PROPERTIES OF LIMITS

Suppose that $\lim_{x\to c} f(x) = L$ and that $\lim_{x\to c} g(x) = K$,

1.
$$n * \lim_{x \to c} f(x) = \lim_{x \to c} n * f(x) = n * L$$

2.
$$\lim_{x \to c} \left[f(x) \right] \pm \lim_{x \to c} \left[g(x) \right] = \lim_{x \to c} \left[f(x) \pm g(x) \right] = L \pm K$$

3.
$$\lim_{x \to c} [f(x) * g(x)] = \lim_{x \to c} [f(x)] * \lim_{x \to c} [g(x)] = L * K$$

$$4. \lim_{x \to c} \left[\frac{f(x)}{g(x)} \right] = \frac{\lim_{x \to c} [f(x)]}{\lim_{x \to c} [g(x)]} = \frac{L}{K}, \text{ provided } \lim_{x \to c} [g(x)] \neq 0$$

5.
$$\lim_{x \to c} [f(x)]^n = \left[\lim_{x \to c} f(x)\right]^n = L^n$$
, where n is any real number

6.
$$\lim_{x \to c} a = a$$
, a is any real number

$$7. \quad \lim_{x \to c} x = c$$

$$8. \lim_{x \to c} x^n = c^n$$

1. Evaluate the following limit using only the properties above

$$\lim_{x \to -2} \left(3x^2 + 5x - 9\right)$$

Now note that if defined $p(x) = 3x^2 + 5x - 9$ and evaluated $\lim_{x \to -2} p(x)$ a quick direct substitution would have yielded that our limit equals p(-2) = -7