

```

import numpy as np

class NeuralNetwork:

    def __init__(self, input_size, hidden_size, output_size):

        self.input_size = input_size

        self.hidden_size = hidden_size

        self.output_size = output_size


        # Initialize weights and biases

        self.weights_input_hidden = np.random.randn(self.input_size, self.hidden_size)

        self.bias_hidden = np.zeros((1, self.hidden_size))

        self.weights_hidden_output = np.random.randn(self.hidden_size, self.output_size)

        self.bias_output = np.zeros((1, self.output_size))


    def sigmoid(self, x):

        return 1 / (1 + np.exp(-x))


    def sigmoid_derivative(self, x):

        return x * (1 - x)


    def forward(self, X):

        # Forward pass

        self.hidden_layer_input = np.dot(X, self.weights_input_hidden) + self.bias_hidden

        self.hidden_layer_output = self.sigmoid(self.hidden_layer_input)


        self.output_layer_input = np.dot(self.hidden_layer_output, self.weights_hidden_output) +
self.bias_output

        self.output = self.sigmoid(self.output_layer_input)


        return self.output

```

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def backward(self, X, y, output, learning_rate):

    # Backpropagation

    error = y - output

    output_delta = error * self.sigmoid_derivative(output)

    hidden_error = output_delta.dot(self.weights_hidden_output.T)

    hidden_delta = hidden_error * self.sigmoid_derivative(self.hidden_layer_output)

    # Update weights and biases

    self.weights_hidden_output += self.hidden_layer_output.T.dot(output_delta) * learning_rate

    self.bias_output += np.sum(output_delta, axis=0, keepdims=True) * learning_rate

    self.weights_input_hidden += X.T.dot(hidden_delta) * learning_rate

    self.bias_hidden += np.sum(hidden_delta, axis=0, keepdims=True) * learning_rate

def train(self, X, y, epochs, learning_rate):

    for epoch in range(epochs):

        output = self.forward(X)

        self.backward(X, y, output, learning_rate)

        if epoch % 100 == 0:

            print(f'Epoch {epoch}: Error {np.mean(np.square(y - output))}')

```

Example usage:

Initialize neural network

input_size = 1

hidden_size = 1

output_size = 1

```
nn = NeuralNetwork(input_size, hidden_size, output_size)
```

```
# Example training data
```

```
X = np.array([[5]]) # Input
```

```
y = np.array([[1]]) # Target output
```

```
# Train the neural network
```

```
nn.train(X, y, epochs=1000, learning_rate=0.1)
```

```
# Make predictions
```

```
predictions = nn.forward(X)
```

```
print("Predictions:", predictions)
```

```
# Example usage:
```

```
# Initialize neural network
```

```
input_size = 2
```

```
hidden_size = 3
```

```
output_size = 1
```

```
nn = NeuralNetwork(input_size, hidden_size, output_size)
```

```
# Example training data
```

```
X = np.array([[0, 0],[1, 0],[0, 1], [1, 1]])
```

```
y = np.array([[1],[0],[1], [0]])
```

```
# Train the neural network
```

```
nn.train(X, y, epochs=987, learning_rate=0.1)
```

```
# Make predictions
```

```
predictions = nn.forward(X)
```

```
print("Predictions:", predictions)
```