

# AIFA

# State Space Search

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# Search Frameworks

- State space search
  - Uninformed/Blind search
  - Informed/Heuristic search
- Problem reduction search
  - Decompose the problem into parts
  - Solve parts best way
  - Integration by parts
- Game tree search
- Advances
  - Memory bound Search
  - Multi-objective Search
  - Learning how to search

# State Space Search

- Basic Search Problem:
  - Given:  $[S, s, O, G]$  where
    - $S$  is the [implicitly specified] set of states
    - $s$  is the start state
    - $O$  is the set of state transition operators
    - $G$  is the set of goal states
  - To find a sequence of state transitions leading from  $s$  to a goal state

# 8 Puzzle Problem

1	3	5
2	7	4
6		8

Start state



1	2	3
4	5	6
7	8	

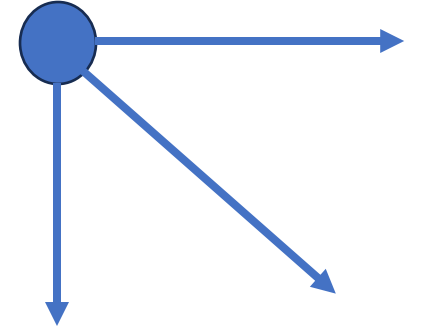
Goal state

# 8 Puzzle Problem

- State description (S)
  - Location of each of the eight tiles (and the blank)
- Start state(s)
  - The starting configuration (s)
- Operators(O)
  - Four operators, for moving the blank left, right, up, or down
  - Not all the operators are applicable in each state
- Goal(G)
  - One or more goal state (given)

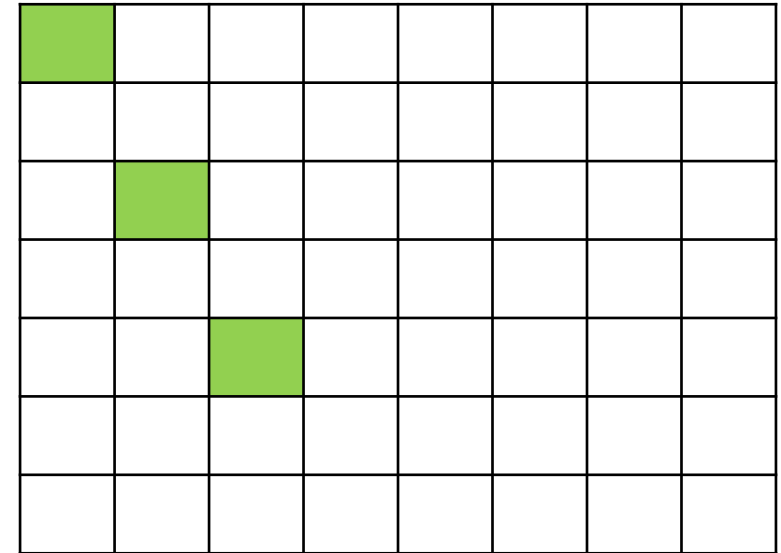
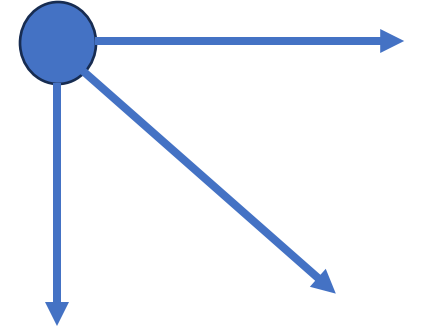
# 8 queens problem

- Placing 8 queens on a chess board, so that none attacks other
- Formulation-1
  - A state is any arrangement of 0 to 8 queens on board
  - Operators add a queen to any square
  - Unsystematic, putting anywhere
  - Not going row-wise or column-wise



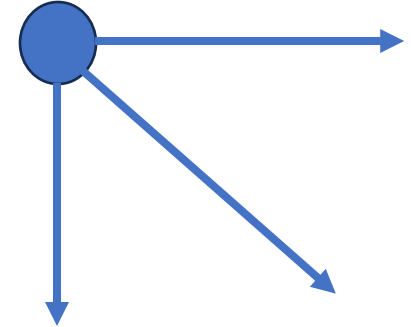
# 8 queens problem

- Placing 8 queens on a chess board, so that none attacks other
- Formulation-2
  - A state is any arrangement of 0 to 8 queens with none attacked
  - Operators place a queen in the leftmost empty column
- Slightly more systematic



# 8 queens problem

- Placing 8 queens on a chess board, so that none attacks other
- Formulation-3
  - A state is any arrangement of 8 queens, one in each column
  - Operators move an attacked queen to another square in the same column
- Iterative refinement
- How to systematically solve such problems?
  - Good formulation reduces search effort
  - Bad formulation increases search effort

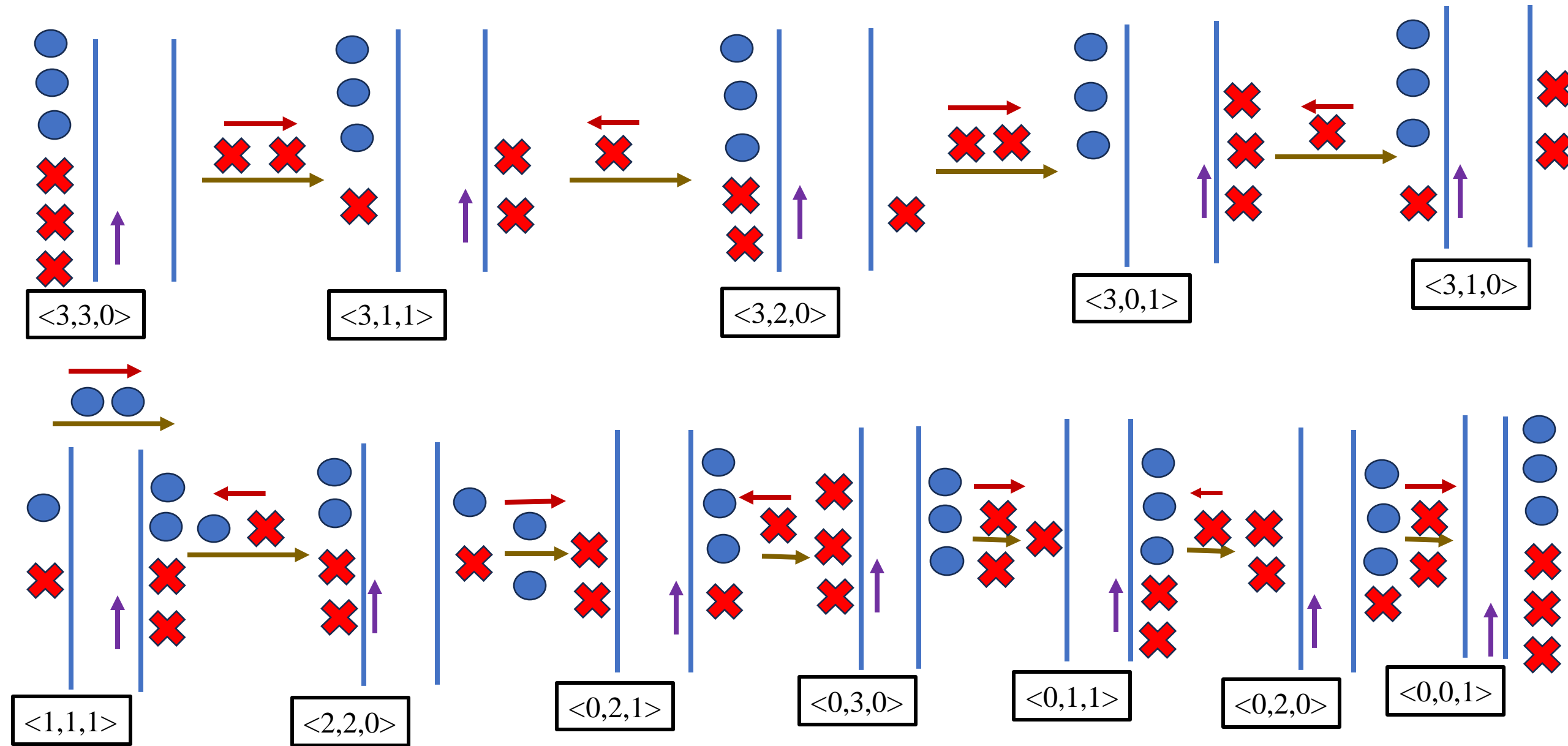




# Missionaries and Cannibals

- Three missionaries and three cannibals are on one side of a river
- A boat that can hold one or two people
- Find a way to get everyone to the other side,
  - without ever leaving a group of missionaries outnumbered by cannibals

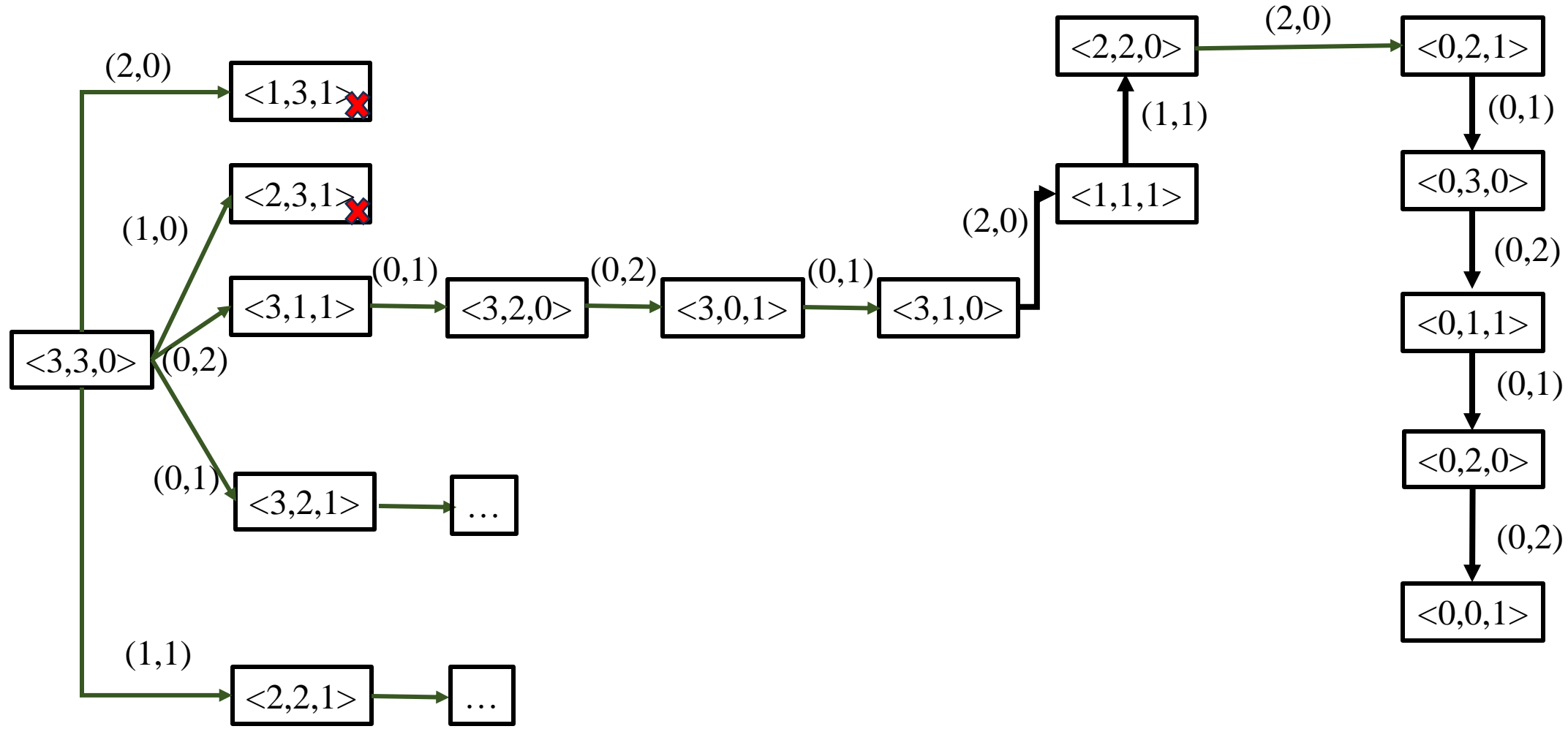
# Missionaries and Cannibals



# Missionaries and Cannibals

- State: ( $\#m$ ,  $\#c$ , 1/0)
  - $\#m$ : Number of missionaries in the first bank
  - $\#c$ : Number of cannibals in the first bank
  - The last bit indicates whether the boat is in the first bank
- 
- Start state: (3,3,0)
  - Goal state: (0,0,1)
  - Operators: Boat carries ( $\#missionaries$ ,  $\#cannibals$ )
  - (1,0), (0,1), (1,1)
  - (2,0), (0,2)

# Missionaries and Cannibals: Search



# Search: Challenges

- Is the search space a graph or tree?
  - While exploring the states same state may appear multiple times
- Is it important to identify such repetitive states?
  - Yes
  - It may lead to infinite loop

Thank You