

**SCHOOL OF
COMPUTING**

DESIGN AND ANALYSIS OF ALGORITHMS
LAB WORKBOOK
WEEK - 7

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CLASS : CSE-B

Question 1: Let there be 14 jobs with the profit of 22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11 with deadlines 3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1

Implement the greedy algorithm for the Job Sequencing with Deadlines and determine the optimal sequence of jobs that maximizes total profit

WORKING:

Q. Let there be 14 jobs with the profit 22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11 with deadline - 3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1

Step 1: No. of Jobs (N) = 14
 profits corresponding to jobs J_1 to J_{14} are P_1 to P_{14}
 $(P_1 \text{ to } P_{14}) = (22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11)$
 $(D_1 \text{ to } D_{14}) = (3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1)$

Step 2: Arrange the jobs in descending order based on profits write corresponding deadlines

Profit	Deadline	Job
30	5	J_5
29	8	J_3
28	2	J_4
27	10	J_7
27	12	J_{12}
26	4	J_9
25	6	J_8
24	3	J_1
22	5	J_6
21	3	J_2
19	13	J_{13}
19	14	J_{14}
14	1	J_{11}
11	1	J_{14}

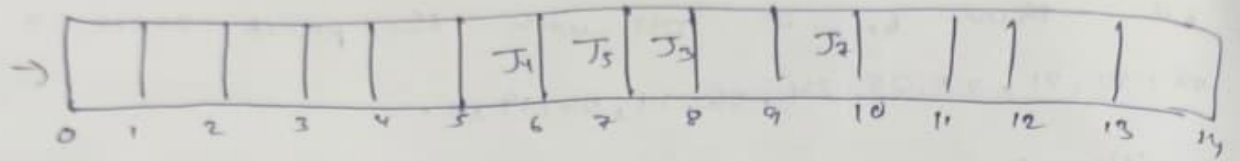
Step 3: Create Slots and Assign Jobs

$J_5, P_5 = 30, D_5 = 5$

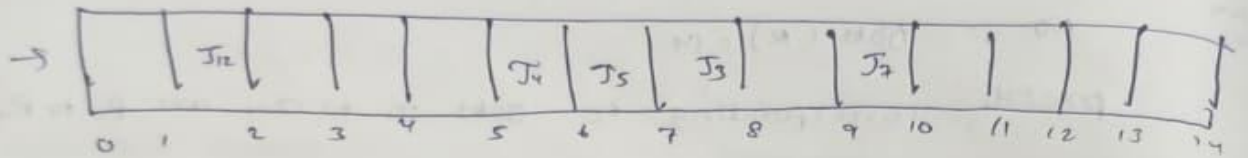
$J_3, P_3 = 29, D_3 = 8$

$J_4, P_4 = 28, D_4 = 2$

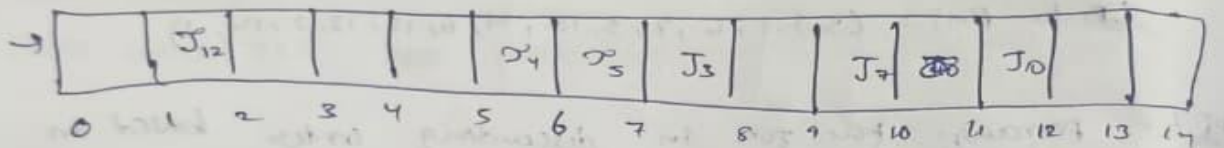
$$J_2, P_2 = 22, Q_2 = 10$$



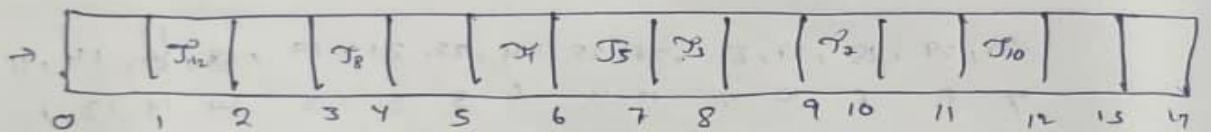
$$J_{11}, P_{11} = 27, Q_{11} = 2$$



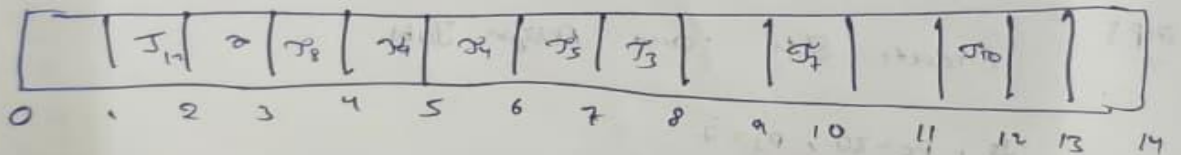
$$J_{10}, P_{10} = 28, Q_{10} = 12$$



$$J_8, P_3 = 25, Q_3 = 4$$

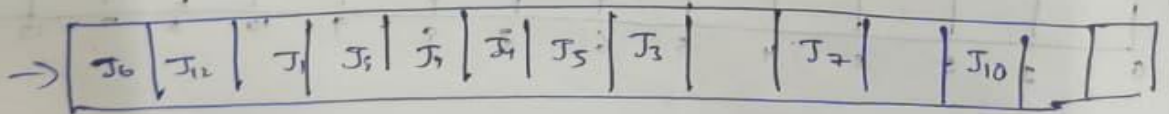


$J_9, P_4 = 24, Q_4 = 6$, As slot [5-6] is filled check. As it is empty.

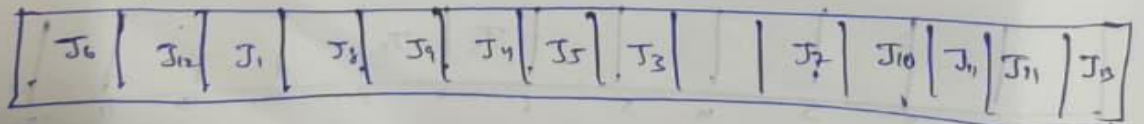


$$J_1, P_1 = 22, P_1 = 3$$

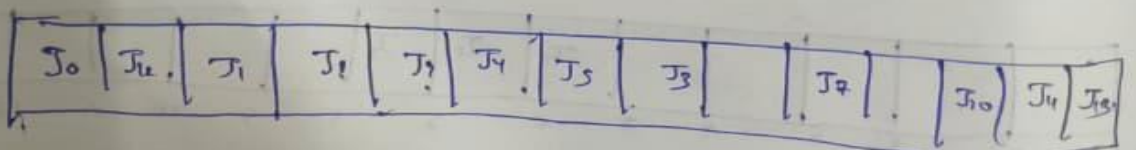
Reject J_2



$$J_{13}, P_{13} = 19$$



$$J_1, P_{11} = 14, P_{11} = 13$$



$J_3, P_{in} = 11, D_{in} = 1$
 As Deadline > 1 , there are no slots left for P_{in}
 So Pruned J_3

Final Job Sequence = $\{J_5, J_3, J_4, J_7, J_{10}, J_{10}, J_9, J_1, J_8, J_{10}, J_{11}\}$

J_5	J_{10}	J_1	J_8	J_9	J_4	J_5	J_3	J_7	J_{10}	J_{11}	J_{12}
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Total profit = $21 + 27 + 22 + 25 + 24 + 28 + 30 + 29 + 27 + 26 + 14 + 19$
 $= 292$

CODE:

```

1  #include <stdio.h>
2  #define MAX 100
3  struct Job
4  {
5      int id;
6      int profit;
7      int deadline;
8  };
9  void sortJobs(struct Job jobs[], int n)
10 {
11     int i, j;
12     struct Job temp;
13
14     for(i = 0; i < n - 1; i++)
15     {
16         for(j = 0; j < n - i - 1; j++)
17         {
18             if(jobs[j].profit < jobs[j + 1].profit)
19             {
20                 temp = jobs[j];
21                 jobs[j] = jobs[j + 1];
22                 jobs[j + 1] = temp;
23             }
24         }
25     }
26 }
27 int findMaxDeadline(struct Job jobs[], int n)
28 {
29     int i, max = jobs[0].deadline;
30
31     for(i = 1; i < n; i++)
32     {
33         if(jobs[i].deadline > max)
34         {
35             max = jobs[i].deadline;
36         }
37     }

```

```
38     return max;
39 }
40 int main()
41 {
42     struct Job jobs[MAX];
43     int n, i, j;
44
45     printf("Enter number of jobs: ");
46     scanf("%d", &n);
47     printf("Enter profits:\n");
48     for(i = 0; i < n; i++)
49     {
50         jobs[i].id = i + 1;
51         scanf("%d", &jobs[i].profit);
52     }
53     printf("Enter deadlines:\n");
54     for(i = 0; i < n; i++)
55     {
56         scanf("%d", &jobs[i].deadline);
57     }
58     sortJobs(jobs, n);
59     int maxDeadline = findMaxDeadline(jobs, n);
60     int slot[MAX];
61     for(i = 1; i <= maxDeadline; i++)
62     {
63         slot[i] = -1;
64     }
65     int totalProfit = 0;
66     for(i = 0; i < n; i++)
67     {
68         for(j = jobs[i].deadline; j >= 1; j--)
69         {
70             if(slot[j] == -1)
71             {
```

```

72         slot[j] = jobs[i].id;
73         totalProfit += jobs[i].profit;
74         break;
75     }
76 }
77 }
78 printf("\nSlot Arrangement:\n");
79 for(i = 1; i <= maxDeadline; i++)
80 {
81     if(slot[i] == -1)
82         printf("Slot %d : _\n", i);
83     else
84         printf("Slot %d : J%d\n", i, slot[i]);
85 }
86 printf("\nMaximum Profit = %d\n", totalProfit);
87 return 0;
88 }

```

OUTPUT:

```

PS D:\raahithya\4TH SEM\DAA\week7> gcc jobSequencing.c -o results
PS D:\raahithya\4TH SEM\DAA\week7> ./results
Enter number of jobs: 14
Enter profits:
22 19 29 28 30 21 27 25 24 26 14 27 19 11
Enter deadlines:
3 3 8 6 7 5 10 4 6 12 13 2 14 1

Slot Arrangement:
Slot 1 : J6
Slot 2 : J12
Slot 3 : J1
Slot 4 : J8
Slot 5 : J9
Slot 6 : J4
Slot 7 : J5
Slot 8 : J3
Slot 9 : _
Slot 10 : J7
Slot 11 : _
Slot 12 : J10
Slot 13 : J11
Slot 14 : J13

Maximum Profit = 292

```

Time Complexity:

1. Sorting the jobs by profit

We used Bubble Sort in the program.

Time complexity: $O(n^2)$

2. Finding maximum deadline

We check all jobs once.

Time complexity: $O(n)$

3. Assigning jobs to slots

For each job, we may check up to d slots. $O(n^2)$

Total Time Complexity

$$O(n^2) + O(n) + O(n^2) = O(n^2)$$

Space Complexity

We use:

- Job array $\rightarrow O(n)$
- Slot array $\rightarrow O(d)$

Total Space: $O(n)$