 10 | Oct-46 | 23.227 |
| 10 | 11 | Nov-46 | 21.672 |

Index



```
#Indexing month_year  
#2 digit year without century while converting 4 digit format,  
#python considers as present century so adjusting the year  
births.index = pd.DatetimeIndex(births.month_year)+pd.DateOffset(years=-100)  
births.info()  
births.head()
```

```
In [7]: births.info()  
<class 'pandas.core.frame.DataFrame'>  
DatetimeIndex: 168 entries, 1946-01-01 to 1959-12-01  
Data columns (total 3 columns):  
#   Column      Non-Null Count  Dtype  
---  ---  
0   obsno       168 non-null    int64  
1   month_year   168 non-null    object  
2   births       168 non-null    float64  
dtypes: float64(1), int64(1), object(1)  
memory usage: 5.2+ KB
```

```
In [8]: births.head()  
Out[8]:
```

| month_year | obsno | month_year | births |
|------------|-------|------------|--------|
| 1946-01-01 | 1 | Jan-46 | 26.663 |
| 1946-02-01 | 2 | Feb-46 | 23.598 |
| 1946-03-01 | 3 | Mar-46 | 26.931 |
| 1946-04-01 | 4 | Apr-46 | 24.740 |
| 1946-05-01 | 5 | May-46 | 25.806 |

Data



#Removing unnecessary variables

```
births = births.drop(['obsno', 'month_year'], axis=1)
births.info()
births.shape #168, 1
births.head()
```

```
In [8]: births.head()
```

```
Out[8]:
```

| | obsno | month_year | births |
|------------|--------------|-------------------|---------------|
| month_year | | | |
| 1946-01-01 | 1 | Jan-46 | 26.663 |
| 1946-02-01 | 2 | Feb-46 | 23.598 |
| 1946-03-01 | 3 | Mar-46 | 26.931 |
| 1946-04-01 | 4 | Apr-46 | 24.740 |
| 1946-05-01 | 5 | May-46 | 25.806 |

old

```
In [10]: births.info()
```

```
<class 'pandas.core.frame.DataFrame'>
```

```
DatetimeIndex: 168 entries, 1946-01-01 to 1959-12-01
```

```
Data columns (total 1 columns):
```

| # | Column | Non-Null Count | Dtype |
|---|---------------|---------------------|---------|
| 0 | births | 168 non-null | float64 |

```
dtypes: float64(1)
```

```
memory usage: 2.6 KB
```

```
In [12]: births.head()
```

```
Out[12]:
```

| | births |
|------------|---------------|
| month_year | |
| 1946-01-01 | 26.663 |
| 1946-02-01 | 23.598 |
| 1946-03-01 | 26.931 |
| 1946-04-01 | 24.740 |
| 1946-05-01 | 25.806 |

#Variable births

```
births.describe()
```

```
'''
```

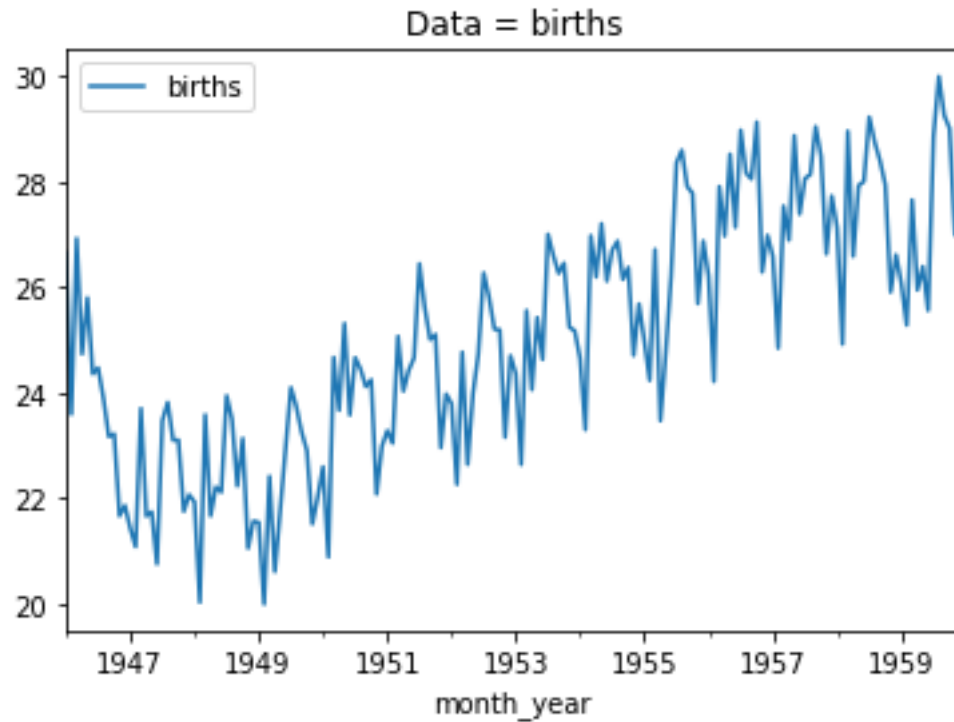
| | births |
|--------------|-------------------|
| count | 168.000000 |
| mean | 25.059310 |
| std | 2.318791 |
| min | 20.000000 |
| 25% | 23.280750 |
| 50% | 24.957000 |
| 75% | 26.878750 |
| max | 30.000000 |

```
'''
```

Plots

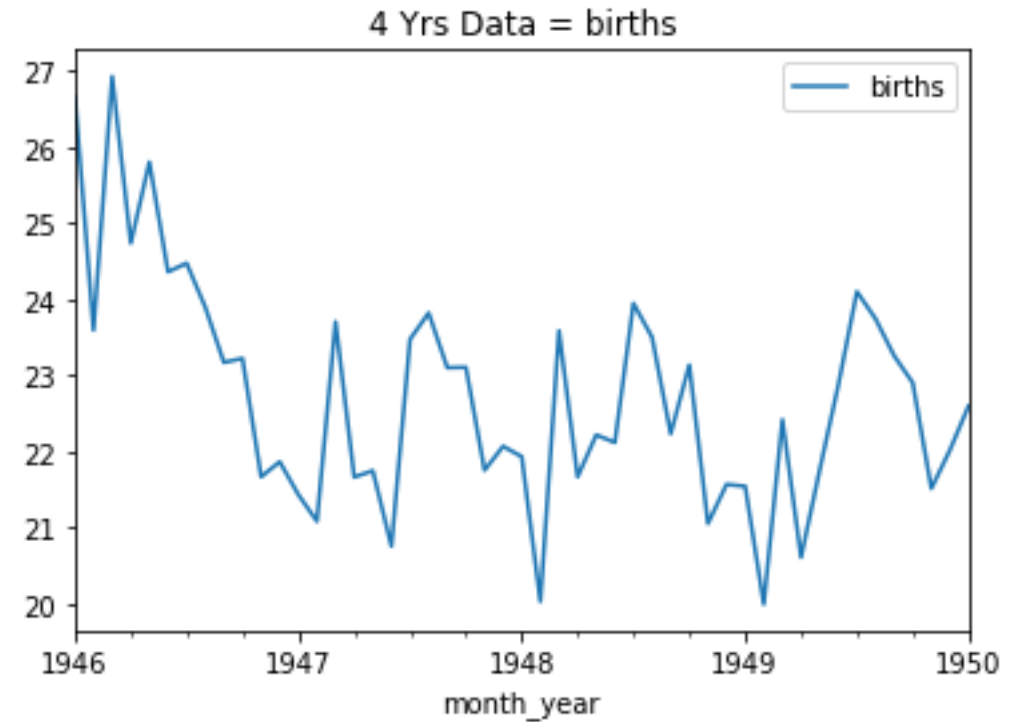


```
#Lineplot  
births.plot()  
plt.title('Data = births')
```



First 4 years means $12 \times 4 = 48$ data points, last will not be considered by python [indexing starts from 0], that's why 49

```
#Only 4 years of data  
births[:49].plot()  
plt.title('4 Yrs Data = births')
```

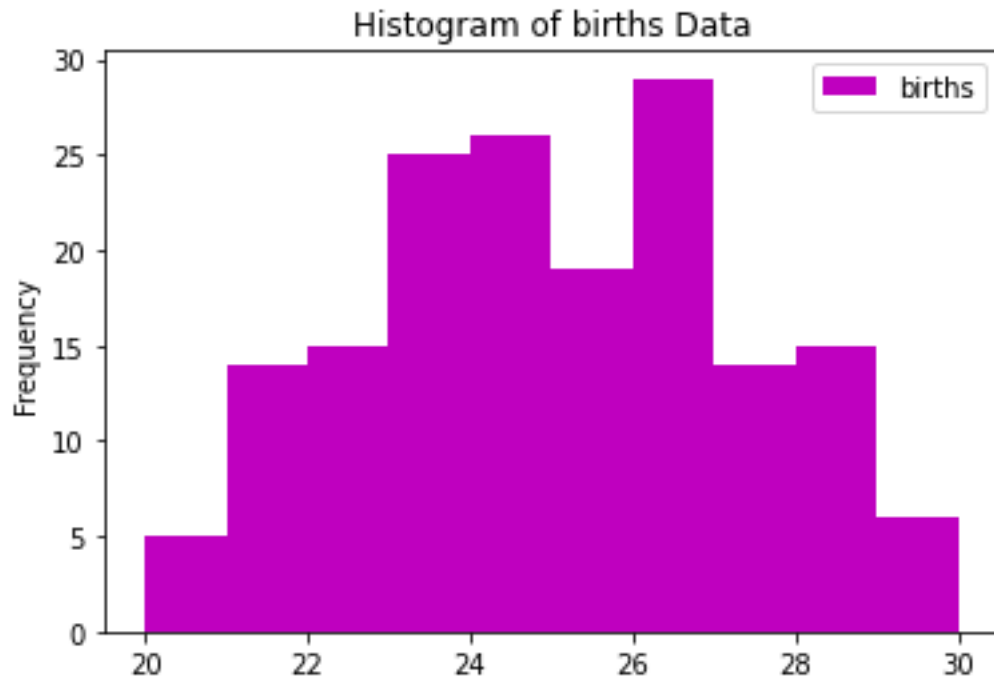


plots



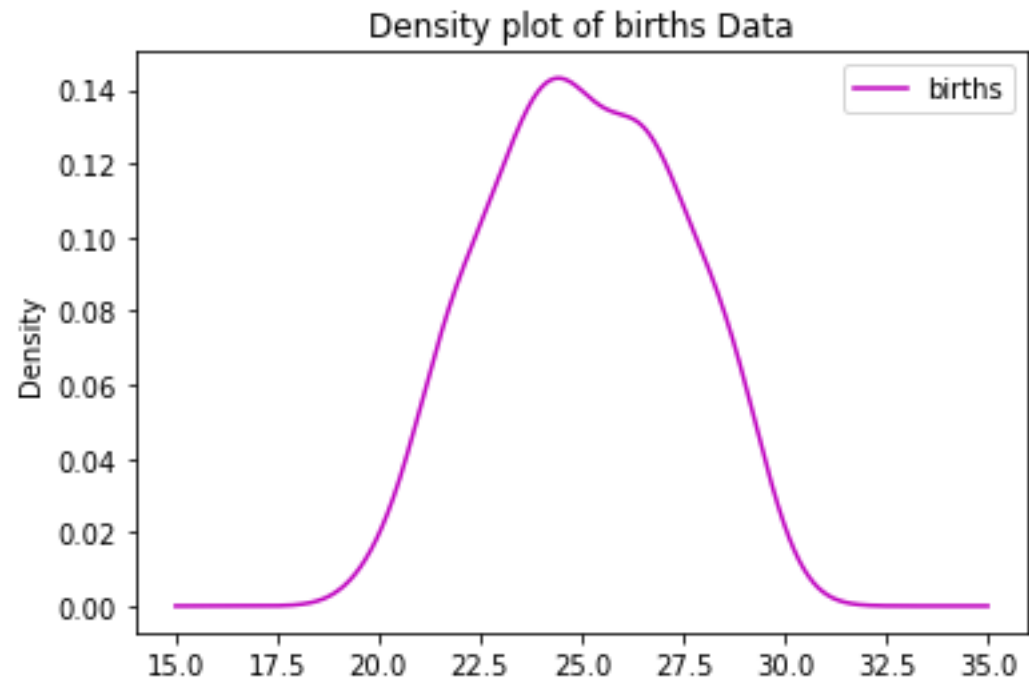
#Histogram

```
births.plot(kind='hist', color = 'm')  
plt.title('Histogram of births Data')
```



#Density plot

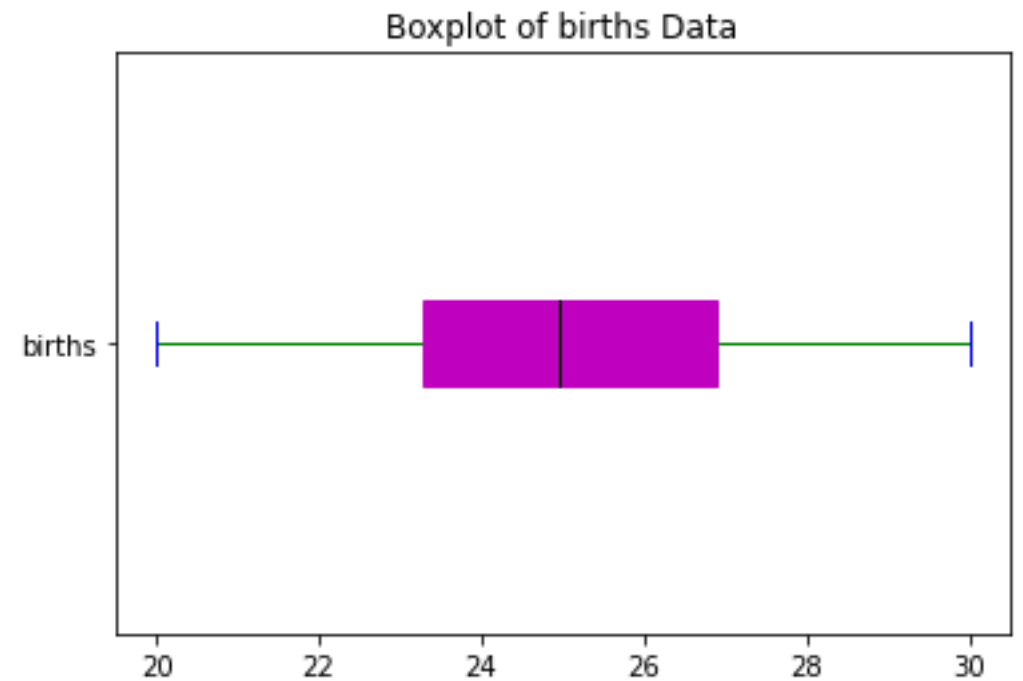
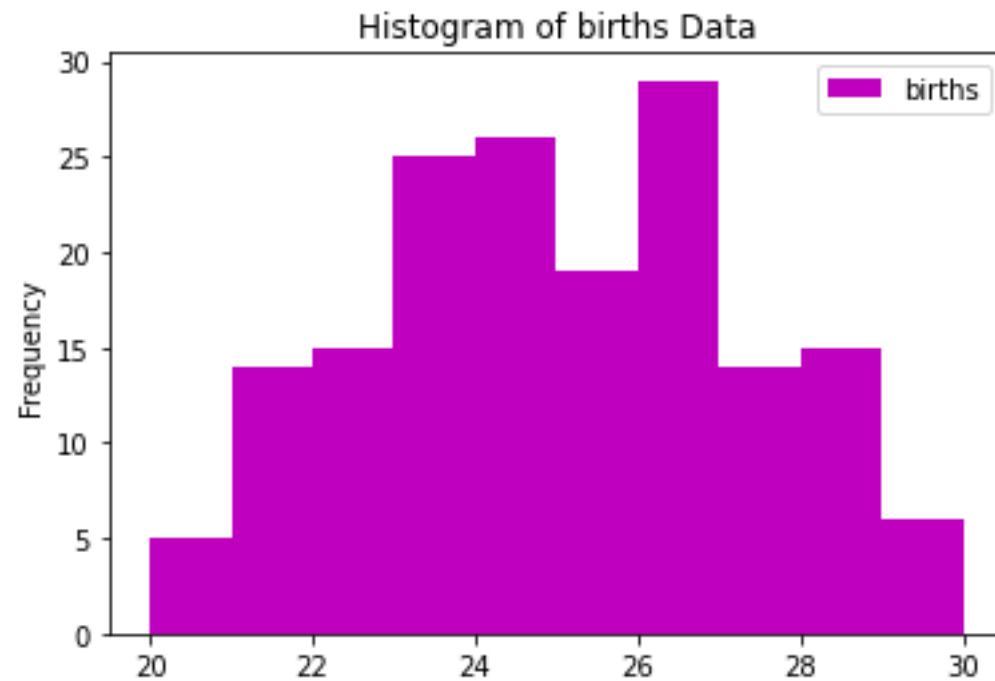
```
births.plot(kind='kde', color = 'm')  
plt.title('Density plot of births Data')
```



Plots

#Boxplot

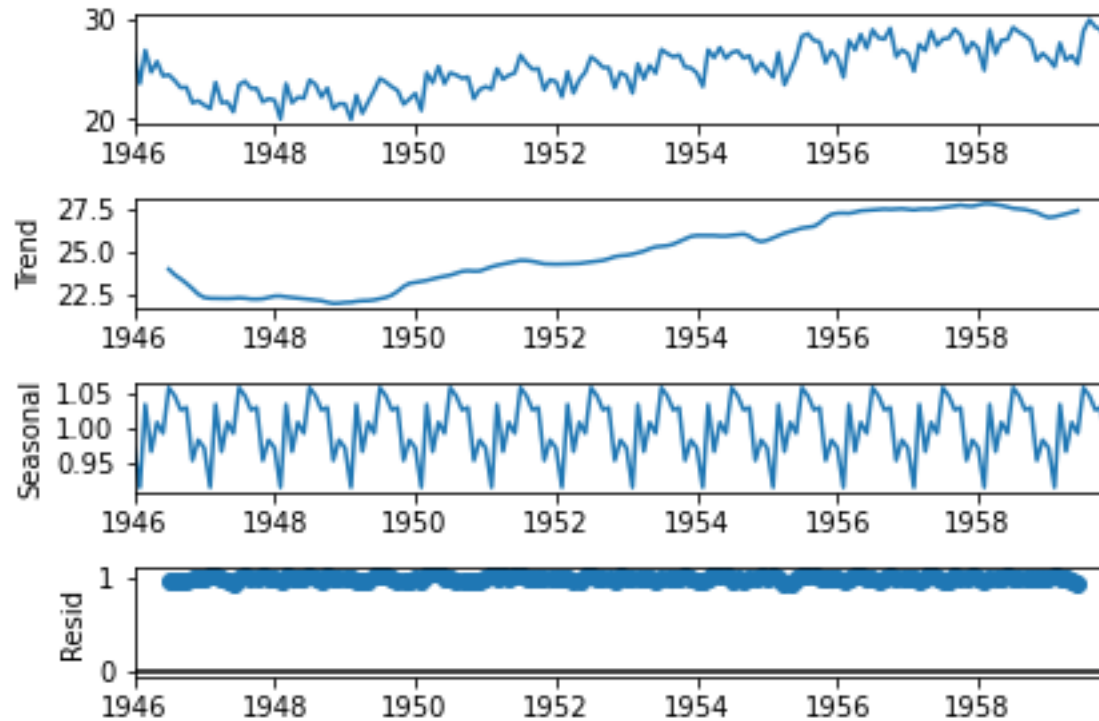
```
props2 = dict(boxes = 'm', whiskers = 'green', medians = 'black', caps = 'blue')
births.plot.box(color = props2 , patch_artist = True, vert = False)
plt.title('Boxplot of births Data')
```



Decompose



```
#Decompose  
from statsmodels.tsa.seasonal import seasonal_decompose  
# Season Decompose with Multiplicative model  
births_dec_m = seasonal_decompose(births, model='multiplicative')
```



Trend

```
births_dec_m.trend.head(20)
```

#First 6 and last 6 values are Na's due calculation of seasonality indices of 12 months

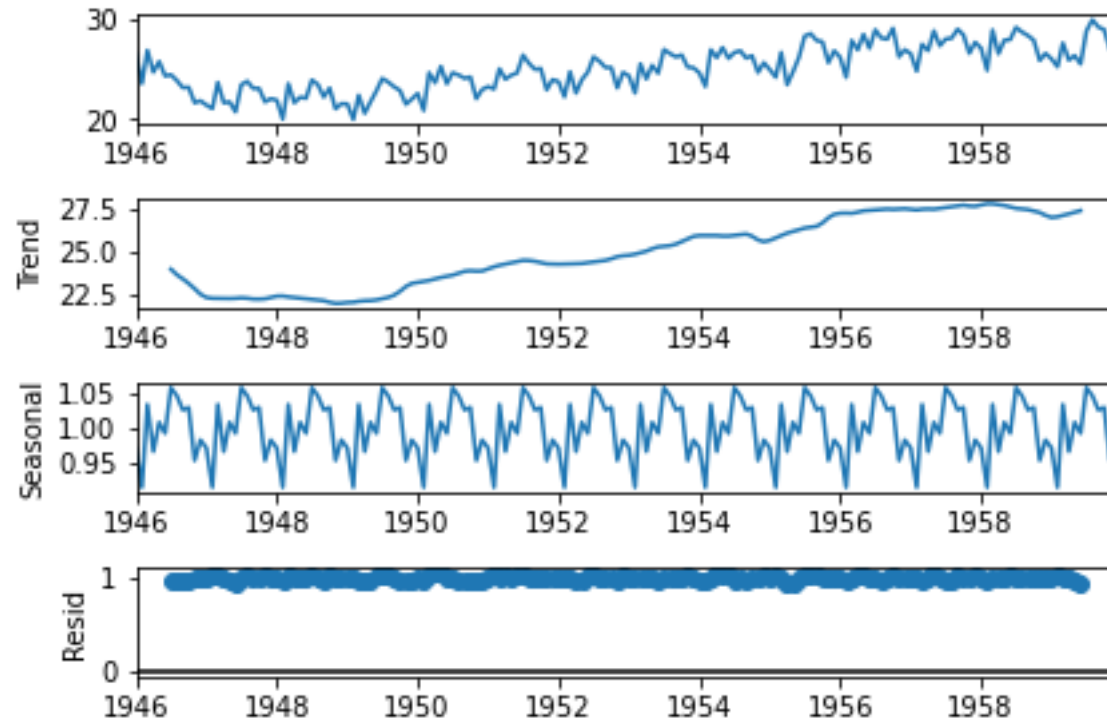
```
In [24]: births_dec_m.trend.head(20)
```

```
Out[24]:
```

```
month_year
```

| | |
|------------|-----------|
| 1946-01-01 | NaN |
| 1946-02-01 | NaN |
| 1946-03-01 | NaN |
| 1946-04-01 | NaN |
| 1946-05-01 | NaN |
| 1946-06-01 | NaN |
| 1946-07-01 | 23.984333 |
| 1946-08-01 | 23.662125 |
| 1946-09-01 | 23.423333 |
| 1946-10-01 | 23.161125 |
| 1946-11-01 | 22.864250 |
| 1946-12-01 | 22.545208 |
| 1947-01-01 | 22.353500 |
| 1947-02-01 | 22.308708 |
| 1947-03-01 | 22.302583 |
| 1947-04-01 | 22.294792 |
| 1947-05-01 | 22.293542 |
| 1947-06-01 | 22.305625 |
| 1947-07-01 | 22.334833 |
| 1947-08-01 | 22.311667 |

```
Name: trend, dtype: float64
```



Seasonality

`births_dec_m.seasonal`



```
In [25]: births_dec_m.seasonal
```

```
Out[25]:
```

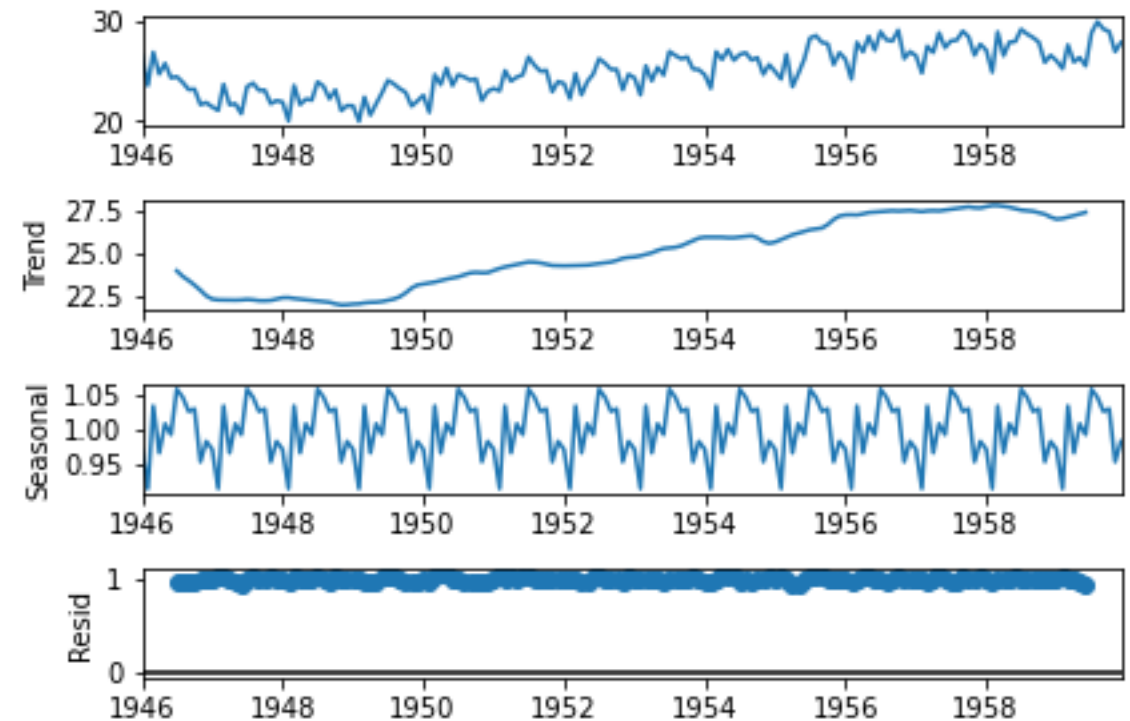
```
month_year
```

```
1946-01-01    0.972903
1946-02-01    0.916649
1946-03-01    1.035164
1946-04-01    0.967842
1946-05-01    1.009504
```

```
...
```

```
1959-08-01    1.047323
1959-09-01    1.027250
1959-10-01    1.030856
1959-11-01    0.955121
1959-12-01    0.984295
```

```
Name: seasonal, Length: 168, dtype: float64
```



Residual



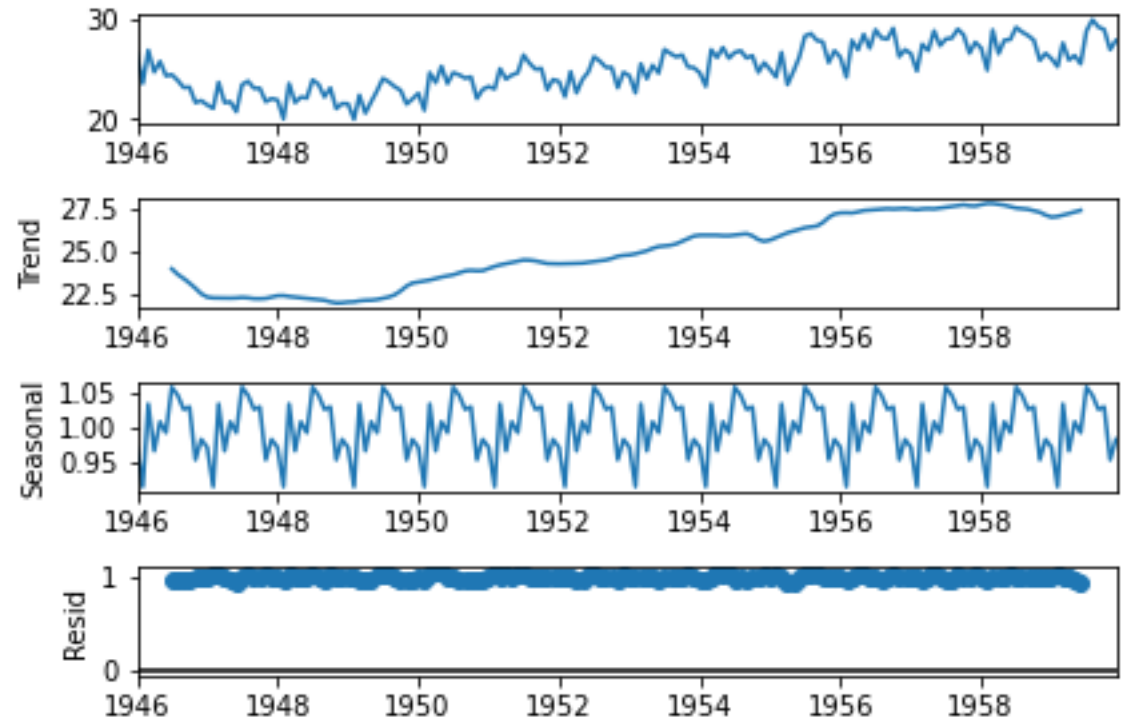
```
births_dec_m.resid.head(20)
```

#First 6 and last 6 values are Na's due calculation of seasonality indices of 12 months

```
In [26]: births_dec_m.resid.head(20)
```

```
Out[26]:
```

| month_year | |
|------------|----------|
| 1946-01-01 | NaN |
| 1946-02-01 | NaN |
| 1946-03-01 | NaN |
| 1946-04-01 | NaN |
| 1946-05-01 | NaN |
| 1946-06-01 | NaN |
| 1946-07-01 | 0.963590 |
| 1946-08-01 | 0.964455 |
| 1946-09-01 | 0.963152 |
| 1946-10-01 | 0.972827 |
| 1946-11-01 | 0.992392 |
| 1946-12-01 | 0.985528 |
| 1947-01-01 | 0.985801 |
| 1947-02-01 | 1.031285 |
| 1947-03-01 | 1.026949 |
| 1947-04-01 | 1.004225 |
| 1947-05-01 | 0.966523 |
| 1947-06-01 | 0.936379 |
| 1947-07-01 | 0.992565 |



Model!

```
#Model with triple exponential smoothing  
# applicable when trend and seasonality exists  
from statsmodels.tsa.holtwinters import ExponentialSmoothing  
  
births_es = ExponentialSmoothing(births, seasonal_periods=12,  
                                trend='add', seasonal='add').fit()  
births_es.summary()
```



Model Summary!

```
'''
                                ExponentialSmoothing Model Results
=====
Dep. Variable:                births    No. Observations:                168
Model:                        ExponentialSmoothing    SSE                63.346
Optimized:                    True        AIC                -131.859
Trend:                        Additive    BIC                -81.875
Seasonal:                     Additive    AICC               -127.268
Seasonal Periods:             12        Date:                Fri, 26 Mar 2021
Box-Cox:                      False     Time:                00:25:39
Box-Cox Coeff.:              None
=====
```



Model Summary!

| ===== | | | |
|--------------------|------------|-------|-----------|
| | coeff | code | optimized |
| ----- | | | |
| smoothing_level | 0.9401515 | alpha | True |
| smoothing_trend | 8.5161e-11 | beta | True |
| smoothing_seasonal | 5.805e-12 | gamma | True |
| initial_level | 27.155582 | l.0 | True |
| initial_trend | 0.0062209 | b.0 | True |
| initial_seasons.0 | -0.5917886 | s.0 | True |
| initial_seasons.1 | -2.0910713 | s.1 | True |
| initial_seasons.2 | 0.9121398 | s.2 | True |
| initial_seasons.3 | -0.7605586 | s.3 | True |
| initial_seasons.4 | 0.3205229 | s.4 | True |
| initial_seasons.5 | -0.1308801 | s.5 | True |
| initial_seasons.6 | 1.4655643 | s.6 | True |
| initial_seasons.7 | 1.2730839 | s.7 | True |
| initial_seasons.8 | 0.7820954 | s.8 | True |
| initial_seasons.9 | 0.8415282 | s.9 | True |
| initial_seasons.10 | -1.0539487 | s.10 | True |
| initial_seasons.11 | -0.3096054 | s.11 | True |
| ----- | | | |

residuals!

```
#Residual given by the model  
births_es_res = births_es.resid  
births_es_res
```



```
In [30]: births_es_res  
Out[30]:  
month_year  
1946-01-01    0.092986  
1946-02-01   -1.566373  
1946-03-01    0.229823  
1946-04-01   -0.510768  
1946-05-01   -0.051871  
...  
1959-08-01    1.421315  
1959-09-01   -0.169169  
1959-10-01   -0.324778  
1959-11-01   -0.150182  
1959-12-01    0.145448  
Length: 168, dtype: float64
```

| births_es_res - Series | | | |
|------------------------|------------|--|--|
| month_year | 0 | | |
| 1946-01-01 00:00:00 | 0.0929857 | | |
| 1946-02-01 00:00:00 | -1.56637 | | |
| 1946-03-01 00:00:00 | 0.229823 | | |
| 1946-04-01 00:00:00 | -0.510768 | | |
| 1946-05-01 00:00:00 | -0.0518709 | | |
| 1946-06-01 00:00:00 | -0.999922 | | |

rmse!

#Squaring residuals/ errors

```
births_es_se = pow(births_es_res,2)
births_es_se.head()
```

#average/mean of squared residuals/ errors

```
births_es_mse = (births_es_se.sum())/len(births_es_se)
print(births_es_mse) #0.3770609200564516
```

#Root of average/mean of squared residuals/ errors

```
births_es_rmse = sqrt(births_es_mse)
print(births_es_rmse) #0.6140528642197279
```



```
In [31]: births_es_se = pow(births_es_res,2)
```

```
In [32]: births_es_se.head()
```

```
Out[32]:
```

```
month_year
1946-01-01    0.008646
1946-02-01    2.453525
1946-03-01    0.052819
1946-04-01    0.260884
1946-05-01    0.002691
dtype: float64
```

```
In [33]: births_es_mse = (births_es_se.sum())/len(births_es_se)
```

```
In [34]: print(births_es_mse) #0.3770609200564516
0.3770609200209467
```

```
In [35]: births_es_rmse = sqrt(births_es_mse)
```

```
In [36]: print(births_es_rmse) #0.6140528642197279
0.6140528641908176
```

Histogram of residulas!

```
#Histogram of residuals  
plt.hist(births_es_res, color = 'm')  
plt.title('births - Residual given by the Model')  
plt.show()
```

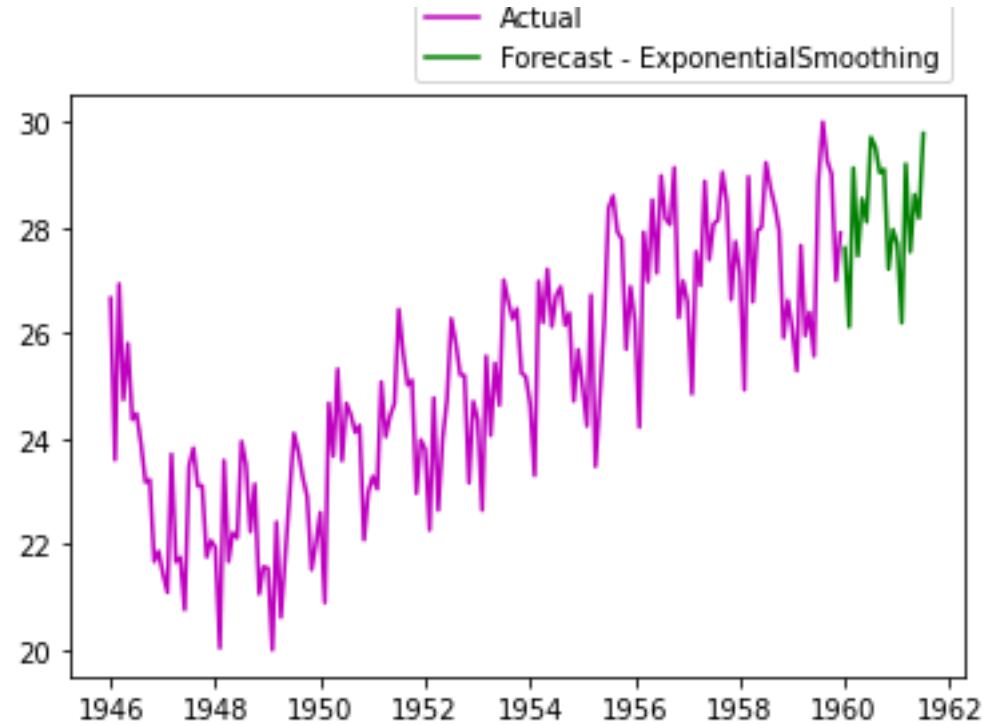


Forecast and plot



```
#forecasting/ predicting
births_pred2 = births_es.forecast(steps=19)
print(births_pred2)

#Plot actual and forecast
plt.plot(births, color = 'm')
plt.plot(births_pred2, color = 'g')
plt.legend(['Actual', 'Forecast - ExponentialSmoothing'],
           bbox_to_anchor=(1, 1), loc=4)
plt.show()
```



Let's try autoarima!

```
# Let's go for autoarima  
#Test for stationarity  
from statsmodels.tsa.stattools import adfuller  
births_adf = adfuller(births)  
births_adf
```



```
In [121]: births_adf  
Out[121]:  
(-0.33128063038051875,  
 0.9209557340544081,  
 13,  
 154,  
 {'1%': -3.473542528196209,  
  '5%': -2.880497674144038,  
  '10%': -2.576878053634677},  
 385.9083089080856)
```

Series is NOT
stationary!

autoarima!

```
# Applying auto - arima to forecast  
#!pip install pmdarima  
  
from pmdarima import auto_arima  
  
births_mod = auto_arima(births)  
births_mod.summary()
```



model!

```
SARIMAX Results
=====
Dep. Variable:          y      No. Observations:      168
Model:                SARIMAX(2, 1, 1)  Log Likelihood      -271.935
Date:                Fri, 26 Mar 2021  AIC              551.870
Time:                00:35:55    BIC              564.342
Sample:              0      HQIC              556.932
                        - 168
Covariance Type:      opg
=====
              coef    std err          z      P>|z|      [0.025      0.975]
-----
ar.L1          0.2509     0.095     2.643     0.008     0.065     0.437
ar.L2          0.3441     0.116     2.977     0.003     0.118     0.571
ma.L1         -0.9143     0.065    -14.166     0.000    -1.041    -0.788
sigma2         1.5133     0.194     7.788     0.000     1.132     1.894
=====
Ljung-Box (L1) (Q):                0.20  Jarque-Bera (JB):                2.24
Prob(Q):                            0.66  Prob(JB):                  0.33
Heteroskedasticity (H):              1.22  Skew:                      0.14
Prob(H) (two-sided):                0.46  Kurtosis:                  2.51
=====

Warnings:
[1] Covariance matrix calculated using the outer product of gradients (complex-step).'''
```

#Residual given by the model

```
births_mod_res = births_mod.resid()  
births_mod_res
```

#Adding index and converting to dataframe

```
births_mod_res1 = pd.DataFrame(births_mod_res, index=births.index)  
births_mod_res1
```

births_mod_res - NumPy object array

| | 0 |
|----|------------|
| 0 | 26.663 |
| 1 | -3.06497 |
| 2 | 1.67623 |
| 3 | -0.538892 |
| 4 | 0.00151674 |
| 5 | -0.954345 |
| 6 | -0.735586 |
| 7 | -0.762661 |
| 8 | -1.30228 |
| 9 | -0.73678 |
| 10 | -1.98186 |

Format Resize ☒ Background color

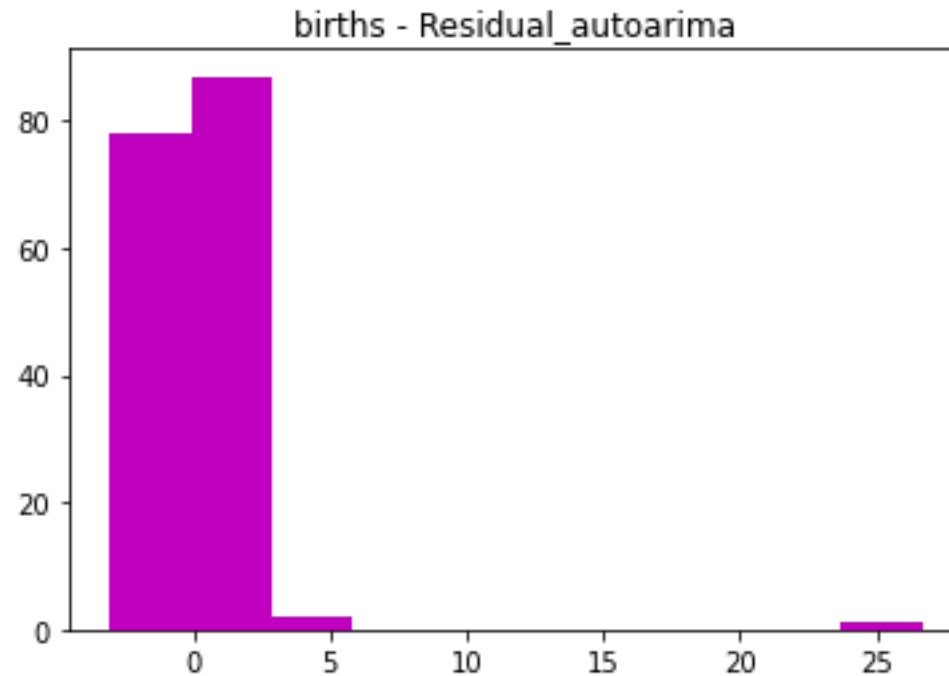
births_mod_res1 - DataFrame

| month_year | 0 |
|---------------------|------------|
| 1946-01-01 00:00:00 | 26.663 |
| 1946-02-01 00:00:00 | -3.06497 |
| 1946-03-01 00:00:00 | 1.67623 |
| 1946-04-01 00:00:00 | -0.538892 |
| 1946-05-01 00:00:00 | 0.00151674 |
| 1946-06-01 00:00:00 | -0.954345 |
| 1946-07-01 00:00:00 | -0.735586 |
| 1946-08-01 00:00:00 | -0.762661 |
| 1946-09-01 00:00:00 | -1.30228 |
| 1946-10-01 00:00:00 | -0.73678 |
| 1946-11-01 00:00:00 | -1.98186 |
| 1946-12-01 00:00:00 | -1.21939 |

< Format Resize ☒ Background color ☒ Column min/max

Histogram of residuals

```
#Histogram of residuals  
plt.hist(births_mod_res1, color = 'm')  
plt.title('births - Residual_autoarima')  
plt.show()
```

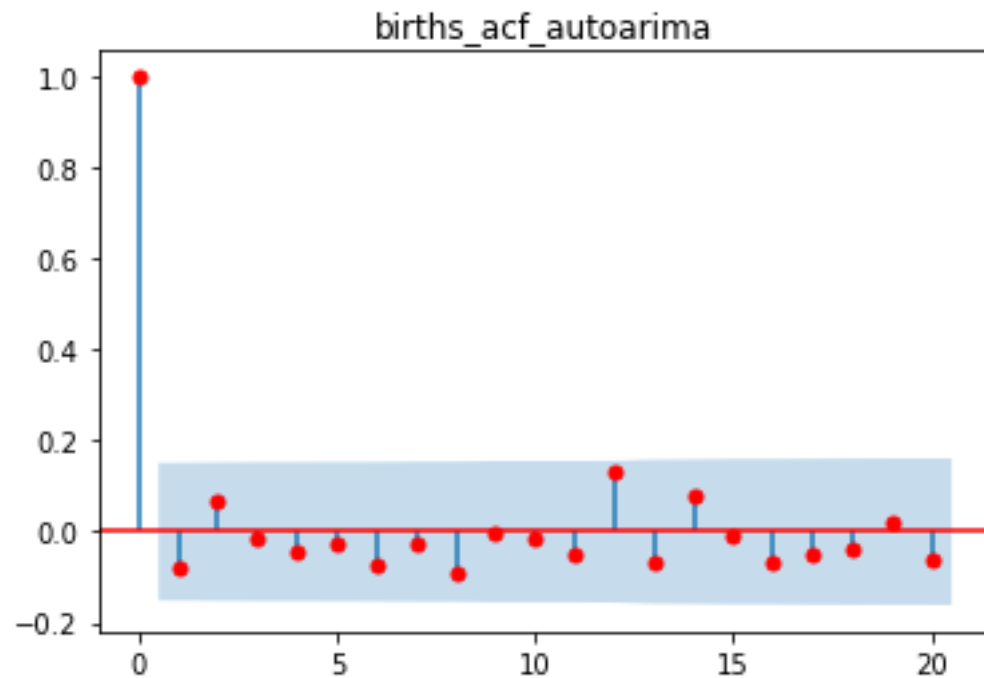


rmse!

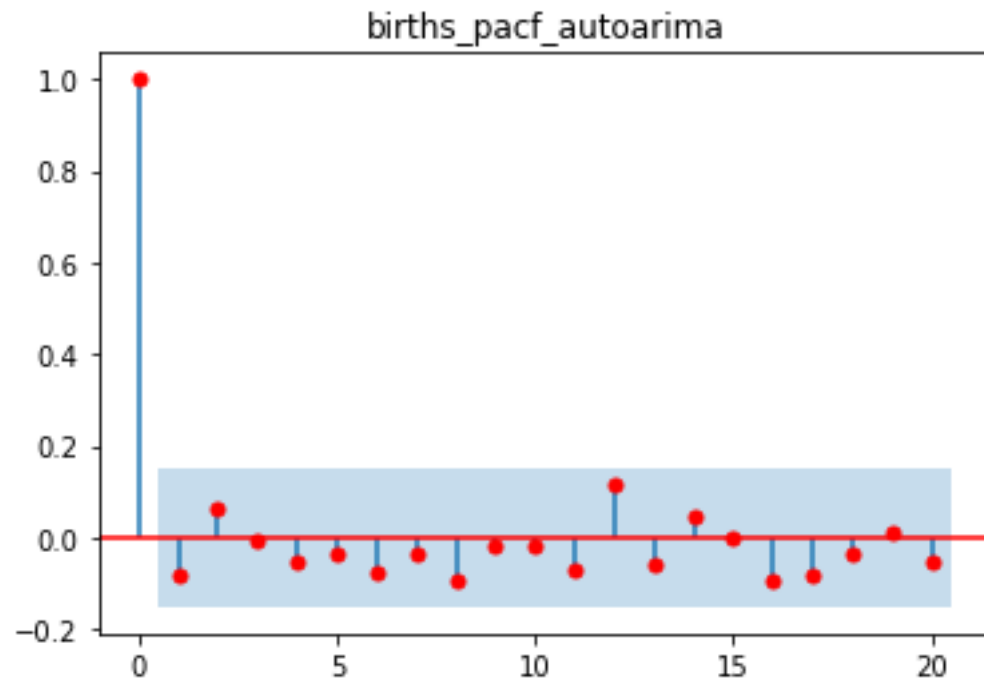
```
# rmse  
#Squaring residuals/ errors  
births_mod_se = pow(births_mod_res1,2)  
births_mod_se.head()  
  
#average/mean of squared residuals/ errors  
births_mod_mse = (births_mod_se.sum())/len(births_mod_se)  
print(births_mod_mse) #5.757373  
  
#Root of average/mean of squared residuals/ errors  
births_mod_rmse = sqrt(births_mod_mse)  
print(births_mod_rmse) #2.399452542080286
```



```
#Plotting acf & pacf - residual  
from statsmodels.graphics.tsaplots import plot_acf  
from statsmodels.graphics.tsaplots import plot_pacf  
  
plot_acf(births_mod_res1, lags=20, color='r',  
         title='births_acf_autoarima')
```




```
plot_pacf(births_mod_res1, lags=20, color = 'r',  
          title='births_pacf_autoarima')
```



Forecast and plot

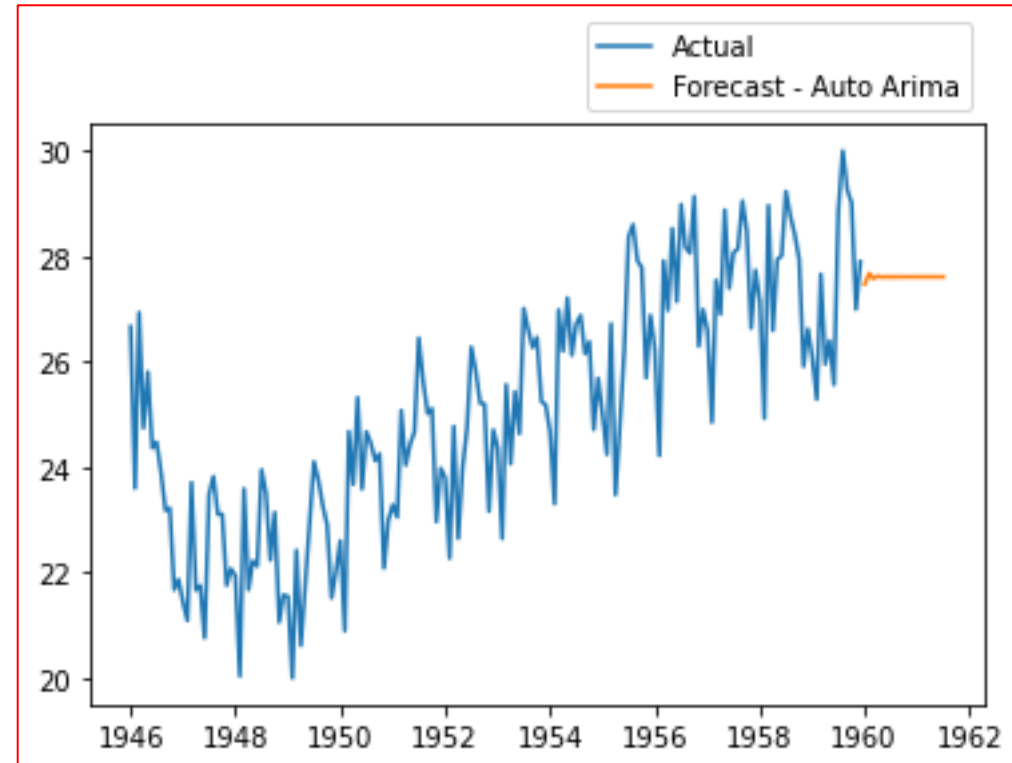
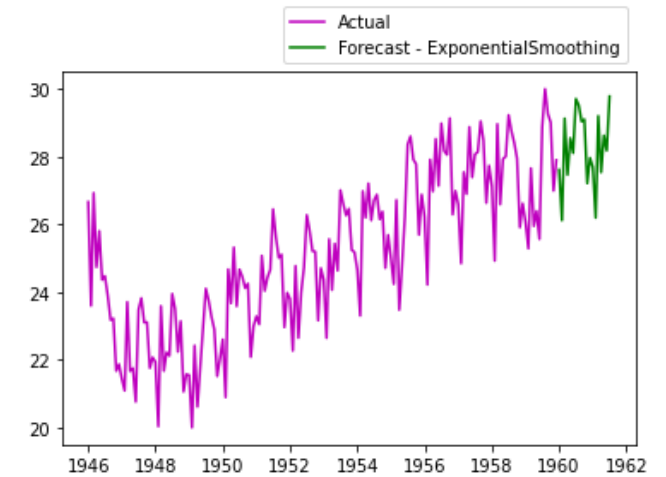
```
#Forecasting next 19 periods
births_mod_pred = births_mod.predict(n_periods=19)
births_mod_pred

#Adding index to forecast and converting to dataframe

births_mod_pred = pd.DataFrame(births_mod_pred,
                               index=pd.date_range(start='1960-01-01',
                                                    periods=19, freq='MS'))

births_mod_pred

#Plot actual and forecast
plt.plot(births)
plt.plot(births_mod_pred)
plt.legend(['Actual', 'Forecast - Auto Arima'],
           bbox_to_anchor=(1, 1), loc=4)
plt.show()
```



Happy Learning!

