# AIFA BEST FIRST SEARCH

16/01/2024

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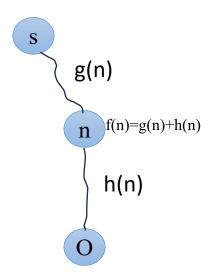
#### BEST-FIRST Tree Search

• Initialize: Set OPEN= $\{s\}$ , CLOSED =  $\{\}$ , f(s) = h(s)

- Fail:
  - If OPEN={}, Terminate with failure

• Select: Select the minimum cost state, n, from OPEN and save in CLOSED

- Terminate:
  - If n∈G, terminate with success



#### **BEST-FIRST** Tree Search

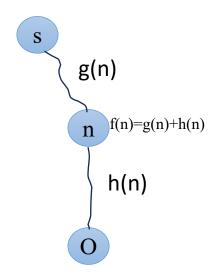
- Expand:
  - For each successor, m, of n:
    - If m∉[OPEN∪CLOSED]
      - Set f(m) = h(m)
      - Insert m in OPEN
    - If m∈[OPENUCLOSED]
      - Set f(m) = h(m)
      - If f(m) has decreased and  $m \in CLOSED$ 
        - Move m to OPEN

- Loop:
  - Go to step 2

BEST-FIRST Tree Search with pruning

# BEST-FIRST Tree Search [pruning]

- Initialize: Set OPEN= $\{s\}$ , CLOSED =  $\{\}$ , f(s) = h(s), CB
- Fail:
  - If OPEN={}, Terminate with failure
- Select: Select the minimum cost state, n, from OPEN and save in CLOSED
- Terminate:
  - If  $n \in G$  and f(n) < CB, CB = f(n), Go to Step 2
  - Else terminate



#### BEST-FIRST Tree Search [pruning]

- Expand:
  - If  $f(n) \le CB$ 
    - For each successor, m, of n:
      - If m∉[OPEN∪CLOSED]
        - Set f(m) = h(m)
        - Insert m in OPEN
    - If m∈[OPEN∪CLOSED]
      - Set f(m) = h(m)
      - If f(m) has decreased and  $m \in CLOSED$ 
        - Move m to OPEN

- Loop:
  - Go to step 2

#### BEST-FIRST Tree Search



# AIFA Hill Climbing Algorithm

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#### Hill Climbing Algorithm

- Evaluate the INITIAL state
  - If it is GOAL return it
  - Else CURRENT← INITIAL
- Loop until the solution is found or no new operators could be applied to CURRENT:
  - Select an operator that has not been applied to the current state [CURRENT] and apply it to produce new state [NEW]
  - Evaluate NEW:
    - If it is GOAL return it
    - Else If NEW > CURRENT, CURRENT← NEW
    - Else go to Loop

#### Hill Climbing Algorithm

Α

D

C

B

D

C

В

Α

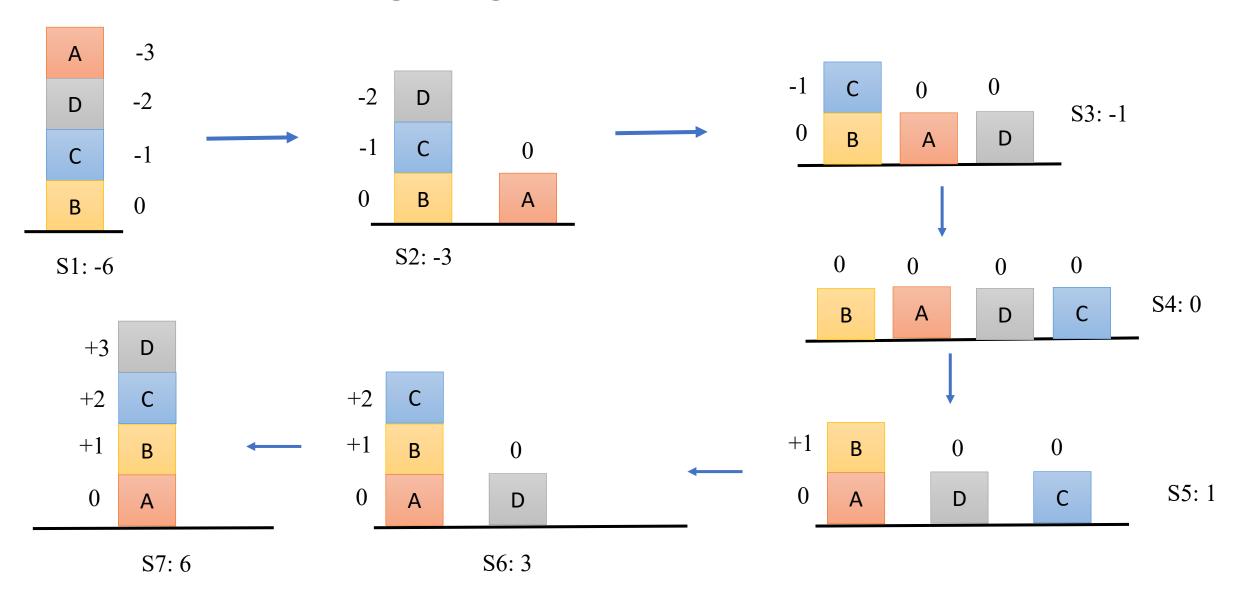
• h(x) = +1 for all the blocks in support structure if the block is positioned correctly

• Otherwise -1 for all the blocks

Start

Goal

# Hill Climbing Algorithm



#### Hill Climbing Algorithm: Drawbacks

- Local Maxima:
  - A local maxima is supposed to be global maxima



- Plateaus:
  - Area of sear h space where evaluation function is flat
  - Requiring random walk

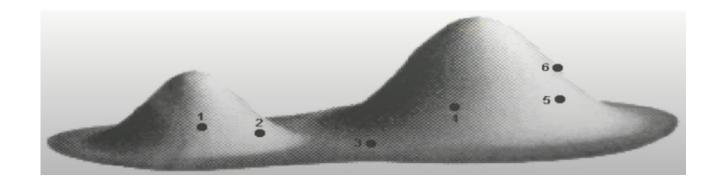


- Ridge:
  - Steep slopes
  - Search direction is not towards the top but towards the side



#### Drawback: Solution

• In each of the previous cases (local maxima, plateaus, & ridge), the algorithm reaches a point at which no progress is being made



- Solution
  - Random-restart-hill-climbing
  - Random initial states are generated
  - Running each until it halts or makes no discernible progress
  - Best result is chosen

#### Hill Climbing Algorithm: Disadvantages

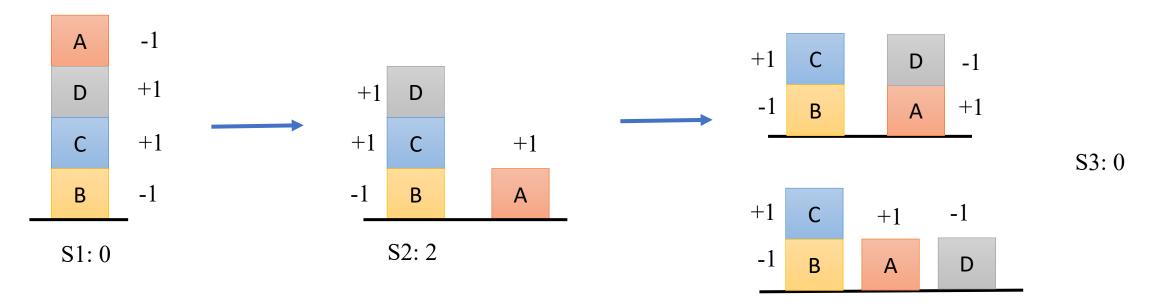
- Hill Climbing uses local information:
  - Decides what to do next by looking only at the "immediate" consequences of its choices
  - Will terminate when at local optimum
  - The order of application of operators can make a big difference
- Global information might be encoded in heuristic functions

# Hill Climbing Algorithm: Disadvantages

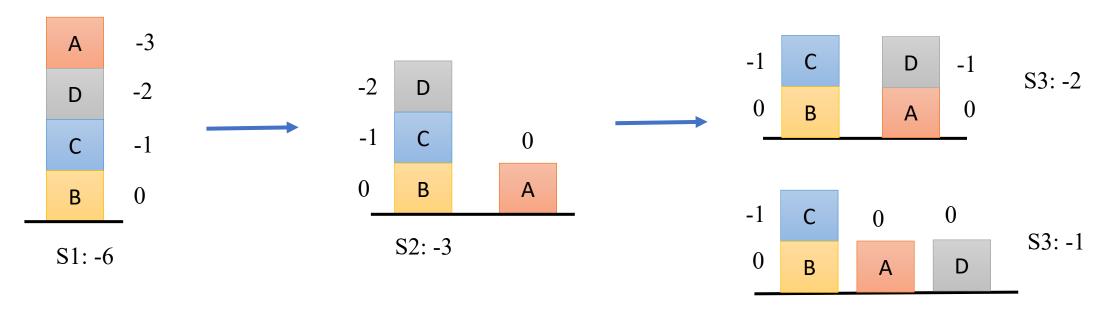


- Local Heuristics
  - +1 for each block that is resting on the thing it is supposed to be resting on
  - -1 for each block that is resting on a wrong thing

# Hill Climbing Algorithm: Local Heuristics

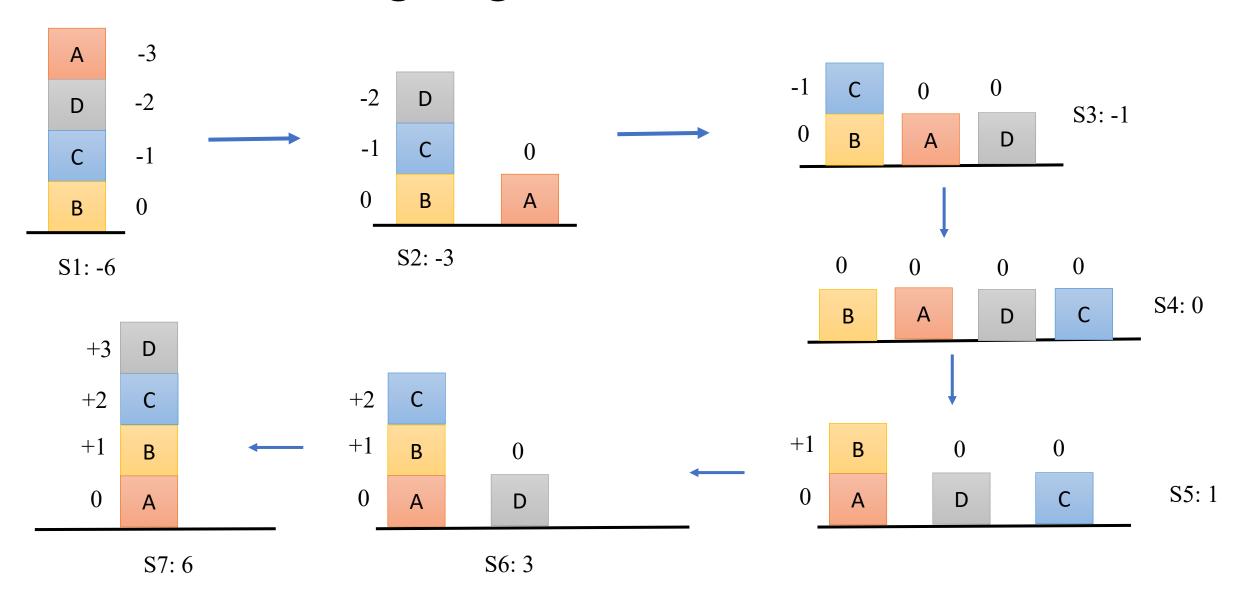


#### Hill Climbing Algorithm: Global Heuristics



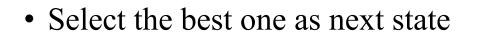
- h(x) = +1 for all the blocks in support structure if the block is positioned correctly
- Otherwise -1 for all the blocks
- There is no local maximum
- Takeaway
  - Sometimes changing the heuristic function is all we need

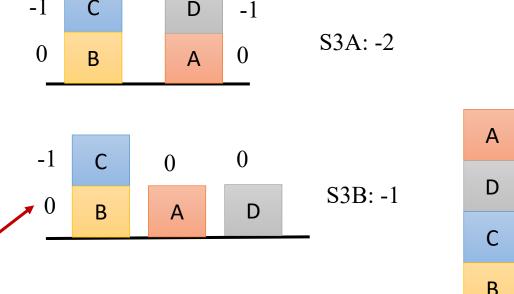
#### Hill Climbing Algorithm: Global Heuristics



#### Steepest-Ascent Hill Climbing Algorithm

- Basic Hill Climbing first applies one operator and gets new state
- Steepest-Ascent Hill Climbing considers all the moves from the current state

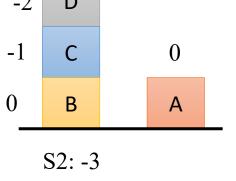




-3

-1

S3C: -6



#### Steepest-Ascent Hill Climbing Algorithm

- Evaluate the INITIAL state
  - If it is GOAL return it
  - Else CURRENT← INITIAL
- Loop until the solution is found or until a complete iteration produces no change to CURRENT:
  - Let SUCC be a state such that any possible successor of the current state will be better than SUCC
  - For each operator that applies to the current state [CURRENT] do
    - Apply the operator and generate a new state [NEW]
    - Evaluate NEW:
      - If it is GOAL return it and quit
      - Else If NEW > SUCC, SUCC← NEW
  - If SUCC>CURRENT
    - CURRENT ← SUCC

# Search with Limited Memory and Time

- Mechanisms for discarding nodes
  - Pruning
  - DFBB
  - Memory Bound A\*
- Mechanisms for redoing nodes
  - IDA\*
- Domain relaxation What is the utility?

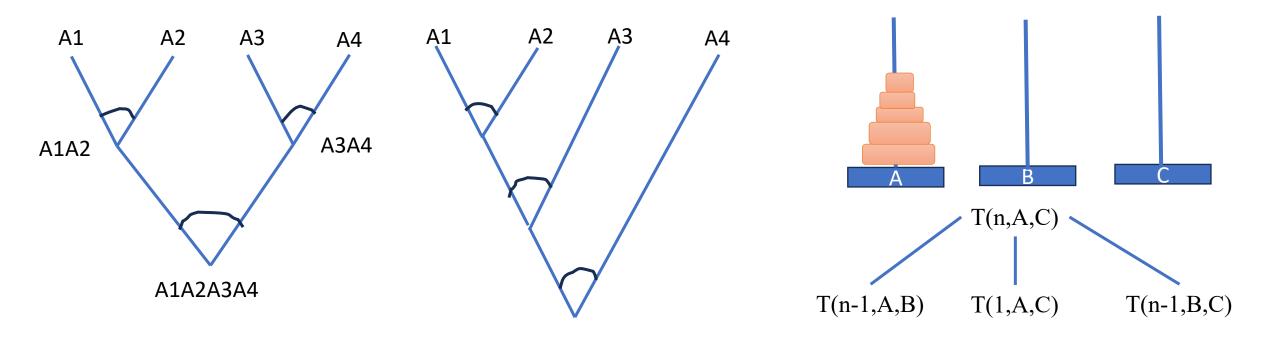
# AIFA Problem Reduction Search

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#### Problem Reduction Search

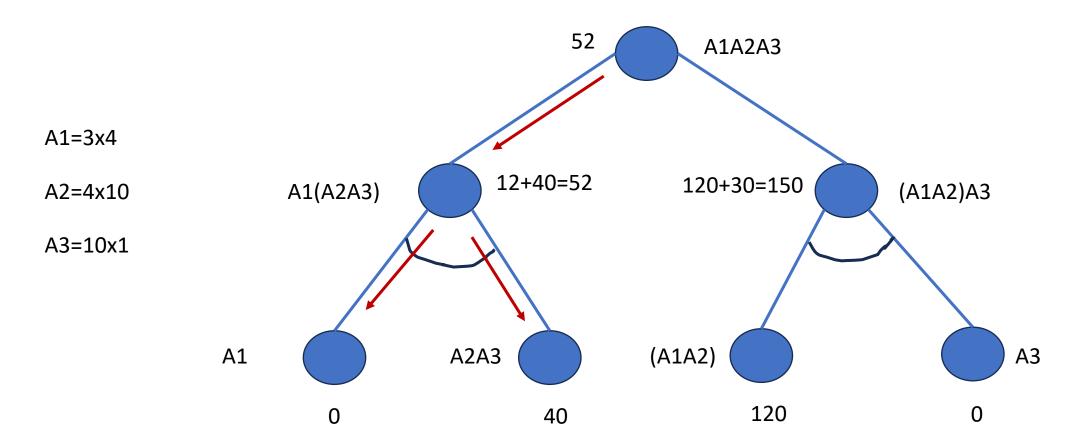
- Planning how best to solve a problem that can be recursively decomposed into sub-problems in multiple ways
  - Matrix multiplication problem
  - Tower of Hanoi
  - Theorem proving



#### Formulation

- AND/OR Graph
  - An OR node represents a choice between possible decompositions
  - An AND node represents a given decomposition
- Game Trees
  - Max/Min nodes
  - Max nodes represent the choice of my opponent
  - Min nodes represent my choice

Each node has a separate optimization criteria



• This is when heuristics is not present

# Thank You